

```

1 (* Exercise 1 *)
2 (* Write a function il2r1 of type int list -> real list that takes a list of integers and returns a list of the same numbers converted to type real. *)
3 fun il2r1 lst = map Real.fromInt lst;
4
5 (* Exercise 2 *)
6 (* Write a function ordlist of type char list -> int list that takes a list of characters and returns the list of the integer codes of those characters. *)
7 fun ordlist lst = map Char.ord lst;
8
9 (* Exercise 3 *)
10 (* Write a function squarelist of type int list -> int list that takes a list of integers and returns the list of the squares of those integers. *)
11 fun squarelist lst = map (fn x => x * x) lst;
12
13 (* Exercise 4 *)
14 (* Write a function multpairs of type (int * int) list -> int list that takes a list of pairs of integers and returns a list of the products of each pair. *)
15 fun multpairs lst = map (fn (a, b) => a * b) lst;
16
17 (* Exercise 5 *)
18 (* Write a function inclist of type int list -> int -> int list that takes a list of integers and an integer increment, and returns the same list of integers but with the integer increment added to each. *)
19 fun inclist lst n = map (fn x => x + n) lst;
20
21 (* Exercise 6 *)
22 (* Write a function sqsum of type int list -> int that takes a list of integers and returns the sum of the squares of those integers. *)
23 fun sqsum lst = foldr (op +) 0 (map (fn x => x * x) lst);
24
25 (* Exercise 7 *)
26 (* Write a function bor of type bool list -> bool that takes a list of boolean values and returns the logical OR of all of them. If the list is empty, your function should return false. *)
27 fun bor lst = foldr (fn (a, b) => a orelse b) false lst;
28
29 (* Exercise 8 *)
30 (* Write a function band of type bool list -> bool that takes a list of boolean values and returns the logical AND of all of them. If the list is empty, your function should return true. *)
31 fun band lst = foldr (fn (a, b) => a andalso b) true lst;
32
33 (* Exercise 9 *)
34 (* Write a function bxor of type bool list -> bool that takes a list of boolean values and returns the logical exclusive OR of all of them. If the list is empty, your function should return false. *)
35 fun bxor lst = foldr (fn (a, b) => if a = b then false else true) false lst;
36
37 (* Exercise 10 *)
38 (* Write a function dupList of type 'a list -> 'a list whose output list is the same as the input list, but with each element of the input list repeated twice in a row. *)
39 fun dupList lst = foldr (fn (a, b) => a::a::b) [] lst;
40

```

```

41 (* Exercise 11 *)
42 (* Write a function mylength of type 'a list -> int that returns the length of a list. *)
43 fun mylength lst = foldr (fn (a, b) => b + 1) 0 lst;
44
45 (* Exercise 12 *)
46 (* Write a function il2absr1 of type int list -> real list that takes a list of integers and returns a list containing the absolute values of those integers, converted to real. *)
47 fun il2absr1 lst = map Real.fromInt (map Int.abs lst);
48
49 (* Exercise 13 *)
50 (* Write a function truecount of type bool list -> int that takes a list of boolean values and returns the number of trues in the list. *)
51 fun truecount lst = foldr (fn (a, b) => if a then b + 1 else b) 0 lst;
52
53 (* Exercise 14 *)
54 (* Write a function maxpairs of type (int * int) list -> int list that takes a list of pairs of integers and returns the list of the max elements from each pair. *)
55 fun maxpairs lst = map (fn (a, b) => if a > b then a else b) lst;
56
57 (* Exercise 15 *)
58 (* Write a function implode that works just like the predefined implode. *)
59 fun implode lst = foldr (fn (a, b) => (Char.toString a) ^ b) "" lst;
60
61 (* Exercise 16 *)
62 (* Write a function lconcat of type 'a list list -> 'a list that takes a list of lists as input and returns the list formed by appending the input lists together in order. *)
63 fun lconcat lst = foldr (fn (a, b) => a @ b) [] lst;
64
65 (* Exercise 17 *)
66 (* Write a function max of type int list -> int that returns the largest element of a list of integers. *)
67 fun max lst = foldr (fn (a, b) => Int.max (a, b)) (hd lst) lst;
68
69 (* Exercise 18 *)
70 (* Write a function min of type int list -> int that returns the smallest element of a list of integers. *)
71 fun min lst = foldr (fn (a, b) => Int.min (a, b)) (hd lst) lst;
72
73 (* Exercise 19 *)
74 (* Write a function member of type 'a * 'a list -> bool so that member(e,L) is true if and only if e is an element of list L. *)
75 fun member (n, lst) = foldr (fn (a, b) => if b orelse a = n then true else false) false lst;
76
77 (* Exercise 20 *)
78 (* Write a function append of type 'a list -> 'a list -> 'a list that takes two lists and returns the result of appending the second one onto the end of the first. *)
79 fun append lst1 lst2 = foldr (fn (a, b) => a::b) lst2 lst1;
80
81 (* Exercise 21 *)
82 (* Define a function less of type int * int list -> int list so that less(e,L) is a list of all the integers in L that are less than e. *)
83 fun less (n, lst) = foldr (fn (a, b) => if a < n then a::b else b) [] lst;
84
85 (* Exercise 22 *)
86 (* Write a function evens of type int list -> int list that takes a list of integers and returns the list of all the even elements from the original list (in the original order). *)
87 fun evens lst = foldr (fn (a, b) => if a mod 2 = 0 then a::b else b) [] lst;
88
89 (* Exercise 23 *)
90 (* Write a function convert of type ('a * 'b) list -> 'a list * 'b list, that converts a list of pairs into a pair of lists, preserving the order of the elements. *)
91 fun convert lst = foldr (fn ((a, b), (c, d)) => (a::c, b::d)) ([], []) lst;
92
93 (* Exercise 24 *)
94 (* Define a function mymap with the same type and behavior as map, but without using map. *)
95 fun mymap f lst = foldr (fn (a, b) => f a::b) [] lst;
96
97 (* Exercise 25 *)
98 (* Represent a polynomial using a list of its (real) coefficients, starting with the constant coefficient and going only as high as necessary. Write a function eval of type real -> real. *)
99 fun eval [] x = 0.0
100 | eval (head::tail) x = real + eval (map (fn y => x * y) tail) x;
101
102 (* Exercise 26 *)
103 (* Define a function mymap2 with the same type and behavior as map. *)
104 fun mymap2 _ [] = []
105 | mymap2 f (head::tail) = f head::mymap2 f tail;
106
107 (* Exercise 27 *)
108 (* Define a function myfoldr with the same type and behavior as foldr. *)
109 fun myfoldr _ x [] = x
110 | myfoldr f x [head] = f (head, x)
111 | myfoldr f x (head::tail) = f (head, (myfoldr f x tail));
112
113 (* Exercise 28 *)
114 (* Define a function myfoldl with the same type and behavior as foldl. *)
115 fun myfoldl _ x [] = x
116 | myfoldl f x (head::tail) = myfoldl f (f (head, x)) tail;

