

Udacity Machine Learning Nanodegree

Capstone Project

Prediction of positive cases of COVID-19 in Peru using  
Time-Series Forecasting

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# 1. Definition

## 1.1. Project Overview

The coronavirus COVID-19 has been classified by the World Health Organization as a public health emergency of international importance. The pandemic began in December 2019 in Wuhan, China and its spread was rapid and global, causing the deaths of thousands of people around the world.

In this scenario, we can say that the current COVID-19 pandemic is devastating, despite the wide implementation of control measures.

In an analysis of the panel of COVID-19 cases in Peru until February 26, 2021, the country's Ministry of Health had confirmed 1,308,722 cases, in addition to 45,903 deaths. The cases are distributed throughout the national territory, with a greater concentration in the capital Lima.

The data for Peru are alarming. In this sense, this project will aim to analyze and predict positive cases of COVID-19 in Peru using Machine Learning techniques such as Time-Series Forecasting.

There are some of real-world applications for this research, such as:

- Estimated population infected by Covid-19 using generalized logistic regression and optimization heuristics
- Interpretation of forecasts of new cases of covid-19
- Prediction of COVID-19 cases in Peru
- Prediction of the number of infections and deaths from COVID-19 in Mexico

The links of each project will be added at the end of this document as references.

My personal motivation for working on prediction of positive cases of COVID-19 is my current job, I work with an epidemiologist doctor I am in charge to analyze the COVID-19 data from Peru frequently so I am familiar with the data then It would like to apply my machine learning knowledge using time-series forecasting to this domain.

## 1.2. Problem Statement

Taking into account the situation that Peru is going through, this project will help epidemiologists to have one more tool to estimate the risk of this pandemic by predicting positive cases of covid-19 in Peru and some control measures can be taken.

To achieve the objective I will analyze the data of the Ministry of Health of Peru and use Machine Learning techniques such as Time-Series Forecast for the predictions of new cases.

## 1.3. Metrics

I used the metric  $R^2$  or Coefficient of Determination.  $R^2$  is a statistical measure of the fitness of the predicted values to the actual values. It indicates how much variance is explained by the model. For example If my metric  $R^2$  value is 0.5, then the model can capture half of the observed variation.

$$R^2 = \frac{\frac{1}{n} \sum_{i=1}^N (y_i - \widehat{y}_i)^2}{\frac{1}{n} \sum_{i=1}^N (y_i - y_i')^2}$$

## 2. Analysis

### 2.1. Data Exploration

For this project I used the open data of the Peruvian Ministry of Health. These published data correspond to the total of reported cases that tested positive for COVID-19, by department, province and district. In addition, within the data set there are data that allow identifying the main characteristics of the patient such as age, sex and date of obtaining the positive result. At the level of update frequency of the report, the Open Data Portal indicates that the Ministry of Health carries out a daily update of the information

I worked with data obtained from March 6 to February 27, 2021, there can be many records in a single day, every record means a single confirmed case of COVID-19, the dataset contains 1,093,938 records.

As my prediction is the number of infections of COVID-19 per day so my labels will be the number of new cases of COVID-19 per day.

The dataset has the following inputs:

- ❑ UUID: Universally unique identifier, identifier of each record
- ❑ DEPARTAMENTO: State where the infected person lives
- ❑ PROVINCIA: Province where the infected person lives
- ❑ DISTRITO: District where the infected person lives
- ❑ METODODX: Method applied such as rapid test, molecular test and antigen test
- ❑ EDAD: Age of the infected person
- ❑ SEXO: Sex of the infected person
- ❑ FECHA\_RESULTADO: Date where the result of the test of the infected person was known

I counted the number of records per day to obtain the number of infected people per date. After that I splitted the data in chronological order.

A sample of this dataset is included with the accompanying git repo and the full dataset can be downloaded from [here](#).

## 2.1.1. Review of Data

- Download of data from portal of peruvian government

```
1 # Download csv from MINSA
2 url="https://cloud.minsa.gob.pe/s/Y8w3wHsEdYQSZRp/download"
3 s=requests.get(url).content
4
5 data = pd.read_csv(io.StringIO(s.decode('utf-8')), sep=';', low_memory=False)
6 data.tail()
```

- Sample of records:

	FECHA_CORTE	UUID	DEPARTAMENTO	PROVINCIA	DISTRITO	METODODX	EDAD	SEXO	FECHA_RESULTADO
0	20210228	7320cabdc1aaca6c59014cae76a134e6	LIMA REGION	HUAROCHIRI	SAN ANTONIO	PR	41.0	FEMENINO	20200526.0
1	20210228	e81602051997ace8340bb8c18fe24c65	APURIMAC	ABANCAY	ABANCAY	PR	32.0	FEMENINO	20200425.0
2	20210228	cecdfb10074dbc011ae05b3cbd320a6f	APURIMAC	ABANCAY	ABANCAY	PR	34.0	FEMENINO	20200429.0
3	20210228	71ecb6bccb248b0bb2ac72ed51b5e979	APURIMAC	ANDAHUAYLAS	ANDAHUAYLAS	PR	40.0	FEMENINO	20200426.0
4	20210228	566af4276cbe9359abe93f9aa86396c3	APURIMAC	ABANCAY	ABANCAY	PR	40.0	FEMENINO	20200428.0

