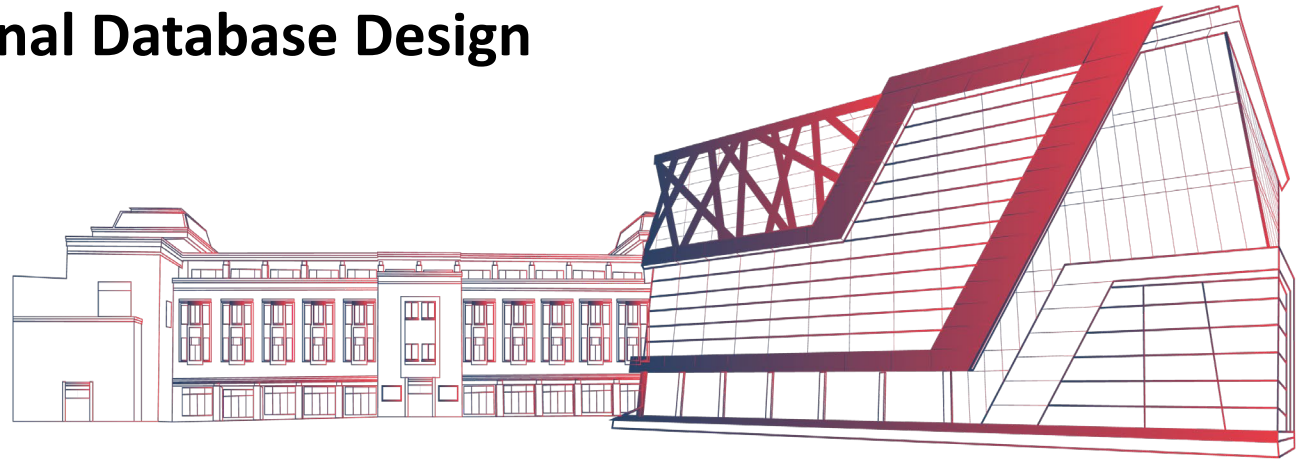


UNIT III

Relational Database Design



Decomposition to Higher Normal Forms

Decomposition to Higher Normal Form Example

Consider a relation with schema $R(A,B,C,D)$ and FDs $\{AB \rightarrow C, C \rightarrow D, D \rightarrow A\}$.

- Indicate all BCNF violations for R.
- Decompose the relations into collections of relations that are in BCNF.

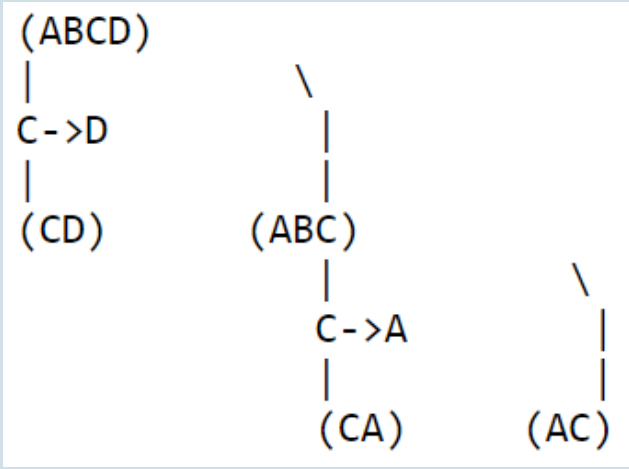
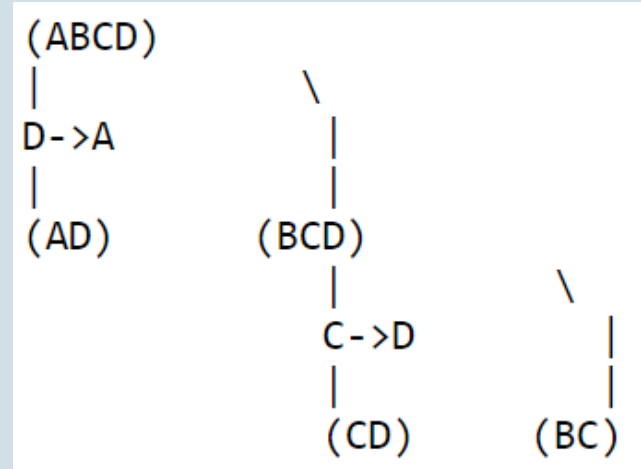
Solution: Attribute closure:

