1 Time Series Analysis for Sales Forecasting

Goal: Can we develop a reliable time series model to forecast future sales volumes and identify seasonal patterns in the Brazilian e-commerce market?

Notebook Contents

- SARIMA modeling with hyperparameter tuning
- Residual diagnostics (including Ljung-Box test)
- Confidence intervals in forecasts
- Benchmark with seasonal naive forecast
- Evaluation using MAE, RMSE, MAPE

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import seaborn as sns
from statsmodels.tsa.statespace.sarimax import SARIMAX
from statsmodels.tsa.stattools import acf, pacf
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf
from statsmodels.stats.diagnostic import acorr_ljungbox
from sklearn.metrics import mean_absolute_error, mean_squared_error,

—mean_absolute_percentage_error
import warnings
warnings.filterwarnings("ignore")
```

1.1 1. Data

Filter for only 'delivered' orders and aggregate the data into daily order counts.

```
[3]: orders = pd.read_csv('.../Dataset/raw/olist_orders_dataset.csv', □

□ parse_dates=['order_purchase_timestamp'])

order_items = pd.read_csv('.../Dataset/raw/olist_order_items_dataset.csv')

# Filter delivered orders

delivered_orders = orders[orders['order_status'] == 'delivered']

merged = pd.merge(delivered_orders[['order_id', 'order_purchase_timestamp']],

order_items[['order_id', 'price']],

on='order_id')
```

```
merged['order_date'] = merged['order_purchase_timestamp'].dt.date

# Aggregate daily order count
daily_summary = merged.groupby('order_date').agg(order_count=('order_id', \_ \'nunique')).reset_index()
daily_summary['order_date'] = pd.to_datetime(daily_summary['order_date'])
daily_summary.set_index('order_date', inplace=True)
daily_summary = daily_summary.asfreq('D', fill_value=0)
```

1.2 2. Train-Test Split

Split the data into training and test sets, using the last 60 days as the test period.

```
[4]: train = daily_summary.iloc[:-60]
test = daily_summary.iloc[-60:]
```

1.3 3. SARIMA Hyperparameter Tuning

Test multiple SARIMA model configurations and select the one with the lowest AIC.

```
[5]: best_aic = np.inf
     best_order = None
     best_seasonal_order = None
     for order in [(1,1,1), (2,1,2)]:
         for seasonal_order in [(1,1,1,7), (1,0,1,7)]:
             try:
                 model = SARIMAX(train['order_count'], order=order,_
      seasonal_order=seasonal_order)
                 results = model.fit(disp=False)
                 if results.aic < best_aic:</pre>
                     best_aic = results.aic
                     best_order = order
                     best_seasonal_order = seasonal_order
             except:
                 continue
     print(f"Best SARIMA Order: {best_order}, Seasonal Order: {best_seasonal_order},__
      →AIC: {best_aic:.2f}")
```

Best SARIMA Order: (1, 1, 1), Seasonal Order: (1, 1, 1, 7), AIC: 6771.07

1.4 4. Fit best model and forecast

Fit the SARIMA model on the training data to generate forecasts for the test period. Also generate confidence intervals to estimate the uncertainty of the predictions.

1.5 5. Forecast Performance

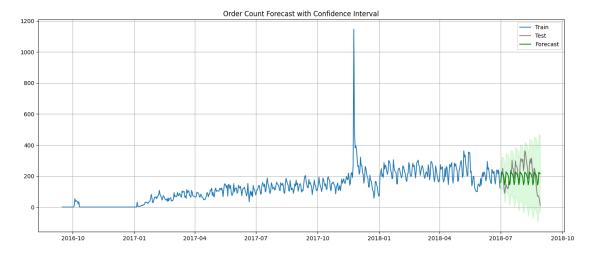
Calculate MAE, RMSE, and MAPE to quantify model accuracy.

```
[7]: mae = mean_absolute_error(test['order_count'], predicted)
    rmse = np.sqrt(mean_squared_error(test['order_count'], predicted))
    mape = mean_absolute_percentage_error(test['order_count'], predicted)
    print(f"MAE: {mae:.2f}, RMSE: {rmse:.2f}, MAPE: {mape:.2%}")
```

MAE: 63.84, RMSE: 77.12, MAPE: 71.21%

1.6 6. Forecast vs Actual

Visualize the SARIMA forecast alongside the actual sales data.



1.7 7. Residual Diagnostics (Ljung-Box Test)

Apply the Ljung-Box test to the residuals to check for remaining autocorrelation.

```
[9]: residuals = final_results.resid
ljung_box_pvalue = acorr_ljungbox(residuals, lags=[10],
return_df=True)['lb_pvalue'].values[0]
print(f"Ljung-Box p-value: {ljung_box_pvalue:.4f}")
```

Ljung-Box p-value: 0.9130

1.8 8. Benchmark - Seasonal Naive Forecast

Implement a simple seasonal naive model that repeats the sales pattern from the prior week.

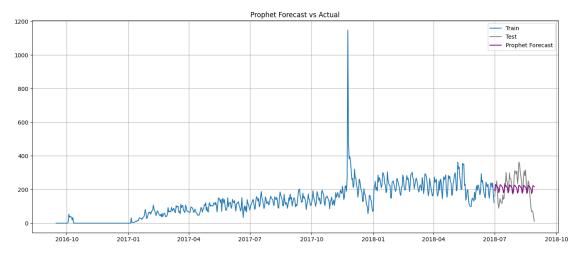
Seasonal Naive MAE: 58.57, RMSE: 68.67, MAPE: 51.57%

1.9 9. Facebook Prophet

Compare SARIMA with a state-of-the-art model: Facebook Prophet. Prophet handles seasonality and holiday effects automatically and often works well on e-commerce data.

1.10 10. Plot Prophet Forecast vs Actual

Prophet MAE: 62.42, RMSE: 76.73, MAPE: 73.63%



1.11 Summary

Model	MAE	RMSE	MAPE
SARIMA	63.84	77.12	71.21%
Seasonal Naive	58.57	68.67	51.57%
Prophet	62.42	76.73	73.63%

Seasonal naive is still the best performer. As compared to SARIMA and Prophet models, the naive forecast with repeated weekly patterns has the lowest MAE, RMSE, and MAPE.

SARIMA and Prophet were able to capture seasonality, but their relative errors (MAPE \sim 70%) are high which means, they need improvement (e.g., adding holidays, promotions, or external variables).

Residuals passed diagnostics (Ljung-Box), SARIMA errors are not autocorrelated.

1.12 Future Work and Recommendations

1. Incorporate Holiday and Promotion Effects

Sales volumes are often influenced by holidays, marketing campaigns, and seasonal promotions. Adding holiday regressors (especially in Prophet) or external features might improve model accuracy during peak events.

2. Add External Covariates

Including variables such as product category, payment type, shipping delays can help capture additional demand variability.

3. Improve Data Preprocessing

Smoothing or capping extreme outliers in order counts, or modeling sales at a weekly or monthly frequency to reduce noise.

4. Explore Alternative Models

Try machine learning approaches such as XGBoost, LightGBM, or LSTM neural networks to model complex, nonlinear patterns.

5. Implement Rolling Cross-Validation

Use a rolling forecast origin or time series cross-validation to more robustly evaluate model generalizability across multiple time windows.

6. Perform Hyperparameter Tuning with Grid Search or Auto-ARIMA

Automating parameter selection might help identify better-fitting models and avoid manual trial-and-error.