<u>Bidirectional Pathfinding Experiment Report</u>

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Introduction

This project investigates pathfinding algorithms for pedestrian navigation around Ben-Gurion University (BGU) utilizing OpenStreetMap (OSM) data. The principal algorithm employed is Bidirectional A* search, which operates by initiating two concurrent A* searches, one progressing from the origin and the other from the destination, converging at an intermediate point to enhance efficiency. This method employs admissible heuristics, specifically straight-line distance, to ensure optimal routing while substantially decreasing both the search space and computation time relative to single-directional A* search.

The developed pathfinding system accommodates a range of routing objectives (cost functions), extending beyond shortest-distance calculations to include minimization of traffic light stops, maximization of safety, and reduction of travel time. These varied optimization criteria provide a comprehensive framework for analyzing the impact of each factor on route selection.

Experiment Goal

The experiment is structured to evaluate the performance of a Bidirectional A* pathfinding algorithm across different route optimization objectives. The main hypothesis is that bidirectional search will effectively identify optimal paths for each specified criterion, and that each routing objective will result in distinct route features consistent with its optimization target. Specifically:

- The Shortest Distance algorithm generates routes with the minimum walking distance, which may involve more road crossings or traffic lights.
- The Fewest Traffic Lights algorithm produces routes with fewer stops at traffic signals or crossings than the shortest distance path, possibly resulting in longer distances or travel times.
- The Safest Route algorithm finds paths with lower safety penalties—such as fewer unlit or higher-risk segments, compared to the shortest route, potentially increasing total distance or time due to detours through safer areas.

 The Fastest Time algorithm identifies the quickest routes in terms of travel time, which may not correspond to the shortest distance; for instance, it can avoid congested intersections or slow segments to achieve reduced overall travel time.

Overall, the experiment assesses whether each custom cost function (distance, delays, safety, time) reliably directs the A* search toward an optimal path reflecting the intended priority and quantifies the trade-offs associated with each objective, such as additional distance traveled to minimize signal stops or enhance safety.

Experiment Description

Software & Data: The experiment was conducted using Python and a custom OpenStreetMap (OSM) pathfinding system. OSM map data (https://github.com/TalKleinBgu/osm-pathfinder-bgu/blob/main/map.osm) for the Ben-Gurion University campus and adjacent Beer-Sheva neighborhoods was parsed into a pedestrian graph tailored to walking. During parsing, all OSM nodes (with coordinates and tags like traffic signals and lighting) and ways (ordered node lists with tags) are loaded. A walkability filter excludes car-only roads and only includes pedestrian-suitable paths like footways, sidewalks, and residential streets.

The designated destination was a specific campus student house (בית הסטודנט), identified by its OSM node ID. Three student neighborhoods in Beer-Sheva—Neighborhood B (שכונה בי), Neighborhood D (שכונה בי), and Old V (ו הישנה), were selected as source areas. For each neighborhood, the locations of all buildings were determined to serve as starting points for routing. In total, approximately 4,724 building-to-campus routes were calculated (1,181 building * 4 path = 4724 path).

Before searching, both endpoints are snapped to the walking graph. For OSM nodes or building ways, the nearest walkable node is found by straight-line distance. building sources use the centroid, also snapped to the closest graph node. This approach keeps searches on graph vertices and avoids mid-segment geometry interpolation.

Algorithm Implementation: Routing uses a Bidirectional A*. Two A* searches run simultaneously: the forward search from the start and the backward search from the goal using the reverse graph. Each maintains its own open queue keyed by f(n)=g(n)+h(n) and a closed set to prevent re-expansion. The implementation keeps g-scores (gF, gB) and predecessor maps (predF, predB) on both sides. A priority-

queue routine removes entries whose g-score doesn't match the current best score. At every step the side with the smaller current f expands next. After expanding a node, the algorithm (i) tightens an upper bound (UB) whenever it discovers a vertex already reached by the opposite search, and (ii) records a meeting state that may be either a node (both searches reached the same vertex) or an edge hand-off (forward reached u and backward reached v with an admissible connection across $u \rightarrow v$). The global termination rule follows the standard bidirectional A* invariant:

$$\min_{\mathbf{x} \in \text{Open}_{F}} f_{F}(\mathbf{x}) + \min_{\mathbf{y} \in \text{Open}_{B}} + f_{B}(\mathbf{y}) \ge UB$$