$A \rightarrow A$	$B \rightarrow B$	$C \rightarrow ACD$	$D \rightarrow AD$
$AB \rightarrow ABCD$	$AC \rightarrow ACD$	$AD \rightarrow AD$	$BC \rightarrow ABCD$
$BD \rightarrow ABCD$	$CD \rightarrow ACD$	$ABC \rightarrow ABCD$	
$ABD \rightarrow ABCD$	$ACD \rightarrow ACD$	$BCD \rightarrow ABCD$	

Thus, the candidate keys are: AB, BC, and BD

Decomposition to Higher Normal Form Example

- $C \rightarrow D$ and $D \rightarrow A$ are violating BCNF
- Decompose the relations into collections of relations that are in BCNF.

Case 1	Case 2
 <p>R1(CD), R2(AC) and R3(BC) but $D \rightarrow A$ and $AB \rightarrow C$ are not preserved</p>	 <p>R1(AD), R2(CD) and R3(BC) but $AB \rightarrow C$ is not preserved</p>

Decomposition to Higher Normal Form Drill

Decompose to highest normal form while satisfying lossless join and dependency preservation properties:

1. Relation R (ABCDE)

$F = \{ AB \rightarrow C, C \rightarrow D, B \rightarrow E \}$

2. Relation R (ABCDEFGHIJ)

$F = \{ AB \rightarrow C, C \rightarrow D, A \rightarrow E, E \rightarrow FG, B \rightarrow H, H \rightarrow IJ \}$

