



## **ME611 - MECHATRONICS**

NATIONAL UNIVERSITY OF SINGAPORE

DEPARTMENT OF MECHANICAL ENGINEERING

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# **Project 1: Your Project Name**

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## Note:

This document is intended to provide a sample structure for the reports in ME303 at the University of Waterloo.

## 1 Summary of the problem

Describe the physical problem under investigation and the briefly summarize the governing equations. Example:

To tie-in the concepts seen in ME303, we will turn our attention to the fascinating physical phenomenon of sonoluminescence. This occurs when a single bubble, usually of micrometer in size, within a liquid emits a short burst of light when imploding under an externally excited acoustic source. As the energy is concentrated into a point source, local temperatures in the collapsing bubble can reach up to 10,000 K for up to 50 pico seconds and visible light is emitted.

The origin of the light emission is an unsolved physical problem and obviously outside the scope of ME303. For project 1, we will be studying the governing equations behind the bubble oscillation leading up to a the light burst.



Figure 1: A goose.

The radius of a bubble under a varying pressure field is defined by the Rayleigh-Plesset equation. This equation is derived using standard conservation law under a number of simplifying assumptions:

$$\rho_l \left( R\ddot{R} + \frac{3}{2}\dot{R}^2 \right) = p_{gas} - P(t) - P_0 + \frac{R}{c} \frac{dp_{gas}}{dt} - 4\mu \frac{\dot{R}}{R} - \frac{2\sigma}{R} \quad (1)$$

In the above equation  $R(t)$  [m] represents the bubble radius. The other terms are:  $\rho_l$  [ $kg \cdot m^3$ ] the density of the liquid,  $p_{gas}$  [Pa] the pressure of the gas inside the bubble,  $P(t)$  [Pa] the imposed oscillatory pressure field,  $P_0$  [Pa] the baseline pressure,  $c$  [m/s] speed of sound in the liquid,  $\mu$  [Pa  $\cdot$  s] molecular viscosity of the liquid and  $\sigma$  [ $kg \cdot s^{-2}$ ] the surface tension at the bubble-water interface.

For more contextual information on the bubble dynamic phenomena, please see the following sources: [1], [2], and [3].

## 2 Questions

**This section answers the individual questions of the project description. For each question, provide an answer and short analysis.**

### Question 1: Forced bubble oscillation

(a)

**References to equations can be written out in latex (1). Similarly, figures 1 and sections 2.1 may also be referenced.**

(b)

**Citations require the mybib.tex file to be extended with the desired references. Students can use JabRef (<http://www.jabref.org>) to construct the mybib.bib file. Students are invited to link their Mendelay, CiteULike and Zotero account directly to Overleaf.**

### 2.1 Question 2: Bubble evolution

## Students' contributions

Mr. Goose and Mrs. Goose worked together to understand the problem and write the numerical codes. The summary of the problem and Q2 were written up by Mr. Goose, Q1 and Q3 were completed by Mrs. Goose. Both students corrected the final report.

## References

- [1] Sascha Hilgenfeldt, Michael P Brenner, Siegfried Grossmann, and Detlef Lohse. Analysis of rayleigh-plesset dynamics for sonoluminescing bubbles. *Journal of Fluid Mechanics*, 365:171–204, 1998. pages 3
- [2] Wayne Kreider, Lawrence A Crum, Michael R Bailey, and Oleg A Sapozhnikov. A reduced-order, single-bubble cavitation model with applications to therapeutic ultrasound. *The Journal of the Acoustical Society of America*, 130(5):3511–3530, 2011. pages 3
- [3] Detlef Lohse. Bubble puzzles. *Physics Today*, 56(2):36–41, 2003. pages 3