- Check the type of data and null values:

```
data.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1332939 entries, 0 to 1332938
Data columns (total 9 columns):
 #   Column                Non-Null Count  Dtype  
---  --
 0   FECHA_CORTE            1332939 non-null int64  
 1   UUID                   1332939 non-null object
 2   DEPARTAMENTO            1332939 non-null object
 3   PROVINCIA              1332939 non-null object
 4   DISTRITO               1332939 non-null object
 5   METODODX               1332939 non-null object
 6   EDAD                   1332633 non-null float64
 7   SEXO                   1332939 non-null object
 8   FECHA_RESULTADO        1330916 non-null float64
dtypes: float64(2), int64(1), object(6)
memory usage: 91.5+ MB
```

```
# check number of nulls
data.isnull().sum()
```

```
FECHA_CORTE            0
UUID                   0
DEPARTAMENTO            0
PROVINCIA              0
DISTRITO               0
METODODX               0
EDAD                   306
SEXO                   0
FECHA_RESULTADO        2023
dtype: int64
```

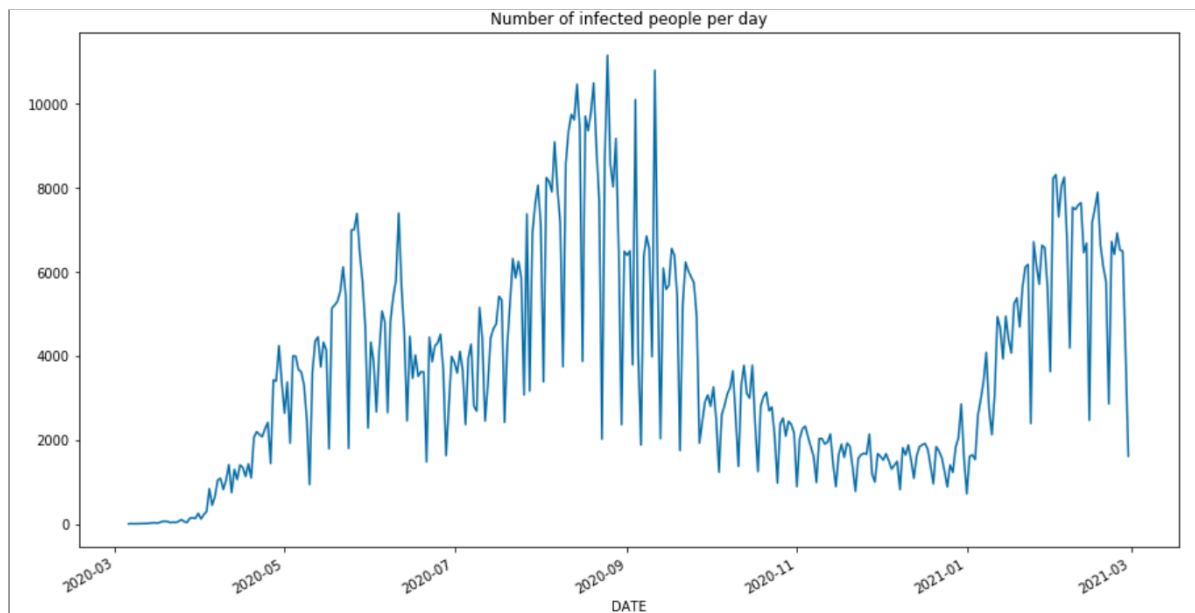
Since I will only check the FECHA\_RESULTADO(date) column and add the total confirmed cases per day I will only change the data type of the FECHA\_RESULTADO column to datetime and impute the null values in the preprocessing step.

## 2.2. Exploratory Visualization

After obtaining the number of people infected with COVID-19 per day, I plotted the confirmed cases by days, by weeks and by month in order to find any pattern of infections during this pandemic in Peru.

### 2.2.1. Confirmed cases per day

```
plt.figure(figsize=(15,8))
df_day = df_group['COUNT'].copy()
df_day.plot(title='Number of infected people per day')
plt.show()
```