3. Relation R (ABC)

$F = \{ AB \rightarrow C, C \rightarrow A \}$



Solution - Decomposition to Higher Normal Form Drill

1. Relation R (ABCDE)

$F = \{ AB \rightarrow C, C \rightarrow D, B \rightarrow E \}$

$AB^+ = A, B, C, D, E$

$A^+ = A$

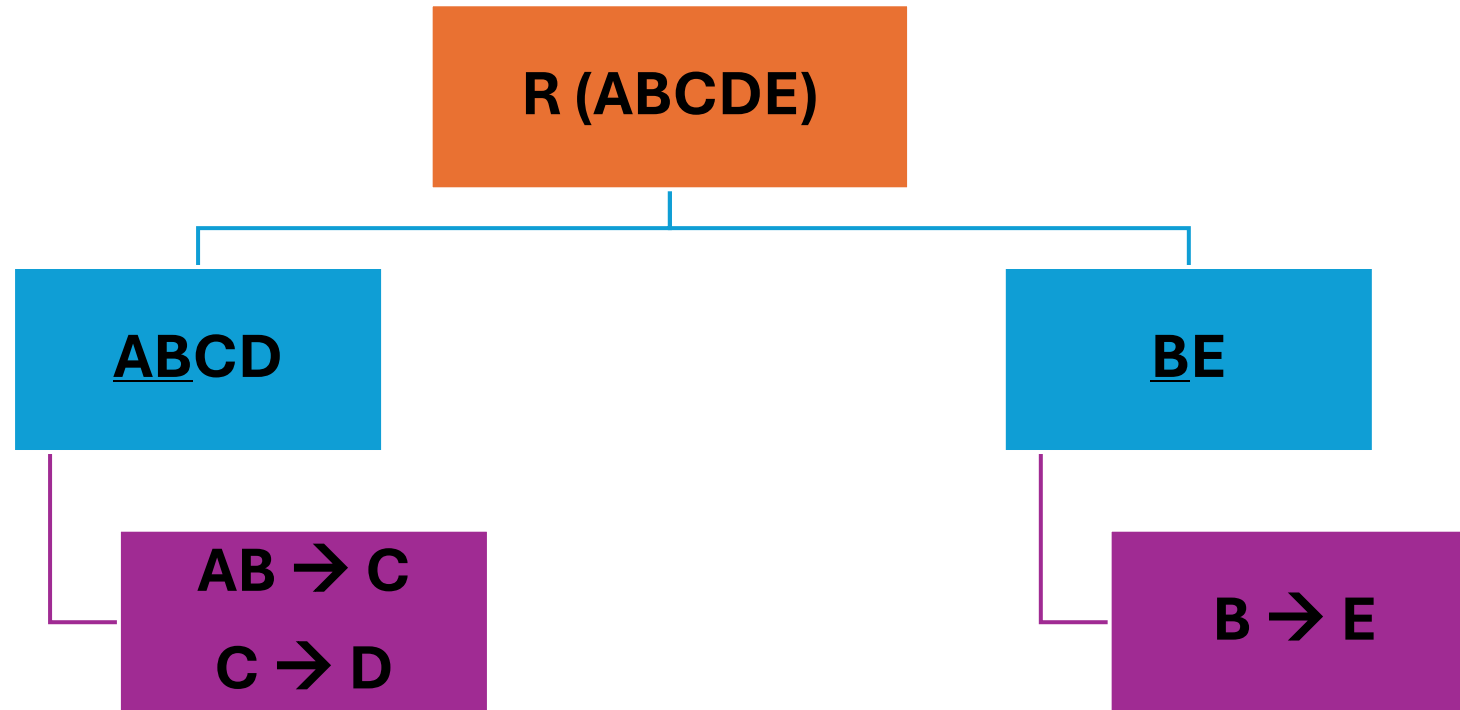
$B^+ = B, E$

FD	$AB \rightarrow C$	$C \rightarrow D$	$B \rightarrow E$
BCNF	✓	X	X
3NF	✓	X	X
2NF	✓	✓	X
1NF	✓	✓	✓

The table is currently in 1NF but not in 2NF because of partial dependency $B \rightarrow E$

Solution - Decomposition to Higher Normal Form Drill (Cont.)

