

# PUNJAB ENGINEERING COLLEGE, CHANDIGARH

## Mid-term Examination (19201)

Programme: B.Tech. (ECE)

Course Name: Signals and Systems

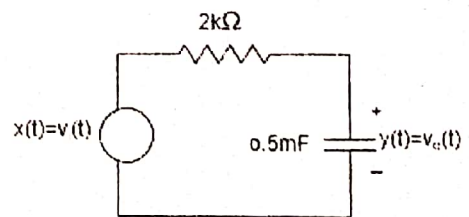
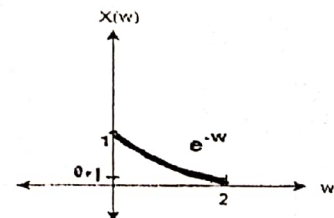
Course Code: ECN 202

Semester: 3<sup>rd</sup>

Time Allowed: 90 min

Maximum Marks: 40

Q. No		Marks
1.	(a) If the input output relation of a system is given by difference equation $y[n] = x[-0.5n + 3]$ and the input signal $x[n]$ is given by $x[n] = \{1, 3, 5, 7\}$ , then evaluate the output $y[n]$ of the system. (b) Find whether this system is a causal system.	3 2
2.	What is the difference between an energy signal and a power signal? Find whether a unit step signal is an energy signal or a power signal. Find its energy or power.	4
3.	Step response of a continuous time system is given by $s(t) = (5 - 4e^{-2t})u(t)$ . Find the response of the system input $\delta(t)$ , where $\delta(t)$ is unit impulse signal.	3
4.	(a) A discrete time LTI system having impulse response $h(n) = \left(\frac{1}{5}\right)^n u(n)$ is given an input $x(n) = 3\left(\frac{1}{5}\right)^{n+1} u(n)$ . Find the output $y(n)$ of this system using convolution sum? (b) Hence find DTFT of $y(n)$ . Mention the properties used, if any. (c) For the same system, verify the convolution property of DTFT.	4 4 4
5.	(a) State and prove the frequency shifting property of Fourier transform. (b) Hence, Find the inverse Fourier transform of signal $X(\omega) = e^{-\omega}$ for $0 \leq \omega \leq 2$ , as shown in figure.	3 4
6.	The following RC low pass filter is given an input $x(t)$ , having a power spectral density of $K$ , where $K$ is constant. Find the power of output $y(t)$ if transfer function of RC low pass filter is given by $\frac{1}{1+j\omega RC}$	4
7.	Find the autocorrelation function of the signal $x(t) = e^{3t} u(-t)$ .	5



**PUNJAB ENGINEERING COLLEGE, CHANDIGARH**

**End-Term Examination**

**November 2019**



**Program: B. Tech.**

**Course Name: Signals and systems**

**Maximum Marks: 60**

**Note:** 1. All questions are compulsory.

2. Unless stated otherwise, the symbols have their usual meanings in context with subject.

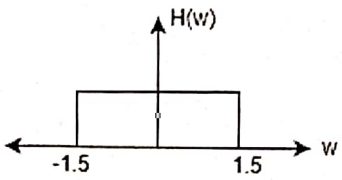
**Year/Semester: 2<sup>nd</sup> /3<sup>rd</sup> sem**

**Course Code: ECN 202**

**Time Allowed: 3 Hours**

S.no.		Marks
1.	<p>(a) Output <math>V_o(t)</math> of a square law demodulator is given by <math>V_o(t) = k_1 V_i(t) + k_2 V_i^2(t)</math>, where <math>V_i(t)</math> is input of square law device and <math>k_1</math> and <math>k_2</math> are constants. Determine whether this system is an LTI system or not?</p> <p>(b) Express the signal given in figure as sum of shifted, scaled or reversed step signals and ramp signals.</p>	<p>3</p> <p>3</p>
2.	<p>(a) How can the concept of convolution be used to multiply two polynomials? Explain with an example.</p> <p>(b) Verify the commutative property of convolution for the two signals <math>x_1(t) = e^{-3t}u(t)</math> and <math>x_2(t) = u(t+3)</math>.</p>	<p>4</p> <p>5</p>
3.	<p>(a) For a signal <math>x(t) = \sin 2t</math>, find its Hilbert transform <math>\hat{x}(t)</math>.</p> <p>(b) Hence, find the Fourier transform of <math>x(t)</math> and <math>\hat{x}(t)</math> and compare their magnitude and phase spectra.</p>	<p>3</p> <p>4</p>
4.	<p>(a) Express <math>g(t)</math> as sum of shifted, scaled or reversed signal <math>f(t)</math>, for <math>f(t)</math> and <math>g(t)</math> shown in figure.</p> <p>(b) Find Fourier transform of <math>g(t)</math> in terms of <math>F(w)</math>, if <math>g(t) \leftrightarrow G(w)</math> and <math>f(t) \leftrightarrow F(w)</math> are Fourier transform pairs.</p>	<p>3</p> <p>3</p>



5.	<p>Input-Output relation of a system is given by difference equation</p> $y[n] - \frac{1}{2}y[n-1] = 2x[n].$ <p>(a) Find transfer function <math>H(z)</math> of the system.</p> <p>(b) Hence, find the impulse response of the system if the system is a causal as well as a stable system.</p> <p>(c) Draw the block diagram implementation of the system.</p>	<p>3</p> <p>3</p> <p>3</p>
6.	<p>(a) The frequency response of an ideal low pass digital filter <math>H(\omega)</math>, having cutoff frequency <math>1.5\text{rad/sec}</math> is shown in figure over one period. Find its impulse response <math>h(n)</math>.</p>  <p>(b) In a series RL circuit, if input voltage is constant voltage source, which has been switched on at <math>t=0</math>, then find current, <math>i(t)</math>, passing through the inductor. Assume all initial conditions to be zero.</p>	<p>4</p> <p>4</p>
7.	Find energy of following signal, $x(t) = \frac{\sin^2 t}{t}$ using the concept of ESD.	5
8.	<p>(a) Discuss the relationship between average information and Entropy of a system using examples.</p> <p>(b) Find the maximum allowable information rate for error free transmission in a channel, if the channel is having usable bandwidth of <math>5\text{kHz}</math> and SNR <math>40\text{ dB}</math>.</p> <p>(c) Why do we use variable length coding techniques. Obtain the redundancy in Huffman code for a discrete source with five symbols, having probabilities <math>0.55, 0.15, 0.15, 0.10, 0.05</math> respectively.</p>	<p>3</p> <p>2</p> <p>5</p>