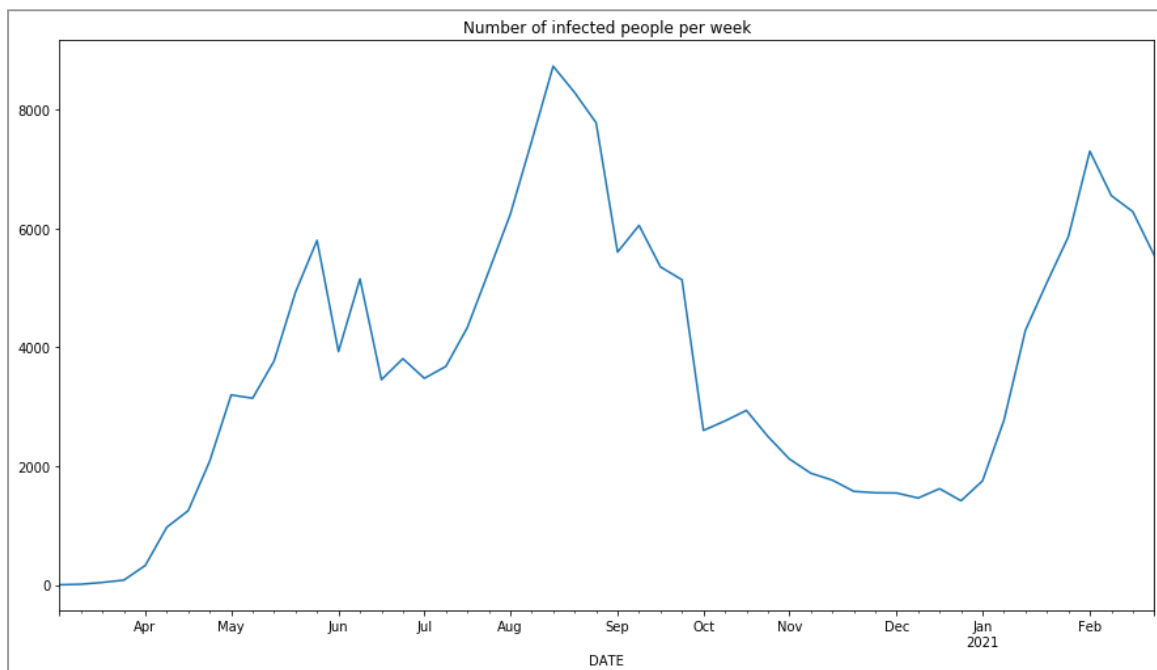


We can clearly see the behavior of the coronavirus in Peru, we can visualize a first wave of infections between July and November of 2020 and the beginning of the second wave from January 1, 2021 to today

### 2.2.2. Confirmed cases per week

```
# resample over week (D)
freq = 'W'
# calculate the mean active power for a day
mean_week_df = df_day.resample(freq).mean()

plt.figure(figsize=(15,8))
mean_week_df.plot(title='Number of infected people per week')
plt.show();
```

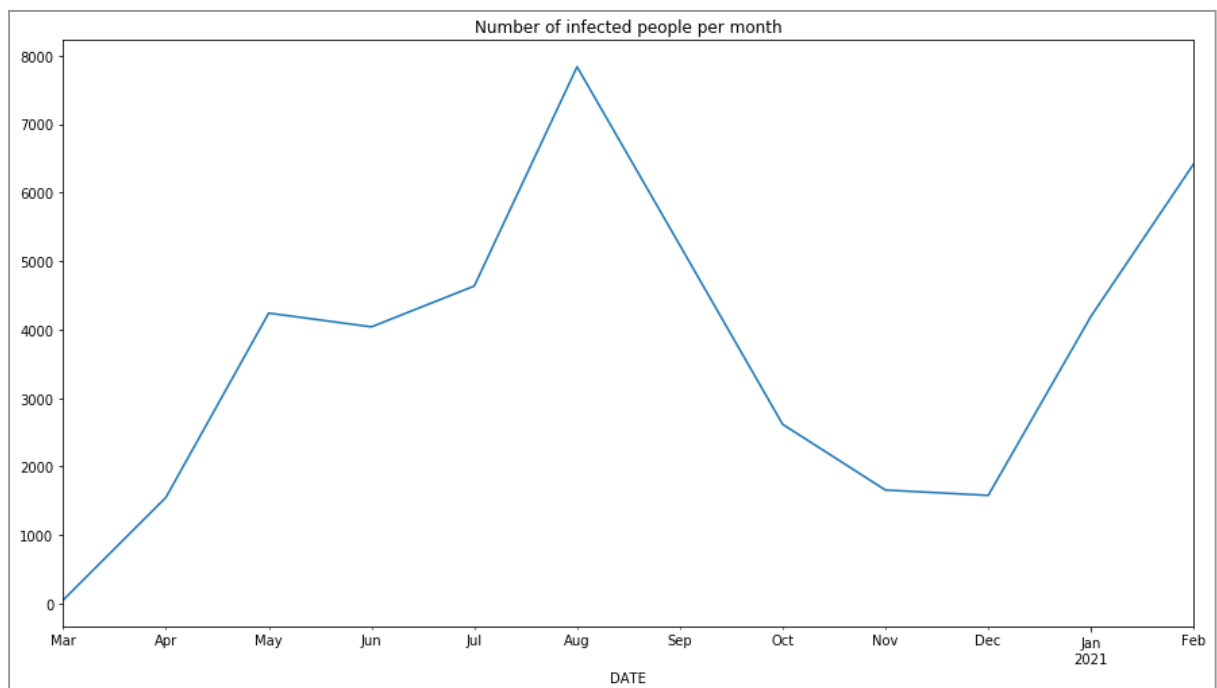


In the same way we can see the two waves produced by the coronavirus in Peru if we plot the data for weeks.

### 2.2.3. Confirmed cases per month

```
freq = 'M'|
mean_month_df = df_day.resample(freq).mean()

# display the mean values
plt.figure(figsize=(15,8))
mean_month_df.plot(title='Number of infected people per month')
plt.show();
```



After viewing the number of positive covid cases per day, weeks and months, we can find clear patterns when viewing the data for days and weeks, but having only a few days, approximately 350 days since the virus started in Peru, I decided to work the problem by grouping the cases for days and thus have more data for training.



## 2.3. Algorithms and Techniques

The proposed solution to this problem is to apply Machine Learning techniques such as Time-Series Forecasting to predict confirmed cases of COVID-19 in Peru.

