LAST TIME: HWS #1

THIS WEEK: A ANALYSIS CRASH COURSE

> MON: DIS SECTION?

WHERE ARE WE GOING WI THIS?

Mull koop Mull koop Mull koop

MAIN GOAL: a CONTOUR INTEGRATION

Swy? powerful tool for doing difficult integrals... IN PARTICULAR, THOSE THE SHOW UP IN GREEN'S PUNCTION ESULATIONS

HWIS LECT APPEL CHI-4 J MY 2016 NOTES

(1 SHOULD REVIEW) = WHY (3(x,y) = (3 (x-y). 与 Lx G(x,y) = S(x-y) ? EPn(x)(量)ⁿ

then LxG(x,y) = [dk eik G(k) dk

= [eik(x,y)] dk

BECOMES ALGEBRAIC

PROBLEM TO SOLVE FOR

CONDUCT MY!

SCIENT BUT TRICKY INTEGRAL

TO GET GILX, Y)

OTHER REASONS WHY THIS IS WORTHWHILE

NATURE "KNOWS" ABOUT @ #s!

> ANALYTICITY ("good behavior") is IMPORTANT IN PHYSICS

eally rest on we sometime of causality in dispersion Relations

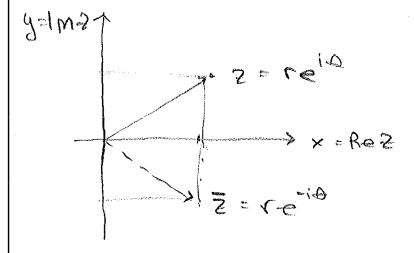
eally rest observation. So we so causality in dispersion Relations

eq conformal mapping: see EAM

(

COMPLEX VARIABLES

 $Z = \times + iy$ $Z = \times + iy$



COMPLEX FUNCTIONS: $f(x,y) \leftrightarrow f(z,z)$ "

THERE IS AN IMPORTANT SENSE OF NICENESS:

ANALYTIC: f has well defined derivative

I many of you already know the punchance

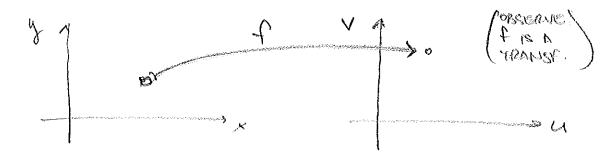
that this boils down to f = f(z)"

Conly.

"nice": the kind of quantity that describes
actual physical quantities

Cel extractory smooth, Differentiable...

"MER DEL DEGNALINE", RS MUST could do



A @ Aunction f(x,y) = u(x,y) + iv(x,y)

IS a MAP from C - C. CAN "DO CALCULUS!

BECAUSE ON RE IS A 2D SPACE, WE CAN EXAMINE INFINITESIMAL CHANGES IN DIFFERENT BIRECTIONS ON DIFFERENT

BUT IN SOME SENSE, OF IS A ONE DIMENSIONAL

of is the gernative

5>50 5-50 P5 1/M +15-7150 P5

supply in whotever 25 you want, supply the man big your

WHAT COUND GO MEDING?

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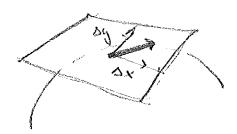
onyway: [4f(82)]

is a machine that takes rectors in Tr. 0 ('Velocities' from 20) }

returns a #.

AS YOU KNOW, SINCE AFLED & TX C, - DUAL SPACE IT IS A LINEAR MAR

df(2.) [sx1isy] = f'(2.) (2.) (2) (2)



BUT WE MSO KNOW

$$|Af|_{2} = \frac{3}{2} |x|_{2} \times + \frac{3}{2} |x|_{2} \times (1)$$

COMPARING (3) WITH (X):

recolling f= u + IV

CANOHY-RIEMANN

CAUCHY-RIEMANN (OR) (DIFFERENTIABLE

WE USED (DX, DY) AS A BASIS FOR TECT

the infinitesimal "velocity"

COULD USE A DIFFERENT BASIS:

$$\frac{d\xi}{dt} = \left(\frac{3x}{3u} + \frac{3y}{3u}\right) + i\left(\frac{3x}{3u} - \frac{3y}{3u}\right)$$

$$\frac{\partial \xi}{\partial \xi} = \left(\frac{\partial x}{\partial u} - \frac{\partial x}{\partial v}\right) + i\left(\frac{\partial x}{\partial v} + \frac{\partial x}{\partial u}\right) = 0$$

BY COUGHY PLEMANN!