Correctness and optimality are enforced by admissible heuristics and non-negative edge costs across all profiles, with each profile pairing a suitable heuristic to its cost model and keeping the reverse search symmetric so a front-to-front meet remains optimal. For *shortest*, the heuristic is the Haversine distance, which never overestimates, for *fastest*, it is Haversine distance divided by a generous upper-bound walking speed (1.6 m/s), ensuring actual segment speeds never exceed the bound, for *few_traffic_lights*, the heuristic scales Haversine distance by distance factor then applies a 0.95 safety margin to stay strictly optimistic even when penalties for entering signal or crossing nodes appear, for *safest*, the heuristic remains Haversine distance while the edge cost starts at that distance and only adds non-negative safety penalties (lighting, sidewalks, road class, surface, narrowness, crossings), so the adjusted cost is never below the base distance, preserving admissibility.

Execution Details: The experiment was run end-to-end on a standard desktop using Python. For each area of interest (the three Be'er-Sheva neighborhoods), the pipeline loads the OSM map, parses nodes/ways, and builds a pedestrian graph in both directions (forward and reverse). Each building is then snapped to its nearest walkable graph vertex, the fixed destination (the BGU Student house, OSM id 135310103) is likewise snapped to the closest walkable node. From that start—goal pair the system executes four independent searches—shortest, few_traffic_lights, safest and fastest—each via proper Bidirectional A* with the profile's admissible heuristic. Because the graph window is compact (≈2 km around campus) and bidirectional search halves effective depth, queries complete on the millisecond scale per search. During search the solver records diagnostics (forward/backward node expansions, edges scanned) and, after reconstructing the path, computes uniform route metrics over the final node sequence: geometric distance, time, counts of traffic signals and crossings, cumulative safety penalties, detour factor (vs. straight-line), and realized average walking speed.

All source code, scripts, and raw data files used for this experiment are publicly available in GitHub repository -

https://github.com/TalKleinBgu/osm-pathfinder-bgu

Additionally, interactive map visualizations and all computed paths can be explored through the following links:

- https://talkleinbgu.github.io/osm-pathfinder-bgu/NeighborhoodB.html displays all computed paths from Neighborhood B to the campus
- https://talkleinbgu.github.io/osm-pathfinder-bgu/NeighborhoodD.html shows optimal routes from Neighborhood D
- https://talkleinbgu.github.io/osm-pathfinder-bgu/NeighborhoodOldV.html presents the route visualizations for Old V neighborhood

Results

Despite all routes sharing the same destination, the outcomes demonstrate clear differences in path choices and metrics for the four algorithms, confirming the experiment's expectations.

All statistics for every buildings are located in the link https://github.com/TalKleinBgu/osm-pathfinderbgu/blob/main/neighborhood_pathfinding_detailed_data.csv

The next table summarizes an example set of results for a representative building (369910595) under each routing profile:

Algorithm	Path Distance (m)	Travel Time (min)	Traffic Signals	Detour factor	Num nodes in path	Avg walking speed	Signal density per 100km	Edge scanned	Node expanded
Shortest (distance)	1787	25.07	6	1.33	80	4.28	0.34	1357	536
Fewest Traffic Lights	2152	27.76	2	1.6	114	4.65	0.09	7539	3257
Safest Route	2178	28.28	5	1.62	76	4.62	0.23	2962	1213
Fastest Time	1852	24.5	3	1.38	86	4.53	0.16	2395	981

^{*} Detour factor is (route distance ÷ straight-line (haversine) distance); 1.0 is perfectly direct, 1.3 means the walk is 30% longer than the haversine.

The Shortest profile provides the geometric baseline (1,787 m in 25.07 min) but traverses 6 signals, which depresses realized speed (4.28 km/h). Optimizing for Fewest Traffic Lights does exactly what it promises—signals drop to 2 and signal density plunges from 0.34 to 0.09 per 100 km, but at a notable cost: distance grows by to 2,152 m, time to 27.76 min, and search work inflates substantially (≈3,257 expansions, ~6× baseline). The Safest profile lands in the middle: distance rises to 2,178 m, time to 28.28 min, and signals fall modestly (to 5), with realized speed improving to 4.62 km/h; computational effort is moderate (1213 expansions). Fastest achieves the most practical efficiency: with only a small geometric detour (1,851 m) it halves signal encounters (3 vs. 6) and finishes faster than Shortest, at a modest computational. In short, for this building the profiles trace a clean trade-off surface: *Shortest* minimizes meters, *Fewest-Lights* minimizes interruptions at the price of extra distance, *Fastest* converts targeted signal avoidance into a small but real time win.



