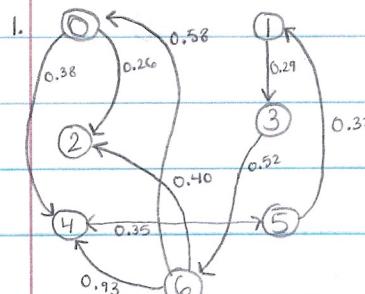
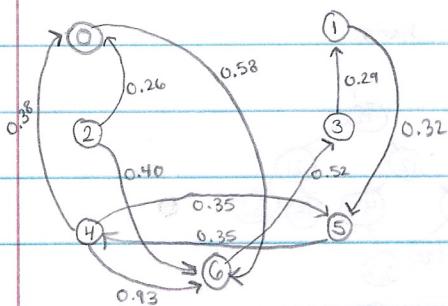


### Review Exercise 4



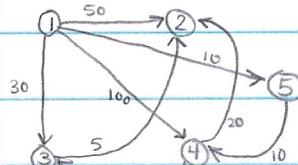
| From: | 1         | 2         | 3         | 4         | 5         | 6         |
|-------|-----------|-----------|-----------|-----------|-----------|-----------|
| 0     | $\infty$  | 0.26<br>0 | $\infty$  | 0.38<br>0 | $\infty$  | $\infty$  |
| 2     | $\infty$  | 0.26<br>0 | $\infty$  | 0.38<br>0 | $\infty$  | $\infty$  |
| 4     | $\infty$  | 0.26<br>0 | $\infty$  | 0.38<br>0 | 0.73<br>4 | $\infty$  |
| 5     | 1.05<br>5 | 0.26<br>0 | $\infty$  | 0.38<br>0 | 0.73<br>4 | $\infty$  |
| 1     | 1.05<br>5 | 0.26<br>0 | 1.34<br>1 | 0.38<br>0 | 0.73<br>4 | $\infty$  |
| 3     | 1.05<br>5 | 0.26<br>0 | 1.34<br>1 | 0.38<br>0 | 0.73<br>4 | 1.86<br>3 |

### Reverse Order



| From | 0         | 1         | 2        | 3         | 4         | 5         | 6         |
|------|-----------|-----------|----------|-----------|-----------|-----------|-----------|
| 2    | 0.26<br>2 | $\infty$  | $\infty$ | $\infty$  | $\infty$  | $\infty$  | 0.40<br>2 |
| 0    | 0.26<br>2 | $\infty$  | $\infty$ | $\infty$  | $\infty$  | $\infty$  | 0.40<br>2 |
| 6    | 0.26<br>2 | $\infty$  | $\infty$ | 0.92<br>6 | $\infty$  | $\infty$  | 0.40<br>2 |
| 3    | 0.26<br>2 | 1.21<br>3 | $\infty$ | 0.92<br>6 | $\infty$  | $\infty$  | 0.40<br>2 |
| 1    | 0.26<br>2 | 1.21<br>3 | $\infty$ | 0.92<br>6 | $\infty$  | 1.53<br>1 | 0.40<br>2 |
| 5    | 0.26<br>2 | 1.21<br>3 | $\infty$ | 0.92<br>6 | 1.88<br>5 | 1.53<br>1 | 0.40<br>2 |

2.

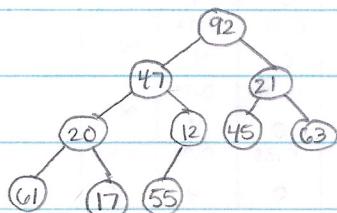


| From: | 1        | 2       | 3       | 4       | 5  |
|-------|----------|---------|---------|---------|----|
| 1     | $\infty$ | 50      | 30      | 100     | 10 |
| 5     | $\infty$ | 1       | 1       | 1       | 1  |
| 4     | $\infty$ | 40<br>1 | 30<br>1 | 20<br>5 | 10 |
| 2     | $\infty$ | 35<br>3 | 30<br>1 | 20<br>5 | 10 |

