RESPUESTAS

DINAMICA DEL PUNTO Y DE SISTEMAS DE PARTICULAS

1 - a)
$$m_{(T)} = 7200 \text{ kg}$$
 , $P_{(T)} = 7.2.10^4 \text{ N}$; b) $m_{(T)} = 7200 \text{ kg}$, $P_{(L)} = 1.2.10^4 \text{ N}$

b)
$$m_{(T)} = 7200 \text{ kg}$$
 , $P_{(L)} = 1,2.10^4 \text{ N}$

$$3 - d = 1000 \text{ m}$$

$$4 - b) t = 40 s$$

c)
$$\Delta x = 50 \text{ cm}$$

d)
$$d = 250 \text{ cm}$$

$$8 - q = 2 Q a / (g + a)$$

9 - a) N = 26 N j b)
$$\mathbf{a} = 6.4 \text{ m/s}^2 \mathbf{i}$$

b)
$$a = 6.4 \text{ m/s}^2 \text{ i}$$

c) No existe N;
$$a = (16 i + 2 j) m/s^2$$

10 - a)
$$a = 2/3$$
 m/s² (hacia arriba sobre el plano)

b)
$$R_N = 178 \text{ N}$$

c)
$$F' = 452 \text{ N}$$

11 - I)
$$a = 1.5 \text{ m/s}^2$$

 $R_N = 496.4 \text{ N}$

II)
$$a = 11.5 \text{ m/s}^2$$

 $R_N = 196.4 \text{ N}$

$$12 - v = 60 \text{ m/s i } - 40 \text{ m/s j}$$

$$13 - a = 2 \text{ m/s}^2$$

$$T = 80 \text{ N}$$

14 - a)
$$a = 0.5 \text{ m/s}^2$$

b)
$$a = 0.47 \text{ m/s}^2$$

$$T = 1 N$$

$$T = 0.95 \text{ N}$$

$$15 - a = 2,22 \text{ m/s}^2$$

b)
$$F = 0.89 N$$

$$16 - a) T = 240 N$$

b)
$$a = 4 \text{ m/s}^2$$

$$18 - a) T_1 = 3 N$$
 ;

$$T_2 = 2 N$$

b)
$$T_1 = 3.3 \text{ N}$$
 ; $T_2 = 2.2 \text{ N}$

$$T_2 = 2.2 \text{ N}$$

c) idem b)

c)
$$T_1 = 2.7 \text{ N}$$

$$T_2 = 1.8 \text{ N}$$

d)
$$T_1 = 0 N$$

$$T_2 = 0 N$$

19 - a)
$$F_c = 12 \text{ N}$$

b)
$$F_c = 9.6 \text{ N}$$

20 - a) $a = 2.80 \text{ m/s}^2$ (hacia abajo por el plano)

b)
$$T = 128 \text{ N}$$

c)
$$R_N = 320 \text{ N}$$

$$21 - a) a = 5 \text{ m/s}^2$$

b)
$$T = 60 \text{ N}$$

c)
$$T' = 120 \text{ N}$$

d)
$$m_A = m_B$$

$$22-a) m = 0.22 Kg.$$

b)
$$v = 2 \text{ m/s}$$

$$23 - a) a = 6 \text{ m/s}^2$$

b)
$$T_1 = 30 \text{ N}$$

$$T_2 = 90 \text{ N}$$

24 -

	a	b	С	d	е
$a_1 (m/s^2)$	0	0	0	1,4	5
$a_2 (m/s^2)$	0	0	5	9	15

$$25 - a) a = 2 \text{ m/s}^2$$

b)
$$T_2 = 48 \text{ N}$$

c)
$$T_1 = 36 \text{ N}$$

26 - ΔP =
$$-\frac{(m_1 - m_2)^2 \cdot g}{m_1 + m_2}$$
 (hay que quitar ΔP de Mg = $m_1 g + m_2 g$)

