

# Train ML Agent

`mlagents-learn MobilRobot.yaml --run-id=1 --force`

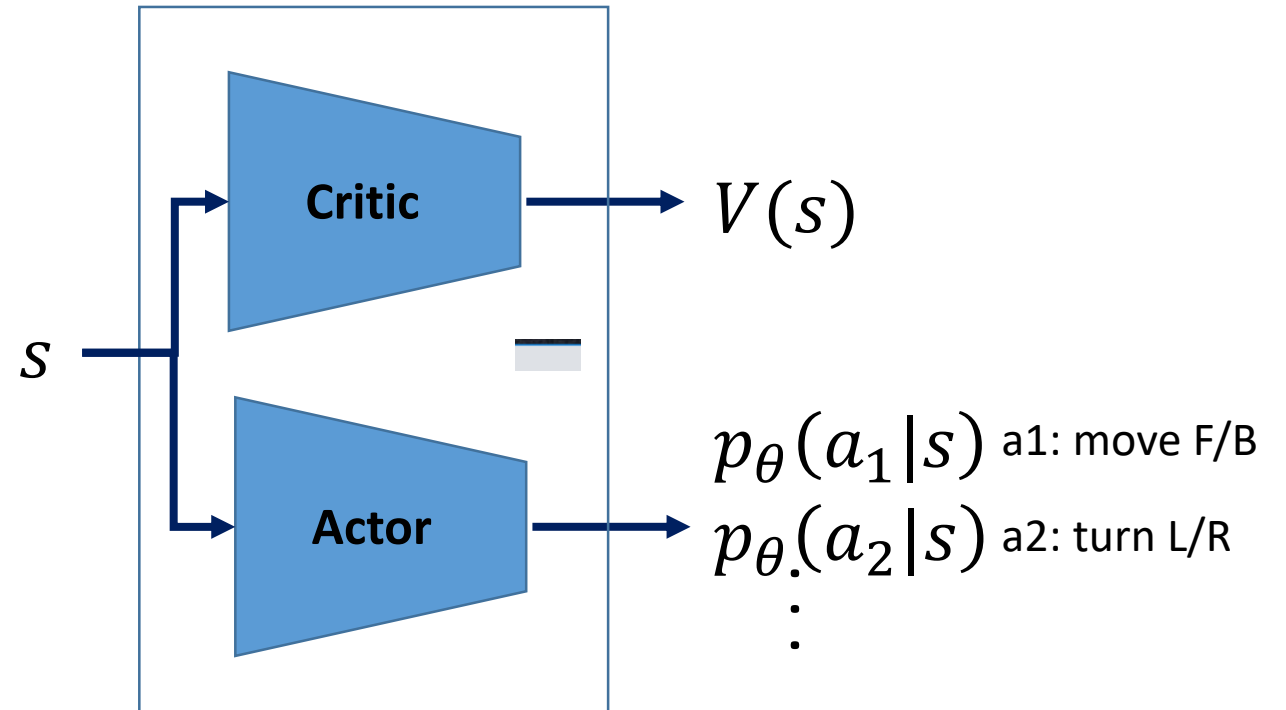
Define hyper parameters

Exemplar PPO-AC code: <https://github.com/TienLungSun/RL-Mobile-Robot/tree/main/LearnPPO-AC>

# Two neural networks

Actor learns the best actions (that can have maximum long-term rewards)  
Critic learns the expected value of the long-term reward.

```
class ActorCritic(nn.Module):  
    def __init__(self, num_inputs, num_outputs, hidden_size1, hidden_size2):  
        super(ActorCritic, self).__init__()  
  
        self.critic = nn.Sequential(  
            nn.Linear(num_inputs, hidden_size1),  
            nn.LayerNorm(hidden_size1),  
            nn.Tanh(),  
            nn.Linear(hidden_size1, hidden_size2),  
            nn.LayerNorm(hidden_size2),  
            nn.Tanh(),  
            nn.Linear(hidden_size2, 1),  
        )  
  
        self.actor = nn.Sequential(  
            nn.Linear(num_inputs, hidden_size1),  
            nn.LayerNorm(hidden_size1),  
            nn.Tanh(),  
            nn.Linear(hidden_size1, num_outputs),  
        )
```



# Two neural networks

```
network_settings:  
  normalize: true  
  hidden_units: 512  
  num_layers: 3  
  vis_encode_type: simple
```

For simple problems where the correct action is a straightforward combination of the observation inputs, this should be small. For problems where the action is a very complex interaction between the observation variables, this should be larger.

For simple problems, fewer layers are likely to train faster and more efficiently. More layers may be necessary for more complex control problems.

