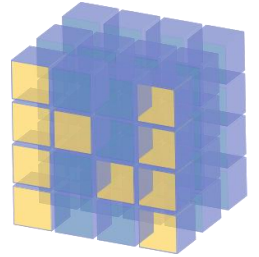


NumPy

# NumPy



- Numerical Python
- Modul/library yang berisi fungsi-fungsi matematis dan saintifik
- Merupakan library yang “wajib”
- Digunakan oleh beberapa library yang lain: scikit-learn, Pandas, OpenCV, dll
- Instalasi (via command prompt): `pip install numpy`

# Import module NumPy

```
import numpy as np
```

# Membuat dan Mencetak Array NumPy

```
a = np.array([1, 2, 3])
```

```
b = np.zeros(5)
```

```
c = np.ones(5)
```

```
d = np.arange(5)
```

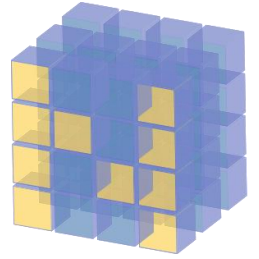
```
print(a) # [1, 2, 3]
```

```
print(b) # [0. 0. 0. 0. 0. ]
```

```
print(c) # [1. 1. 1. 1. 1.]
```

```
print(d) # [0 1 2 3 4]
```

# Array Python dan NumPy



- Array Numpy berbeda dengan array Python
- Array NumPy lebih baik dalam hal ukuran data, kecepatan, dan fungsionalitas

# Array Python dan NumPy

```
# Array Python
```

```
a = [1, 2, 3]
```

```
# Array NumPy
```

```
b = np.array([1, 2, 3])
```

```
print(type(a))
```

```
# <class 'list'>
```

```
print(type(b))
```

```
# <class 'numpy.ndarray'>
```

# Properti Array NumPy

```
a = np.array([1, 2, 3])
```

```
print(a.size)
```

```
# 3
```

```
print(a.shape)
```

```
# (3,)
```

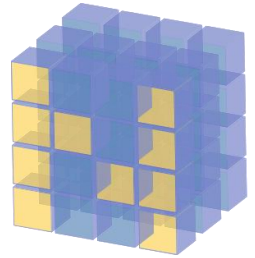
```
print(a.ndim)
```

```
# 1
```

```
print(a.dtype)
```

```
# int32
```

# Tipe Data



- Tipe data pada suatu array NumPy harus sama/seragam
- Beberapa tipe data yang tersedia di NumPy: `bool`, `int8`, `int16`, `int32`, `int64`, `uint8`, `uint16`, `uint32`, `uint64`, `float16`, `float32`, `float64`, `complex64`, `complex128`



# Menentukan Tipe Data

```
a = np.array([1, 2, 3], np.uint8)
```

```
print(a.dtype)
```

```
# uint8
```

# Mengubah Tipe Data

```
a = a.astype(np.int32)
```

```
print(a.dtype)
```

```
# int32
```

# Operasi Aritmetik

```
a = np.array([1, 2, 3])  
b = np.zeros(a.shape)
```

```
# Dengan perulangan  
for i in range(a.size):  
    b[i] = a[i] + 1
```

```
print(b)  
# [2 3 4]
```

# Operasi Aritmetik

```
a = np.array([1, 2, 3])
```

```
b = a + 1  
# [2 3 4]
```

```
c = a - 1  
# [0 1 2]
```

```
d = a * 3  
# [2 4 6]
```

# Operasi Aritmetik

```
e = a / 2  
# [0.5 1 1.5]
```

```
f = a // 2  
# [0 1 1]
```

```
g = a ** 2  
# [1 4 9]
```

# Statistik

```
a = np.arange(11, 21)  
# [11 12 13 14 15 16 17 18 19 20]
```

```
print(np.mean(a))  
# 15.5
```

```
print(np.var(a))  
# 8.25
```

```
print(np.std(a))  
# 2.8722813232690143
```

# Statistik

```
print(np.sum(a))  
# 155
```

```
# Peak-to-peak (max-min)  
print(np.ptp(a))  
# 9
```

# Histogram

```
a = np.random.randint(0, 10, 20)
# [7 4 9 5 3 5 8 3 1 3 7 1 6 5 7 9 3 3 1 0]

hist = np.histogram(a)[0]

print(hist)
# [3 2 3 3 1 0 0 3 2 3]
```