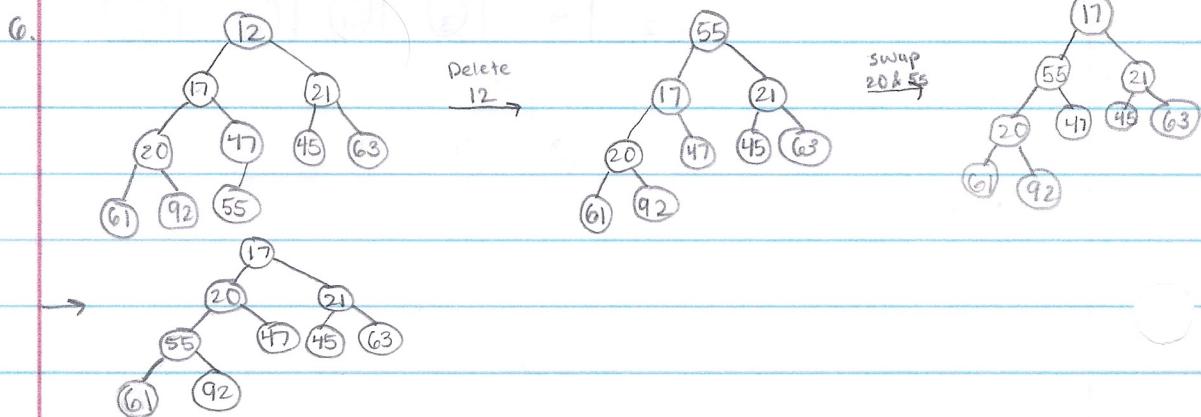
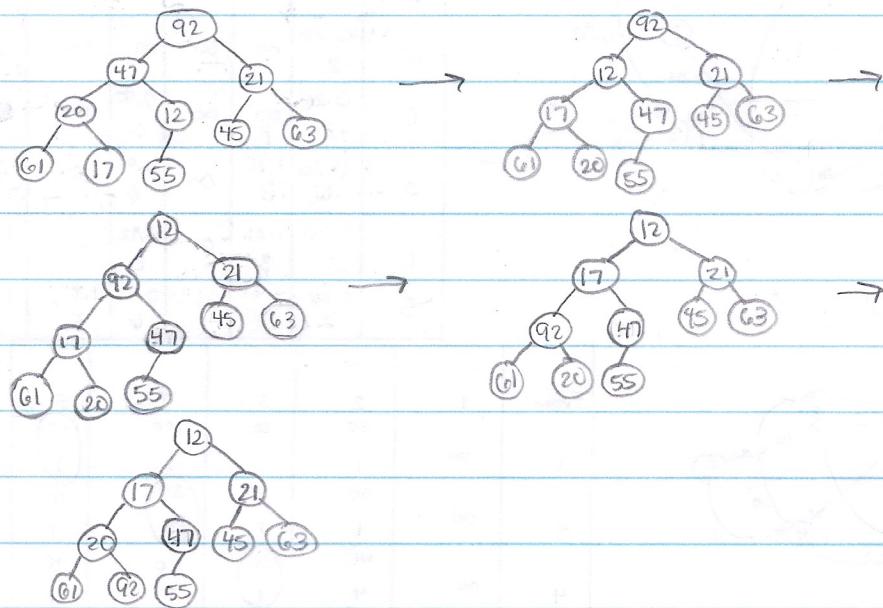
### 3. Structure-Property and Heap Order Property

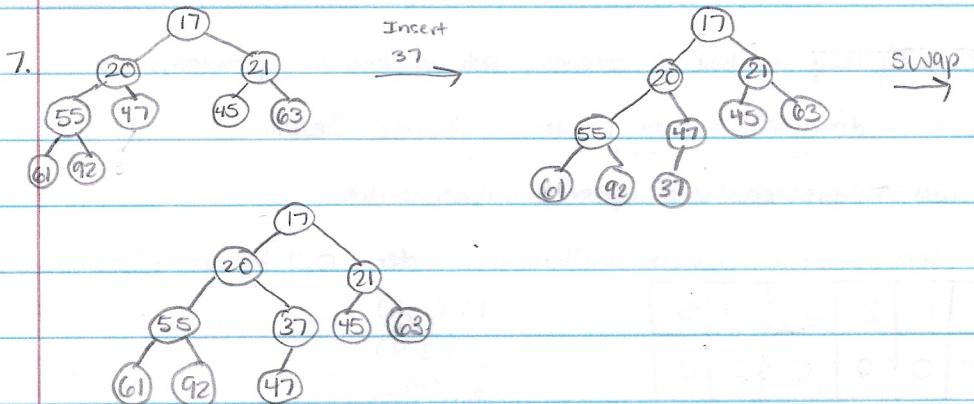
4.