$$(27 - a) v = 12 m/s$$
 hacia la derecha

b) x = 10 m hacia la derecha de la posición inicial

c) L = 26 m y d = 10 m

28 - a)
$$a_M = 2.5 \text{ m/s}^2$$
 ; $a_m = 5 \text{ m/s}^2$

$$a_m = 5 \text{ m/s}^2$$

b)
$$T = 75 \text{ N}$$

$$29 - \Delta x = 5 \text{ cm}$$

$$30 - a) ke = k_1 + k_2$$

b)
$$ke = k_1 k_2 / (k_1 + k_2)$$
 c) $ke = k_1 + k_2$

c)
$$ke = k_1 + k_2$$

$$31 - d = 3,75 \text{ cm}$$

$$32 - k = 250 \text{ N/m}$$

$$33 - F = 2 N$$

$$34 - x = 27.5 \text{ cm}$$

$$35 - \Delta x = 0.2 \text{ m}$$

$$36 - a) a_A = 12.5 \text{ m}/\text{s}^2$$

b)
$$a_A = 6.5 \text{ m/s}^2$$

$$a_p = 0$$

$$a_{\rm B} = 0$$

$$a_{\rm B} = 4 \text{ m/ s}^2$$

c)
$$L = 25 \text{ cm}$$
.

$$37 - a) k = 40 N/m$$
;

b)
$$a = 20/3 \text{ m/ s}^2$$
 c) $\Delta x = 0.6 \text{ m}$

c)
$$\Delta x = 0.6 \text{ m}$$

$$38 - F = 50 N$$

$$39 - a) Fm = 2.5 N$$

b) cae con a =
$$7 \text{ m/ s}^2$$

$$40 - a) P = 40 N$$

b)
$$\mu_e = 0.25$$

$$41 - a) T = 2 N$$

b)
$$T_{12} = 3.2 \text{ N}$$
, $T_{23} = 1.6 \text{ N}$, $a = 2 \text{ m/s}^2$

$$42 - a$$
) Fr = $9 N$

b)
$$\mu_c = 0.56$$

$$43 - a)$$
 fr = $2 N$

b)
$$\mu_c = 0.028$$

$$44 - a) F = 44 N$$

b)
$$\mu_c = 0.256$$

$$c)F = 36.8 N$$

$$45 - a) fr = 5,2 N$$

b)
$$t = 2.9 \text{ s}$$

c)
$$d = 31.8 \text{ m}$$

$$d) t = 5,16 s$$

e)
$$v = 12,33 \text{ m/s}$$

$$46 - a) m = 5 kg$$

b)
$$fr = 10 \text{ N}$$

$$47 - a) a = 4 m/s^2$$

b)
$$T = 60 \text{ N}$$

c)
$$fr = 10 \text{ N}$$

$$48 - a) F = 63 N$$

b)
$$T = 25 \text{ N}$$

49 - a)
$$a = 5.2 \text{ m/s}^2$$

b)
$$T = 192 N$$

c)
$$t = 0.385 \text{ s}$$
; $h = 0.39 \text{ m}$

$$50 - a) \mu_e = 0.66$$

$$b) \mu_c = 0.29$$

51 - a) no se mueve, a = 0;

T = 20 N

fr = 4 N (hacia arriba por el plano) ; fr = 9.6 N

- b) se mueve hacia la izquierda con a = 0.8 m/s^2 c) no se mueve a = 0;
 - T = 30 N
- T = 21.6 Nfr = 6 N
- d) m' = 1.36 kg; se mueve hacia la derecha con $a = 0.435 \text{ m/s}^2$; T = 32.14 N; fr = 6.4 N
- 52 a) fr = 36 N; $\mu_e = 0.75$
- b) $a = 0.5 \text{ m/s}^2$ hacia la izquierda

c) $|a_2| = 5.71 \text{ m/s}^2$

El carrito 1 sube con $|a_1|$ = 11,66 m/s² hasta que se detiene y luego desciende con $|a_1| = 3,66 \text{ m/s}^2$