# Pengurutan

```
a = np.random.randint(0, 10, 20)
# [7 4 9 5 3 5 8 3 1 3 7 1 6 5 7 9 3 3 1 0]

print(np.sort(a))
# [0 1 1 1 3 3 3 3 3 4 5 5 5 6 7 7 7 8 9 9]
```

# Memotong Array

```
a = np.arange(11, 21)
```

| Indeks | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|--------|----|----|----|----|----|----|----|----|----|----|
| Nilai  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |

# Memotong Array

```
print(a[2:5])  
# [13 14 15]
```

|        |    |    |    |    |    |    |    |    |    |    |
|--------|----|----|----|----|----|----|----|----|----|----|
| Indeks | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| Nilai  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |

# Memotong Array

```
print(a[:5])  
# [11 12 13 14 15]
```

|        |    |    |    |    |    |    |    |    |    |    |
|--------|----|----|----|----|----|----|----|----|----|----|
| Indeks | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| Nilai  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |

# Memotong Array

```
print(a[5:])  
# [16 17 18 19 20]
```

| Indeks | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
|--------|----|----|----|----|----|----|----|----|----|----|
| Nilai  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |

# Memotong Array

```
print(a[:-1])
```

```
# [11 12 13 14 15 16 17 18 19]
```

|        |    |    |    |    |    |    |    |    |    |    |
|--------|----|----|----|----|----|----|----|----|----|----|
| Indeks | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| Nilai  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |

# Memotong Array

```
print(a[2:7:2])  
# [13 15 17]
```

|        |    |    |    |    |    |    |    |    |    |    |
|--------|----|----|----|----|----|----|----|----|----|----|
| Indeks | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| Nilai  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |

# Memotong Array

```
idx = [1, 4, 8]
```

```
print(a[idx])  
# [12 15 19]
```

|        |    |    |    |    |    |    |    |    |    |    |
|--------|----|----|----|----|----|----|----|----|----|----|
| Indeks | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  |
| Nilai  | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |



# Bantuan

```
np.info(np.mean)
```

```
mean(a, axis=None, dtype=None, out=None, keepdims=<no value>)
```

Compute the arithmetic mean along the specified axis.

Returns the average of the array elements. The average is taken over

the flattened array by default, otherwise over the specified axis.

`float64` intermediate and return values are used for integer inputs.

...

**Matriks**

# Membuat Matriks

```
A = np.array([[11, 12, 13, 14],  
              [15, 16, 17, 18],  
              [19, 20, 21, 22],  
              [23, 24, 25, 26]])
```

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <b>11</b> | <b>12</b> | <b>13</b> | <b>14</b> |
| <b>15</b> | <b>16</b> | <b>17</b> | <b>18</b> |
| <b>19</b> | <b>20</b> | <b>21</b> | <b>22</b> |
| <b>23</b> | <b>24</b> | <b>25</b> | <b>26</b> |

# Membuat Matriks

```
A = np.arange(11, 27).reshape(4, 4)
```

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <b>11</b> | <b>12</b> | <b>13</b> | <b>14</b> |
| <b>15</b> | <b>16</b> | <b>17</b> | <b>18</b> |
| <b>19</b> | <b>20</b> | <b>21</b> | <b>22</b> |
| <b>23</b> | <b>24</b> | <b>25</b> | <b>26</b> |

# Membuat Matriks

```
B = np.zeros((4, 4), dtype=np.int8)
```

|   |   |   |   |
|---|---|---|---|
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

# Membuat Matriks

```
C = np.ones((4, 4), dtype=np.int8)
```

|          |          |          |          |
|----------|----------|----------|----------|
| <b>1</b> | <b>1</b> | <b>1</b> | <b>1</b> |
| <b>1</b> | <b>1</b> | <b>1</b> | <b>1</b> |
| <b>1</b> | <b>1</b> | <b>1</b> | <b>1</b> |
| <b>1</b> | <b>1</b> | <b>1</b> | <b>1</b> |

# Membuat Matriks

```
D = np.full((4, 4), 5, dtype=np.int8)
```

|   |   |   |   |
|---|---|---|---|
| 5 | 5 | 5 | 5 |
| 5 | 5 | 5 | 5 |
| 5 | 5 | 5 | 5 |
| 5 | 5 | 5 | 5 |

