

1. More on Boolean function forms

a. Boolean function from last time

- i. True when either, but not both, of the first two variables is true
- ii. Truth table below

Index	A	B	C	f(A, B, C)	Minterm	Maxterm
0	0	0	0	0	$m_0 = \overline{A}\overline{B}\overline{C}$	$M_0 = A + B + C$
1	0	0	1	0	$m_1 = \overline{A}\overline{B}C$	$M_1 = A + B + \overline{C}$
2	0	1	0	1	$m_2 = \overline{A}B\overline{C}$	$M_2 = A + \overline{B} + C$
3	0	1	1	1	$m_3 = \overline{A}BC$	$M_3 = A + \overline{B} + \overline{C}$
4	1	0	0	1	$m_4 = A\overline{B}\overline{C}$	$M_4 = \overline{A} + B + C$
5	1	0	1	1	$m_5 = A\overline{B}C$	$M_5 = \overline{A} + B + \overline{C}$
6	1	1	0	0	$m_6 = AB\overline{C}$	$M_6 = \overline{A} + \overline{B} + C$
7	1	1	1	0	$m_7 = ABC$	$M_7 = \overline{A} + \overline{B} + \overline{C}$

b. Sum-of-products

- i. $f = \overline{A}B\overline{C} + \overline{A}BC + A\overline{B}\overline{C} + A\overline{B}C = m_2 + m_3 + m_4 + m_5$
- ii. Can simplify using equivalence laws to reduce number of gates

c. Product-of-sums

- i. Can also simplify using laws of equivalence

2. Karnaugh maps

a. Hamming distance

		AB			
		00	01	11	10
C	0	0	0	d	0
	1	1	0	d	0

Three variable Karnaugh map

		AB			
		00	01	11	10
CD	00	0	0	0	1
	01	1	1	0	1
	11	d	0	d	0
	10	d	0	d	0

Four variable Karnaugh map

3. Terminology

a. Literal

b. Don't cares

c. Implicant

d. Prime implicant

i. Essential prime implicant

e. Cover

f. Cost of a circuit

4. Minimization

a. Generate all prime implicants

b. Eliminate prime implicants that overlap until you find the essential implicants

5. Examples

a. $f_1 = m0 + m1 + m4 + m5 + m7 = \Sigma(0, 1, 4, 5, 7)$

		<i>AB</i>			
		00	01	11	10
<i>C</i>	0				
	1				

b. $f_2 = \Sigma(6, 8, 9, 10, 11, 12, 13, 14)$

		<i>AB</i>			
		00	01	11	10
<i>CD</i>	00				
	01				
	11				
	10				

c. Further example with don't cares and wrapping

i. $f_3 = m0 + D2 + D5 + D7 + m8 + m10$

		<i>AB</i>			
		00	01	11	10
<i>CD</i>	00				
	01				
	11				
	10				

d. Whether or not don't cares are included depends on your desired use case