# COMS3008A: Parallel Computing Introduction to MPI I

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## **Expected Learning Outcome**

- Understanding message passing programming model
- Apply the basic set of MPI functions to write simple MPI programs
- Compile and run MPI program on a cluster



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## Message Passing Model

- The usual underlying hardware: a collection of processors, each with its own local memory (or address space).
- A process: a task
  - A process is (traditionally) a program counter and address space.
  - Processes may have multiple threads (program counters and associated stacks) sharing a single address space.
- Every process can communicate with every other processes.



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#### **MPI**

- MPI (Message Passing Interface) standard is the most popular message passing specification that supports parallel programming.
- MPI is a message passing library specification.
- MPI is for communication among processes, which have separate address spaces.
- Inter-process communication consists of
  - synchronization
  - movement of data from one process' address space to another's.



## The Message Passing Model and MPI cont.

- MPI is not
  - a language or compiler specification
  - a specific implementation or product
- MPI is for parallel computers, clusters, and heterogeneous networks.
- MPI versions:
  - MPI-1 supports the classical message-passing programming model: basic point-to-point communication, collectives, datatypes, etc. MPI-1 was defined (1994) by a broadly based group of parallel computer vendors, computer scientists, and applications developers.
  - MPI-2 was released in 1997. MPI-2.1 (2008) and MPI-2.2 (2009) with some corrections to the standard and small features
  - MPI-3 (2012) added several new features to MPI.
  - MPI-4 (2021) added several new features to MPI.
  - MPI-5 (in proposal stage).
  - The Standard itself: at http://www.mpi-forum.org. All MPI officials releases, in both postscript and HTML.

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## The Minimal set of MPI Functions

MPI_Init	Initializes MPI.
MPI_Finalize	Terminates MPI.
MPI_Comm_size	Determines the number of processes.
MPI_Comm_rank	Determines the label of the calling process.
MPI_Send	Sends a message.
MPI_Recv	Receives a message.



## Starting and Terminating MPI Programs

- int MPI\_Init(int \*argc, char \*\*\*argv)

  The parameters are from the parameters of the main C program.
  - Initialization: must call this prior to other MPI functions
- int MPI\_Finalize()
  - Must call at the end of MPI program
- Return codes

```
MPI_SUCCESS
MPI_ERROR
```



#### Communicators

- MPI\_Comm: communicator communication domain
  - Group of processes that can communicate with one another
  - Supplied as an argument to all MPI message passing functions
  - Process can belong to multiple communication domain
- MPI\_COMM\_WORLD: root communicator includes all the processes



## Communicator Inquiry Functions

- int MPI\_Comm\_size(MPI\_Comm comm, int \*size)
  - Determine the number of processes
- int MPI\_Comm\_rank(MPI\_Comm comm, int \*rank)
  - index of the calling process
  - value: 0 communicator size 1



## Simple MPI Program — "Hello World"

```
#include <mpi.h>
   #include <stdio.h>
2
    int main(int argc, char *argv[])
      int num_procs, myrank;
5
     MPI Init (&argc, &argv);
     MPI Comm size (MPI COMM WORLD, &num procs);
     MPI Comm rank (MPI COMM WORLD, &myrank);
10
     printf("From process %d out of %d, Hello World!\n",
12
        myrank, num procs);
     MPI Finalize();
15
      return 0;
16
17
```

## Simple MPI Program cont.

- Header file for MPI program #include <mpi.h>
- Each active MPI process executes its own copy of the program.
- The first MPI function call made by every MPI process is the call to MPI\_Init, which allows the system to do any setup needed to handle further calls to the MPI library.
- When MPI has been initialized, every active process becomes a member of a communicator called MPI\_COMM\_WORLD.



## Simple MPI Program cont.

- A communicator defines a communication domain a set of processes that are allowed to communicate with each other – a communication context.
- A default communicator: MPI\_COMM\_WORLD, which includes all the processes started by the user.
- Communicators are used as arguments to all message transfer MPI routines.
- A process can belong to many different (possibly overlapping) communication domains.



## Simple MPI Program cont.

- A process calls function MPI\_Comm\_rank to determine its rank within a communicator.
- It calls MPI\_Comm\_size to determine the total number of processes in a communicator.

```
int id, p;
MPI_Comm_rank(MPI_COMM_WORLD, &id);
MPI_Comm_size(MPI_COMM_WORLD, &p);
```

 After a process has completed all of its MPI library calls, it calls function MPI\_Finalize, allowing the system to free up resources (such as memory) that have been allocated to MPI, and shuts down MPI environment.