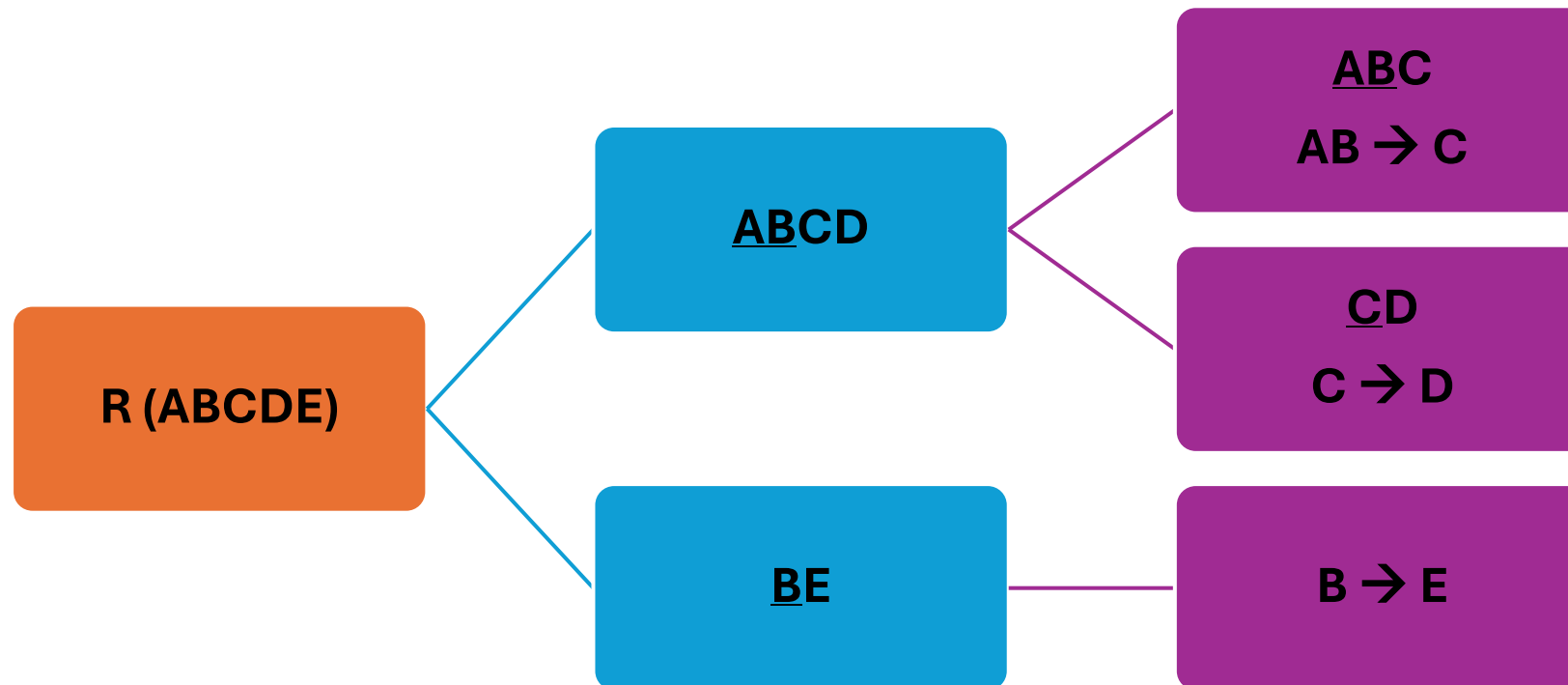
- 2NF Decomposition



2NF, Lossless Join and Dependency Preservation satisfied

Solution - Decomposition to Higher Normal Form Drill (Cont.)

- 3NF Decomposition



3NF, BCNF, Lossless Join and Dependency Preservation satisfied

Solution - Decomposition to Higher Normal Form Drill (Cont.)

