

## 0.1. NCERT 12.10.5.9

Find the position vector of a point  $\mathbf{R}$  which divides the line joining two points  $\mathbf{P}$  and  $\mathbf{Q}$  whose Position Vectors are  $2\mathbf{a} + \mathbf{b}$  and  $\mathbf{a} - 3\mathbf{b}$  externally in the ratio  $1 : 2$ .

**Solution:** let us assume  $\mathbf{a}$  and  $\mathbf{b}$  and the given ratio is

Symbol	Value	Description
$\mathbf{a}$	$\begin{pmatrix} 1 \\ -3 \end{pmatrix}$	vector $\mathbf{a}$
$\mathbf{b}$	$\begin{pmatrix} 0 \\ 2 \end{pmatrix}$	vector $\mathbf{b}$
$k$	2	ratio

Table 1: Vectors  $\mathbf{a}$  and  $\mathbf{b}$ , ratio  $k$

using section formula

$$\mathbf{R} = \frac{\mathbf{Q} - k.\mathbf{P}}{1 - k} \quad (1)$$

where  $\mathbf{P}$  and  $\mathbf{Q}$  depends on  $\mathbf{a}$  and  $\mathbf{b}$  then,

$$\mathbf{P} = (2\mathbf{a} + \mathbf{b}) = 2 \begin{pmatrix} 1 \\ -3 \end{pmatrix} + \begin{pmatrix} 0 \\ 2 \end{pmatrix} = \begin{pmatrix} 2 \\ -4 \end{pmatrix} \quad (2)$$

$$\mathbf{Q} = (\mathbf{a} - 3\mathbf{b}) = \begin{pmatrix} 1 \\ -3 \end{pmatrix} - 3 \begin{pmatrix} 0 \\ 2 \end{pmatrix} = \begin{pmatrix} 1 \\ -9 \end{pmatrix} \quad (3)$$

where  $\mathbf{R}$  can be calculated as

$$\mathbf{R} = \frac{(\mathbf{a} - 3\mathbf{b}) - k.(2\mathbf{a} + \mathbf{b})}{1 - k} \quad (4)$$

by substituting  $\mathbf{a}$  and  $\mathbf{b}$  values we get  $\mathbf{R}$  as

$$\mathbf{R} = \begin{pmatrix} 3 \\ 1 \end{pmatrix} \quad (5)$$

Symbol	Value	Description
$\mathbf{P}$	$(2\mathbf{a} + \mathbf{b})$	position vector $\mathbf{P}$
$\mathbf{Q}$	$(\mathbf{a} - 3\mathbf{b})$	position vector $\mathbf{Q}$
$\mathbf{R}$	$\frac{\mathbf{Q} - k.(\mathbf{P})}{1 - k}$	position vector $\mathbf{R}$

Table 2: Vectors  $\mathbf{P}$ ,  $\mathbf{Q}$ ,  $\mathbf{R}$

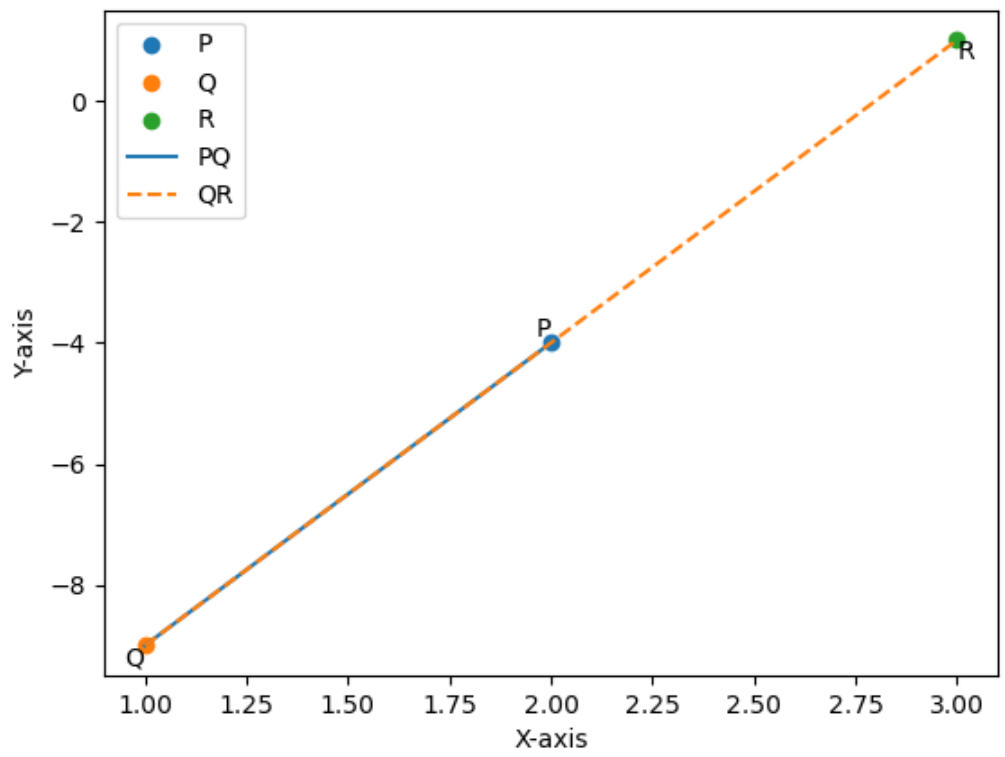


Figure 1: Point vectors  $\mathbf{P}$ ,  $\mathbf{Q}$ ,  $\mathbf{R}$