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A Complete Guide to Stepwise Regression in R

Stepwise regression is a procedure we can use to build a regression model from a set of predictor variables by entering and removing predictors in a stepwise manner into the model until there is no statistically valid reason to enter or remove any more.

The goal of stepwise regression is to build a regression model that includes all of the predictor variables that are statistically significantly related to the response variable.

This tutorial explains how to perform the following stepwise regression procedures in R:

- Forward Stepwise Selection
- Backward Stepwise Selection
- Both-Direction Stepwise Selection

For each example we'll use the built-in mtcars dataset:

```
#view first six rows of mtcars
head(mtcars)

mpg cyl disp hp drat wt qsec vs am gear carb
Mazda RX4 21.0 6 160 110 3.90 2.620 16.46 0 1 4 4
```

```
Mazda RX4 Wag
                 21.0
                           160 110 3.90 2.875 17.02
                                                             4
                                                                  4
Datsun 710
                 22.8
                           108 93 3.85 2.320 18.61
                                                     1 1
                                                             4
                                                                  1
                 21.4
                           258 110 3.08 3.215 19.44 1
                                                                  1
Hornet 4 Drive
Hornet Sportabout 18.7
                           360 175 3.15 3.440 17.02 0 0
                                                             3
                                                                  2
                        8
Valiant
                 18.1
                        6 225 105 2.76 3.460 20.22 1 0
                                                             3
                                                                  1
```

We will fit a multiple linear regression model using *mpg* (miles per gallon) as our response variable and all of the other 10 variables in the dataset as potential predictors variables.

For each example will use the built-in step() function from the stats package to perform stepwise selection, which uses the following syntax:

step(intercept-only model, direction, scope)

where:

- intercept-only model: the formula for the intercept-only model
- direction: the mode of stepwise search, can be either "both",
 "backward", or "forward"
- scope: a formula that specifies which predictors we'd like to attempt to enter into the model

Example 1: Forward Stepwise Selection

The following code shows how to perform forward stepwise selection:

```
#define intercept-only model
intercept_only <- lm(mpg ~ 1, data=mtcars)

#define model with all predictors
all <- lm(mpg ~ ., data=mtcars)</pre>
```

```
#perform forward stepwise regression
forward <- step(intercept_only, direction='forward', scope=formula(all)</pre>
#view results of forward stepwise regression
forward$anova
            Deviance Resid. Df Resid. Dev
                                                 AIC
   Step Df
1
        NA
                  NA
                            31 1126.0472 115.94345
                            30
2
  + wt -1 847.72525
                                 278.3219 73.21736
3 + cyl -1 87.14997
                            29
                                 191.1720
                                            63.19800
  + hp -1 14.55145
                            28
                                  176.6205 62.66456
#view final model
forward$coefficients
(Intercept)
                     wt
                                cyl
 38.7517874 -3.1669731 -0.9416168 -0.0180381
```

Note: The argument trace=0 tells R not to display the full results of the stepwise selection. This can take up quite a bit of space if there are a large number of predictor variables.

Here is how to interpret the results:

- First, we fit the intercept-only model. This model had an AIC of 115.94345.
- Next, we fit every possible one-predictor model. The model that
 produced the lowest AIC and also had a statistically significant
 reduction in AIC compared to the intercept-only model used the
 predictor wt. This model had an AIC of 73.21736.
- Next, we fit every possible two-predictor model. The model that
 produced the lowest AIC and also had a statistically significant
 reduction in AIC compared to the single-predictor model added
 the predictor *cyl*. This model had an AIC of **63.19800**.

- Next, we fit every possible three-predictor model. The model that
 produced the lowest AIC and also had a statistically significant
 reduction in AIC compared to the two-predictor model added the
 predictor hp. This model had an AIC of 62.66456.
- Next, we fit every possible four-predictor model. It turned out that none of these models produced a significant reduction in AIC, thus we stopped the procedure.

The final model turns out to be:

$$mpg \sim 38.75 - 3.17*wt - 0.94*cyl - 0.02*hyp$$

Example 2: Backward Stepwise Selection

The following code shows how to perform backward stepwise selection:

```
#define intercept-only model
intercept_only <- lm(mpg ~ 1, data=mtcars)</pre>
#define model with all predictors
all <- lm(mpg ∼ ., data=mtcars)
#perform backward stepwise regression
backward <- step(all, direction='backward', scope=formula(all), trace=0</pre>
#view results of backward stepwise regression
backward$anova
    Step Df
              Deviance Resid. Df Resid. Dev
                                                 AIC
1
         NA
                    NA
                              21
                                   147.4944 70.89774
2 - cyl 1 0.07987121
                              22
                                   147.5743 68.91507
   - vs 1 0.26852280
                              23
                                   147.8428 66.97324
                                   148.5283 65.12126
4 - carb 1 0.68546077
                              24
5 - gear 1 1.56497053
                              25
                                   150.0933 63.45667
6 - drat 1 3.34455117
                              26
                                   153.4378 62.16190
                              27
                                   160.0665 61.51530
7 - disp 1 6.62865369
```

Here is how to interpret the results:

- First, we fit a model using all p predictors. Define this as M_p.
- Next, for k = p, p-1, ... 1, we fit all k models that contain all but one of the predictors in M_k, for a total of k-1 predictor variables.
 Next, pick the best among these k models and call it M_{k-1}.
- Lastly, we pick a single best model from among M₀...M_p using AIC.

The final model turns out to be:

Example 3: Both-Direction Stepwise Selection

The following code shows how to perform both-direction stepwise selection:

```
#define intercept-only model
intercept_only <- lm(mpg ~ 1, data=mtcars)

#define model with all predictors
all <- lm(mpg ~ ., data=mtcars)

#perform backward stepwise regression
both <- step(intercept_only, direction='both', scope=formula(all), trace
#view results of backward stepwise regression</pre>
```

```
both$anova
            Deviance Resid. Df Resid. Dev
                                                 AIC
   Step Df
1
                            31 1126.0472 115.94345
        NA
                  NA
2
  + wt -1 847.72525
                            30
                                 278.3219
                                           73.21736
3 + cyl -1 87.14997
                            29
                                 191.1720
                                            63.19800
  + hp -1
                                 176.6205
            14.55145
                            28
                                            62.66456
#view final model
both$coefficients
(Intercept)
                     wt
                                cyl
                                              hp
 38.7517874 -3.1669731 -0.9416168 -0.0180381
```

Here is how to interpret the results:

- First, we fit the intercept-only model.
- Next, we added predictors to the model sequentially just like we
 did in forward-stepwise selection. However, after adding each
 predictor we also removed any predictors that no longer provided
 an improvement in model fit.
- · We repeated this process until we reached a final model.

The final model turns out to be:

Note that forward stepwise selection and both-direction stepwise selection produced the same final model while backward stepwise selection produced a different model.

Additional Resources

How to Test the Significance of a Regression Slope How to Read and Interpret a Regression Table A Guide to Multicollinearity in Regression