2. Relation R (ABCDEFGHIJ)

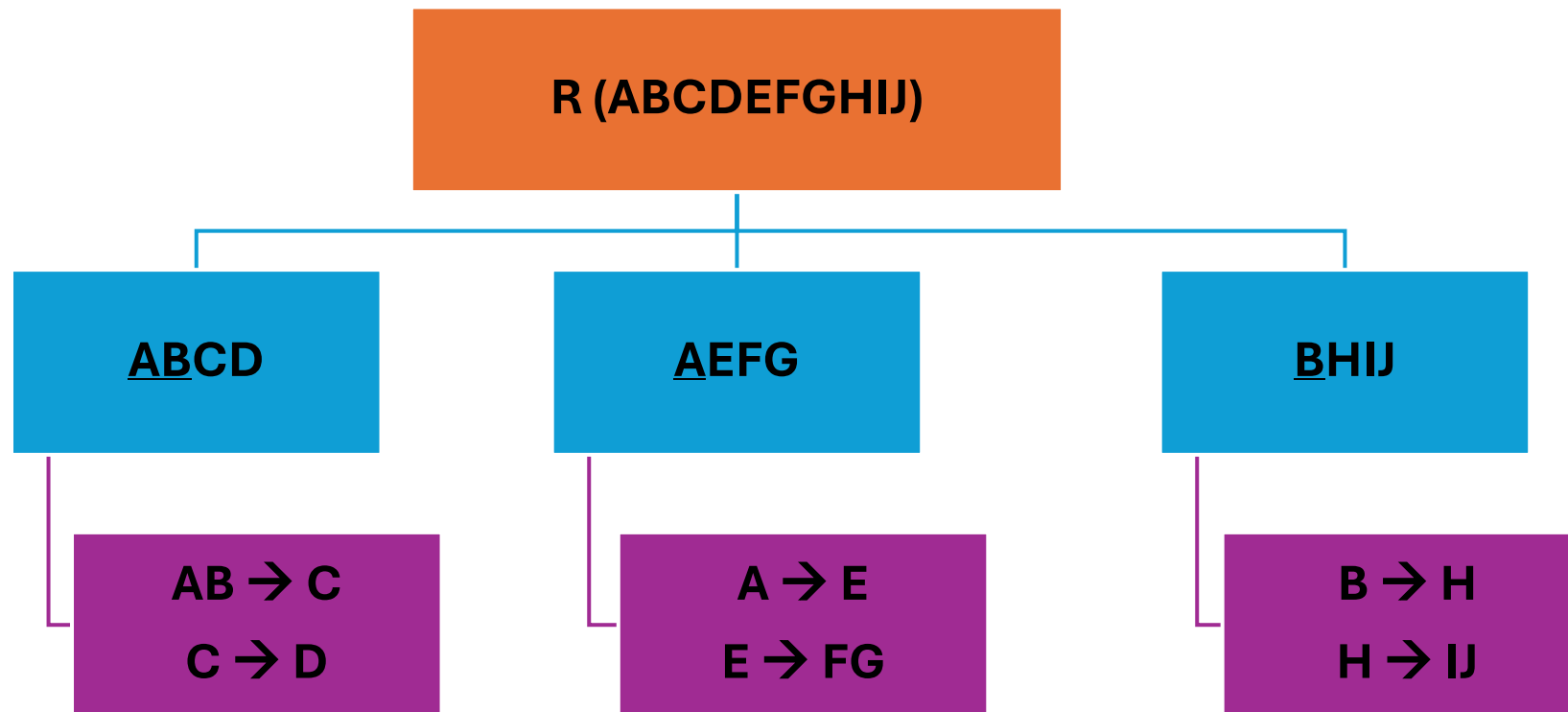
$F = \{ AB \rightarrow C, C \rightarrow D, A \rightarrow E, E \rightarrow FG, B \rightarrow H, H \rightarrow IJ \}$

$AB^+ = A, B, C, D, E, F, G, H, I, J$

FD	$AB \rightarrow C$	$C \rightarrow D$	$A \rightarrow E$	$E \rightarrow FG$	$B \rightarrow H$	$H \rightarrow IJ$
BCNF	✓	X	X	X	X	X
3NF	✓	X	X	X	X	X
2NF	✓	✓	X		X	

Solution - Decomposition to Higher Normal Form Drill (Cont.)