First I will extract the data from the Open Data Portal of the Peruvian Ministry of Health. I will review the datatype of the columns, I will check the meaning of each column using the data dictionary obtained from the portal website and I will review the null data and I will make some visualizations to better understand the data.

The next step will be to clean and preprocess the data of COVID-19.

After that I will create training and test sets of time series separating them chronologically and I will apply the algorithm taught in classes DeepAR, DeepAR is a supervised learning built-in algorithm for forecasting time series that uses recurrent neural networks. I will create the image for the estimator "forecasting-deepar" after that I am going to instance the Estimator with SageMaker and set the hyperparameters. Afterwards I will launch the training job and deploy my estimator.

Then I will make predictions and I will use the evaluation metrics such as coefficient of determination to compare the performance of the training set against the test set.

## 2.4. Benchmark

For the benchmark model, we will use the algorithms outlined in the paper "Prediction of the number of infections and deaths from COVID-19 in Mexico" (CONACyT-CONABIO, Inder Tecuapetla-Gómez, 2020) [1]. The paper considers the semi parametric regression model:

$$y_i = \beta_0 + \beta_1 x_i + \sum_{j=1}^K u_j (x_i - \tau_j)^3 + \varepsilon_i, \quad 1 \leq i \leq n$$

This model is equivalent to a mixed linear model where  $y_i$  represents the number of new cases per day

Metrics	R <sup>2</sup>
For new cases	0.9999211

For new deaths	0.9996476
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### 3. Methodology

#### 3.1. Data Preprocessing

Since I am familiar with the data I will make the following steps for preprocessing:

- Loading libraries

```
import pandas as pd
import numpy as np
import unicodedata
import datetime as dt
import io
import requests
import matplotlib.pyplot as plt
```

- I reviewed the number of columns and its meaning of the dataset

```
data.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1332939 entries, 0 to 1332938
Data columns (total 9 columns):
#   Column                Non-Null Count  Dtype
---  -
0   FECHA_CORTE           1332939 non-null int64
1   UUID                  1332939 non-null object
2   DEPARTAMENTO           1332939 non-null object
3   PROVINCIA             1332939 non-null object
4   DISTRITO              1332939 non-null object
5   METODODX              1332939 non-null object
6   EDAD                  1332633 non-null float64
7   SEXO                  1332939 non-null object
8   FECHA_RESULTADO       1330916 non-null float64
dtypes: float64(2), int64(1), object(6)
memory usage: 91.5+ MB
```

- I removed the columns UUID since this column doesn't add any information to my problem

```
# Remove the UUID column
data_clean = data.drop(columns=['UUID'], axis=1)
```

- I removed records with null values in the column 'EDAD' and 'FECHA\_RESULTADO', since this column is important because it indicates the date of the infection.

```
# remove null values
data_clean = data_clean.dropna(subset=['FECHA_RESULTADO'])
data_clean = data_clean.dropna(subset=['EDAD'])
print(data_clean.isnull().sum())
data_clean.shape
```

```
FECHA_CORTE           0
DEPARTAMENTO           0
PROVINCIA              0
DISTRITO              0
METODODX              0
EDAD                  0
SEXO                  0
FECHA_RESULTADO        0
dtype: int64

(1330610, 8)
```

Of this way I no longer have any null value in my columns

- We can see that the FECHA\_COLUMN format is not a proper, since it should have the date format

FECHA_RESULTADO
20200526.0
20200425.0
20200429.0
20200426.0
20200428.0

- Since the FECHA\_RESULTADO column does not have a date format, we are going to format it

```
# format date
data_clean['FECHA_RESULTADO'] = data_clean['FECHA_RESULTADO'].apply(lambda x: str(x)[0:4] +
                                                                    '-' + str(x)[4:6] +
                                                                    '-' + str(x)[6:8])
```

Convert to datetime type

```
data_clean['FECHA_RESULTADO'] = pd.to_datetime(data_clean['FECHA_RESULTADO'], format='%Y-%m-%d')
data_clean.head()
```

- Rename the FECHA\_RESULTADO for an english name "DATE"

```
data_clean = data_clean.rename({'FECHA_RESULTADO': 'DATE'}, axis = 1)
data_clean
```

- Since we have decided to work the data grouping them by day I grouped the number of rows per day, so in this way I will get the total number of infected cases by date.

```
df_group = data_clean.groupby(['DATE']).size().reset_index(name='COUNT')
df_group = df_group.set_index('DATE')
df_group.head()
```

COUNT	
DATE	
2020-03-06	1
2020-03-07	5
2020-03-08	2
2020-03-09	3
2020-03-10	1

## 3.2. Implementation

### 3.2.1. Splitting the data chronologically

I created a function to make a time series. I used the whole dataset for the test set.

```
def make_time_series(df, freq='D', start_idx=0):
    # store time series
    time_series = []

    end_idx = len(df)
    data = df[start_idx:end_idx]

    t_start = dt.datetime.strptime(data.index[0], '%Y-%m-%d')
    t_end = dt.datetime.strptime(data.index[-1], '%Y-%m-%d')

    index = pd.date_range(start=t_start, end=t_end, freq=freq)
    time_series.append(pd.Series(data=data, index=index))

    # return list of time series
    return time_series
```

time\_series variable will be used as a test set:

```
freq='D' # daily recordings

time_series = make_time_series(df_day, freq=freq)
time_series
```