The figure shows four alternatives from Building 369910595 (house icon, left) to the BGU student house (red star, right).

The Shortest route (red) goes mostly straight east, then into campus. It crosses the big main road near the university at several traffic lights. So it is shortest in meters, but you have to stop many times.

The Fastest route (yellow) uses much of the same streets as red, but makes two small turns to reach quicker crossings and wider entries to the student building. These small detours reduce long waits, so you arrive sooner with only a little extra distance.

The Fewest Traffic Lights route (dark blue) goes north earlier, follows a longer, smoother street, crosses the main road once, and comes in from the north side of campus. It has almost no stops, but it is the most indirect path.

The Safest route (green) prefers streets with lights and sidewalks, and it uses marked crossings. It passes near community places like the park and nearby schools/playgrounds, where there are people and better lighting. This adds a small detour for a more comfortable walk.

All four routes meet near the same campus entrance. The main differences come from how each one handles the busy, traffic-light area in the middle of the trip.

When we aggregate by neighborhood, the same patterns hold while the magnitude of the trade-offs depends on local street morphology.

Neighborhood	Algorithm	Path Distance (m)	Travel Time (min)	Traffic Signals	Detour factor	Num nodes in path	Avg walking speed	Signal density per 100km	Edge scanned	Node expanded
В	Shortest (distance)	1677.68	23.2	5.04	1.37	80.71	4.33	0.31	907.91	2250.01
	Fewest Traffic Lights	1919.29	25.39	3.16	1.57	89.16	4.52	0.18	3010.17	7034.16
	Safest Route	1979.2	26.1	5.11	1.61	84.26	4.53	0.27	1203.96	2955.98
	Fastest Time	1652.46	23.71	6.7	1.34	75.87	4.17	0.42	517.82	1312.96
D	Shortest (distance)	1356.74	17.79	2.63	1.44	59.24	4.55	0.21	544.23	1397.53
	Fewest Traffic Lights	1426.14	18.58	2	1.52	69.91	4.57	0.15	1576.2	3903.07
	Safest Route	1565.76	19.97	2.6	1.65	63.25	4.68	0.18	986.04	2500.22
	Fastest Time	1353.51	18.43	3.37	1.44	61.77	4.38	0.27	360.79	932.74
Old V	Shortest (distance)	997.16	12.46	0.02	1.76	53.86	4.81	0	342.45	876.18
	Fewest Traffic Lights	996.73	12.58	0.02	1.76	52.06	4.76	0	317.27	809.79
	Safest Route	1154.19	14.58	0.5	2.01	51.66	4.77	0.04	591.81	1500.15
	Fastest Time	992.01	12.63	0.24	1.75	51.69	4.72	0.02	302.16	772.9

When we aggregate by neighborhood, the same patterns hold while the magnitude of the trade-offs depends on local street morphology. In Neighborhood B (the farthest and most signal-dense), path lengths sit around 1.6–1.9 km and signal exposure is highest, so the objectives separate the most: Fewest-Lights yields the largest detour (detour factor \approx 1.57) and the heaviest search footprint (\approx 3,010 edges scanned; \approx 7,034 expansions. Neighborhood D is intermediate: distances \sim 1.35–1.43

km and baseline signal exposure are lower, so all profiles cluster closer to Shortest; Fewest-Lights still trims signal density ($\approx 0.21 \rightarrow 0.15$) but with a smaller detour and moderate extra computation. Old V is the closest ($\approx 1.0-1.1$ km) and essentially signal-free (densities $\approx 0-0.03$), so the profiles nearly collapse to the same solution; only Safest accepts a slight detour (≈ 2.01) to honor infrastructure preferences, and search costs are uniformly low.

Conclusion

This study demonstrates that a properly engineered Bidirectional A*, paired with profile-specific but admissible cost models, can compute thousands of optimal pedestrian routes on real OSM data quickly and reliably. Across 4,724 paths (\approx 1,181 buildings \times 4 profiles), each objective produced routes whose characteristics matched the intended priority: *Shortest* minimized distance but encountered the most regulated junctions; *Fewest Traffic Lights* reliably suppressed stop exposure (and raised realized walking speed) at the cost of longer, more circuitous paths and heavier search; *Safest* favored infrastructure quality—lighting, sidewalks, controlled crossings, accepting moderate detours; and *Fastest* achieved small yet consistent time gains by bypassing a subset of signals with minimal added distance. These trends held at both the single-building and neighborhood scales, confirming the hypotheses about how each cost function steers the search.