|   |    |    |    |    |    |    |    |    |    |    |
|---|----|----|----|----|----|----|----|----|----|----|
|   | 92 | 47 | 21 | 20 | 12 | 45 | 63 | 61 | 17 | 55 |
| 0 | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 |



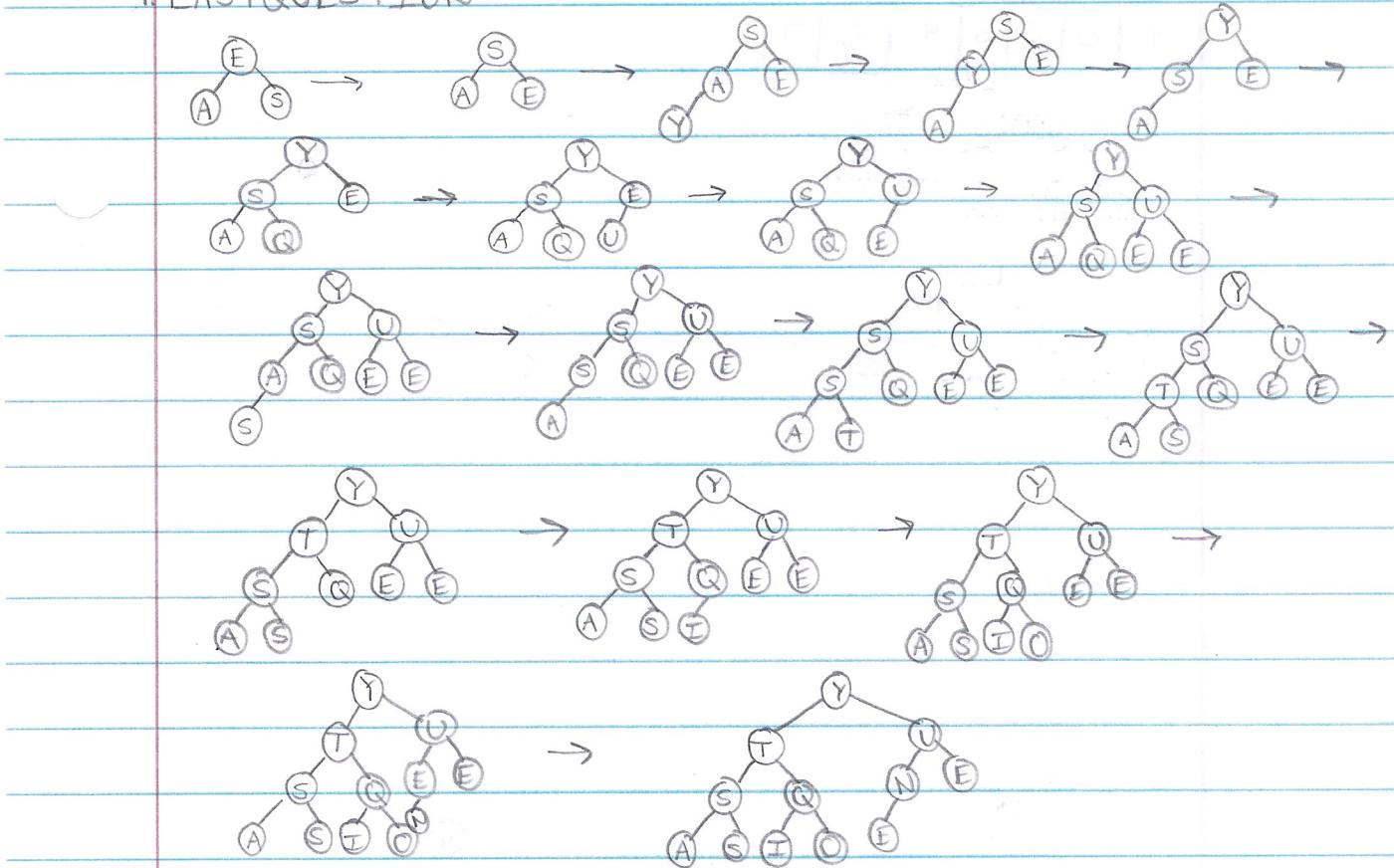
5. No, the resulting tree in problem 4 is not a heap.