# Interact with training environment to collect data

```
while frame < max_frames
  get s1
  for step in range( N):
     $(s_1, a_1, r_1, s_2), v_1, \log p_1$ 
     $(s_2, a_2, r_2, s_3), v_2, \log p_1$ 
    ...
     $(s_N, a_N, r_N, s_{N+1}), v_N, \log p_1$ 
  calculate GAE
  use GAE to update NN
```

```
keep_checkpoints: 5
max_steps: 5000000
time_horizon: 1000
summary_freq: 30000
threaded: true
```

---

# Interact with training environment to collect data

```
while frame_idx < max_frames and not early_stop: #Ru
    if(__printDetails):
        print("Frame = ", frame_idx, end=", ")
    log_probs = []
    values = []
    states = []
    actions = []
    rewards = []
    masks = []
    entropy = 0

    step_result = env.get_steps(behaviorName)
    DecisionSteps = step_result[0]
    state = DecisionSteps.obs[0]
    if(__printDetails):
        print("step", end = ":")
    for step in range(num_steps):
        if(__printDetails and (step+1) % 5==0):
            print(step+1, end = ", ")
        state = torch.FloatTensor(state).to(device)
        dist, value = model(state)

        action = dist.sample()
        if(int(torch.isnan(torch.min(action))) == 1)
            print("Error: distribution=", dist, "%.2
        env.set_actions(behaviorName, np.array(actio
```

keep\_checkpoints: 5  
max\_steps: 5000000  
time\_horizon: 1000  
summary\_freq: 30000  
threaded: true

---

This parameter trades off between a less biased, but higher variance estimate (long time horizon) and more biased, but less varied estimate (short time horizon). In cases where there are frequent rewards within an episode, or episodes are prohibitively large, a smaller number can be more ideal. This number should be large enough to capture all the important behavior within a sequence of an agent's actions.

# Interact with training environment to collect data

```
In [18]: frame_idx = 0
max_frames = 5000 #15000
env.reset()
early_stop = False
__printDetails = False

while frame_idx < max_frames and not early_stop: #
    if(__printDetails):
        print("Frame = ", frame_idx, end=" ", ")
    log_probs = []
    values = []
    states = []
    actions = []
    rewards = []
    masks = []
    entropy = 0

    step_result = env.get_steps(behaviorName)
    DecisionSteps = step_result[0]
    state = DecisionSteps.obs[0]
    if(__printDetails):
        print("step", end = ":")
    for step in range(num_steps):
        if(__printDetails and (step+1) % 5==0):
            print(step+1, end = ", ")
        state = torch.FloatTensor(state).to(device
        dist, value = model(state)
```

```
keep_checkpoints: 5
max_steps: 5000000
time_horizon: 1000
summary_freq: 30000
threaded: true
```

By default, model updates can happen while the environment is being stepped. This violates the on-policy assumption of PPO slightly in exchange for a training speedup. To maintain the strict on-policy of PPO, you can disable parallel updates by setting threaded to false.

# Calculate GAE

```
In [4]: def compute_gae(next_value, rewards, masks, values, gamma=0.99, tau=0.95):  
        values = values + [next_value]  
        gae = 0  
        returns = []  
        for step in reversed(range(len(rewards))):  
            delta = rewards[step] + gamma * values[step + 1] * masks[step] - values[step]  
            gae = delta + gamma * tau * masks[step] * gae  
            returns.insert(0, gae + values[step])  
        return returns
```

$\Delta$  = reward of this step + expected  
reward of next step

$gae = \Delta + \text{accumulated gae}$

$\text{Return} = gae + v$

$$\Delta_{20} = r_{20} + \gamma * v_{21} * mask_{20} - v_{20}$$

$$gae_{20} = \Delta_{20} + \gamma * \tau * mask_{20} * gae_{initial}$$

$$return_{20} = gae_{20} + v_{20}$$

$$\Delta_{19} = r_{19} + \gamma * v_{20} * mask_{19} - v_{19}$$

$$gae_{19 \sim 20} = \Delta_{19} + \gamma * \tau * mask_{19} * gae_{20}$$

$$return_{19} = gae_{19 \sim 20} + v_{19}$$

...

$$\Delta_1 = r_1 + \gamma * v_2 * mask_1 - v_1$$

$$gae_{1 \sim 20} = \Delta_1 + \gamma * \tau * mask_1 * gae_{2 \sim 20}$$

$$return_1 = gae_{1 \sim 20} + v_1$$

# Calculate GAE

```
def compute_gae(next_value, rewards, masks, values, gamma=0.99, tau=0.95):
    values = values + [next_value]
    gae = 0
    returns = []
    for step in reversed(range(len(rewards))):
        delta = rewards[step] + gamma * values[step + 1] * masks[step] - values[step]
        gae = delta + gamma * tau * masks[step] * gae
        returns.insert(0, gae + values[step])
    return returns
```

hyperparameters:

batch\_size: 2048  
buffer\_size: 20480  
learning\_rate: 0.0003  
beta: 0.005  
epsilon: 0.2  
lambda: 0.95

reward\_signals:

extrinsic:

gamma: 0.995  
strength: 1.0

$$\Delta_{20} = r_{20} + \gamma * v_{21} * mask_{20} - v_{20}$$

$$gae_{20} = \Delta_{20} + \gamma * \tau * mask_{20} * gae_{initial}$$

$$return_{20} = gae_{20} + v_{20}$$

$$\Delta_{19} = r_{19} + \gamma * v_{20} * mask_{19} - v_{19}$$

$$gae_{19 \sim 20} = \Delta_{19} + \gamma * \tau * mask_{19} * gae_{20}$$

$$return_{19} = gae_{19 \sim 20} + v_{19}$$

...