$$53 - I)$$
 a) fr = $32 N$

b)
$$a = 2.16 \text{ m/s}^2$$

c)
$$T = 121,6$$
 N

II) a)
$$fr = 140 \text{ N}$$

b)
$$a = 0$$

c)
$$T = 100 \text{ N}$$

$$54 - a) x = 1.16 t^2$$

b)
$$f = f_{BA} = 27 \text{ N}$$

$$56 - a) d = 1,67 m$$

b)
$$f = -75 \text{ N i} + 100 \text{ N j}$$

$$57 - v = 3,16 \text{ m/s}$$

$$58 - \mu_e = 0.11$$

$$59 - m = 2,25 \text{ kg}$$

$$R = 0.82 \text{ m}$$

$$60 - T_1 = 0.52 \text{ N}$$

$$T_2 = 0.48 \text{ N}$$

$$61 - \theta = 11,39^{\circ}$$

$$62 - b) v = 2,4 m/s$$

c)
$$T = 4.6 \text{ N}$$

$$63 - T = 1,85 s$$

$$64 - m_T \approx 6.10^{24} \text{ kg}$$

$$65 - g_P = 8.1 \text{ m} / \text{s}^2$$

66-
$$T^2 = \frac{4\pi^2}{G_0 M_0}$$
 . R^3

$$67 - r \approx 4.2.10^7 \text{ m}$$

$$v = 11113 \text{ km/h}$$

$$68 - v = 7.5 \text{ km/s}$$

69 - d = 7,2 m del cuerpo de masa mayor

$$70 - M_S \approx 2.10^{30} \text{ kg}$$

$$71 - d = 4,386 \cdot 10^8 \text{ km}$$

72 - a)
$$F = (2,65 i + 2,48 j).10^{-11} N$$

b)
$$F = (-7.37 i - 15 j).10^{-11} N$$

$$73 - d = 3,45 \cdot 10^5 \text{ km}$$
 de la Tierra

$$74 - R_P = R_T$$

$$75 - k_v = 100 \text{ N s / m}$$

76- a)
$$f = 3.33 \cdot 10^{-2} \text{ N}$$

b)
$$k_v = 7.4 \cdot 10^{-2} \text{ N s/m}$$

b)
$$\eta = 0.79 \text{ N s/m}^2$$

$$78 - b) F = -2.10^{-3} N$$

$$F = 0$$

$$79 - a) I = -20 \text{ Ns } j$$

b)
$$p = -20 \text{ Ns i} + 10 \text{ Ns j}$$

c)
$$v(3s) = -2 \text{ m/s } i + 1 \text{ m/s } j$$

$$80 - a) L_p = 0$$

 $80 - a) L_p = 0$; $L_N = 0$; $L_{E_I} = -800 J$

$$81 - a) L_F = 3 J$$

b) $L_r = a d + 1/2 b d^2$

$$82 - a) v (3 s) = 11 m/s$$

b)
$$v (5 m) = 12.6 m/s$$

v (6 s) = 14 m/s v (10 m) = 15 m/s

83 - a)
$$L_{AB} > 0$$

b) $L_{BC} = 0$

c)
$$L_{CD} < 0$$

d) $L_{DE} > 0$

$$84 - L_{fe} = 3,4.10^{-13} \text{ J}$$

$$85 - b) v(0) = 1 m/s$$

$$v(1) = 1 \text{ m/s}$$
; $v(2) = 3 \text{ m/s}$;

v(5) = 0

c)
$$I = -0.5 \text{ kg m/s i}$$

$$86 - a) I = 1000 Ns$$

b)
$$v = 10 \text{ m/s}$$

c)
$$L_F = 5.10^3 \text{ J}$$

$$87 - a) p = 1.5 \cdot 10^5 \text{ kgm/s}$$

b) I:
$$v = 30 \text{ m/s}$$

II:
$$v = 22,36 \text{ m/s}$$

88 - a)
$$L_R = 0$$

c) $L_T = 64 \text{ kJ}$

b)
$$T = 640 \text{ N}$$

d)
$$L_{fr} = -16 \text{ kJ}$$

$$89 - a) L_R = 240 J$$

b)
$$v = 8 \text{ m/s}$$

$$90 - a) Ec = 2 kJ$$

b)
$$v = 20 \text{ m/s}$$

c)
$$v = 10 \text{ m/s}$$

$$91 - h = 20 \text{ m}$$

$$92 - a) L_F = 2430 J$$

93 - a)
$$L_E = -10 \, d^2 \, (J)$$

b)
$$d = 3 \text{ m}$$

$$95 - a) v_A = v_B = v_o$$

$$v_C = \sqrt{v_0^2 + gh}$$

b)
$$|\mu_c| = \frac{v_o^2 + 2gh}{2\overline{EDg}}$$

$$96 - a) fr = 3.5 N$$

b)
$$d = 24 \text{ m}$$

$$97 - fr = 4375 N$$

$$98 - a$$
) $v_B = 4,47 \text{ m/s}$ b) $v_C = 3,46 \text{ m/s}$ c) $T_C = 9 \text{ N}$ $T_B = 15 \text{ N}$

b)
$$v_c = 3,46 \text{ m/s}$$

c)
$$T_c = 9 \text{ N}$$

$$\Gamma_{\rm B} = 15$$
 N

d) $a_A = 10 \text{ m/s}^2 \text{ vertical hacia abajo}$

 $a_B = 20 \text{ m/s}^2 \text{ vertical hacia arriba}$

 $a_c = 14.4 \text{ m/s}^2$ formando un ángulo de 33.7° medidos desde la cuerda hacia la derecha

