

Adjacency List Representation:

- Vertex A:
 - $A \rightarrow B$ (4)
 - $A \rightarrow C$ (2)
- Vertex B:
 - $B \rightarrow C$ (5)
 - $B \rightarrow D$ (10)
- Vertex C:
 - $C \rightarrow D$ (3)
- Vertex D:
 - No outgoing edges.

Step 1: Initialization

We'll apply Dijkstra's Algorithm to find the shortest path from source vertex A to all other vertices.

Initial Setup:

- Set the distance to the source vertex A as 0, and the distance to all other vertices as ∞ .
- The graph has four vertices: A, B, C, D.

Vertex	Distance
A	0
B	∞
C	∞
D	∞

Step 2: Apply Dijkstra's Algorithm

Iteration 1: Start from Vertex A

- The current vertex is A with a distance of 0.
- Update the distances to the neighbors of A:

- o $A \rightarrow B$ (4): $\text{Distance}(B) = 0 + 4 = 4$
- o $A \rightarrow C$ (2): $\text{Distance}(C) = 0 + 2 = 2$
- **Updated Distance Table:**

Vertex	Distance
A	0
B	4
C	2
D	∞

Iteration 2: Choose the next vertex (C)

- The smallest distance among unvisited vertices is 2 (from vertex C).
- The current vertex is C with a distance of 2.
- Update the distances to the neighbors of C:
 - o $C \rightarrow D$ (3): $\text{Distance}(D) = 2 + 3 = 5$
- Updated Distance Table:

Vertex	Distance
A	0
B	4
C	2
D	5

Iteration 3: Choose the next vertex (B)

- The smallest distance among unvisited vertices is 4 (from vertex B).
- The current vertex is B with a distance of 4.
- Update the distances to the neighbors of B:
 - o $B \rightarrow C$ (5): $\text{Distance}(C) = 4 + 5 = 9$
 - o $\text{Distance}(C) = 4 + 5 = 9$ (but $\text{Distance}(C) = 2$, so no update is needed).
 - o $B \rightarrow D$ (10): $\text{Distance}(D) = 4 + 10 = 14$ (but $\text{Distance}(D) = 5$, so no update is needed).

- Updated Distance Table (no change in distances):

Vertex	Distance
A	0
B	4
C	2
D	5

Iteration 4: Choose the next vertex (D)

- The smallest distance among unvisited vertices is 5 (from vertex D), and there are no more neighbors to update.
- The algorithm terminates.

Final Shortest Distances from Source A:

Vertex	Distance from A
A	0
B	4
C	2
D	5

Conclusion

Using Dijkstra's Algorithm, we found the shortest distances from source vertex A to all other vertices:

- $A \rightarrow A$: Distance = 0
- $A \rightarrow B$: Distance = 4
- $A \rightarrow C$: Distance = 2
- $A \rightarrow D$: Distance = 5