

# RED-LE: A Revised Algorithm for Active Queue Management

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**Abstract**—The random early detection (RED) algorithm was developed in 1993. Nearly three decades later, several improved variants have been proposed by scientists. The use of a (pure) linear function for computing packet drop probability has turned out to be a disadvantage, leading to the problem of large delays. Such a problem may be addressed by using linear and non-linear (i.e. as exponential) packet drop probability functions. This paper proposes a revised RED active queue management algorithm named RED-linear exponential (RED-LE). This variant involves an interplay of linear and exponential drop functions, in order to improve the performance of the original RED algorithm. More importantly, at low and moderate network traffic loads, the RED-LE algorithm employs the linear drop action. However, for high traffic loads, RED-LE employs the exponential function for computing the packet drop probability rate. Experimental results have shown that RED-LE effectively controls congestion and offers an improved network performance under different traffic loads.

**Keywords**—active queue management, network congestion, routers, RED-LE, simulation.

## 1. Introduction

Network congestion may be described as a condition in which the amount of incoming data packets (generated traffic) is greater than the amount that the network's available resources are capable of accommodating [1]–[5]. The problem of network congestion affects the quality of service (QoS), as it leads to high packet delays, loss rates, and low throughput [2], [4], [5]–[9].

A router plays an important role in the process of controlling network congestion, as it allows to achieve improved network performance rates [9]. Router-based congestion control algorithms, such as active queue management (AQM), effectively circumvent network congestion by dropping packets at an early stage, before the buffer becomes full and sends a feed-back signal to sources in order to reduce their transmission rates [10]–[12].

The most prominent type of an AQM algorithm is random early detection (RED), developed by Floyd and Jacobson in 1993 [11]. RED continues to serve as a basis for many new AQM algorithms [12]. Upon the arrival of each packet at the router, RED updates the average queue size (denoted  $avg$ ) which is used as an indicator for congestion detection.

To perform this computation, the current status of the queue is examined.

If the router's queue is non-empty,  $avg$  value is determined using the exponential weighted moving average (EWMA) mechanism in the following manner:

$$avg = (1 - W_q)avg' + (W_q \times q_{cur}) , \quad (1)$$

where  $W_q \in [0, 1]$  represents a preset weighting factor,  $avg'$  represents the previously computed average queue size, and  $q_{cur}$  represents the current queue size.

However, if the router's queue is empty,  $avg$  is determined as:

$$avg = (1 - W_q)^n \times avg' , \quad (2)$$

with

$$n = f(q\_current\_time - q\_idle\_time) , \quad (3)$$

where  $q\_current\_time$  denotes the current time,  $q\_idle\_time$  denotes the beginning of queue idle time, and  $f(t)$  denotes a linear function of time  $t$ .

The probability of dropping a packet in RED depends on  $avg$  in the following manner:

$$P_b = \begin{cases} 0, & \text{if } avg \in [0, minTH) \\ maxP(\frac{avg - minTH}{maxTH - minTH}), & \text{if } avg \in [minTH, maxTH) \\ 1, & \text{if } avg \geq maxTH \end{cases} , \quad (4)$$

where  $minTH$  is the router's minimum queue threshold,  $maxTH$  represents the router's maximum queue threshold,  $maxP$  represents the maximum packet drop probability, and  $P_b$  stands for the initial packet dropping probability.

In RED, if  $avg \in [0, minTH)$  then no packet will be dropped and if  $avg \in [minTH, maxTH)$ , then the packets are randomly dropped with the probability of:

$$P_b = maxP(\frac{avg - minTH}{maxTH - minTH}) . \quad (5)$$

Finally, if  $avg \geq maxTH$ , then the packet is forced to be dropped, with a probability of one. The final packet drop probability  $P_a$  therefore given by:

$$P_a = \frac{P_b}{1 - count \times P_b} , \quad (6)$$

where  $count$  represents the number of packets that arrived since the last dropped packet.

There are several models in literature that modify the linear probability function of RED algorithm in an attempt to overcome its weaknesses. In this paper, another improvement-aiming modification is suggested, known as the random early detection-linear exponential (RED-LE) algorithm. The RED-LE algorithm uses both linear and exponential packet drop functions instead of a (pure) linear packet drop probability function of RED, while retaining RED's other characteristics.