 $99 - a) \alpha = 45^{\circ}$

b)
$$v_c = 0.96 \text{ m/s}$$

100 - v = 1.41 m/s

$$101 - h = 2.5 R$$

 $102 - \Delta x = 10 \text{ cm}$

$$103 - a) d = 3 m$$

b) v = 5.37 m/s

c)
$$d = 2,775 \text{ m}$$
 y $v = 3,1 \text{ m/s}$

104 - 5000 m

$$105 - \Delta x = 1 \text{ m}$$

106 - No llega al resorte

$$107 - v = 4 \text{ m/s}$$

$$108 - h = 19,9 \text{ m}$$

109 - a) h = 11,96 m respecto de la posición

b) $v = 16 \, \text{m/s}$ de máximo acortamiento

$$110 - a)$$
 Lfr = -750 J

b) v = 25 m/s

c)
$$L_P = 7000 J$$

111 - a) d = 2,1 m por debajo de la posición inicial sobre el plano

$$112 - a$$
) $|fr| = 0.3 N$

b)
$$v_B = 5 \text{ m/s}$$

$$c) - 0.36 J$$

$$113 - a) Ep = 2 kJ$$

b)
$$x = 15 \text{ m}$$

$$116 - I) a) k = 100 N/m$$

II) a)
$$k = 33,33 \text{ N/m}$$

b)
$$h' = 0.5 \text{ m}$$

$$v = 1,66 \text{ m/s}$$

II) a)
$$k = 33.33 \text{ N/m}$$

b)
$$h' = 0.5 \text{ m}$$

$$v = 0.745 \text{ m/s}$$

117 - P = 0.43 HP

$$118 - P = 8.4 \text{ kW}$$

$$120 - x_G = 0.5.10^{-8}$$
 cm

$$121 - r = 4900 \text{ km}$$

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122 - b) \Delta x = 0.8 \text{ m}
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$$123 - x_{cm} = 4 \text{ m}$$

$$124 - (1,5 \text{ m}; 2 \text{ m})$$

125 - a)
$$\mathbf{r}_{CM}(0) = -0.4 \text{ m} \mathbf{j}$$
 ; $\mathbf{v}_{CM}(0) = (0.6; 0.36) \text{ m/s}$; $\mathbf{a}_{CM}(0) = 0$

b)
$$\mathbf{r}_{CM}(4s) = (2,4; 1,04) \text{ m}$$
; $\mathbf{v}_{CM}(4s) = (0,6; 0,36) \text{ m/s}$; $\mathbf{a}_{CM}(4s) = 0$

c)
$$Ec(t) = 1.82 J$$
 ; $Ec_{CM}(t) = 1.244 J$

$$126 - a) a 1,2 m de A$$
 b) $AC' = 7,5 m$

$$127 - b) d = 4,4 m$$

128 - a)
$$F = 2 N$$
 b) $v = 4 m/s$ c) $L_F = 1.2 J$

$$129 - v_A = 22413 \text{ km/h}$$
 $v_B = 29740 \text{ km/h}$

$$130 - v = 6 \text{ m/s}$$
 b) $L_F = 810 \text{ J}$

a)
$$x_{CM} = 2 \text{ m} + 1.33 \text{ m/s t}$$
 $v_{CM} = 1.33 \text{ m/s};$ $p_{CM} = 20 \text{ kg m/s}$

b)
$$x_{CM} = 2 \text{ m} - 1{,}33 \text{ m/s}$$
 t $v_{CM} = -1{,}33 \text{ m/s}$; $p_{CM} = -20 \text{ kg m/s}$

c)
$$x_{CM} = 2 \text{ m}$$
 ; $p_{CM} = 0 \text{ m/s}$;