[ 2020-03-06	1.0
2020-03-07	5.0
2020-03-08	2.0
2020-03-09	3.0
2020-03-10	1.0
...	
2021-02-24	6928.0
2021-02-25	6523.0
2021-02-26	6498.0
2021-02-27	4124.0
2021-02-28	1615.0
Freq: D, Name: COUNT, Length: 360, dtype: float64]	

Function to create a training time series, I want to predict the 2 last weeks then I removed the last 14 days for the training set.

```
# create truncated, training time series
def create_training_series(complete_time_series, prediction_length):
    # get training series
    time_series_training = []

    for ts in complete_time_series:
        time_series_training.append(ts[:-prediction_length])

    return time_series_training
```

```

prediction_length = 14 # 2 last weeks

time_series_training = create_training_series(time_series, prediction_length)
time_series_training

[2020-03-06      1.0
 2020-03-07      5.0
 2020-03-08      2.0
 2020-03-09      3.0
 2020-03-10      1.0
 ...
 2021-02-10    7592.0
 2021-02-11    7649.0
 2021-02-12    6462.0
 2021-02-13    6686.0
 2021-02-14    2467.0
Freq: D, Name: COUNT, Length: 346, dtype: float64]

```

Visualization of the training and test time series

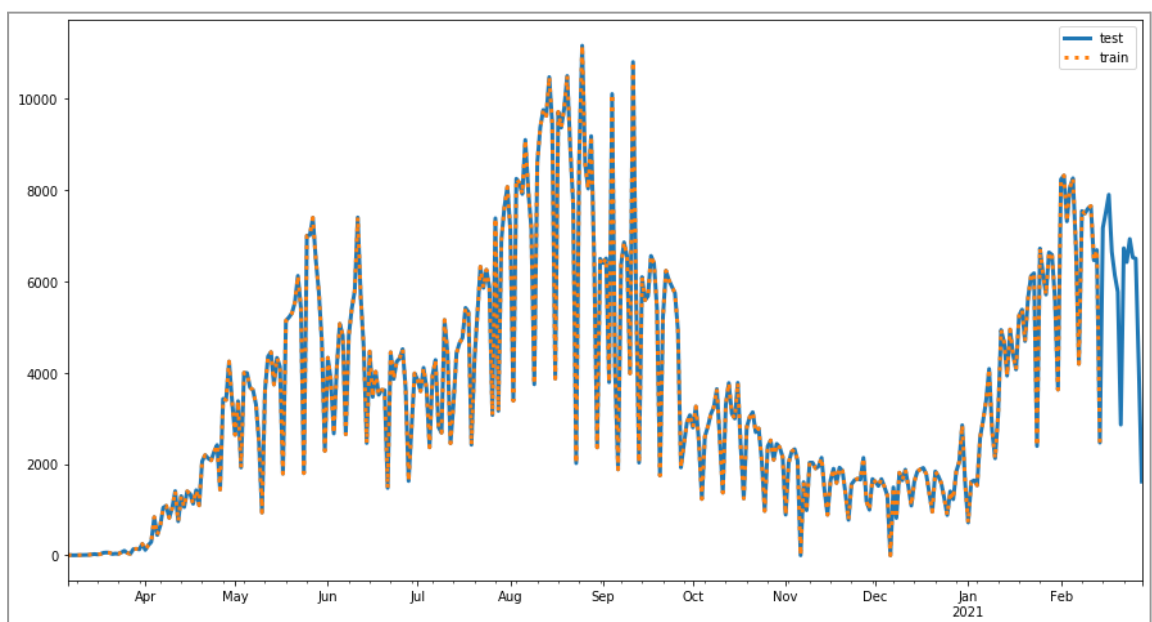
```

time_series_idx = 0 # just we have one time-serie

plt.figure(figsize=(15,8))
time_series[time_series_idx].plot(label='test', lw=3)
time_series_training[time_series_idx].plot(label='train', ls=':', lw=3)

plt.legend()
plt.show()

```



### 3.2.2. Convert to JSON

Since DeepAR algorithm expects training data in a JSON format, with the fields such as **start**, **target**. I create a function to convert the series to json format

```
def series_to_json_obj(ts):  
    json_obj = {"start": str(ts.index[0]), "target": list(ts)}  
    print(json_obj)  
    return json_obj
```

### 3.2.3. Saving Data, Locally

I imported json library formatting data and I created a directory to save the data locally.

```
import json  
import os # and os for saving  
  
def write_json_dataset(time_series, filename):  
    with open(filename, 'wb') as f:  
        # for each of our times series, there is one JSON line  
        for ts in time_series:  
            json_line = json.dumps(series_to_json_obj(ts)) + '\n'  
            json_line = json_line.encode('utf-8')  
            f.write(json_line)  
        print(filename + ' saved.')
```

```
# save this data to a local directory  
data_dir = 'json_covid_data'  
  
# make data dir, if it does not exist  
if not os.path.exists(data_dir):  
    os.makedirs(data_dir)
```

```
# directories to save train/test data  
train_key = os.path.join(data_dir, 'train.json')  
test_key = os.path.join(data_dir, 'test.json')  
  
# write train/test JSON files  
write_json_dataset(time_series, train_key)  
write_json_dataset(time_series_training, test_key)
```