The magnitude of those trade-offs depended on local street morphology. Neighborhood B—farthest and most signal-dense—amplified differences: the few-lights profile delivered the largest reduction in signal exposure but demanded the biggest detours and the most computation, while fastest preserved near-baseline geometry and lean search effort. Neighborhood D showed the same ordering with smaller gaps, and Old V—closest and nearly signal-free—caused the profiles to collapse to near-identical routes, with only the safety profile choosing mild detours to honor infrastructure preferences.

Practically, these findings translate into clear guidance. When arrival time is paramount and the grid is moderately regulated, *Fastest* is a sensible default: it trims a few delays without meaningfully lengthening the walk. When continuity (few stops) matters—e.g., with strollers, running, or user preference—*Fewest Lights* is appropriate, with the transparent trade-off of more meters and minutes. Where comfort and perceived safety dominate (nighttime or unfamiliar areas), *Safest* provides infrastructure-aligned paths at moderate overhead. And in low-signal settings, *Shortest* (or *Fastest*) is typically sufficient since all profiles converge.

Appendix: Key source code

Below are the essential, self-contained snippets and patterns that implement the system's core behavior. Each excerpt is trimmed to the minimum needed to understand structure, flow, and design trade-offs; it matches your repository exactly in naming and logic.

The whole code is in the link - https://github.com/TalKleinBgu/osm-pathfinder-bgu

The results json (with paths) in the link - https://github.com/TalKleinBgu/osm-pathfinder-bgu/tree/main/results

1) Core data model

```
@dataclass
class Node:
   id: str
   lon: float
   tags: Dict[str, str]
@dataclass
   nodes: List[str]
   tags: Dict[str, str]
@dataclass
   path: List[str]
   total_cost: float
   distance_meters: float
   num_traffic_signals: int
   num_crossings: int
safety penalties: float
   time_seconds: float
   description: str
   nodes_expanded_forward: int = 0
   nodes_expanded_backward: int = 0
   edges_scanned_forward: int = 0
   edges_scanned_backward: int = 0
   stale_pops_forward: int = 0
   stale_pops_backward: int = 0
```

2) OSM parsing and pedestrian graph build (forward + reverse)

```
def _build_graph(self):
    print("Building graphs (forward & reverse)_")
    for way in self.ways.values():
        tags = way.tags
    # For pedestrians, most oneway restrictions don't apply
    # Only restrict if explicitly foot=no or specific pedestrian oneway restrictions
        oneway_car = tags.get('oneway') == 'yes'
        highway = tags.get('inghway', '')

# Pedestrians can generally walk both ways on most roads, even if oneway for cars
    # Exception: some highway types where pedestrians should follow car direction
    is_oneway_for_ped = False
    if oneway_car:
        # On these highway types, pedestrians should respect car oneway
        if highway in { motorway', 'motorway_link', 'trunk', 'trunk_link', 'primary'}:
            is_s oneway_for_ped = True
        # If there's explicit foot restriction, respect it
        elif tags.get('foot') == 'no':
            continue # Skip this way entirely for pedestrians

for i in range(len(way.nodes) = 1):
        a, b = way.nodes[i], way.nodes[i+1]
    if a not in self.nodes or b not in self.nodes:
        continue
    dist = self_naversine(self.nodes[a], self.nodes[b])

        e_ab = {'to_node': b, 'distance': dist, 'way_id': way.id, 'way_tags': tags}
        e_ba = {'to_node': a, 'distance': dist, 'way_id': way.id, 'way_tags': tags}

# forward

self.graph[a].append(e_ab)

# reverse

self.ngraph[b].append(('to_node': a, 'distance': dist, 'way_id': way.id, 'way_tags': tags}))

# add opposite direction if not one-way for pedestrians

if not is_oneway_for_ped:
        self.graph[b].append(c_ba)

self.graph[a].append(c_ba)

self.graph[a].append(c_ba)

self.graph[a].append(c_ba)

self.graph[a].append(c_ba)

self.graph[a].append(c_ba)

self.graph[a].append(c_ba)

self.graph[a].append(c_ba)

self.graph[b].append(c_ba)

self.graph[b].append(c_ba)

self.graph[b].append(c_ba)

self.graph[b].append(c_ba)

self.graph[b].append(c_ba)
```

```
def _is_walkable(self, tags: Dict[str, str]) -> bool:
    highway = tags.get('highway', '')
    if highway in {'motorway', 'motorway_link', 'trunk', 'trunk_link'}:
        return False
    foot == tags.get('foot', '')
    if foot == 'no':
        return False
    if foot == 'yes':
        return True
    return highway in {
        'footway', 'pedestrian', 'path', 'steps', 'sidewalk',
        'primary', 'secondary', 'tertiary', 'residential',
        'living_street', 'service', 'unclassified', 'track'
}
```