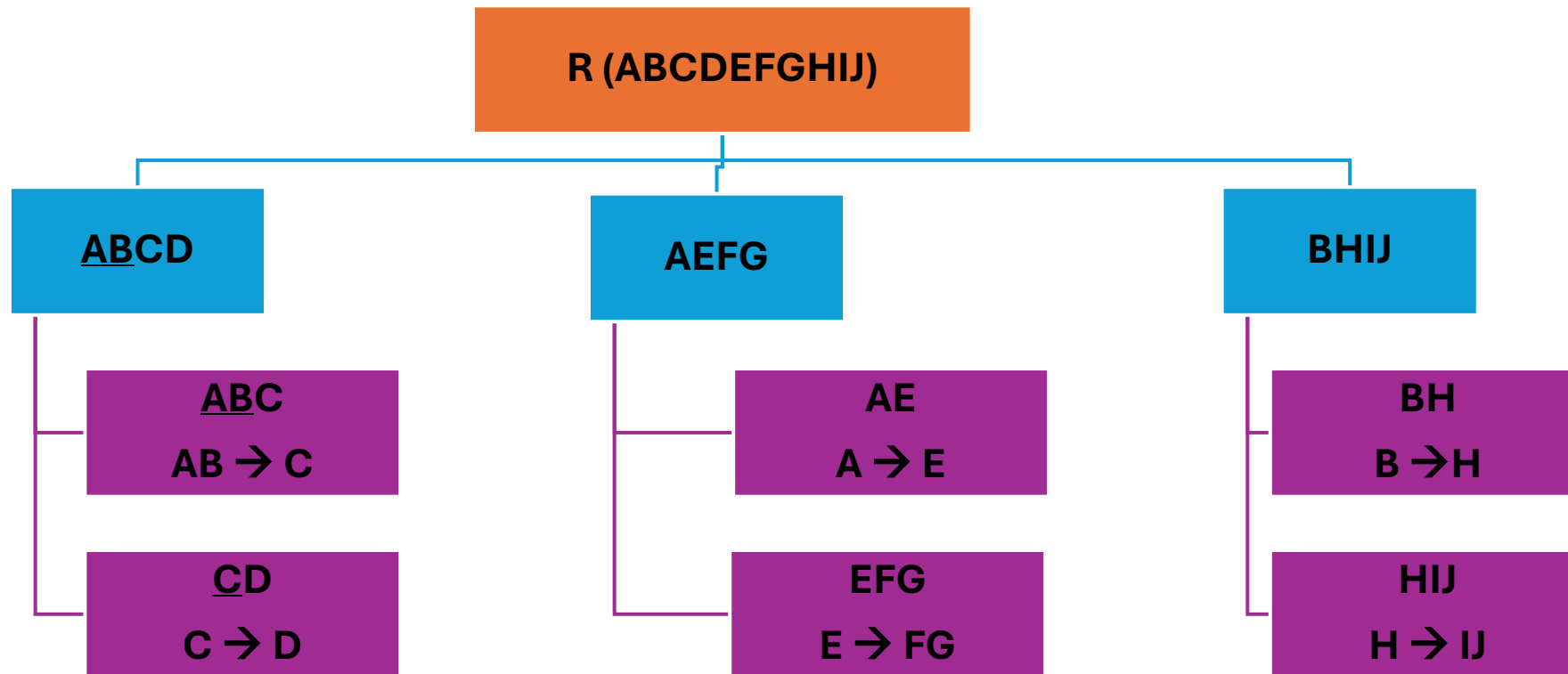
- 2NF Decomposition



2NF, Lossless Join and Dependency Preservation satisfied

Solution - Decomposition to Higher Normal Form Drill (Cont.)

- 3NF Decomposition



3NF, BCNF, Lossless Join and Dependency Preservation satisfied

Solution - Decomposition to Higher Normal Form Drill (Cont.)

3. Relation R (ABC)

$$F = \{ AB \rightarrow C, C \rightarrow A \}$$

$$AB^+ = A, B, C$$

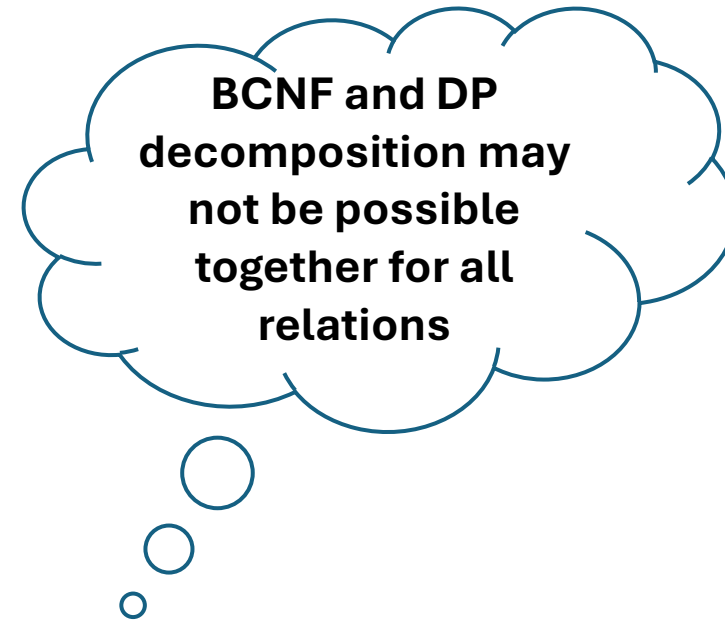
$$CB^+ = B, C, A$$

The relation is in 3NF but not BCNF

Case1: If R1 (BC) and R2 (AC)

Lossless Join Decomposition and BCNF are satisfied but dependency preservation is violated.