Low values correspond to relying more on the current value estimate (which can be high bias), and high values correspond to relying more on the actual rewards received in the environment (which can be high variance).

In situations when the agent should be acting in the present in order to prepare for rewards in the distant future, this value should be large. In cases when rewards are more immediate, it can be smaller. Must be strictly smaller than 1.



# Data collected from different agents

```
next_state = torch.FloatTensor(next_state).to(device)
_, next_value = model(next_state)
returns = compute_gae(next_value, rewards, masks, values)

returns = torch.cat(returns).detach()
log_probs = torch.cat(log_probs).detach()
values = torch.cat(values).detach()
states = torch.cat(states)
actions = torch.cat(actions)
advantage = returns - values
```

hyperparameters:

batch\_size: 2048

buffer\_size: 20480

learning\_rate: 0.0003

larger buffer\_size corresponds to more stable training updates

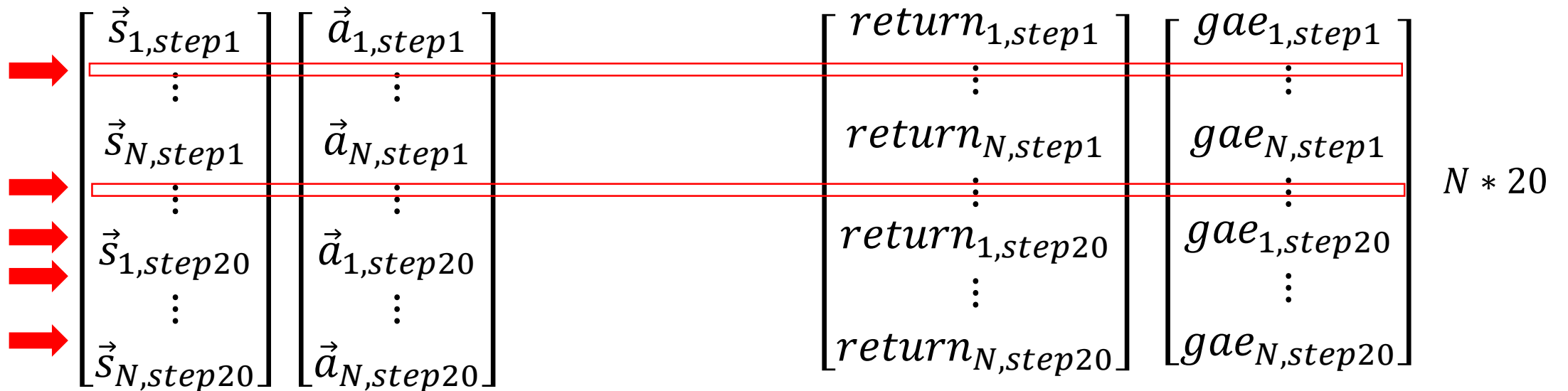
$$\begin{matrix}
 N * 20 & \begin{bmatrix} \vec{s}_{1,step1} \\ \vdots \\ \vec{s}_{N,step1} \\ \vdots \\ \vec{s}_{1,step20} \\ \vdots \\ \vec{s}_{N,step20} \end{bmatrix} & \begin{bmatrix} \vec{a}_{1,step1} \\ \vdots \\ \vec{a}_{N,step1} \\ \vdots \\ \vec{a}_{1,step20} \\ \vdots \\ \vec{a}_{N,step20} \end{bmatrix} & \begin{bmatrix} v_{1,step1} \\ \vdots \\ v_{N,step1} \\ \vdots \\ v_{1,step20} \\ \vdots \\ v_{N,step20} \end{bmatrix} & \begin{bmatrix} return_{1,step1} \\ \vdots \\ return_{N,step1} \\ \vdots \\ return_{1,step20} \\ \vdots \\ return_{N,step20} \end{bmatrix} & \begin{bmatrix} gae_{1,step1} \\ \vdots \\ gae_{N,step1} \\ \vdots \\ gae_{1,step20} \\ \vdots \\ gae_{N,step20} \end{bmatrix}
 \end{matrix}$$

# Sampling a batch of data to train NN

```
In [5]: import numpy as np

def ppo_iter(mini_batch_size, states, actions, log_probs, returns, advantage):
    batch_size = states.size(0)
    for _ in range(batch_size // mini_batch_size):
        rand_ids = np.random.randint(0, batch_size, mini_batch_size)
        yield states[rand_ids, :], actions[rand_ids, :], log_probs[rand_ids, :]
```

