

## Logistic Regression as a Neural Network

### -Binary classification-

Results 0 or 1 is the output

- For classifying images,

Dim of img =  $64 \times 64 \times 3^{(\text{RGB})}$

$n_x = 12288$

For  $m$  training examples,  
 $\{(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), \dots (x^{(m)}, y^{(m)})\}$

$m_{\text{test}}$  and  $m_{\text{train}}$

$$\rightarrow X = \begin{bmatrix} | & | & | & | & | \\ x^{(1)} & x^{(2)} & \dots & x^{(m)} & n_x \\ | & | & | & | & | \end{bmatrix} \quad \underbrace{\qquad \qquad \qquad}_{m}$$

$X.\text{shape} = (n_x, m)$

$$\rightarrow Y = \begin{bmatrix} y^{(1)}, y^{(2)}, \dots, y^{(m)} \end{bmatrix} \quad \underbrace{\qquad \qquad \qquad}_{m}$$

$Y.\text{shape} = (1, m)$

## \* Logistic Regression

Ex. to check whether a given image is a cat image or not

For given  $x$ ,

Here  $x$  is a feature vector.

We want  $\hat{y} = P(y=1|x)$

Probability of given image being a cat image.

Parameters :  $w, b$

Output :  $\hat{y} = \sigma(\cancel{w^T} + w^T x + b)$

Sigmoid f<sup>N</sup> :  $\sigma(z) = \frac{1}{1 + e^{-z}}$

Cost function

$$LF: L(\hat{y}, y) = - (y \log \hat{y} + (1-y) \log(1-\hat{y}))$$

If  $y = 1$ ,  $L(\hat{y}, y) = -\log \hat{y}$

∴ want  $\hat{y}$  large

If  $y = 0$ ,  $L(\hat{y}, y) = -\log(1-\hat{y})$

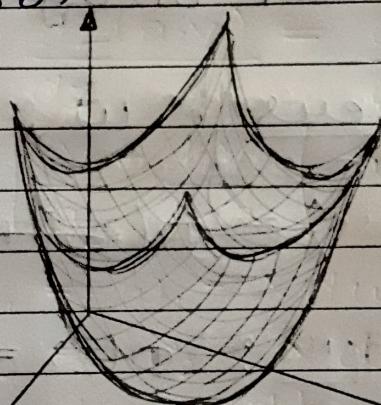
∴ want  $\hat{y}$  to be small

$$CF : J(w, b) = \frac{1}{m} \sum_{i=1}^m L(\hat{y}, y)$$

$\Rightarrow$  Loss function computes error for a single training example while cost function is the average LF error for all training examples.

### Gradient Descent

$$J(w, b)$$



Global minima

GD makes  $J(w, b)$  take small steps until it reaches the global minima.

$$w = w_0 - \alpha \frac{\partial J(w)}{\partial w} \dots \text{repeat}$$

$\alpha \Rightarrow$  learning rate

$\frac{\partial J(w)}{\partial w} \Rightarrow$  slope at each step

## ° Computation graphs

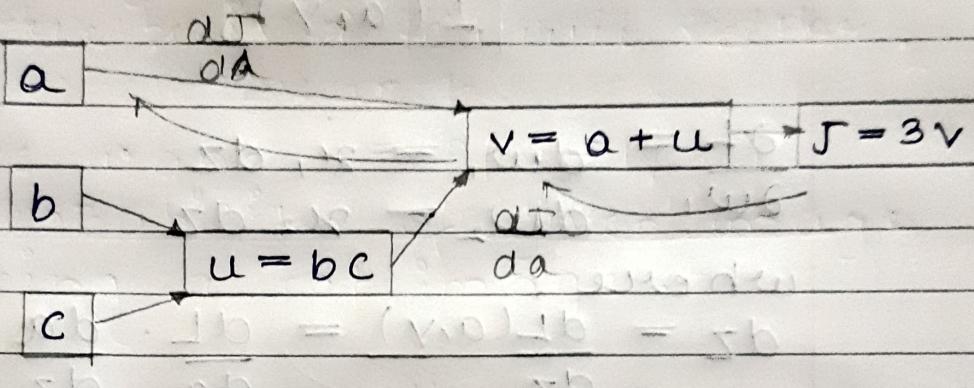
$$J(a, b, c) = 3(a + bc)$$

We do,

$$u = bc$$

$$v = a + u$$

$$J = 3v$$



## ° Derivatives of comp graphs

$$\frac{dJ}{dv} = 3 \times \frac{dv}{da} = 1$$

$$\frac{dJ}{da} = \frac{dJ}{dv} \cdot \frac{dv}{da} = 3$$

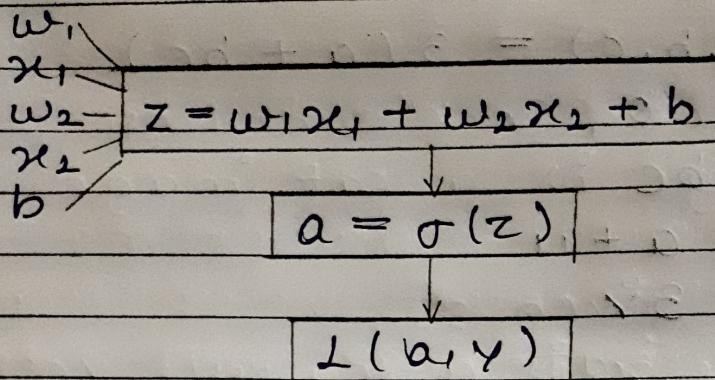
$$\frac{dJ}{da} = \frac{dJ}{dv} \cdot \frac{dv}{da} = 3$$

similar for  $b, c$

$$\frac{d \text{ final output var}}{d \text{ var}} \frac{d(\text{var})}{d \text{ VAR}}$$

for the code ↗

• Log Reg. Derivatives



$$\frac{\partial L}{\partial w_1} = \frac{dL}{dw_1} = x_1 \frac{da}{dz}$$

$$\frac{\partial L}{\partial w_2} = \frac{dL}{dw_2} = x_2 \frac{da}{dz}$$

where,

$$\frac{da}{dz} = \frac{dL(a, y)}{dz} = \frac{\partial L}{\partial a} \cdot \frac{da}{dz}$$

$$da = \left[ \frac{-y}{a} + \frac{1-y}{1-a} \right] \cdot a(1-a) = a - y$$

$$\begin{cases} w_1 = w_1 - \alpha d w_1 \\ w_2 = w_2 - \alpha d w_2 \\ b = b - \alpha d b \end{cases}$$

→ For m training examples,

$$w_1 = w_1 - \alpha \sum d w_1 / m$$

$$w_2 = w_2 - \alpha \sum d w_2 / m$$

since we compute CF (avg),  
 $\sum d w_i / m = \frac{1}{m} \sum d w_i$   
 and  $d b / m$

M	T	W	T	F	S	S
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We keep updating using previous formula\*

Note : Blunt method uses 2 for loops, one to go thru m training ex; & 2<sup>nd</sup> one thru each features. This is solved using 'vectorization.'