Case 2: If we decompose such that dependency preservation and lossless join is satisfied, then BCNF is not satisfied.



Normalization Summary

DB Design Goal	1NF	2NF	3NF	BCNF
Achieve 0% Redundancy	X	X	X	✓ (over FDs)
LLJ Satisfied	✓	✓	✓	✓
DP Satisfied	✓	✓	✓	X✓

Best accurate form is 3NF because dependency preservation and lossless join properties are more important

Multi-valued Dependency (MVD)

A **multi-valued dependency (MVD)** $X \twoheadrightarrow Y$ specified on relation schema R , where X and Y are both subsets of R , specifies the following constraint:

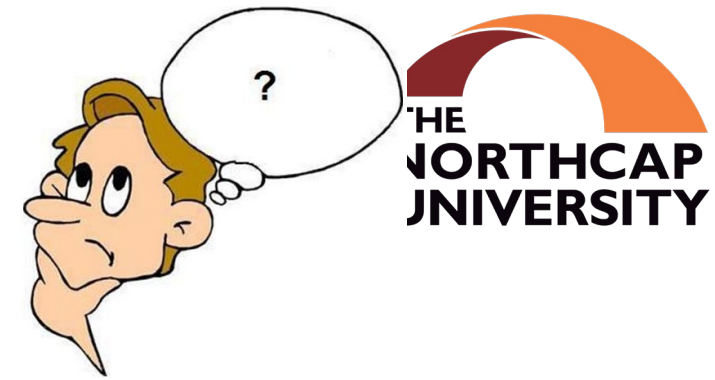
If two tuples t_1 and t_2 exist in R such that $t_1[X] = t_2[X]$, then two tuples t_3 and t_4 should also exist in R with the following properties, where we use Z to denote $(R - (X \cup Y))$:

$$t_4[X] = t_3[X] = t_1[X] = t_2[X]$$

$$t_3[Y] = t_1[Y] \text{ and } t_4[Y] = t_2[Y]$$

$$t_3[Z] = t_2[Z] \text{ and } t_4[Z] = t_1[Z]$$

MVD Example



Student

StudentName	CourseDiscipline	Activities
Amit	Mathematics	Singing
Akash	Mathematics	Dancing
Yuvraj	Computers	Cricket
Akash	Mathematics	Singing
Akash	Literature	Dancing
Akash	Literature	Singing

Therefore, multivalued dependency:

StudentName \twoheadrightarrow CourseDiscipline

StudentName \twoheadrightarrow Activities

MVD Rules



- **Complementation:** If $X \twoheadrightarrow Y$, and Z is all the other attributes i.e. $Z = (R - (X \cup Y))$, then $X \twoheadrightarrow Z$.

Eg. $R(ABCD)$ if $A \twoheadrightarrow B$ then, $A \twoheadrightarrow CD$

- **Trivial MVD:** An MVD $X \twoheadrightarrow Y$ in R is called a **trivial MVD** if

(a) Y is a subset of X , or (b) $X \cup Y = R$

Eg. $R(ABCD) \{ AB \twoheadrightarrow A, AB \twoheadrightarrow CD \}$ Trivial MVD

$\{ AB \twoheadrightarrow C \}$

Non-trivial MVD

- **Split/ Merge:** Non-trivial MVDs are not allowed to split or merge unlike FDs

Eg. $[X \twoheadrightarrow YZ] \neq [X \twoheadrightarrow Y, X \twoheadrightarrow Z]$