The rest of the paper is organized as follows. A review of related works on the RED algorithm is provided in Section 2. A description of RED-LE is given in Section 3. The simulation configuration is presented and the results are discussed in Section 4. Finally, a brief conclusion is given in Section 5.

## 2. Related Works

To increase the throughput of RED, Floyd developed, in [13], the gentle RED (GRED) variant in which a linear function is employed to compute the packet drop probability when  $avg$  lies within the  $minTH$  and  $maxTH$  queue threshold range – Eq. (5) – while another linear function is employed to compute the packet drop probability when  $avg$  is within the  $maxTH$  and  $2 \times maxTH$  threshold range – Eq. (7):

$$P_b = maxP + (1 - maxP) \frac{avg - minTH}{maxTH} . \quad (7)$$

To ensure higher stability, Giménez *et al.* developed a new RED variety called BetaRED, which involves a beta distribution function to compute the packet drop probability instead of a linear function when  $avg$  value is within the  $minTH$  and  $maxTH$  threshold range [12].

In [14], an attempt to reduce the number of input parameters for RED was made by Abdel-Jaber, known as Exponential RED (RED-E) in which a (pure) exponential drop function given in Eq. (8) is employed to compute the packet drop probability when  $avg$  value is between the  $minTH$  and  $maxTH$  queue thresholds.

$$P_b = \begin{cases} 0, & \text{if } avg \in [0, minTH) \\ \frac{e^{avg} - e^{minTH}}{e^{maxTH} - e^{minTH}}, & \text{if } avg \in [minTH, maxTH) \\ 1, & \text{if } avg \geq maxTH \end{cases} . \quad (8)$$

To increase RED's throughput, Zhang *et al.* proposed, in [15], the MRED variety in which a quadratic function is employed to compute the packet drop probability when  $avg$  is within the  $minTH$  and  $maxTH$  queue threshold range given by Eq. (9), while a linear function is employed to compute the packet drop probability when  $avg$  is within the  $maxTH$  and  $2 \times maxTH$  queue threshold range as stated in Eq. (10).

$$P_b = maxP \frac{avg^2 - minTH^2}{maxTH^2 - minTH^2} , \quad (9)$$

$$P_b = maxP + (1 - maxP) \frac{avg - minTH}{maxTH} . \quad (10)$$

To achieve a trade-off between delay and throughput performance metrics, Paul *et al.* suggested, in [16], the Smart RED (SmRED) scheme, given in Eq. (11), in which a quadratic function is employed to compute the packet drop probability when  $avg$  lies within the  $minTH$  and  $Target$  queue threshold range, while a linear function is employed to compute the packet drop probability when  $avg$  lies within the  $Target$  and  $maxTH$  queue threshold range:

$$P_b = \begin{cases} 0, & \text{if } avg \in [0, minTH) \\ maxP \left( \frac{avg - minTH}{maxTH - minTH} \right)^2, & \text{if } avg \in [minTH, Target) \\ maxP \sqrt{\frac{avg - minTH}{maxTH - minTH}}, & \text{if } avg \in [Target, maxTH) \\ 1, & \text{if } avg \geq maxTH \end{cases} \quad (11)$$

in which

$$Target = minTH + \frac{maxTH - minTH}{2} . \quad (12)$$

In order to obtain improved throughput, Suwannapong and Khunboa developed, in [17], yet another variety of RED, named Congestion Control RED (CoCo-RED) which involves both linear and an exponential drop functions. The linear function is employed when  $avg$  value is within the  $minTH$  and  $maxTH$  queue threshold range, while the exponential function is employed when  $avg$  value is within the  $maxTH$  and  $K$  queue threshold range:

$$P_b = \begin{cases} 0, & \text{if } avg \in [0, minTH) \\ maxP \frac{avg - minTH}{maxTH - minTH}, & \text{if } avg \in [minTH, maxTH) \\ ab^{avg}, & \text{if } avg \in [maxTH, K) \end{cases} \quad (13)$$

in which

$$a = \frac{1}{\left( e^{\frac{\ln(1/maxP)}{K - maxTH}} \right)^{maxTH}} \times maxP \quad (14)$$

and

$$b = e^{\frac{\ln(1/maxP)}{K - maxTH}} . \quad (15)$$

Feng *et al.* [18] proposed a three-section RED (TRED) which employs the usage of a non-linear drop action, a linear drop action, and a non-linear drop function for low, moderate, and high buffer occupancy rates, respectively. TRED results in high throughput at high traffic loads and achieves a reduced delay at high traffic loads.