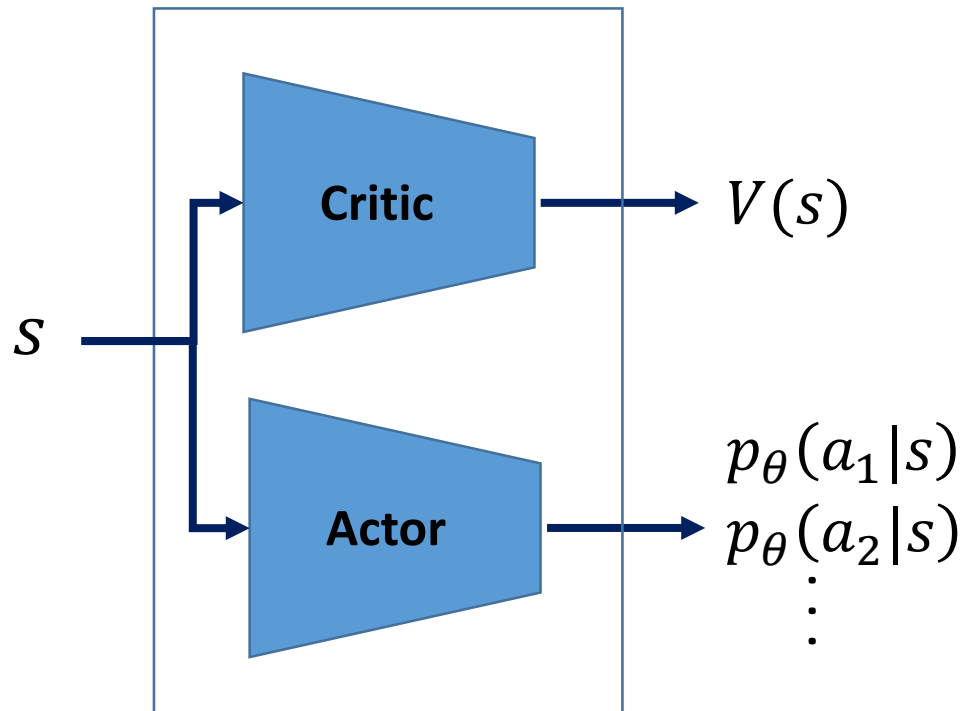
hyperparameters:  
batch\_size: 2048



# Update NN

```
In [6]: def ppo_update(ppo_epochs, mini_batch_size, state,
        for _ in range(ppo_epochs):
            for state, action, old_log_probs, return_ in minibatch_loader():
                dist, value = model(state)
                entropy = dist.entropy().mean()
                new_log_probs = dist.log_prob(action)
```

hyperparameters:  
batch\_size: 2048  
buffer\_size: 20480  
learning\_rate: 0.0003



$$L = c_v L_v + L_{\pi} + c_{reg} L_{reg}$$

$$L_v = MSE(return - v)$$

$$return_i = gae_{i \sim 20} + v_i$$

$$gae_{i \sim 20} = \Delta_i + \gamma * \tau * mask_i * gae_{i+1 \sim 20}$$

$$\Delta_i = r_i + \gamma * v_{i+1} * mask_i - v_i$$

# Update NN

```
def ppo_update(ppo_epochs, mini_batch_size, states, actions, log_probs, returns, advantages):
    for _ in range(ppo_epochs):
        for state, action, old_log_probs, return_, advantage in ppo_iter(mini_batch_size,
                                                                           returns,
                                                                           advantages):
            dist, value = model(state)
            entropy = dist.entropy().mean()
            new_log_probs = dist.log_prob(action)

            ratio = (new_log_probs - old_log_probs).exp()
            surr1 = ratio * advantage
            surr2 = torch.clamp(ratio, 1.0 - clip_param, 1.0 + clip_param) * advantage

            actor_loss = - torch.min(surr1, surr2).mean()
            critic_loss = (return_ - value).pow(2).mean()

            loss = 0.5 * critic_loss + actor_loss - 0.001 * entropy

            optimizer.zero_grad()
            loss.backward()
            optimizer.step()
    return float(loss)
```

beta: 0.005  
epsilon: 0.2  
lambda: 0.95  
num\_epoch: 3

The larger the batch\_size, the larger it is acceptable to make this. Decreasing this will ensure more stable updates, at the cost of slower learning.

# Update NN

For PPO, we recommend decaying learning rate until max\_steps so learning converges more stably. Linear decays the learning\_rate linearly, reaching 0 at max\_steps, while constant keeps the learning rate constant for the entire training run.

epsilon: 0.2

lambd: 0.95

num\_epoch: 3

learning\_rate\_schedule: linear

# Update NN

```
def ppo_update(ppo_epochs, mini_batch_size, states, actions, log_probs, returns, advantages, clip_param=0.2):
    for _ in range(ppo_epochs):
        for state, action, old_log_probs, return_, advantage in zip(states, actions, log_probs, returns, advantages):
            dist, value = model(state)
            entropy = dist.entropy().mean()
            new_log_probs = dist.log_prob(action)

            ratio = (new_log_probs - old_log_probs).exp()
            surr1 = ratio * advantage
            surr2 = torch.clamp(ratio, 1.0 - clip_param, 1.0 + clip_param)

            actor_loss = - torch.min(surr1, surr2).mean()
            critic_loss = (return_ - value).pow(2).mean()

            loss = 0.5 * critic_loss + actor_loss - 0.001 * entropy

            optimizer.zero_grad()
            loss.backward()
```

$$L = c_v L_v + L_\pi + \beta L_{reg}$$

behaviors:

MobileRobot:

trainer\_type: ppo

hyperparameters:

batch\_size: 2048

buffer\_size: 20480

learning\_rate: 0.0003

beta: 0.005

Increasing beta will ensure more random actions are taken. Beta should be adjusted such that the entropy slowly decreases alongside increases in reward. If entropy drops too quickly, increase beta. If entropy drops too slowly, decrease beta.