# Properti Matrix

```
print(A.ndim)  
# 2
```

```
print(A.shape)  
# (4, 4)
```

```
h, w = A.shape
```

```
print(A.size)  
# 16
```



# Transpose Matriks

$$E = A.T$$

|    |    |    |    |
|----|----|----|----|
| 11 | 12 | 13 | 14 |
| 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 |
| 23 | 24 | 25 | 26 |



|    |    |    |    |
|----|----|----|----|
| 11 | 15 | 19 | 23 |
| 12 | 16 | 20 | 24 |
| 13 | 17 | 21 | 25 |
| 14 | 18 | 22 | 26 |

# Determinan Matriks

```
F = np.arange(2, 6).reshape(2, 2)
```

```
print(F)  
# [[2 3]  
   [4 5]]
```

```
print(np.linalg.det(F))  
# -2.0
```

# Eigenvalue dan Eigenvector

```
F = np.arange(2, 6).reshape(2, 2)
```

```
print(F)  
# [[2 3]  
   [4 5]]
```

```
print(np.linalg.eig(F))  
# (array([-0.27491722,  7.27491722]),  
   array([[ -0.79681209, -0.49436913],  
          [ 0.60422718, -0.86925207]]))
```

# Operasi Matriks

```
G = np.empty(A.shape, A.dtype)
h, w = G.shape
```

```
# Dengan perulangan
for y in range(h):
    for x in range(w):
        G[y, x] = A[y, x] + 2
```

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 |

# Operasi Matriks

$$H = A + 2$$

|    |    |    |    |
|----|----|----|----|
| 11 | 12 | 13 | 14 |
| 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 |
| 23 | 24 | 25 | 26 |



|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 |

# Operasi Matriks

$$I = A - 2$$

|    |    |    |    |
|----|----|----|----|
| 11 | 12 | 13 | 14 |
| 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 |
| 23 | 24 | 25 | 26 |



|    |    |    |    |
|----|----|----|----|
| 9  | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 |

# Operasi Matriks

$$J = A * 2$$

|    |    |    |    |
|----|----|----|----|
| 11 | 12 | 13 | 14 |
| 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 |
| 23 | 24 | 25 | 26 |



|    |    |    |    |
|----|----|----|----|
| 22 | 24 | 26 | 28 |
| 30 | 32 | 34 | 36 |
| 38 | 40 | 42 | 44 |
| 46 | 48 | 50 | 52 |

# Operasi Matriks

$$K = A / 2$$

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| <b>11</b> | <b>12</b> | <b>13</b> | <b>14</b> |
| <b>15</b> | <b>16</b> | <b>17</b> | <b>18</b> |
| <b>19</b> | <b>20</b> | <b>21</b> | <b>22</b> |
| <b>23</b> | <b>24</b> | <b>25</b> | <b>26</b> |



|             |            |             |            |
|-------------|------------|-------------|------------|
| <b>5.5</b>  | <b>6.</b>  | <b>6.5</b>  | <b>7.</b>  |
| <b>7.5</b>  | <b>8.</b>  | <b>8.5</b>  | <b>9.</b>  |
| <b>9.5</b>  | <b>10.</b> | <b>10.5</b> | <b>11.</b> |
| <b>11.5</b> | <b>12.</b> | <b>12.5</b> | <b>13.</b> |



# Operasi Matriks

# Element-wise product

$$L = A * E$$

|    |    |    |    |
|----|----|----|----|
| 11 | 12 | 13 | 14 |
| 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 |
| 23 | 24 | 25 | 26 |

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 |

|     |     |     |     |
|-----|-----|-----|-----|
| 143 | 168 | 195 | 224 |
| 255 | 288 | 323 | 360 |
| 399 | 440 | 483 | 528 |
| 575 | 624 | 675 | 728 |

# Operasi Matriks

# Matrix product

$$M = A @ E$$

|    |    |    |    |
|----|----|----|----|
| 11 | 12 | 13 | 14 |
| 15 | 16 | 17 | 18 |
| 19 | 20 | 21 | 22 |
| 23 | 24 | 25 | 26 |

|    |    |    |    |
|----|----|----|----|
| 13 | 14 | 15 | 16 |
| 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 |
| 25 | 26 | 27 | 28 |

|      |      |      |      |
|------|------|------|------|
| 970  | 1020 | 1070 | 1120 |
| 1274 | 1340 | 1406 | 1472 |
| 1578 | 1660 | 1742 | 1824 |
| 1882 | 1980 | 2078 | 2176 |