In order to increase throughput, Zhou *et al.* proposed, in [19], another variant named non-linear RED (NLRED) in which a quadratic function is employed to compute the packet drop probability when  $avg$  value is between the  $minTH$  and  $maxTH$  queue thresholds.

To reduce the packet loss rate, Kumhar *et al.* developed, in [20], quadratic RED (QRED) in which a quadratic function is deployed to compute the packet drop probability

when  $avg$  value lies within the  $minTH - maxTH$  queue threshold range:

$$P_b = \left( \frac{avg - minTH}{K - minTH} \right)^2 \quad (16)$$

or

$$P_b = 1 - \left( \frac{K - avg}{K - minTH} \right)^2, \quad (17)$$

in which  $K$  represents the buffer size.

To achieve increased throughput, Adamu *et al.* developed, in [21], the flexible RED (FXRED) algorithm. At low and moderate traffic loads, i.e. when  $avg$  value lies within the  $minTH$  and  $\Delta$  queue threshold range, FXRED uses a non-linear function to drop packets. However, at high traffic loads, i.e. when  $avg$  value lies within the  $\Delta$  and  $maxTH$  queue threshold range, FXRED switches to a linear pattern for aggressive drop action. In FXRED,  $\Delta$  was chosen in the following manner:

$$\Delta = \frac{minTH + maxTH}{2}. \quad (18)$$

Furthermore, to improve throughput performance, the self-adaptive RED (SARED) algorithm developed by Adamu *et al.* in [4] is quite similar to RED, except that either a quadratic or linear drop function is employed when  $avg$  lies within the  $minTH$  and  $maxTH$  threshold range. The quadratic drop function is employed for lower and moderate buffer occupancies, while a linear drop function is employed for higher buffer occupancies, respectively.

### 3. Random Early Detection-Linear Exponential (RED-LE)

The proposed algorithm is named random early detection-linear exponential (simply denoted by RED-LE). This revised RED algorithm involves an interplay of linear and exponential drop functions in order to increase the performance of the original RED algorithm. The improved packet drop probability is:

$$P_b = \begin{cases} 0, & \text{if } avg \in [0, minTH) \\ 2maxP \frac{avg - minTH}{maxTH - minTH}, & \text{if } avg \in [minTH, Target) \\ e^{\log(maxP) \frac{2(maxTH - avg)}{maxTH - minTH}}, & \text{if } avg \in [Target, maxTH) \\ 1, & \text{if } avg \geq maxTH \end{cases} \quad (19)$$

in which

$$Target = \frac{maxTH + minTH}{2}. \quad (20)$$

Considering the curve given in Fig. 1, RED-LE breaks the section between  $minTH$  and  $maxTH$  queue thresholds

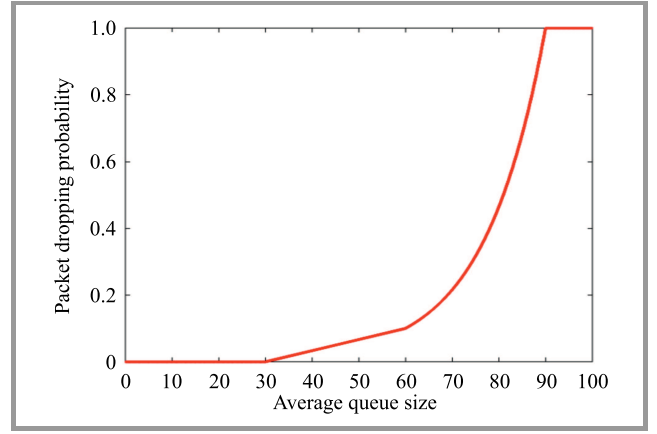


Fig. 1. RED-LE's drop probability function curve.

into two parts which include both a linear drop function and an exponential drop function, such that:

- At low and moderate traffic loads which account for cases with  $minTH \leq avg < Target$ , the packet drop function is expressed as:

$$P_b = 2maxP \frac{avg - minTH}{maxTH - minTH}. \quad (21)$$

$Target$  is a mid-point threshold defined according to Eq. (20).