### 3.2.4. Uploading Data to S3

To make this data accessible to an estimator, I uploaded it to S3. I saved in the default S3 bucket.

```
sagemaker_session = sagemaker.Session()
role = get_execution_role()
bucket = sagemaker_session.default_bucket()
```

```
prefix='deepar-covid'
train_prefix = '{}/{}/'.format(prefix, 'train')
test_prefix = '{}/{}/'.format(prefix, 'test')

# uploading data to S3, and saving locations
train_path = sagemaker_session.upload_data(train_key, bucket=bucket, key_prefix=train_prefix)
test_path = sagemaker_session.upload_data(test_key, bucket=bucket, key_prefix=test_prefix)
```

### 3.2.5. Create container image

I configured the container image to be used for the region that I am running in.

```
from sagemaker.amazon.amazon_estimator import get_image_uri
from sagemaker import image_uris

image_name = image_uris.retrieve("forecasting-deepar", boto3.Session().region_name)
```

### 3.2.6. Instantiate an Estimator

I define the estimator that will launch the training job

```

from sagemaker.estimator import Estimator

# dir to save model artifacts
s3_output_path = "s3://{}/{}/output".format(bucket, prefix)

# instantiate a DeepAR estimator
estimator = Estimator(sagemaker_session=sagemaker_session,
                      image_uri=image_name,
                      role=role,
                      train_instance_count=1,
                      train_instance_type='ml.c4.xlarge',
                      output_path=s3_output_path
                      )

```

### 3.2.7. Set a previous hyperparameters

I started with general hyperparameters such as context\_length will be equal to prediction\_length, time-freq will be days "D", and epochs will be 50:

```

freq='D'
context_length=14
prediction_length = 14
hyperparameters = {
    "epochs": "50",
    "time_freq": freq,
    "prediction_length": str(prediction_length),
    "context_length": str(context_length),
    "num_cells": "50",
    "num_layers": "3",
    "mini_batch_size": "128",
    "learning_rate": "0.001",
}

# set the hyperparams
estimator.set_hyperparameters(**hyperparameters)

```

### 3.2.8. Create a Training Job

I launched the training job, SageMaker will start an EC2 instance, download the data from S3, start training the model and save the trained model.

```

data_channels = {
    "train": train_path,
    "test": test_path
}

estimator.fit(inputs=data_channels)|

```

### 3.2.9. Deploy and Create a Predictor

After we trained a model, we can use it to perform predictions by deploying it to a predictor endpoint.

```
from sagemaker.deserializers import JSONDeserializer
from sagemaker.serializers import IdentitySerializer
```

```
# create a predictor
predictor = estimator.deploy(
    initial_instance_count=1,
    instance_type='ml.t2.medium',
    serializer=IdentitySerializer(content_type="application/json"),
    deserializer=JSONDeserializer()
)

-----!CPU times: user 294 ms, sys: 16.9 ms, total: 311 ms
Wall time: 8min 33s
```

### 3.2.10. Create a JSON Prediction Request

DeepAR predictor expects as input data a JSON format with some parameters then we create a function to handle that:

```
def json_predictor_input(input_ts, num_samples=50, quantiles=['0.1', '0.5', '0.9']):
    instances = []
    for k in range(len(input_ts)):
        instances.append(series_to_json_obj(input_ts[k]))

    configuration = {"num_samples": num_samples,
                    "output_types": ["quantiles"],
                    "quantiles": quantiles}

    request_data = {"instances": instances,
                   "configuration": configuration}

    json_request = json.dumps(request_data).encode('utf-8')

    return json_request
```

Get predictions:

```
input_ts = time_series_training#time_series_training
target_ts = time_series# testing_series

# get formatted input time series
json_input_ts = json_predictor_input(input_ts)
json_prediction = predictor.predict(json_input_ts)

print(json_prediction)
```

### 3.2.11. Decoding Predictions

The predictor returns JSON-formatted prediction so we need to extract the predictions and data that we want to visualize. I created a function to get the quantiles:

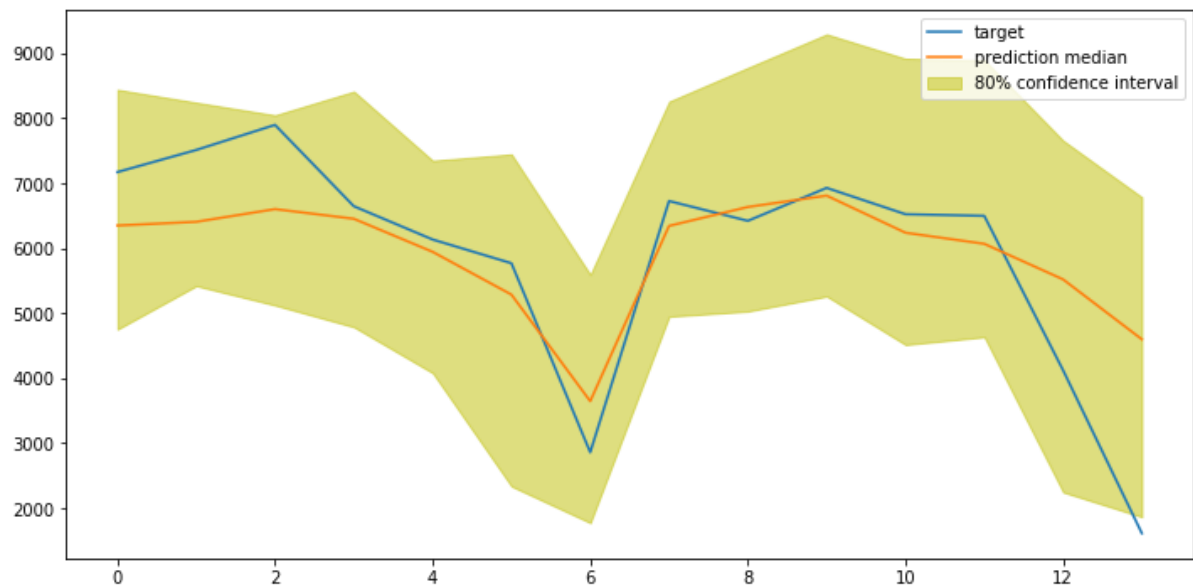
```
def decode_prediction(prediction_data, encoding='utf-8'):
    prediction_list = []
    for k in range(len(prediction_data['predictions'])):
        prediction_list.append(pd.DataFrame(data=prediction_data['predictions'][k]['quantiles']))
    return prediction_list
```

See results of predictions:

```
# get quantiles/predictions
prediction_list = decode_prediction(json_prediction)

print(prediction_list[0])
```

	0.1	0.9	0.5
0	4753.615234	8440.416016	6349.240234
1	5422.078125	8241.997070	6405.902832
2	5123.753418	8047.131348	6601.577637
3	4788.378906	8412.750000	6453.002930
4	4081.870117	7348.327148	5944.466309
5	2338.499512	7446.619629	5286.479004
6	1776.761108	5594.989258	3646.732910
7	4950.728516	8258.001953	6343.213379
8	5030.231445	8778.042969	6634.191406
9	5261.708496	9292.825195	6809.065430
10	4516.209961	8916.866211	6238.389648
11	4635.677734	8894.954102	6067.936523
12	2249.022217	7657.090820	5520.764160
13	1867.773438	6785.363281	4598.700684



### 3.2.12. Check predictions and metrics

In my first attempt I got a poor metric, I will refine my hyperparameters in the next step.

```
from sklearn.metrics import r2_score
target_ts_metric = target_ts[0][-14:].values
pred_ts_metric = prediction_list[0]['0.5'].values
print(r2_score(target_ts_metric, pred_ts_metric))
```

```
0.6261934647994614
```

### 3.3. Refinement

I will check some hyperparameters in order to get a better metric.

My intuition is that the data set being pretty small with a rather short time-series, three layers tend to overfit more so I will decrease to two layers, also I will get a smaller learning rate in order to learn longer and I increased the number of epochs.

```
freq='D'
context_length=14 # same as prediction_length
prediction_length = 14
hyperparameters = {
    "epochs": "250",
    "time_freq": freq,
    "prediction_length": str(prediction_length),
    "context_length": str(context_length),
    "num_cells": "50",
    "num_layers": "2",
    "mini_batch_size": "128",
    "learning_rate": "0.0001",
    "early_stopping_patience": "10"
}
```

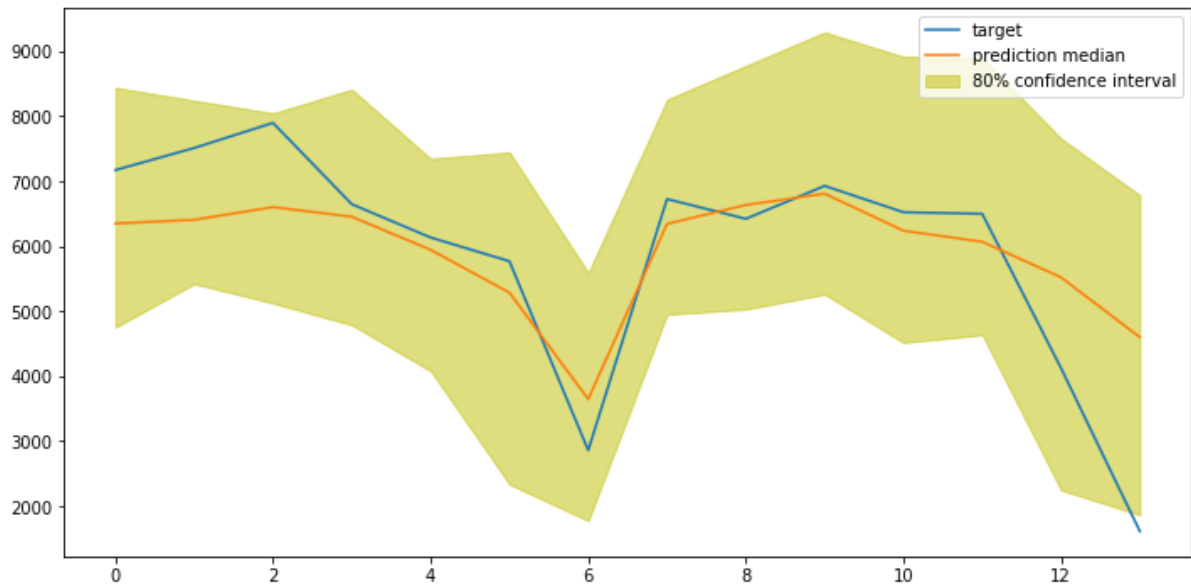
## 4. Results

### 4.1. Model Evaluation and Validation

After that I changed the hyperparameters and the evaluation metrics increased to 0.85448.

```
from sklearn.metrics import r2_score
target_ts_metric = target_ts[0][-14:].values
pred_ts_metric = prediction_list[0]['0.5'].values
print(r2_score(target_ts_metric, pred_ts_metric))

0.8544873557245587
```