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## Compiling and Running MPI Programs

- MPI is a library. Applications can be written in C, C++ or Fortran and appropriate calls to MPI can be added where required
- Compilation
  - Regular applications: gcc test.c -o test
  - MPI applications: mpicc hello\_world.c -o test
- Execution
  - Regular applications: ./test
  - MPI applications (running with 16 processes):
    - mpiexec -n 16 ./test or
    - mpirun -np 16 ./test



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## Installing MPI standard implementation

MPI standard implementation can be already provided as part of the OS, often as MPICH<sup>1</sup> or OpenMPI<sup>2</sup>. If it is not, it can usually be installed through the provided package management, e.g., apt in Ubuntu:

- for MPICH, sudo apt-get install libmpich-dev
- for OpenMPI,
   sudo apt-get install libopenmpi-dev



<sup>&</sup>lt;sup>1</sup>MPICH. *High performance portable MPI*. https://www.mpich.org/.

<sup>&</sup>lt;sup>2</sup>Open MPI. Open source high performance computing. https://www.open-mpi.org/.

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#### **Data Communication**

- Data communication in MPI: One process sends a copy of data to another process (or a group of processes), and the other process receives it.
- Communication requires the following information:
  - Sender: the receiver, data count, data type, a user defined tag for the message
  - Receiver: the sender, data count, data type, the tag for the message



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## MPI Basic (Blocking) Send

```
int MPI_Send(void *buf,int count,MPI_Datatype datatype,
    int dest,int tag,MPI_Comm comm)
```

- The message buffer is described by buf, count, datatype.
- The target process is specified by dest and comm.
  - dest is the rank of the target process in the communicator specified by comm.
- tag is a user-defined type for the message
- When this function returns, the data has been delivered to the communication system and the send buffer (described by buf, count, datatype) can be reused. The message may not have been received by the target process.



## MPI Basic (Blocking) Receive

```
int MPI_Recv(void *buf,int count,MPI_Datatype datatype,
    int source,int tag,MPI_Comm comm,MPI_Status *status)
```

- Waits until a matching (on source, datatype, tag, comm) message is received from the communication system, and the buffer can be used.
- Source is the rank of sender in communicator comm, or MPI\_ANY\_SOURCE.
- status contains further information: The MPI type MPI\_Status is a struct with at least three members MPI\_SOURCE, MPI\_TAG, and MPI\_ERROR.
- MPI\_STATUS\_IGNORE can be used if we don't need any additional information



# Simple Communication in MPI

```
#include <mpi.h>
2 #include <stdio.h>
4 int main(int argc, char ** argv) {
     int rank, data[100];
7
     MPI_Init(&argc, &argv);
     MPI_Comm_rank(MPI_COMM_WORLD, &rank);
8
   //Array data needs to be initialized
      if (rank == 0)
10
          MPI Send (data, 100, MPI INT, 1, 0, MPI COMM WORLD
11
     else if (rank == 1)
12
          MPI Recv (data, 100, MPI INT, 0, 0, MPI COMM WORLD
13
             , MPI STATUS IGNORE);
     MPI Finalize();
15
      return 0;
16
```

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# MPI Datatypes

MPI Datatype	C Datatype
MPI_CHAR	signed char
MPI_SHORT	signed short int
MPI_INT	signed int
MPI_LONG	signed long int
MPI_UNSIGNED_CHAR	unsigned char
MPI_UNSIGNED_SHORT	unsigned short int
MPI_UNSIGNED	unsigned int
MPI_UNSIGNED_LONG	unsigned long int
MPI_FLOAT	float
MPI_DOUBLE	double
MPI_LONG_DOUBLE	long double



## Sending and Receiving Messages

- MPI allows specification of wildcard arguments for both source and tag.
- If source is set to MPI\_ANY\_SOURCE, then any process of the communication domain can be the source of the message.
- If tag is set to MPI\_ANY\_TAG, then messages with any tag are accepted.
- Only a receiver can use wildcard arguments. Sender must use a process rank and nonnegative tag.
- On the receive side, the message must be of length equal to or less than the length field specified.



## Sending and Receiving Messages

- On the receiving end, the status variable can be used to get information about the MPI\_Recv operation.
- The corresponding data structure contains:

```
typedef struct MPI_Status {
  int MPI_SOURCE;
  int MPI_TAG;
  int MPI_ERROR;
};
```

 The MPI\_Get\_count function returns the source, tag and number of elements of datatype received



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## Benchmarking the Performance

- Running time:
  - MPI provides a function called MPI\_Wtime that returns a double-precision floating-point number of seconds that have elapsed since some point of time in the past.
  - Function MPI\_Wtick returns a floating-point number that is the time in seconds between successive ticks of the clock, i.e., the precision of the result returned by MPI\_Wtime.

```
double MPI_Wtime()
double MPI_Wtick()
```



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## Example 1: Rotating a token around a ring