- At high traffic load which account for cases where  $Target \leq avg < maxTH$ , the packet drop function is expressed as:

$$P_b = e^{\log(maxP) \frac{2(maxTH - avg)}{maxTH - minTH}}. \quad (22)$$

Using Eq. (22), a more aggressive drop action will be achieved at high load.

It is worth to mention that  $Target$  serves the purpose of distinguishing between two traffic scenarios: lower and moderate buffer occupancies, and higher buffer occupancies. A detailed pseudo-code for RED-LE is presented in Algorithm 1.

### 4. Simulations

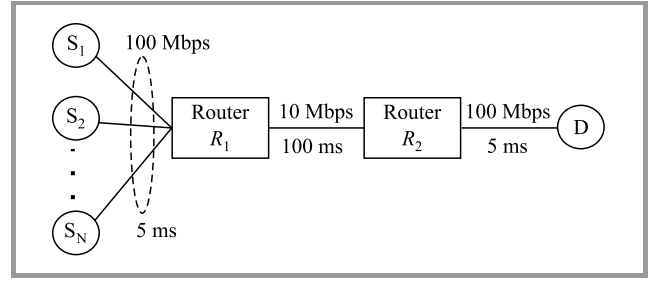
In this section, the proposed RED-LE AQM algorithm is implemented using the ns-3 simulator [22]. The effectiveness of RED-LE is evaluated and compared against two algorithms, namely TRED and RED\_E, under three different network traffic loads: low, moderate, and high. The simulation double dumbbell topology (shown in Fig. 2) consists of  $N$  TCP connecting sources transmitting to one sink (denoted by D) via two routers  $R_1$  and  $R_2$ . These two routers  $R_1$  (with the algorithm implemented) and  $R_2$  are connected together via a bottleneck link with a capacity of 10 Mbps and a propagation delay of 100 ms. Other hosts are connected to the routers via 100 Mbps links characterized by a propagation delay of 5 ms. The  $N$  number of

**Algorithm 1.** Detailed RED-LE's algorithm

```

1: Initialization:
2:  $avg = 0$ 
3:  $count = -1$ 
4: Upon every packet arrival do
5: Calculate the average queue size  $avg$ 
6: if router's queue is non-empty then
7:    $avg = (1 - W_q)avg' + (W_q \times q_{cur})$ 
8: else
9:   Compute  $n$  in which
10:   $n = f(q_{current\_time} - q_{idle\_time})$ 
11:   $avg = (1 - W_q)^n \times avg'$ 
12: end if
13: if  $avg < minTH$  then
14:   Accept the packet
15:   Set  $count = count - 1$ 
16: else if  $minTH \leq avg < Target$  then
17:   Set  $count = count + 1$ 
18:   Based on the linear drop function compute the final
   drop probability  $P_a$ :
19:    $P_b = 2maxP(\frac{avg - minTH}{maxTH - minTH})$ 
20:    $P_a = P_b / (1 - count \times P_b)$ 
21:   Drop arriving packet according to  $P_a$ 
22:   Set  $count = 0$ 
23: else if  $Target \leq avg < maxTH$  then
24:   Set  $count = count + 1$ 
25:   Based on the exponential drop function compute the
   final drop probability  $P_a$ :
26:    $P_b = e^{\log(maxP) \frac{2(maxTH - avg)}{maxTH - minTH}}$ 
27:    $P_a = P_b / (1 - count \times P_b)$ 
28:   Drop arriving packet according to  $P_a$ 
29:   Set  $count = 0$ 
30: else if  $maxTH \leq avg$  then
31:   Drop arriving packet
32:   Set  $count = 0$ 
33: end if
34: if  $count = -1$  then
35:   When the router's queue becomes empty
36:   Set  $q_{idle\_time} = q_{current\_time}$ 
37: end if
38:
39: Saved variables:
40:  $avg$ : average queue size
41:  $q_{idle\_time}$ : beginning of queue idle time
42:  $count$ : packets since last dropped packet
43:
44: Preset input parameters:
45:  $minTH$ : router's queue minimum threshold
46:  $maxTH$ : router's queue maximum threshold
47:  $maxP$ : maximum packet drop probability
48:  $W_q$ : weighting factor
49:
50: Other:
51:  $P_b$ : current packet marking probability
52:  $q_{cur}$ : current queue size
53:  $q_{current\_time}$ : current time
54:  $f(t)$ : a linear function of time  $t$ 

```

**Fig. 2.** Network topology.

flows was varied to indicate various levels of traffic loads in the network. The TCP implementation used is New Reno. The buffer size was set to 250 packets, while simulation time was set to 100 s. Other configurations are shown in Table 1.