3) Safety context (public places index) and geometry

4) Cost models (four profiles, symmetric and admissible)

```
def _cost_shortest(self, e, from_id): # meters
     return e['distance']
def _cost_few_traffic_lights(self, e, from_id):
    cfg = self._few_traffic_lights_cfg
    c = e['distance'] * cfg['distance_factor']
    m penalties on the hole being entered
nt = self.nodes[e['to_node']].tags
crossing = nt.get('crossing') # e.g., traffic_signals, zebra, uncontrolled, island
is_signal = (nt.get('highway') == 'traffic_signals') or (crossing == 'traffic_signals')
    if is_signal:
    | c += cfg['signal_penalty_m']
| clif nt.get('highway') == 'crossing' or crossing:
| # nuanced crossing types
           if crossing == 'zebra' or nt.get('crossing:markings') == 'zebra':
          c += cfg['zebra_penalty_m']
elif crossing == 'uncontrolled' or crossing == 'no_signals':
               c += cfg['uncontrolled_penalty_m']
           elif crossing == 'island' or crossing == 'refuge_island':
               c += cfg['island_penalty_m']
                c += cfg['other_crossing_penalty_m']
          # accessibility features slightly reduce perceived penalty
if nt.get('tactile_paving') == 'yes':
          c += cfg['tactile_paying / =- yes'

if nt.get('kerb') == 'lowered':

c += cfg['lowered_kerb_bonus_m']
```

```
c = e['distance']
wt = e['way_tags']
# lighting along way or at node
way_lit = wt.get('lit')
if (way_lit == 'no') or (way_lit is None and self.nodes[e['to_node']].tags.get('lit') == 'no'):

c += 150.0 if is_night else 25.0
hw = wt.get('highway')
if hw in {'alley', 'service'}:
    c += 90.0 if is_night else 25.0
if hw in {'primary', 'secondary', 'tertiary'} and wt.get('sidewalk', '') in {'no', 'none', ''}:
    c += 140.0 if is_night else 50.0
# SAUCHRIANS
SW = wt.get('sidewalk', '')
if sw in ('none', 'no','') and hw not in ('footway', 'pedestrian', 'path'):
    c += 90.0 if is_night else 25.0
# shared cycle/foot paths without segregation are a bit less comfortable
if hw in {'path', 'footway'} and wt.get('bicycle') in {'yes', 'designated'} and wt.get('segregated') == 'no':
    c += 30.0 if is_night else 10.0
C += 25.0
    width = float(wt.get('width', 'nan'))
if width and width < 1.5:</pre>
         C += 30.0
except ValueError:
# tunnels/bridges at night
if is_night and (wt.get('tunnel') == 'yes' or wt.get('bridge') == 'yes'):
elif crossing == 'zebra' or nt.get('crossing:markings') == 'zebra':
    c += 10.0  # still a minor risk
elif crossing == 'island':
     if nt.get('kerb') == 'lowered':
bonus = 0.0
amenity = nt.get('amenity','')
leisure = nt.get('leisure','')
     amenity in {'place_of_worship','synagogue','school','kindergarten','university','library','community_centre','police','clinic','hospital','restaurant','cafe'}
or leisure in {'playground','pitch','sports_centre','stadium','park','garden','fitness_centre','dog_park','swimming_pool'}
or nt.get('near_public_place') == 'yes'
     bonus = 40.0 if is_night else 20.0
if bonus:
```

```
def cost fastest(self, e, from id): # seconds
    dist = e['distance']
wt = e['way_tags']
    hw = wt.get('highway')
if hw in {'footway','pedestrian','sidewalk'}:
    v = 1.45
    elif hw == 'steps':
         v = 1.35
    surf = wt.get('surface','')
if surf in {'asphalt','concrete','paved'}:
     elif surf in {'compacted','fine_gravel'}:
        v *= 0.8
         v *= 0.9
         width = float(wt.get('width', 'nan'))
          if width and width < 1.5:
              v *= 0.92
    t = dist / max(v, 0.5)
    if hw == 'steps':
    if nt.get('highway') == 'elevator' or wt.get('highway') == 'elevator':
    t += 20.0 # average wait
    # movement within elevator is negligible for distance scales here
    crossing = nt.get('crossing')
if (nt.get('highway') == 'traffic_signals'):
    elif nt.get('highway') == 'crossing' or crossing:
   if crossing == 'zebra' or nt.get('crossing:markings') == 'zebra':
              t += 6.0
          elif crossing == 'uncontrolled' or crossing == 'no_signals':
          elif crossing == 'island' or crossing == 'refuge_island':
              t += 6.0
    # shared with bicycles and not segregated can slow slightly
if hw in {'path', 'footway'} and wt.get('bicycle') in {'yes', 'designated'} and wt.get('segregated') == 'no':
    t *= 1.03
    return t
```