$[X \rightarrow YZ] = [X \rightarrow Y, X \rightarrow Z]$

Fourth Normal Form

A relational schema R is in 4NF iff

a) X is superkey in every non-trivial FD $X \rightarrow Y$ in R (i.e. BCNF)

and

b) X is superkey in every non-trivial MVDs $X \twoheadrightarrow Y$

Non-trivial FD

$X \rightarrow Y$

X: superkey

and

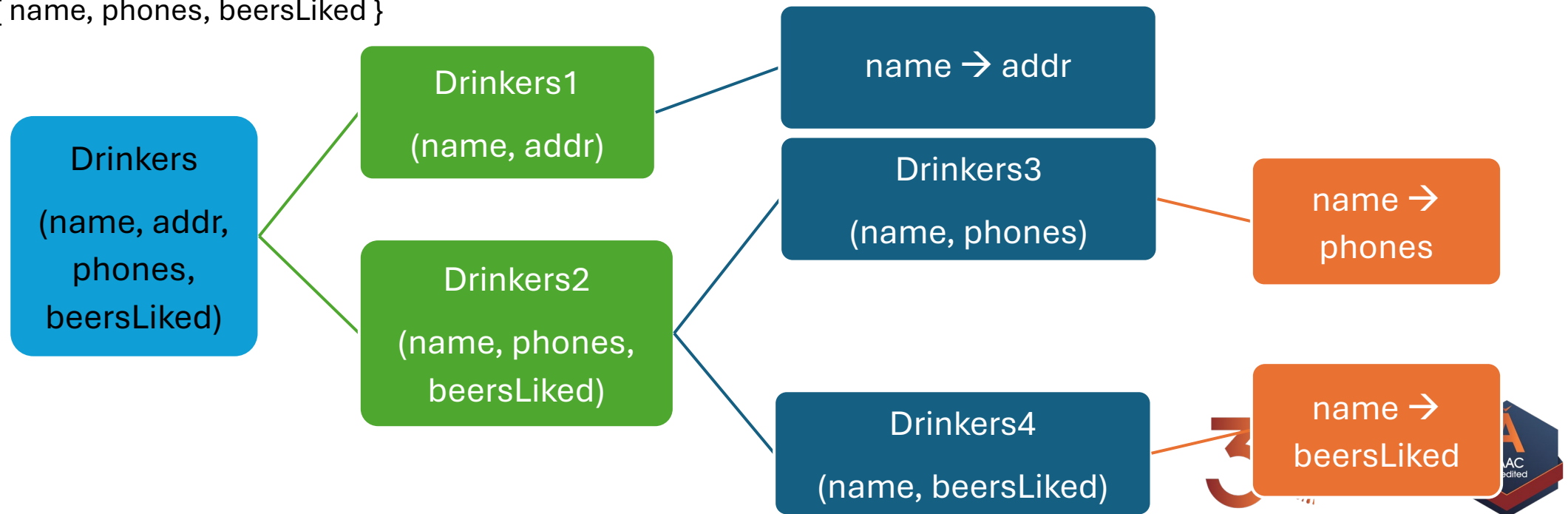
Non-trivial MVD

$X \twoheadrightarrow Y$

X: superkey

Fourth Normal Form Example

- **Relation Drinkers(name, addr, phones, beersLiked)**
- FD: name \rightarrow addr
- MVD's: name $\rightarrow\rightarrow$ phones
name $\rightarrow\rightarrow$ beersLiked
- Key is { name, phones, beersLiked }



Fifth (Project - join) Normal Form (PJNF)

A relational schema R is in 5NF iff

a) It is in 4NF

and

b) Does not have any join dependency and joining should satisfy lossless decomposition i.e. the decomposed sub-relations can be joined in any order and all joins should be lossless.



Normalization Summarization

PROS

Removes data redundancy

Solves INSERT, UPDATE, and DELETE anomalies

This makes it easier to maintain the information in the database in a consistent state

CONS

It leads to more tables in the database

More join operations needed to retrieve information from tables which is expensive to do

Database speed is bit slow because SELECT and JOINS are processed

Thanks!!