Table 1  
Simulation setup

Input parameter	Algorithm	Value
$minTH$	TRED, RED_E & RED-LE	30 packets
$Target$	RED-LE	60 packets
$maxTH$	TRED, RED_E & RED-LE	90 packets
$maxP$	TRED & RED-LE	0.1
$W_q$	TRED, RED_E & RED-LE	0.002

**4.1. Scenario 1 – Low Load**

In this scenario, the number of connecting sources is set to 5. As shown in Fig. 3a, the RED-LE algorithm reduces the average queue size better than both TRED and RED\_E algorithms. As shown in Table 2, RED-LE reduced the queue size by 1.9437% and 14.1522% compared with TRED and RED\_E, respectively.

Delay performance is shown in Fig. 3b, RED-LE outperformed both TRED and RED\_E. As shown in Table 3, delays in RED-LE were by 0.0226% and 0.1140% shorter when compared with TRED and RED\_E, respectively.

Figure 3c shows throughput performance. RED\_E clearly outperformed both TRED and RED-LE, although the results of RED-LE were better than those of TRED. A detailed analysis is presented in Table 4.

**4.2. Scenario 2 – Moderate Load**

In this scenario, the number of connecting sources is set to 20. As shown in Fig. 4a, the proposed RED-LE algorithm is clearly more efficient at reducing the average queue size than both TRED and RED\_E algorithms. As shown in Table 2, RED-LE reduced it by 5.2565% and 29.7475% percentage decrement when compared with TRED and RED\_E, respectively.

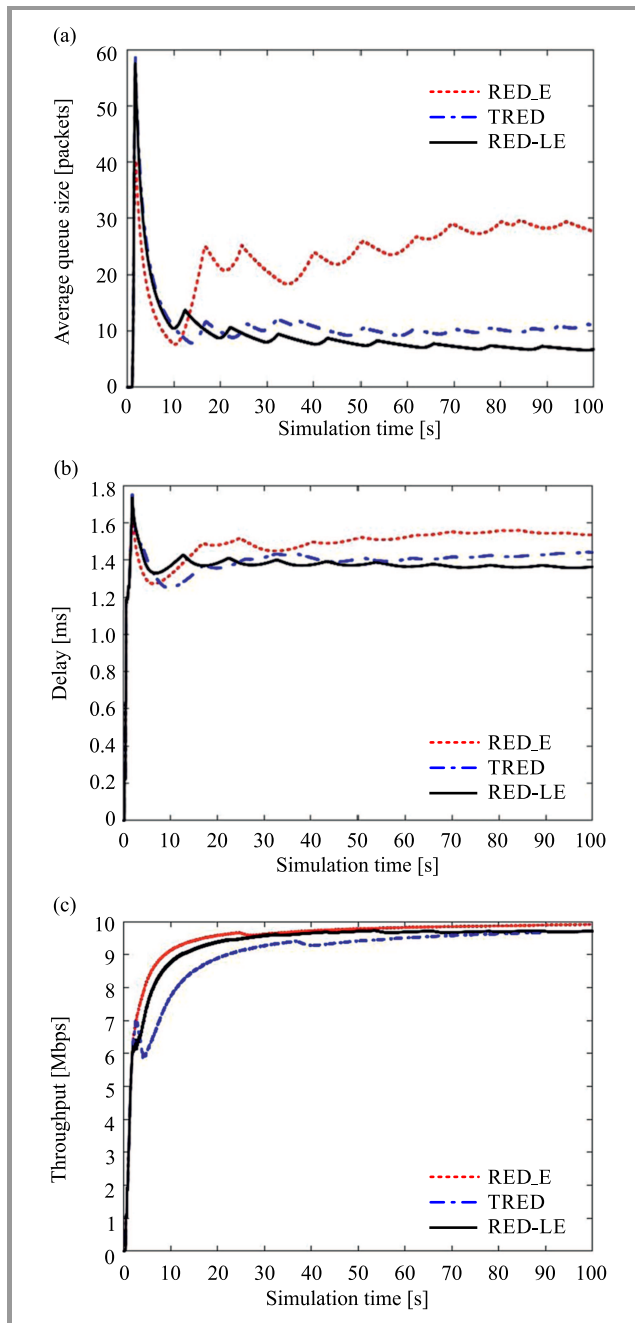
Delay performance is shown in Fig. 4b, RED-LE satisfactorily outperformed both TRED and RED\_E. As shown