```

Second Part:

```
1 (* Exercise 2 *)
2 (* Define a function member of type 'a * 'a list -> bool so that member(e,L) is true if and only if e is an element of the list L. *)
3 fun member (n, []) = false
4 | member (n, head::tail) =
5     if n = head then true
6     else member (n, tail);
7
8 (* Exercise 3 *)
9 (* Define a function less of type int * int list -> int list so that less(e,L) is a list of all the integers in L that are less than e. *)
10 fun less (n, []) = []
11 | less (n, head::tail) =
12     if head < n then head::less (n, tail)
13     else less (n, tail);
14
15 (* Exercise 4 *)
16 (* Define a function repeats of type 'a list -> bool so that repeats(L) is true if and only if the list L has two equal elements next to each other. *)
17 fun repeats [] = false
18 | repeats [a] = false
19 | repeats (a::b::tail) =
20     if a = b then true else repeats (b::tail);
21
22 (* Exercise 5 *)
23 (* Represent a polynomial using a list of its (real) coefficients, starting with the constant coefficient and going only as high as necessary. Write a function eval of type real * real list -> real *)
24 fun eval ([], _) = 0.0
25 | eval (head::tail, x) =
26     let
27         fun evalHelper ([], _) = 0.0
28         | evalHelper (head::tail, x) =
29             x * head + evalHelper (tail, x * x);
30     in
31         head + evalHelper (tail, x)
32     end;
33
34
35
36
37
38
39
40
41
42
43
44
45
46
47
48
49
50
51
52
53
54
55
56
57
58 (* In the following exercises, implement sets as lists. *)
59 (* Exercise 8 *)
60 (* Write a function to test whether an element is a member of a set. *)
61 fun memberSet ([], _) = false
62 | memberSet (head::tail, element) =
63     if head = element then true
64     else memberSet (tail, element);
```

Week 4 Assignment > quicksort.sml

```
1 fun partition (pivot, nil) = (nil, nil)
2 | partition (pivot, target::rest) =
3     let
4         val (small, big) = partition(pivot, rest)
5     in
6         if target < pivot
7         then (target::small, big)
8         else (small, target::big)
9     end
10
11 fun quicksort nil = nil
12 | quicksort [a] = [a]
13 | quicksort (first::rest) =
14     let
15         val (lessthan, greater) = partition(first, rest)
16     in
17         quicksort(lessthan) @ [first] @ quicksort(greater)
18     end
19
```

Week 4 Assignment > ≡ intersectConstruct2.sml

```
1 fun isMember ([], _) = false
2 | isMember (head::tail, element) =
3 |     if head = element then
4 |         true
5 |         else isMember (tail, element)
6
7 fun intersection([], y) = []
8 | intersection(first::rest, y) =
9 |     if isMember(y, first) then
10 |         first :: intersection(rest, y)
11 |         else intersection(rest, y)
```

Union Constructor (incomplete)

Week 4 Assignment > ≡ unionConstructor2.sml

```
1 fun isMember ([], _) = false
2 | isMember (head::tail, element) =
3 |     if head = element then
4 |         true
5 |         else isMember (tail, element)
6
7 fun unionConstructor ([], y) = y
8 | unionConstructor (first::rest, y) =
9 |     if isMember(y, first) then
10 |         union(y, rest)
11 |         else first::union(rest, y)
12
13
```

(* Exercise 11 *)

(* Write a function to construct the powerset of any set. *)

```
fun consPowerset [] = [[]]
| consPowerset (head::tail) =
    let
        fun powersetHelper ([], element) = [[]]
        | powersetHelper ([]:tail, element) = [[element]]@powersetHelper (tail, element)
        | powersetHelper (head::tail, element) = [head, head@element]@powersetHelper (tail, element);
    in
        powersetHelper (consPowerset tail, head)
    end;
```