# Update NN

Setting epsilon small will result in more stable updates, but will also slow the training process.

buffer\_size: 20480  
learning\_rate: 0.0003  
beta: 0.005  
epsilon: 0.2

```
def ppo_update(ppo_epochs, mini_batch_size, states, actions, log_probs, returns, advantages, clip_param=0.2):  
    for _ in range(ppo_epochs):  
        for state, action, old_log_probs, return_, advantage in ppo_iter(mini_batch_size, states, actions, log_probs, returns, advantages):  
            dist, value = model(state)  
            entropy = dist.entropy().mean()  
            new_log_probs = dist.log_prob(action)  
  
            ratio = (new_log_probs - old_log_probs).exp()  
            surr1 = ratio * advantage  
            surr2 = torch.clamp(ratio, 1.0 - clip_param, 1.0 + clip_param) * advantage  
  
            actor_loss = - torch.min(surr1, surr2).mean()  
            critic_loss = (return_ - value).pow(2).mean()
```

$$J_{PPO2}^{\theta'}(\theta) = \sum_{(s_t, a_t)} \min \left( \frac{p_{\theta}(a_t|s_t)}{p_{\theta'}(a_t|s_t)} A^{\theta'}(s_t, a_t), \text{clip} \left( \frac{p_{\theta}(a_t|s_t)}{p_{\theta'}(a_t|s_t)}, 1 - \varepsilon, 1 + \varepsilon \right) A^{\theta'}(s_t, a_t) \right)$$

# How to find the optimal parameters?

$$\tau = (s_1, a_1, r_1, s_2, a_2, r_2, \dots s_T, a_T)$$

$$p_{\theta}(\tau) = p(s_1)p_{\theta}(a_1|s_1)p(s_2|s_1, a_1)p_{\theta}(a_2|s_2)p(s_3|s_2, a_2) \dots$$

$$R(\tau) = \sum_{t=1}^T r_t$$

$$\bar{R}_{\theta} = \sum R(\tau) p_{\theta}(\tau) = E_{\tau \sim p_{\theta}(\tau)}[R(\tau)]$$

Max  $E[\bar{R}_{\theta}]$

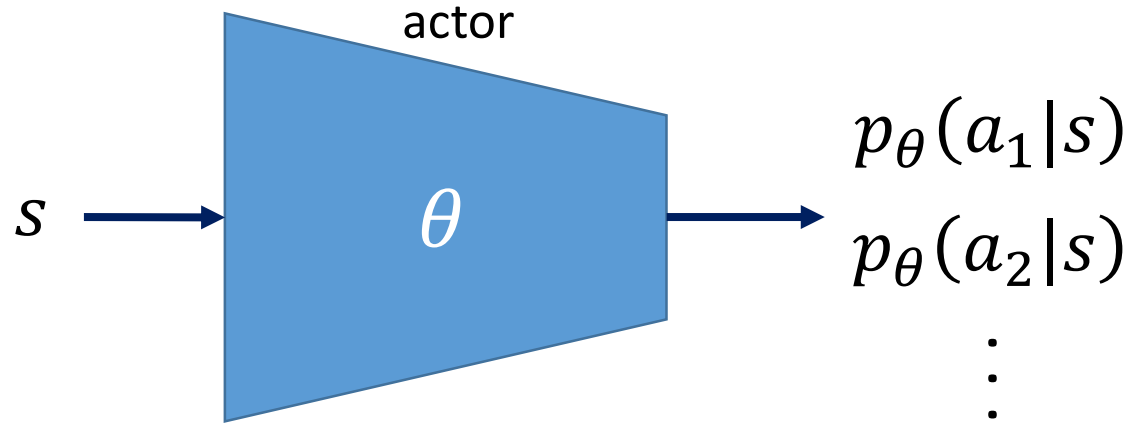
$$\max_{\theta} E[\bar{R}_{\theta}]$$

Gradient of the  
expected value

$$\begin{aligned} \nabla \bar{R}_{\theta} &= \sum R(\tau) \nabla p_{\theta}(\tau) = E_{\tau \sim p_{\theta}(\tau)}[R(\tau) \nabla \log p_{\theta}(\tau)] \approx \frac{1}{N} \sum_{n=1}^N R(\tau^n) \nabla \log p_{\theta}(\tau^n) \\ &= \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} R(\tau^n) \nabla \log p_{\theta}(a_t^n | s_t^n) \end{aligned}$$



Use  $\nabla \bar{R}_\theta$  to update policy network



$$\theta^{\pi'} \leftarrow \theta^\pi + \eta \nabla \bar{R}_\theta$$

$$\nabla \bar{R}_\theta = \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} R(\tau^n) \nabla \log p_\theta(a_t^n | s_t^n)$$