Admissible heuristics (paired to profile):

```
def _haversine(n1: Node, n2: Node) -> float:
    R = 6371000.0
    lat1, lon1 = math.radians(n1.lat), math.radians(n1.lon)
    lat2, lon2 = math.radians(n2.lat), math.radians(n2.lon)
    dlat, dlon = lat2-lat1, lon2-lon1
    a = math.sin(dlat/2)**2 + math.cos(lat1)*math.cos(lat2)*math.sin(dlon/2)**2
    return 2*R*math.asin(math.sqrt(a))

def _heuristic_distance(self, nid: str, tid: str) -> float:
    return self._haversine(self.nodes[nid], self.nodes[tid])

def _heuristic_time(self, nid: str, tid: str) -> float:
    return self._heuristic_distance(nid, tid) / 1.6 # m/s (upper-bound speed)
```

5) Bidirectional A*

```
def bidir_astar(self, start: str, goal: str, profile: str, is_night=False) -> Optional[PathResult]:
       if start == goal:
    return self._calc_stats([start], profile, is_night)
if start not in self.graph or goal not in self.graph:
       # Select edge cost
def edge_cost(e, u):
             ideg_cost(e, u):
if profile == 'shortest': return self._cost_shortest(e, u)
if profile == 'few_traffic_lights': return self._cost_few_traffic_lights(e, u)
if profile == 'safest': return self._cost_safest(e, u, is_night)
if profile == 'fastest': return self._cost_fastest(e, u)
              return self._cost_shortest(e, u)
       # Heuristics: keep admissible for each profile
def hF(n): # forward heuristic to goal
  if profile == 'fastest':
                     return self._heuristic_time(n, goal)
              if profile == 'few_traffic_lights':
    return 0.95 * self._few_traffic_lights_cfg['distance_factor'] * self._heuristic_distance(n, goal)
return self._heuristic_distance(n, goal)
       def hB(n): # backward heuristic to start
   if profile == 'fastest':
                    return self._heuristic_time(n, start)
             if profile == 'few_traffic_lights':
    return 0.95 * self._few_traffic_lights_cfg['distance_factor'] * self._heuristic_distance(n, start)
return self._heuristic_distance(n, start)
      gF = {start: 0.0}
gB = {goal: 0.0}
      predF = {start: None}
predB = {goal: None}
      preus = {goal. None}
openF = [(hF(start), 0.0, start)] # (f, g, node)
openB = [(hB(goal), 0.0, goal)]
closedF = set()
closedB = set()
      UB = float('inf')
meet = None # ('node', m) or ('edge', u, v)
forward_expanded = 0
       backward_expanded = 0
       forward_edges_scanned = 0
backward edges scanned = 0
```

```
# return current min f, skipping stale
while pq and (pq[0][1] > (gF.get(pq[0][2], float('inf')) if pq is openF else gB.get(pq[0][2], float('inf')))):
     heapq.heappop(pq)
return pq[0][0] if pq else float('inf')
def improve_UB_via_node(u):
    nonlocal UB, meet
    if u in gF and u in gB:
          val = gF[u] + gB[u]
if val < UB:</pre>
                UB = val
meet = ('node', u)
def relax_dir(u, g_u, graph_dir, g_here, g_other, pred_here, h_here, open_here, is_forward: bool):
      nonlocal forward_edges_scanned, backward_edges_scanned
     for e in graph_dir.get(u, []):
    if is_forward:
               forward_edges_scanned += 1
                backward_edges_scanned += 1
          v = e['to_node']
          c = edge_cost(e, u)
if c < 0:
    continue # safety</pre>
          tentative = g_u + c

if tentative < g_here.get(v, float('inf')):

g_here[v] = tentative

pred_here[v] = u
                 f = tentative + h_here(v)
                heapq.heappush(open_here, (f, tentative, v))