#### Example 1

Consider a set of n processes arranged in a ring. Process 0 sends a token message, say "Hello!", to process 1; process 1 passes it to process 2; process 2 to process 3, and so on. Process n-1 sends back the message to process 0. Write an MPI program that performs this simple token ring.



```
MPI_Init(&argc,&argv);
 2 MPI_Comm_size(MPI_COMM_WORLD, &nproces);
  3 MPI_Comm_rank (MPI_COMM_WORLD, &myrank);
5 if (myrank == 0)
prev = nproces - 1;
7 else
8 prev = myrank - 1;
9 if (myrank == (nproces - 1))
next = 0;
11 else
next = myrank + 1;
13 if (myrank == 0)
strcpy(token, "Hello!");
MPI_Send(token, MSG_SZ, MPI_CHAR, next, tag,
                        MPT COMM WORLD):
16 MPI_Recv(token, MSG_SZ, MPI_CHAR, prev, tag,
                        MPI_COMM_WORLD, MPI_STATUS_IGNORE);
printf("Process %d received token %s from process %d.\n", proc
                             myrank, token, prev);
```

```
DATE: Wed Sep 29 16:26:19 SAST 2021
2 Job is running on nodes mscluster[30,47,50,55]
4 SLURM: sbatch is running on mscluster0.ms.wits.ac.za
5 SLURM: job ID is 141789
6 SLURM: submit directory is /home-mscluster/hwang/PC/
     mpi_lab1
7 SLURM: number of nodes allocated is 4
8 SLURM: number of tasks is 8
9 SLURM: job name is PC mpi com
11 Process 1 received token Hello! from process 0.
12 Process 7 received token hR???- from process 6.
13 Process 0 received token h?p??- from process 7.
14 Process 2 received token hRU7?- from process 1.
15 Process 3 received token h?^??- from process 2.
16 Process 4 received token h?? from process 3.
17 Process 6 received token h?^P?- from process 5.
18 Process 5 received token h?6??- from process 4.
```



```
1 if (myrank == 0) {
2 strcpy(token, "Hello World!");
  MPI_Send(token, MSG_SZ, MPI_CHAR, next, tag,
3
       MPI COMM WORLD);
  MPI_Recv(token, MSG_SZ, MPI_CHAR, prev, tag,
       MPI COMM WORLD, MPI STATUS IGNORE);
printf("Process %d received token %s from process %d.\n
       ", myrank, token, prev);
7 else {
   MPI Recv(token, MSG SZ, MPI CHAR, prev, tag,
       MPI COMM WORLD, MPI STATUS IGNORE);
   MPI Send (token, MSG SZ, MPI CHAR, next, tag,
9
      MPI COMM WORLD);
   printf("Process %d received token %s from process %d.\n
10
       ", myrank, token, prev);
```

```
DATE: Wed Sep 29 16:26:19 SAST 2021
2 Job is running on nodes mscluster[30,47,50,55]
4 SLURM: sbatch is running on mscluster0.ms.wits.ac.za
5 SLURM: job ID is 141789
6 SLURM: submit directory is /home-mscluster/hwang/PC/
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9 SLURM: job name is PC mpi com
11 Process 1 received token Hello World! from process 0.
12 Process 2 received token Hello World! from process 1.
13 Process 3 received token Hello World! from process 2.
14 Process 4 received token Hello World! from process 3.
15 Process 5 received token Hello World! from process 4.
16 Process 6 received token Hello World! from process 5.
17 Process 7 received token Hello World! from process 6.
18 Process O received token Hello World! from process 7.
```



# Example 2: The Sieve of Eratosthens – finds primes between 2 and *n*

### Example 2

- Create a list of integers 2, 3, 4, ..., n, none of which is marked.
- 2 Set k to 2, the first unmarked number on the list.
- 3 Repeat until  $k^2 > n$ 
  - Mark all multiples of k between  $k^2$  and n
  - Find the smallest number greater than k that is unmarked. Set k to this new value.
- The unmarked numbers are primes



	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60

Table: Integers from 2 to 60

	2	3	5	7	9	11	13	15	17	19	
21		23	25	27	29	31	33	35	37	39	
41		43	45	47	49	51	53	55	57	59	

Table: Sieve = 2

		2	3	5	7		11	13		17	19	
ſ			23	25		29	31		35	37		
ſ	41		43		47	49		53	55		59	١.