# Tips to calculate $\nabla \bar{R}_\theta$

$$\nabla \bar{R}_\theta = \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} R(\tau^n) \nabla \log p_\theta(a_t^n | s_t^n)$$

Add a baseline to  
calculate the reward

$$\nabla \bar{R}_\theta \approx \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} (R(\tau^n) - b) \nabla \log p_\theta(a_t^n | s_t^n), \quad b \approx E[R(\tau)]$$

$$\nabla \bar{R}_\theta \approx \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} \left( \sum_{t'}^{T_n} r_{t'}^n - b \right) \nabla \log p_\theta(a_t^n | s_t^n)$$

Assign suitable time  
delayed credit

$$\nabla \bar{R}_\theta \approx \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} \left( \sum_{t'}^{T_n} \gamma^{t'-t} r_{t'}^n - b \right) \nabla \log p_\theta(a_t^n | s_t^n), \gamma < 1$$

$$A^\theta(s_t, a_t) = \left( \sum_{t'}^{T_n} \gamma^{t'-t} r_{t'}^n - b \right)$$

# Off-policy $\nabla \bar{R}_\theta$

On-policy

$$\nabla \bar{R}_\theta \approx \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} A^\theta(s_t, a_t) \nabla \log p_\theta(a_t^n | s_t^n), \gamma < 1 \quad A^\theta(s_t, a_t) = \left( \sum_{t'}^{T_n} \gamma^{t'-t} r_{t'}^n - b \right)$$

Importance sampling

$$\begin{aligned} E_{x \sim p}[f(x)] &= E_{x \sim q} \left[ f(x) \frac{p(x)}{q(x)} \right] \\ \text{Var}_{x \sim q} \left[ f(x) \frac{p(x)}{q(x)} \right] &= E_{x \sim q} \left[ \left( f(x) \frac{p(x)}{q(x)} \right)^2 \right] - \left( E_{x \sim q} \left[ f(x) \frac{p(x)}{q(x)} \right] \right)^2 \\ &= E_{x \sim p} \left[ f(x)^2 \frac{p(x)}{q(x)} \right] - (E_{x \sim p}[f(x)])^2 \end{aligned}$$

Off-policy

$$\nabla \bar{R}_\theta = E_{(s_t, a_t) \sim \pi_{\theta'}} \left[ \frac{p_\theta(a_t | s_t)}{p_{\theta'}(a_t | s_t)} A^{\theta'}(s_t, a_t) \nabla \log p_\theta(a_t^n | s_t^n) \right]$$

# Loss function derived from $\nabla \bar{R}_\theta$

Off-policy

$$\nabla \bar{R}_\theta = E_{(s_t, a_t) \sim \pi_{\theta'}} \left[ \frac{p_\theta(a_t | s_t)}{p_{\theta'}(a_t | s_t)} A^{\theta'}(s_t, a_t) \nabla \log p_\theta(a_t^n | s_t^n) \right]$$

Sampling efficiency

Loss function

$$J^{\theta'}(\theta) = E_{(s_t, a_t) \sim \pi_{\theta'}} \left[ \frac{p_\theta(a_t | s_t)}{p_{\theta'}(a_t | s_t)} A^{\theta'}(s_t, a_t) \right]$$

Proximal policy  
optimization (PPO)

$$J_{PPO}^{\theta'}(\theta) = J^{\theta'}(\theta) - \beta KL(\theta, \theta')$$

$$J_{PPO2}^{\theta'}(\theta) = \sum_{(s_t, a_t)} \min \left( \frac{p_\theta(a_t | s_t)}{p_{\theta'}(a_t | s_t)} A^{\theta'}(s_t, a_t), \text{clip} \left( \frac{p_\theta(a_t | s_t)}{p_{\theta'}(a_t | s_t)}, 1 - \varepsilon, 1 + \varepsilon \right) A^{\theta'}(s_t, a_t) \right)$$

# Actor-critic strategy to calculate $\nabla \bar{R}_\theta$

$$\nabla \bar{R}_\theta \approx \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} \left( \sum_{t'=t}^{T_n} \gamma^{t'-t} r_{t'}^n - b \right) \nabla \log p_\theta(a_t^n | s_t^n)$$

$$G_t^n = \sum_{t'=t}^{T_n} \gamma^{t'-t} r_{t'}^n \quad \text{unstable when sampling amount is not large enough}$$

Use expected value to reduce sampling variance

$$\nabla \bar{R}_\theta \approx \frac{1}{N} \sum_{n=1}^N \sum_{t=1}^{T_n} \left( \sum_{t'=t}^{T_n} \gamma^{t'-t} r_{t'}^n - b \right) \nabla \log p_\theta(a_t^n | s_t^n)$$

$E[G_t^n] = Q^{\pi_\theta}(s_t^n, a_t^n)$  Expected value of  $G_t^n$

$V^{\pi_\theta}(s_t^n)$  Expected value of  $b$

Use one neural network that estimates  $V$

$$Q^{\pi_\theta}(s_t^n, a_t^n) = E[r_t^n + V^{\pi_\theta}(s_{t+1}^n)] = r_t^n + V^{\pi_\theta}(s_{t+1}^n)$$

$$Q^{\pi_\theta}(s_t^n, a_t^n) - V^{\pi_\theta}(s_t^n) = r_t^n + V^{\pi_\theta}(s_{t+1}^n) - V^{\pi_\theta}(s_t^n)$$

$$A^\theta(s_t, a_t) = (r_t^n + V^{\pi_\theta}(s_{t+1}^n) - V^{\pi_\theta}(s_t^n))$$