# Memotong Matriks

```
N = A[1:3, :]
```

```
N = A[1:3]
```

```
print(N)
```

```
# [[15 16 17 18]
```

```
#  [19 20 21 22]]
```

|   | 0  | 1  | 2  | 3  |
|---|----|----|----|----|
| 0 | 11 | 12 | 13 | 14 |
| 1 | 15 | 16 | 17 | 18 |
| 2 | 19 | 20 | 21 | 22 |
| 3 | 23 | 24 | 25 | 26 |

# Memotong Matriks

```
0 = A[1:]
```

```
print(0)
```

```
# [[15 16 17 18]
```

```
#  [19 20 21 22]
```

```
#  [23 24 25 26]]
```

|   | 0  | 1  | 2  | 3  |
|---|----|----|----|----|
| 0 | 11 | 12 | 13 | 14 |
| 1 | 15 | 16 | 17 | 18 |
| 2 | 19 | 20 | 21 | 22 |
| 3 | 23 | 24 | 25 | 26 |

# Memotong Matriks

```
P = A[1:, 1:3]
```

```
print(P)
```

```
# [[16 17]
```

```
#  [20 21]
```

```
#  [24 25]]
```

|   | 0  | 1  | 2  | 3  |
|---|----|----|----|----|
| 0 | 11 | 12 | 13 | 14 |
| 1 | 15 | 16 | 17 | 18 |
| 2 | 19 | 20 | 21 | 22 |
| 3 | 23 | 24 | 25 | 26 |

# Memotong Matriks

```
Q = A[:, 1:3]
```

```
print(Q)
```

```
# [[16 17]
```

```
#  [20 21]
```

```
#  [24 25]]
```

|   | 0  | 1  | 2  | 3  |
|---|----|----|----|----|
| 0 | 11 | 12 | 13 | 14 |
| 1 | 15 | 16 | 17 | 18 |
| 2 | 19 | 20 | 21 | 22 |
| 3 | 23 | 24 | 25 | 26 |

# **Array 3-D**

# Membuat Array 3-D

```
A = np.arange(11, 59).reshape((4, 4, 3))
```

|    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|
|    |    |    |    | 13 | 16 | 19 | 22 |
|    |    |    |    |    |    |    |    |
|    |    |    | 12 | 15 | 18 | 21 | 34 |
|    |    |    |    |    |    |    |    |
| 11 | 14 | 17 | 20 |    | 33 |    | 46 |
| 23 | 26 | 29 | 32 |    | 45 |    | 58 |
| 35 | 38 | 41 | 44 |    | 57 |    |    |
| 47 | 50 | 53 | 56 |    |    |    |    |



# Dimensi Array 3-D

```
print(A.ndim)  
# 3
```

```
print(A.shape)  
# (4, 4, 3)
```

```
h, w = A.shape[:2]
```

```
print(A.size)  
# 48
```