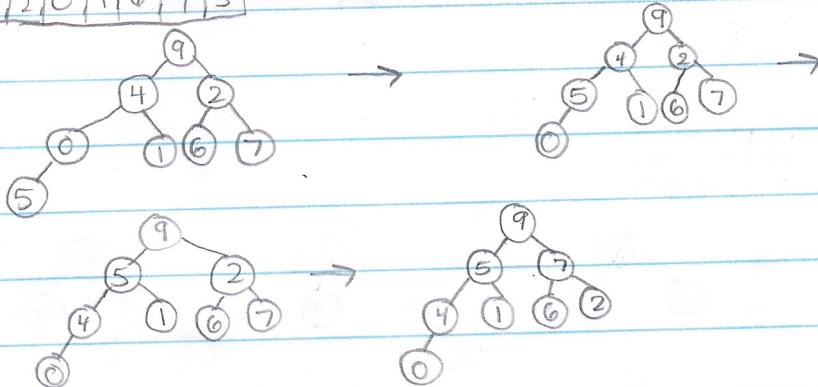
8. Yes, an array in decreasing order is considered a max-oriented heap.

9. EASY QUESTION



Heapsort Exercise

10. 9 4 2 0 1 6 7 5



① 9 5 7 4 1 6 2 0

0 5 7 4 1 6 2 9

② 7 5 6 4 1 0 2 9

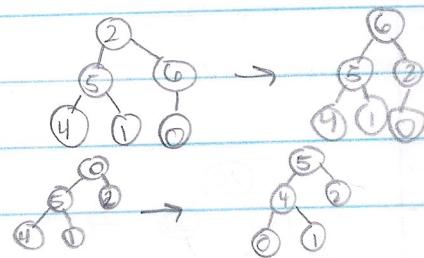
2 5 6 4 1 0 7 9

③ 6 5 2 4 1 0 7 9

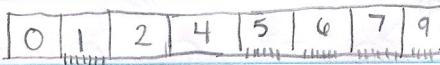
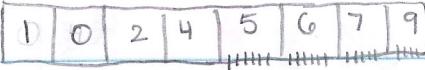
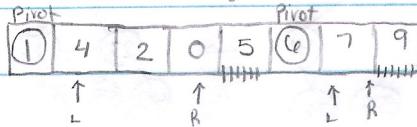
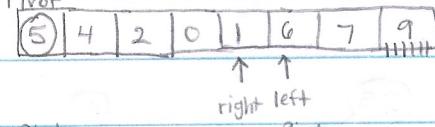
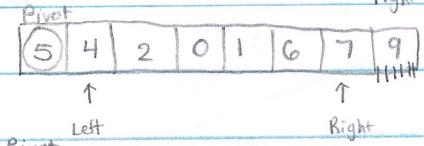
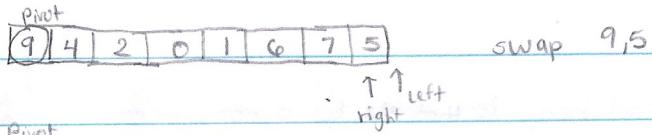
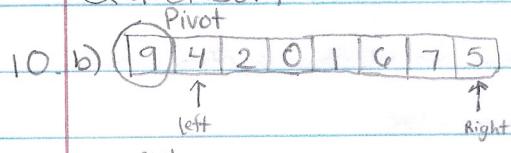
0 5 2 4 1 6 7 9

④ 5 4 2 0 1 6 7 9

1 4 2 0 5 6 7 9



## Quicksort



11. DP is commonly used method of optimally solving complex problems by breaking them down into simpler problems ; Richard Bellman.

12. Overlapping subproblems and optimal substructures

13. Fibonacci series, optimal matrix multiplication order, 0/1 knapsack problem

| H | W | 0 | 1 | 2 | 3 | 4 | 5 |                      |
|---|---|---|---|---|---|---|---|----------------------|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1: (2,3)             |
| 1 | 0 | 0 | 3 | 3 | 3 | 3 | 3 | 2: (3,4)<br>3: (4,5) |
| 2 | 0 | 0 | 3 | 4 | 4 | 4 | 7 | 4: (5,6)             |
| 3 | 0 | 0 | 3 | 4 | 5 | 5 | 7 |                      |
| 4 | 0 | 0 | 3 | 4 | 5 | 5 | 7 |                      |