Table 3

Performance in terms of delay [ms]

Traffic load	AQM algorithm		
	TRED	RED_E	RED-LE
Low	1.3918	1.4832	1.3692
Moderate	5.8040	6.4856	5.6263
High	15.2848	16.8606	14.3817

Figure 4c shows throughput performance. RED\_E clearly obtained the highest value when compared with TRED and RED-LE. An analysis is presented in Table 4.



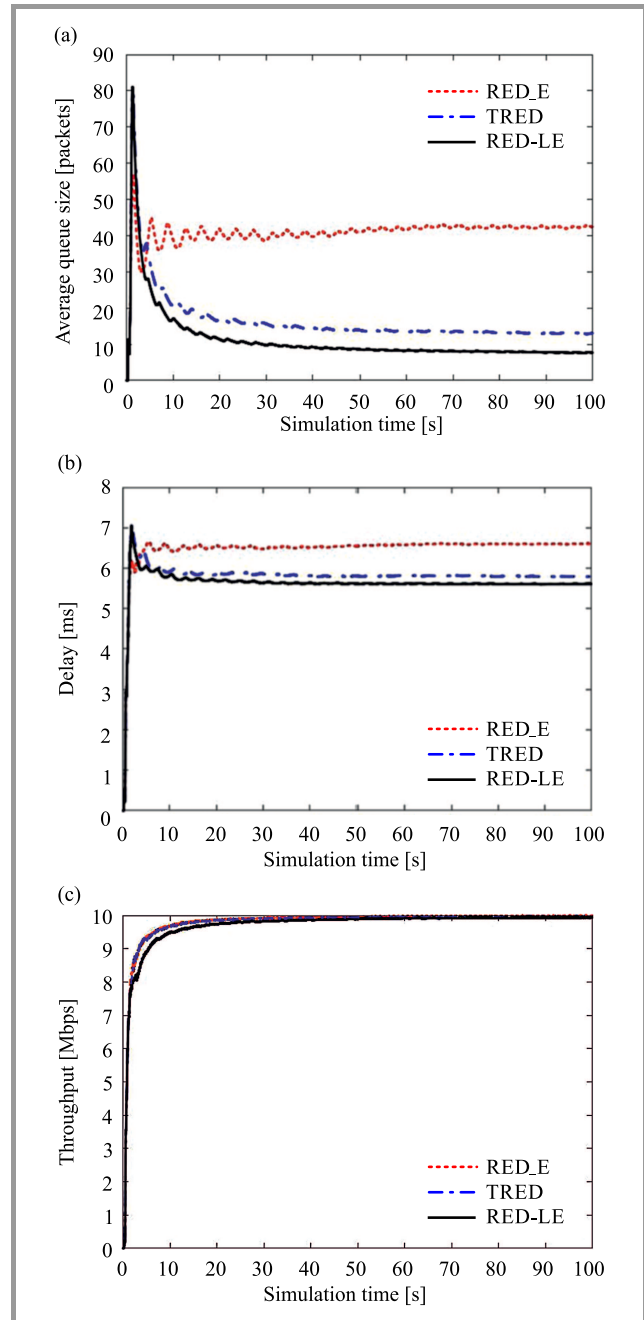
**Fig. 3.** Low load condition graphs: (a) average queue size, (b) delay, (c) throughput.

Table 2

Performance in terms of average queue size [packets]

Traffic load	AQM algorithm		
	TRED	RED_E	RED-LE
Low	11.1701	23.3786	9.2264
Moderate	16.3599	40.8509	11.1034
High	40.7549	62.0096	27.9556

in Table 3, RED-LE reduced the delay by 0.1777% and 0.8593% compared with TRED and RED\_E, respectively.