# Color Channel

**B = A[:, :, 0]**

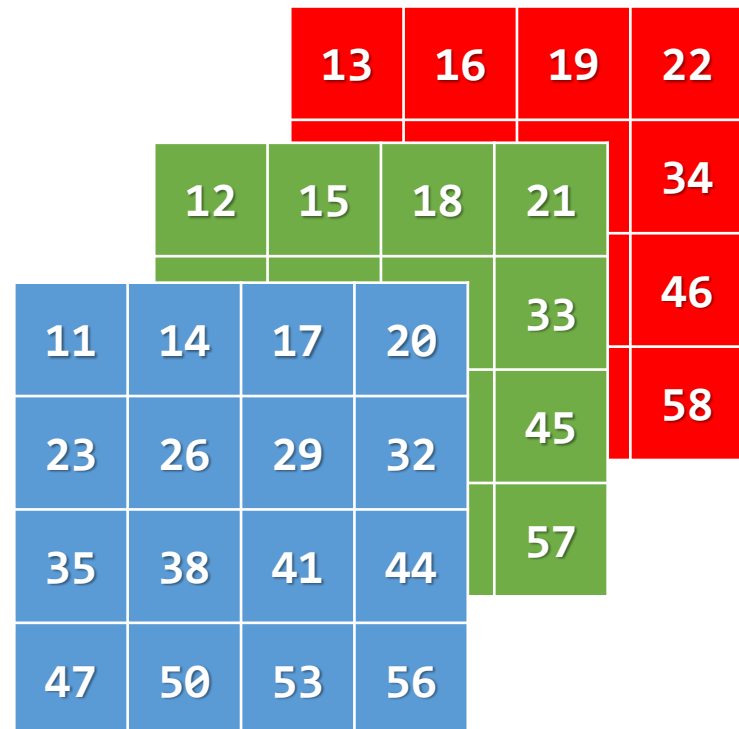
**B = A[... , 0]**

**G = A[:, :, 1]**

$$\mathbf{G} = \mathbf{A}[\dots, 1]$$

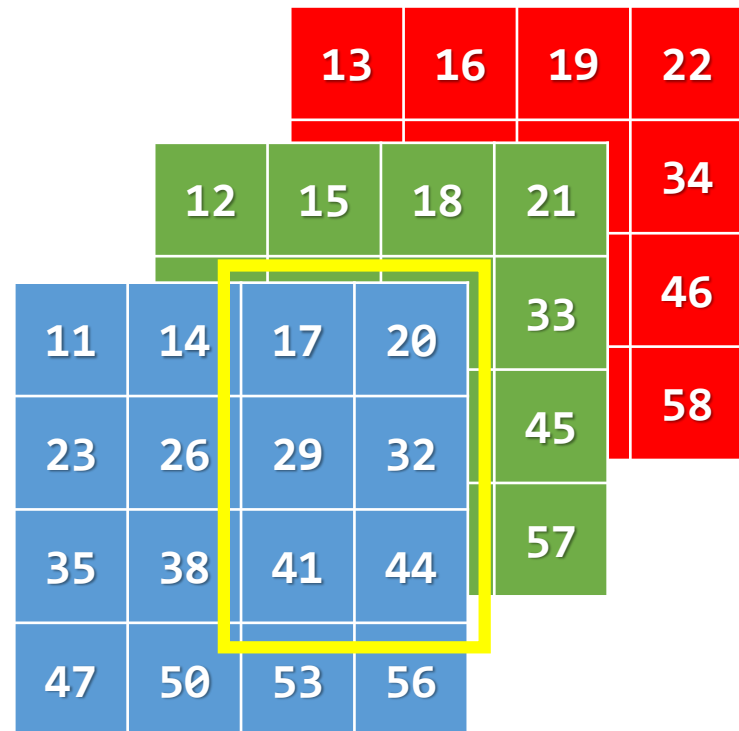
**R = A[:, :, 2]**

**R = A[... , 2]**



# Cropping

```
crop = A[:3, 2:, 0]
```



# Stack

```
stack = np.hstack((B, G, R))
```

|    |    |    |    |    |    |    |    |    |    |    |    |
|----|----|----|----|----|----|----|----|----|----|----|----|
| 11 | 14 | 17 | 20 | 12 | 15 | 18 | 21 | 13 | 16 | 19 | 22 |
| 23 | 26 | 29 | 32 | 24 | 27 | 30 | 33 | 25 | 28 | 31 | 34 |
| 35 | 38 | 41 | 44 | 36 | 39 | 42 | 45 | 37 | 40 | 43 | 46 |
| 47 | 50 | 53 | 56 | 48 | 51 | 54 | 57 | 49 | 52 | 55 | 58 |

# Stack

```
stack = np.hstack((B, G, R))
```

|    |    |    |    |
|----|----|----|----|
| 11 | 14 | 17 | 20 |
| 23 | 26 | 29 | 32 |
| 35 | 38 | 41 | 44 |
| 47 | 50 | 53 | 56 |
| 12 | 15 | 18 | 21 |
| 24 | 27 | 30 | 33 |
| 36 | 39 | 42 | 45 |
| 48 | 51 | 54 | 57 |
| 13 | 16 | 19 | 22 |
| 25 | 28 | 31 | 34 |
| 37 | 40 | 43 | 46 |
| 49 | 52 | 55 | 58 |

# Thresholding

```
th = 40  
print(B > th)  
# [[False False False False]  
#   [False False False False]  
#   [False False  True  True]  
#   [ True  True  True  True]]
```

|    |    |    |    |
|----|----|----|----|
| 11 | 14 | 17 | 20 |
| 23 | 26 | 29 | 32 |
| 35 | 38 | 41 | 44 |
| 47 | 50 | 53 | 56 |