FO! A FUNCTION IS AWANYTI'C @ Z.

If [CR EQ HOLDS] (>) [27/22 =0]

neat application:
supersymmetric theories
ARE IMMUNE TO SOME
avanum corrections;
Protected by
Avallicity!

one last term: u +v are 2D HARMONIK. IF & ANAUTIK

= 0

29 80: AMALYTIC FUNCTIONS ARE A SHORTCUT FOR RD ELECTROSTATICS, FHIRD FLOW, ...

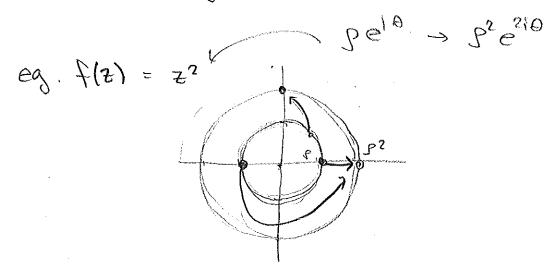
(functions as mops from (-> C) see Byron & Foller

A PREWDE TO CONFORMAL MAPING

f(z) takes a promber, gives a promber of promber of promber.

ed t(s) = 6,0 s

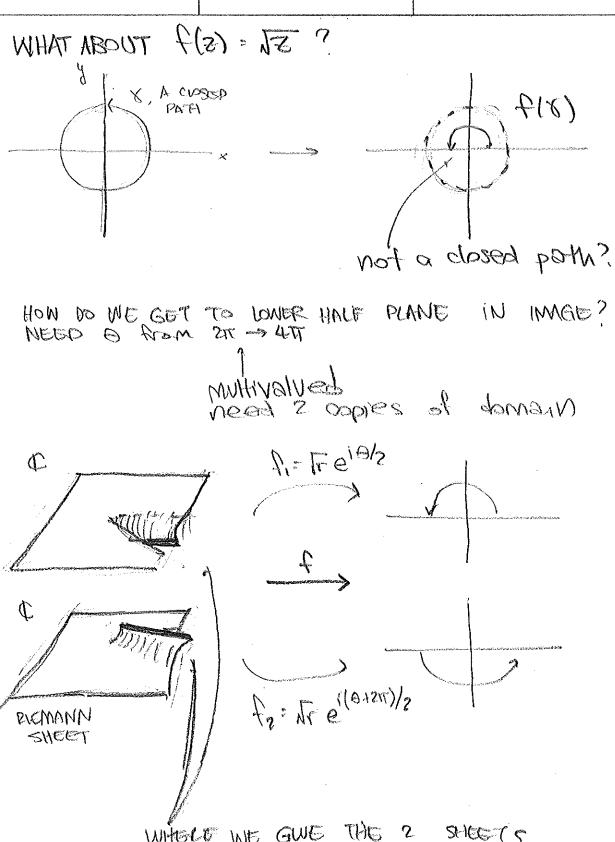
Rotates by a in counter doctalize an,



SAVARE MODULUS, DOUBLE ANGLE

es f(2) - 2 + 20 a + 16

Lyust a shift



WHELE WE GUE THE 2 SHEETS TOGETHER IS CALLED A BRANCH CUT ? DITHIAMA Sh = (4)7 81

... WHERE? I lead to specify where

cour three Bernal

C ove choke!

PRANCH CUT GLOBAL PROPERTY

WHY IT'S IMPORTANT (PRACTICAL):

my your proce than gou interded

Meaning: CAREFUL W contour integrals!

 $\frac{\text{barran}}{\log 2} = \ln(r_1 r_2) + \left[\frac{\log 2r}{\log 2}\right] = 1/(r_1 r_2) + \frac{\log 2r}{\log 2}$

every time you go around, so to A MEN STEET because of Just Keeps on moreasing

is log enolytic? enogwhere but 200,

A PIECEWISE" DEFINITION WET SINGLE VANUED

BUT REALLY: the date-home message is DO NOT CROSS A REPANCY CUT WHEN YOU INTEGRATE!

PREVIEW! & CONTOUR INTEGRALS WILL
BE ALL ABOUT TAKING CLOSED
LOOP PATHS IN & PLANE

BUT IF INTERPAND HAS

Lyst vove some featon

... make sure you do not cressill