## 4.2. Justification

The final model did not exceed the Benchmark model, it is very likely that it is due to the little data or so much variability of the covid data or we could do research to find better hyperparameters.

However I think it is a good score, I am going to use this model to predict the covid data for the next few weeks and will improve the algorithm over time.

Model	R2
DeepAR	85%
BenchMark Regression model	9999211%

## Predicting the Future

I would like to know how many covid-19 infections will be in Peru for the next week so the target parameters of the predictor will be an empty list because this week has no data. I started my prediction at the beginning of March, after that I get and decode the prediction response

```
start_date = '2021-03-01'
timestamp = '00:00:00'

# formatting start_date
start_time = start_date + ' ' + timestamp

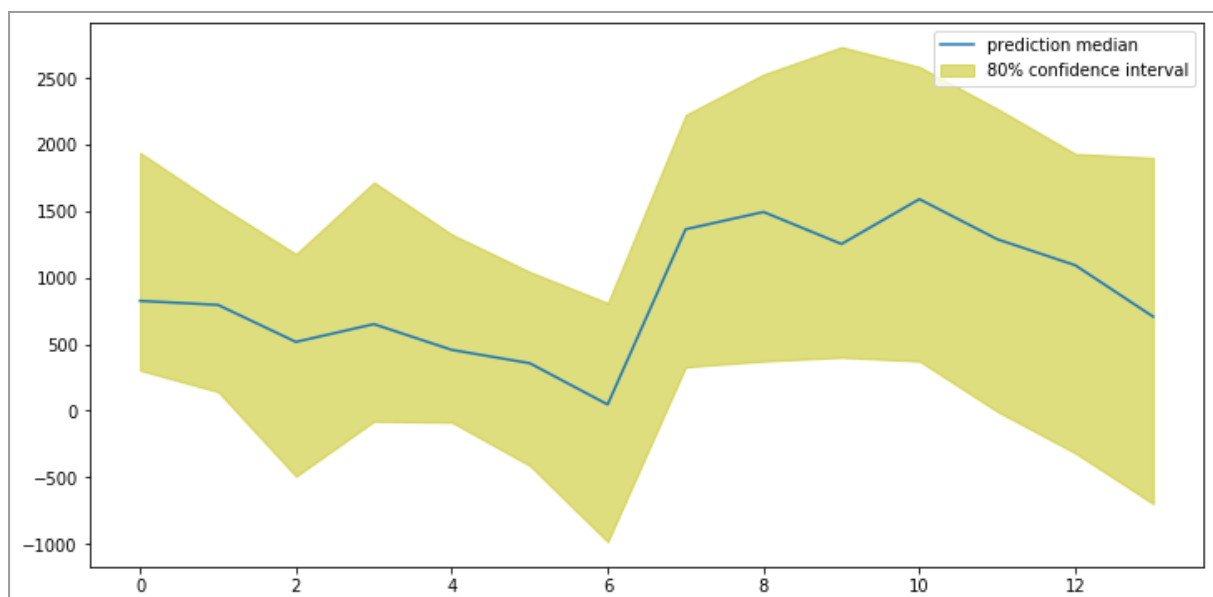
request_data = {"instances": [{"start": start_time, "target": []}],
                "configuration": {"num_samples": 50,
                                  "output_types": ["quantiles"],
                                  "quantiles": ['0.1', '0.5', '0.9']}}

json_input = json.dumps(request_data).encode('utf-8')

print('Requesting prediction for '+start_time)
```

```
# get prediction response
json_prediction = predictor.predict(json_input)

prediction_march = decode_prediction(json_prediction)
```





We can see how many confirmed cases will be in the next 14 days

### prediction\_march

	0.1	0.9	0.5
0	303.074799	1939.250732	824.907288
1	142.609955	1546.614502	794.869385
2	-492.904114	1178.477295	516.716187
3	-79.539917	1717.063232	650.337280
4	-87.222260	1325.477051	456.989563
5	-412.086365	1043.897095	356.901245
6	-985.091187	810.658447	46.637665
7	328.371948	2223.531494	1362.629272
8	372.151550	2527.424072	1493.013184
9	400.483978	2733.230469	1252.137817
10	371.970032	2584.092773	1589.176758
11	-6.176483	2268.825928	1287.738770
12	-318.479706	1930.701782	1092.667358
13	-699.346802	1900.874023	706.151123]

## Conclusion

- It was great to work with real data, especially because of a problem that all countries are experiencing. I learned that it takes a little more time to analyze the data and understand it.
- I learned to use machine learning methods like DeepAr to solve series time problems
- I will improve my techniques to tune hyperparameters and try with other machine learning models

## References

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