# Thresholding

$B[B > th] = 255$

|     |     |     |     |
|-----|-----|-----|-----|
| 11  | 14  | 17  | 20  |
| 23  | 26  | 29  | 32  |
| 35  | 38  | 255 | 255 |
| 255 | 255 | 255 | 255 |

# Thresholding

$B[B > th] = 255$

$B[B \leq th] = 0$

|     |     |     |     |
|-----|-----|-----|-----|
| 0   | 0   | 0   | 0   |
| 0   | 0   | 0   | 0   |
| 0   | 0   | 255 | 255 |
| 255 | 255 | 255 | 255 |



# Thresholding

```
B = np.where(B > th, 255, 0)
```

|     |     |     |     |
|-----|-----|-----|-----|
| 0   | 0   | 0   | 0   |
| 0   | 0   | 0   | 0   |
| 0   | 0   | 255 | 255 |
| 255 | 255 | 255 | 255 |

# Brightness

```
h, w = G.shape
add = 220

for y in range(h):
    for x in range(w):
        if G[y, x] + add <= 255:
            G[y, x] += add
        else:
            G[y, x] = 255
```

|    |    |    |    |
|----|----|----|----|
| 12 | 15 | 18 | 21 |
| 24 | 27 | 30 | 33 |
| 36 | 39 | 42 | 45 |
| 48 | 51 | 54 | 57 |

|     |     |     |     |
|-----|-----|-----|-----|
| 232 | 235 | 238 | 241 |
| 244 | 247 | 250 | 253 |
| 255 | 255 | 255 | 255 |
| 255 | 255 | 255 | 255 |

# Brightness

```
h, w = G.shape  
add = 220
```

```
for y in range(h):  
    for x in range(w):  
        G[y, x] = G[y, x] + add if G[y, x] + add <= 255  
    else 255
```

|    |    |    |    |
|----|----|----|----|
| 12 | 15 | 18 | 21 |
| 24 | 27 | 30 | 33 |
| 36 | 39 | 42 | 45 |
| 48 | 51 | 54 | 57 |

|     |     |     |     |
|-----|-----|-----|-----|
| 232 | 235 | 238 | 241 |
| 244 | 247 | 250 | 253 |
| 255 | 255 | 255 | 255 |
| 255 | 255 | 255 | 255 |

# Brightness

```
h, w = G.shape  
add = 220
```

```
G[G > 255 - add] = 255  
G[G <= 255 - add] += add
```

|    |    |    |    |
|----|----|----|----|
| 12 | 15 | 18 | 21 |
| 24 | 27 | 30 | 33 |
| 36 | 39 | 42 | 45 |
| 48 | 51 | 54 | 57 |

|     |     |     |     |
|-----|-----|-----|-----|
| 232 | 235 | 238 | 241 |
| 244 | 247 | 250 | 253 |
| 255 | 255 | 255 | 255 |
| 255 | 255 | 255 | 255 |

# Brightness

```
h, w = G.shape  
add = 220
```

```
G[G > 255 - add] = 255  
G[G <= 255 - add] += add
```

|    |    |    |    |
|----|----|----|----|
| 12 | 15 | 18 | 21 |
| 24 | 27 | 30 | 33 |
| 36 | 39 | 42 | 45 |
| 48 | 51 | 54 | 57 |

|     |     |     |     |
|-----|-----|-----|-----|
| 232 | 235 | 238 | 241 |
| 244 | 247 | 250 | 253 |
| 255 | 255 | 255 | 255 |
| 255 | 255 | 255 | 255 |

# Brightness

```
h, w = G.shape  
add = 220
```

```
gray = np.where(gray <= 255 - add, gray + add, 255)
```

|    |    |    |    |
|----|----|----|----|
| 12 | 15 | 18 | 21 |
| 24 | 27 | 30 | 33 |
| 36 | 39 | 42 | 45 |
| 48 | 51 | 54 | 57 |

|     |     |     |     |
|-----|-----|-----|-----|
| 232 | 235 | 238 | 241 |
| 244 | 247 | 250 | 253 |
| 255 | 255 | 255 | 255 |
| 255 | 255 | 255 | 255 |

**Alhamdulillah.**