# Temporal difference to calculate V

$$A^\theta(s_t, a_t) = (r_t^n + V^{\pi_\theta}(s_{t+1}^n) - V^{\pi_\theta}(s_t^n))$$

Monte-Carlo approach

$$V^{\pi_\theta}(s_a) \leftrightarrow G_a$$

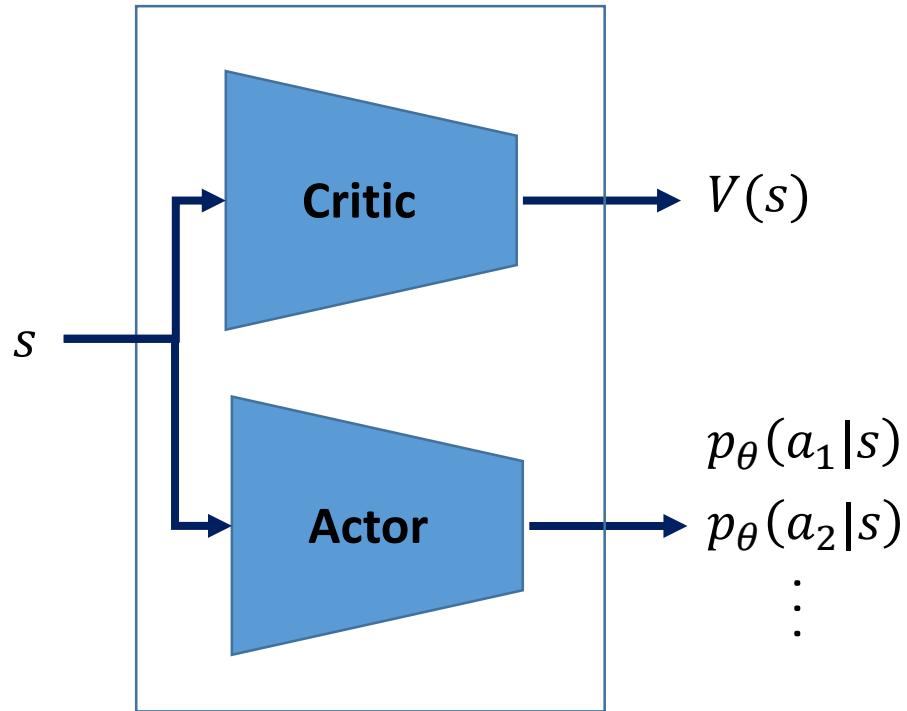
Until the end of the episode, the cumulated reward is  $G_a$