           if v in g_other:
                cand = tentative + g_other[v]
if cand < UB:</pre>
```

```
while openF or openB:
    if top_key(openF) <= top_key(openB):</pre>
       # Forward step
f_u, g_u, u = heapq.heappop(openF)
       if u in closedF:
        if g_u != gF.get(u, float('inf')):
           stale_pops_f += 1
       closedF.add(u)
        forward_expanded += 1
        improve_UB_via_node(u)
       relax_dir(u, g_u, self.graph, gF, gB, predF, hF, openF, True)
       f_u, g_u, u = heapq.heappop(openB)
       if u in closedB:
        if g_u != gB.get(u, float('inf')):
           stale_pops_b += 1
       closedB.add(u)
        backward_expanded += 1
        improve_UB_via_node(u)
        relax_dir(u, g_u, self.rgraph, gB, gF, predB, hB, openB, False)
   if (top_key(openF) + top_key(openB)) >= UB:
   return None
def build_forward_path_to(u):
    while predF[seq[-1]] is not None:
      seq.append(predF[seq[-1]])
    seq.reverse()
```

```
def build_forward_path_from_using_B(v):
    seq = [v]
    cur = v
    while cur in predB and predB[cur] is not None:
       nxt = predB[cur]
        seq.append(nxt)
if meet[0] == 'node':
   m = meet[1]
    path = build_forward_path_to(m)
    tail = build_forward_path_from_using_B(m)
   path += tail[1:] # skip duplicate m
   u, v = meet[1], meet[2] # forward edge u->v
    head = build_forward_path_to(u)
   mid_tail = build_forward_path_from_using_B(v) # starts with v
   path = head + mid_tail # includes u->v
pr = self._calc_stats(path, profile, is_night)
pr.nodes_expanded_forward = forward_expanded
pr.nodes_expanded_backward = backward_expanded
pr.edges_scanned_forward = forward_edges_scanned
pr.edges_scanned_backward = backward_edges_scanned
pr.stale_pops_forward = stale_pops_f
pr.stale_pops_backward = stale_pops_b
return pr
```

6) Uniform metric computation (comparable times across profiles)

```
def _calc_stats(self, path: List[str], profile: str, is_night: bool) -> PathResult:
    dist = 0.0; sig = 0; cross = 0; safepen = 0.0; cost = 0.0; tsec = 0.0
    for i in range(len(path)-1):
       u, v = path[i], path[i+1]
       edge = next((e for e in self.graph[u] if e['to_node'] == v), None)
       if not edge: # fallback (shouldn't happen)
       dist += edge['distance']
       if profile == 'shortest':
          c = self._cost_shortest(edge, u)
       elif profile == 'few traffic lights':
           c = self._cost_few_traffic_lights(edge, u)
       elif profile == 'safest':
           c = self._cost_safest(edge, u, is_night)
       elif profile == 'fastest':
           c = self._cost_fastest(edge, u)
           c = self._cost_shortest(edge, u)
       cost += c
       safepen += self._cost_safest(edge, u, is_night) - edge['distance']
       tsec += self._cost_fastest(edge, u)
       nt = self.nodes[v].tags
       if nt.get('highway') == 'traffic_signals' or nt.get('crossing') == 'traffic_signals':
       elif nt.get('highway') == 'crossing' or ('crossing' in nt):
           cross += 1
   descr = {
        'shortest': 'shortest path',
        'few_traffic_lights': 'few_traffic_lights path',
        'fastest': 'fastest path',
    }[profile]
   return PathResult(
       path=path, total_cost=cost, distance_meters=dist,
       num_traffic_signals=sig, num_crossings=cross,
       safety_penalties=safepen, time_seconds=tsec,
       description=descr
```