**Fig. 4.** Moderate load condition graphs: (a) average queue size, (b) delay, (c) throughput.

Table 4  
Performance in terms of throughput [Mbps]

Traffic load	AQM algorithm		
	TRED	RED_E	RED-LE
Low	9.0105	9.4899	9.3054
Moderate	9.7709	9.7915	9.6858
High	9.7917	9.8696	9.5417

#### 4.3. Scenario 3 – High Load

In this scenario, the number of connecting sources is set to 50. Again, as shown in Fig. 5a, the proposed RED-LE

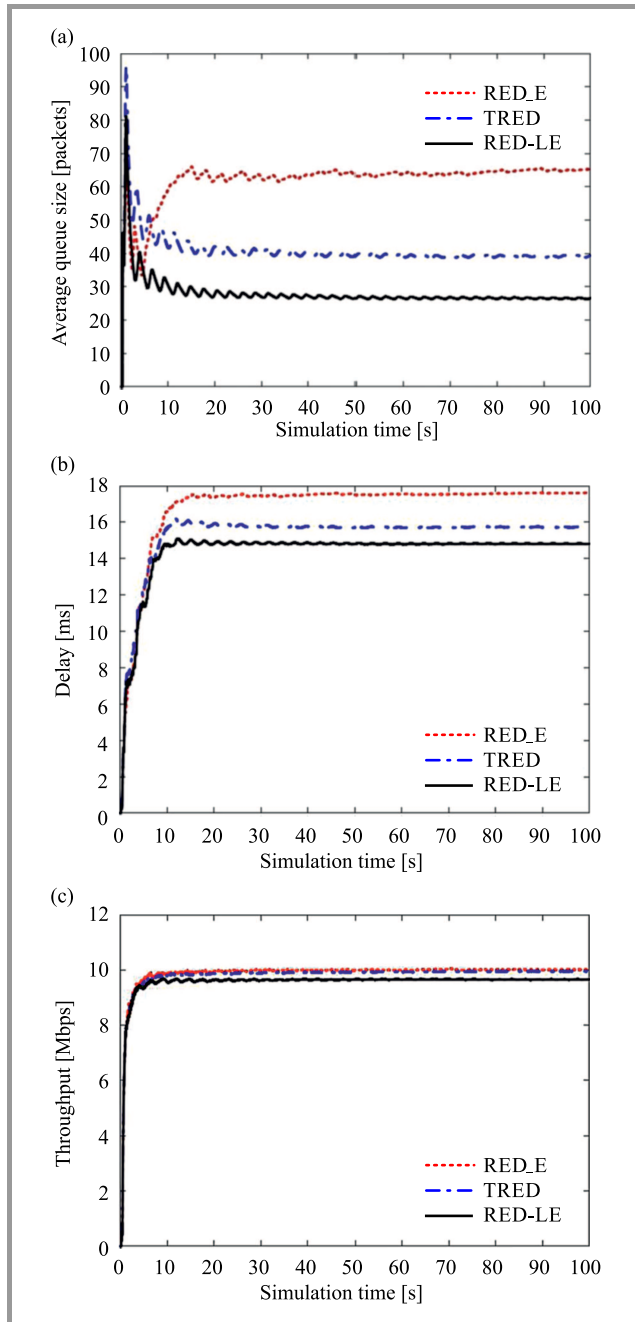


Fig. 5. High load condition graphs: (a) average queue size, (b) delay, (c) throughput.

algorithm clearly outperformed both TRED and RED\_E algorithms in terms of maintaining a small average queue size. As presented in Table 2, RED-LE reduced the queue size by 12.7993% and 34.0540% compared with TRED and RED\_E, respectively.

The delay plot for the three algorithms is shown in Fig. 5b. RED-LE clearly obtained shorter delays than both TRED and RED\_E. As presented in Table 3, RED-LE reduced them by 0.9031% and 2.4789% compared with TRED and RED\_E, respectively.

Figure 5c shows throughput performance. RED\_E obtained the highest value when compared with both TRED and RED-LE. A more detailed analysis is presented in Table 4.

## 5. Conclusion

In this study, a modest modification is introduced to the packet drop probability function of the RED algorithm. More specifically, a RED-linear exponential (RED-LE) algorithm was suggested for implementation in routers. A comparison was made between the RED-LE algorithm and two other AQM algorithms, namely TRED and RED\_E, under various traffic load scenarios in a widely-used network simulator. From experimental results, it can be concluded that RED-LE ensures better and more efficient congestion control by obtaining reduced average queue size and delay values.

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