Temporal-difference  
approach

$$V^{\pi_\theta}(s_t) + r_t = V^{\pi_\theta}(s_{t+1})$$

$$V^{\pi_\theta}(s_t) - V^{\pi_\theta}(s_{t+1}) \leftrightarrow r_t$$

# Train the network



TD Error

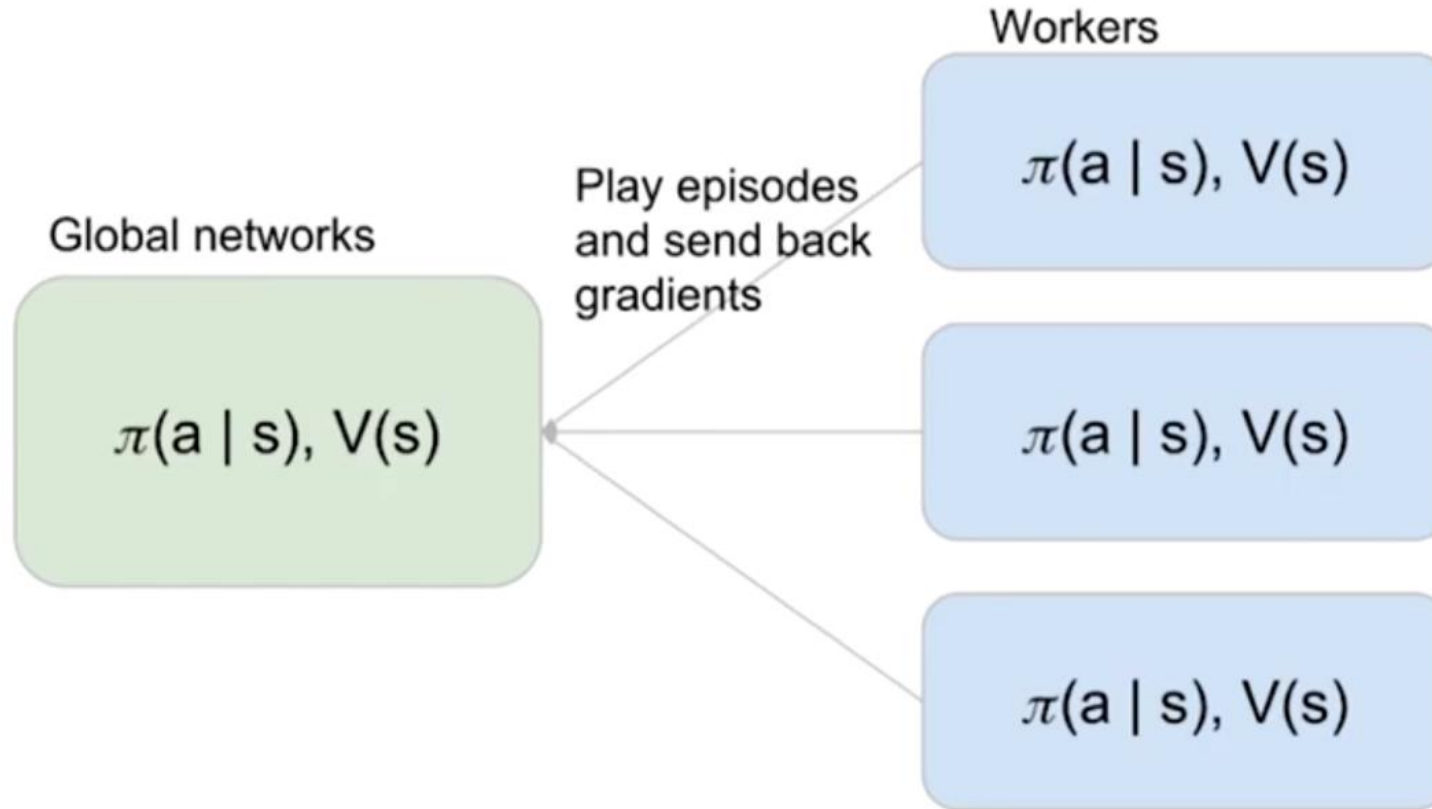
$$L = L_{\pi} + c_v L_v + c_{reg} L_{reg}$$

$$A^{\theta}(s_t, a_t) = G_t^n - V^{\pi_{\theta}}(s_t^n) = Q^{\pi_{\theta}}(s_t^n, a_t^n) - V^{\pi_{\theta}}(s_t^n) = r_t^n + \gamma V^{\pi_{\theta}}(s_{t+1}^n) - V^{\pi_{\theta}}(s_t^n)$$

$$L_v = (G_t^n - V^{\pi_{\theta}}(s_t^n))^2 = (r_t^n + \gamma V^{\pi_{\theta}}(s_{t+1}^n) - V^{\pi_{\theta}}(s_t^n))^2$$

$$L_{\pi} = \sum_{(s_t, a_t)} \min \left( \frac{p_{\theta}(a_t|s_t)}{p_{\theta'}(a_t|s_t)} A^{\theta'}(s_t, a_t), \text{clip} \left( \frac{p_{\theta}(a_t|s_t)}{p_{\theta'}(a_t|s_t)}, 1 - \varepsilon, 1 + \varepsilon \right) A^{\theta'}(s_t, a_t) \right)$$

# A3C



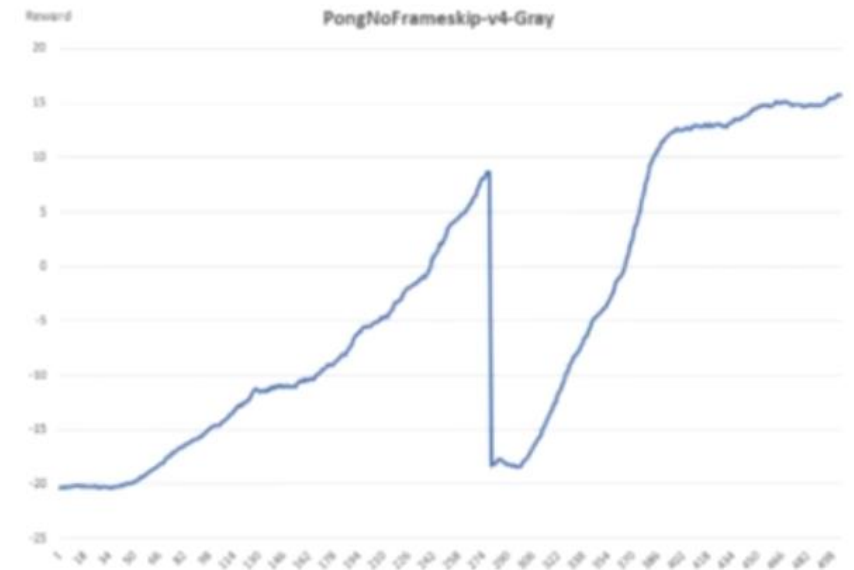
Reference: <https://youtu.be/iCV3vOl8IMk>



# A3C

## Stability

- Each episode will progress randomly
- Each action is sampled probabilistically
- Occasionally, performance of agent can drop off due to bad update
  - Well, this can still happen with A3C so don't think you are immune



Reference: <https://youtu.be/iCV3vOl8IMk>