II) choque elástico

a)
$$x_{CM} = 2 \text{ m} + 1.33 \text{ m/s t}$$
 $v_{CM} = 1.33 \text{ m/s};$ $p_{CM} = 20 \text{ kg m/s}$

b)
$$x_{CM} = 2 \text{ m} - 1{,}33 \text{ m/s}$$
 ; $p_{CM} = -20 \text{ kg m/s}$

c)
$$x_{CM} = 2 \text{ m}$$
 $v_{CM} = 0 \text{ m/s}$; $p_{CM} = 0$

$$132 - v = 1,58 \text{ m/s}$$

133 - a)
$$v'_A = -2 \text{ m/s}$$
 ; $v'_B = 8 \text{ m/s}$
b) $I_A = -1200 \text{ N.s}$; $I_B = 1200 \text{ N.s}$

135 -
$$E_1 = 2.5 J$$
 $E_2 = 1 J$

$$136 - v_1 = 4.9 \text{ m/s}$$

$$a_1 = 100 \text{ m/s}^2$$

$$a_2 = 25 \text{ m/s}^2$$

$$137 - \Delta x = 16 \text{ m}$$

$$138 - a) v = -1 \text{ m/s } \mathbf{j}$$

b)
$$v = 1.2 \text{ m/s } i - 0.9 \text{ m/s } j$$

$$139 - a) d = 64 cm$$

b)
$$t = 0.8 s$$

$$140 - a) v = 83.5 \text{ m/s}$$

b)
$$m = 92.5 g$$

$$141 - d = 5 \text{ m}$$

$$142 - a) m = 50 kg$$

b)
$$\mu_c = 0.8$$

$$143 - v_1 = 3 \text{ m/s}$$

$$v_2 = -1 \text{ m/s}$$

$$144 - \mu_c = 0.53$$

$$145 - v = 25 \text{ km/h}$$

$$\alpha = 37^{\circ}$$

146 - a)
$$v'_1 = -28 \text{ m/s}$$
 ; $v'_2 = 2 \text{ m/s}$

146 - a)
$$v'_1 = -28 \text{ m/s}$$
 ; $v'_2 = 2 \text{ m/s}$ (Tomando positivo hacia la derecha)

b)
$$v_2 = 0$$

c) $v_1 = -22 \text{ m/s}$

;
$$\Delta Ec = -1000 J$$
;
; $\Delta Ec = -787.5 J$

$$v_2 = 1,25 v_1^0$$

$$148 - Ec_1 = 400 J$$

$$Ec_2 = 1300 J$$

$$149 - n = 4$$

150 - d = 19437 m a partir de la posición de disparo

$$151 - v_i = \sqrt{\frac{Fl(2M + m)}{Mm}}$$

$$v_2 = \sqrt{2} v_1$$

152 - a)
$$|v_1| = 67,25 \text{ m/s}$$

b)
$$Ec = 3.23 \text{ kJ}$$

$$\alpha$$
 = -132° (respecto de la dirección de la velocidad de la masa mayor – eje x > 0)

FLUIDOS

RESPUESTAS

2 - Sube 0,5 cm por encima del nivel original

$$3 - L = 1/4 \rho g A (h_2 - h_1)^2$$

$$4 - a) F = f (A / a)$$
; b) 13,89 kgf; c) $h_A = 0.21 cm$

c)
$$h_A = 0.21 \text{ cm}$$

$$5 - A = 6 m^2$$

$$6 - n = 5$$

$$7 - \rho_m = 0.666 \text{ g/cm}^3$$

$$\rho_a = 0.74 \text{ g/cm}^3$$

$$8 - \Gamma i = 0,287 \,\mathrm{m}$$

$$9 - v = 0.167 \text{ m/s}$$

10 - a)
$$Q = 2.10^{-3} \text{ m}^3/\text{s}$$
; $v = 2.5 \text{ m/s}$; b) $p_2 = 2.57 \cdot 10^5 \text{ N/m}^2$

$$v = 2.5 \text{ m/s}$$

b)
$$p_2 = 2.57 \cdot 10^5 \text{ N/m}^3$$

11- a)
$$v = 6.25 \text{ m/s}$$

;
$$b p = 1 \text{ kgf/cm}^2 = 10^5 \text{ Pa}$$

$$12 - h' = H - h$$

$$13 - Q = 0.034 \text{ m}^3/\text{s}$$

$$14 - h = H / 2$$

b)
$$X_M = H$$