Table: Sieve = 3



	2	3	5	7		11	13		17	19	
		23			29	31			37		
41		43		47	49		53			59	

Table: Sieve = 5

	2	3	5	7		11	13		17	19	
		23			29	31			37		
41		43		47			53			59	

Table: Sieve = 7



### The Sieve of Eratosthens – parallelization

- The key parallel computation is step 3.(a)
- Communications among the sub problems; Two communications are needed to perform step 3.(b): a reduction and a broadcast.
- To simplify the problem, let's eliminate the reduction by assuming  $n/p > \sqrt{n}$ , then the first process is responsible for finding the next value of k.
- Decomposing the problem: data decomposition
  - Block decomposition: the range of array elements for each process i is  $|in/p| \sim |(i+1)n/p| 1$ .
  - Block-cyclic decomposition



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# Collective Communication and Computation Operations

- MPI provides an extensive set of functions for performing common collective communication operations.
- Each of these operations is defined over a group corresponding to the communicator.
- All processors in a communicator must call these operations.



### Collective Communication Operations

The barrier synchronization operation is performed in MPI using:

```
int MPI_Barrier(MPI_Comm comm)
```

#### The one-to-all broadcast operation is:

```
int MPI_Bcast(void *buf, int count,MPI_Datatype datatyp
int source, MPI_Comm comm)
```

• The all-to-one reduction operation is:



# **Predefined Reduction Operations**

Operation	Meaning	Datatypes
MPI_MAX	Maximum	C integers and floating point
MPI_MIN	Minimum	C integers and floating point
MPI_SUM	Sum	C integers and floating point
MPI_PROD	Product	C integers and floating point
MPI_LAND	Logical AND	C integers
MPI_BAND	Bit-wise AND	C integers and byte
MPI_LOR	Logical OR	C integers
MPI_BOR	Bit-wise OR	C integers and byte
MPI_LXOR	Logical XOR	C integers
MPI_BXOR	Bit-wise XOR	C integers and byte
	max-max value-location	
MPI_MINLOC	min-min value-location	Data-pairs



# A Simple Reduction Program

```
#include "mpi.h"
#include <stdio.h>
3 #include <math.h>
4 int main(int argc, char **argv) {
    int n, numprocs, myrank, myval, sum;
5
    MPI Init (&argc, &argv);
6
    MPI Comm size (MPI COMM WORLD, &numprocs);
7
    MPI Comm rank (MPI COMM WORLD, &myrank);
8
    if (mvrank == 0) {
9
      printf("Enter the number to be broadcasted: (0 guits
10
          .)"):
      scanf("%d", &n);
12
    MPI_Bcast(&n, 1, MPI_INT, 0, MPI_COMM_WORLD);
13
    //printf("Rank %d received %d\n", myrank + 1, n);
14
    mvval = n * 2;
15
    MPI_Reduce(&myval, &sum, 1, MPI_INT, MPI_SUM, 0,
16
       MPI COMM WORLD);
    if (myrank==0)
      printf("Sum = %d \n", sum);
18
    MPI Finalize();
19
    return 0;
20
21
```



### Function Prototypes

```
int MPI_Init(int *argc, char ***argv)
int MPI_Finalize()
int MPI_Comm_size(MPI_Comm comm, int *size)
int MPI_Comm_rank(MPI_Comm comm, int *rank)
int MPI_Reduce(void *sendbuf, void *recvbuf, int count,
    MPI_Datatype datatype, MPI_Op op, int root, MPI_Comm comm)
int MPI_Bcast(void *buf, int count, MPI_Datatype datatype
    int root, MPI_Comm comm)
double MPI_Wtime()
double MPI_Wtick()
```



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#### What is MPICH

- MPICH is a high-performance and widely portable open-source implementation of MPI
- It provides all features of MPI that have been defined so far (including MPI-1, MPI-2.0, MPI-2.1, MPI-2.2, and MPI-3.0)
- http://www.mpich.org
- Compiling MPI program using MPICH
  - For C programs: mpicc test.c -o test
  - For C++ programs: mpicxx test.cpp -o test
  - To link to a math library: mpicc test.c -o test -lm



# Running MPI programs with MPICH

- Launch 16 processes on the local node:
   mpiexec -n 16 ./test
- Launch 16 processes on 4 nodes (each has 4 cores) mpiexec -hosts h1:4,h2:4,h3:4,h4:4 -n 16 ./test Runs the first four processes on h1, the next four on h2, etc. (h1, h2, h3, h4 are host names separated by comma.) mpiexec -hosts h1,h2,h3,h4 -n 16 ./test Runs the first process on h1, the second on h2, etc., and wraps around. So, h1 will have the 1st, 5th, 9th and 13th processes.



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### Summary

#### We learnt

- Basic set of MPI functions to write simple MPI programs
  - Initialize and finalize MPI
  - Inquire the basic MPI execution environment
  - Basic point to point communication: send and receive
  - Basic collective communication: broadcast and reduction
- Developing MPI programs through examples
- Compiling and running MPI programs
- Useful resources: Introduction to Parallel Computing and Introduction to Parallel Computing: From Algorithms to Programming on State-of-the-Art Platforms.



#### References I

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