

1. More on CLAs

a. $C_{i+1} = G_i + P_i C_i$, where C is the carry

i. $G_i = A_i B_i$, $P_i = A_i \oplus B_i$

ii. Can expand this out

1. $C_1 = G_0 + P_0 * C_0$

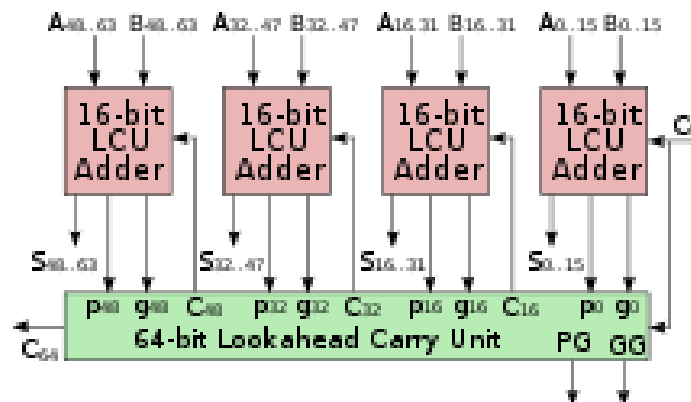
2. $C_2 = G_1 + P_1 * C_1 = G_1 + P_1 * (G_0 + P_0 * C_0) = G_1 + P_1 * G_0 + P_1 * P_0 * C_0$

3. $C_3 = G_2 + P_2 * C_2 = G_2 + P_2 * (G_1 + P_1 * C_1) = G_2 + P_2 * (G_1 + P_1 * (G_0 + P_0 * C_0))$
 $= G_2 + (P_2 * G_1) + (P_2 * P_1 * G_0) + (P_2 * P_1 * P_0 * C_0)$

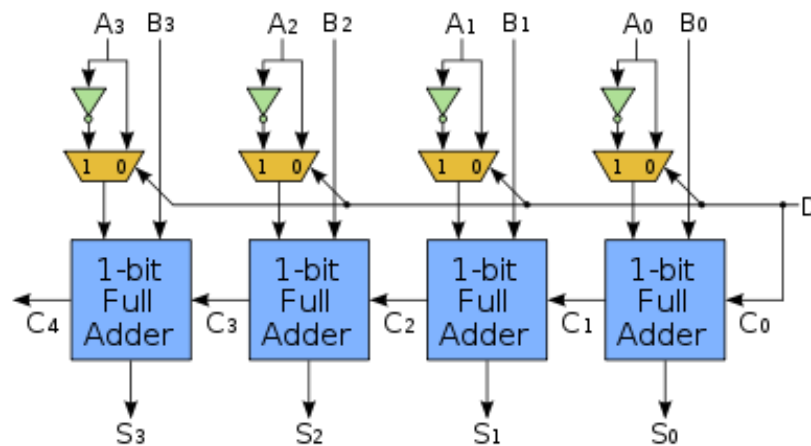
4. $C_4 = G_3 + P_3 * C_3 = G_3 + P_3 * G_2 + (P_3 * P_2 * G_1) + (P_3 * P_2 * P_1 * G_0) + (P_3 * P_2 * P_1 * P_0 * C_0)$

b. Process

c. Can expand this 4-bit adder to further levels, like a 64-bit unit



2. Subtractors



3. Comparators

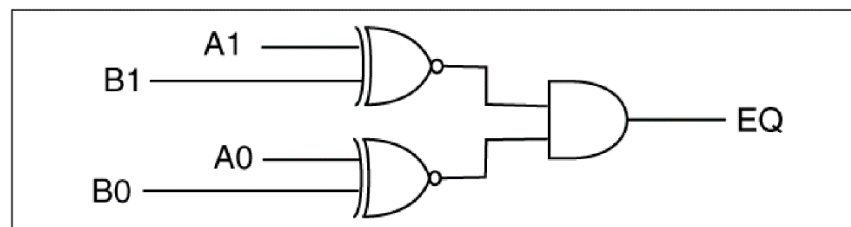


Figure 11.10: The final circuit for the 2-bit comparator as equation (e) in Figure 11.9.

4. Arithmetic logic unit (ALU)

- a. Each cell of the ALU has one of each type of gate in it

5. Error detection and correction

- a. Error types
 - b. Will focus on errors that involve bits changing value
 - c. Measure of size of error
- d. Three possible outcomes
- e. Will look at SECDED

6. Parity

a. Errors with a Hamming distance of 1

b. *Even parity*

i. *Odd parity*

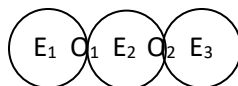
ii. Example for even parity

1. C denotes the position of the check bit

2. C1001 ->

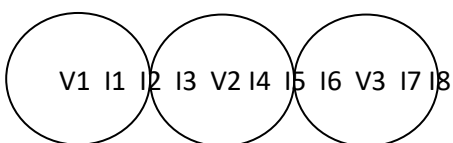
3. C1101 ->

iii. Even parity creates valid code words



Circles have a radius of one Hamming distance.

c. Two bit errors



Circles have a radius of two Hamming distance.