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import random
import math

# --- PARAMETERS ---
POPULATION_SIZE = 50
GENE_LENGTH = 30
GENERATIONS = 100
MUTATION_RATE = 0.05
CROSSOVER_RATE = 0.7

# Terminals (constants, variable 'x') and Functions
TERMINALS = ['x', '1', '2', '3', '4', '5']
FUNCTIONS = ['+', '-', '*', '/', 'sin', 'cos']

# Target Cost Function (to minimize)
def cost_function(x):
    """ Example cost function to minimize. Replace with your target function. """
    return x**2 - 10 * math.sin(2 * x)

# --- GENE EXPRESSION CLASS ---
class GeneExpression:
    def __init__(self):
        self.gene = self._random_gene()
        self.cached_fitness = None # To store fitness value

    def _random_gene(self):
        """ Initialize a random gene sequence. """
        return [random.choice(TERMINALS + FUNCTIONS) for _ in range(GENE_LENGTH)]

    def decode_gene(self, x):
        """ Decode the gene into a mathematical expression and evaluate it. """
        stack = []
        for token in self.gene:
            if token in TERMINALS:
                stack.append(float(x) if token == 'x' else float(token))
            elif token in FUNCTIONS:
                if len(stack) >= 1 and token in ['sin', 'cos']:
                    arg = stack.pop()
                    stack.append(math.sin(arg) if token == 'sin' else math.cos(arg))
                elif len(stack) >= 2:
                    b, a = stack.pop(), stack.pop()
                    if token == '+': stack.append(a + b)
                    elif token == '-': stack.append(a - b)
                    elif token == '*': stack.append(a * b)
                    elif token == '/' and b != 0: stack.append(a / b)
                else:
                    return float('inf') # Malformed gene
        return stack[0] if len(stack) == 1 else float('inf')

    def fitness(self, x):
        """ Evaluate fitness: minimize cost_function(output). """
        if self.cached_fitness is None:
            try:
                result = self.decode_gene(x)
                self.cached_fitness = abs(cost_function(result))
            except:
                self.cached_fitness = float('inf')
        return self.cached_fitness

# --- GENETIC OPERATIONS ---
def selection(population, fitnesses):
    """ Tournament selection: Select the best from random candidates. """
    tournament_size = 3
    candidates = random.sample(list(zip(population, fitnesses)), tournament_size)
    return min(candidates, key=lambda c: c[1])[0]

def crossover(parent1, parent2):
    """ Perform single-point crossover between two parents. """
    if random.random() < CROSSOVER_RATE:
        point = random.randint(1, GENE_LENGTH - 1)
        child1 = GeneExpression()
        child2 = GeneExpression()
        child1.gene = parent1.gene[:point] + parent2.gene[point:]
        child2.gene = parent2.gene[:point] + parent1.gene[point:]
        return child1, child2
    return parent1, parent2

def mutate(individual):
    """ Apply mutation by altering random parts of the gene. """
    for i in range(GENE_LENGTH):
        if random.random() < MUTATION_RATE:

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individual.gene[i] = random.choice(TERMINALS + FUNCTIONS)

# --- MAIN EVOLUTION FUNCTION ---
def geneExpression():
    # Initialization
    population = [GeneExpression() for _ in range(POPULATION_SIZE)]
    x_value = random.uniform(-10, 10) # Random input to test optimization

    # Evolutionary loop
    for generation in range(GENERATIONS):
        fitnesses = [ind.fitness(x_value) for ind in population]
        best_idx = fitnesses.index(min(fitnesses))

        if generation % 10 == 0: # Print every 10th generation
            print(f"Generation {generation}: Best Fitness = {fitnesses[best_idx]:.5f}")
            print(f"Best Gene: {population[best_idx].gene}")

        # Elitism: Preserve the best individual
        new_population = [population[best_idx]]

        # Create next generation
        while len(new_population) < POPULATION_SIZE:
            parent1 = selection(population, fitnesses)
            parent2 = selection(population, fitnesses)
            child1, child2 = crossover(parent1, parent2)
            mutate(child1)
            mutate(child2)
            new_population.extend([child1, child2])

        population = new_population

    # Final Solution
    final_fitnesses = [ind.fitness(x_value) for ind in population]
    best_idx = final_fitnesses.index(min(final_fitnesses))
    print("\nOptimized Solution:")
    print(f"Best Gene: {population[best_idx].gene}")
    print(f"Best Fitness: {final_fitnesses[best_idx]:.5f}")

if __name__ == "__main__":
    geneExpression()

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↩ Generation 0: Best Fitness = inf  
 Best Gene: ['5', '5', '1', '3', '-', '\*', 'sin', 'cos', '2', '3', '1', 'cos', 'sin', '5', '4', '-', '-', '5', '\*', 'sin', '-', '5',  
 Generation 10: Best Fitness = 0.27239  
 Best Gene: ['3', '5', 'cos', 'cos', '5', '3', '/', '2', '/', 'x', '+', '2', '/', '-', '4', '+', '2', 'x', 'sin', '+', 'sin', '+', '1  
 Generation 20: Best Fitness = 0.27239  
 Best Gene: ['/', '5', '+', '3', 'x', '3', '2', '5', '5', 'x', '/', '3', '-', '2', '4', 'x', '1', '1', '2', '\*', '/', 'x', '\*', '3',  
 Generation 30: Best Fitness = 0.27239  
 Best Gene: ['3', 'cos', '-', 'x', '1', 'sin', '2', '5', '4', '/', '5', 'cos', '-', 'sin', '4', 'sin', '3', '1', '1', '+', 'cos', 'x  
 Generation 40: Best Fitness = 0.27239  
 Best Gene: ['3', '5', 'x', 'x', '-', 'sin', 'sin', '5', '4', '1', '5', 'cos', 'sin', 'sin', '4', '4', '3', '1', '1', '1', 'cos', 'x  
 Generation 50: Best Fitness = 0.27239  
 Best Gene: ['\*', '2', '4', '/', '4', '4', '2', '5', '\*', '3', '\*', 'cos', '4', 'cos', '3', '4', '1', '1', '-', '4', '2', '3', 'sin',  
 Generation 60: Best Fitness = 0.27239  
 Best Gene: ['x', '5', '1', '1', '\*', '/', '\*', '/', '3', '/', '\*', 'x', '4', '3', '3', '2', '3', '5', '\*', 'cos', '+', '3', '5', '4  
 Generation 70: Best Fitness = 0.27239  
 Best Gene: ['3', '2', 'x', 'sin', '-', '1', '-', '3', '4', '/', '4', '-', '+', '3', '3', '4', 'sin', '+', 'cos', '+', '+', '-', '2',  
 Generation 80: Best Fitness = 0.00112  
 Best Gene: ['3', '2', '-', '3', '3', '5', '-', '3', '4', '/', '4', 'x', '+', '-', '3', '4', 'sin', '3', '1', '\*', '/', '-', '-', '4  
 Generation 90: Best Fitness = 0.00112  
 Best Gene: ['3', 'x', '-', '3', '3', '/', 'sin', '1', '4', '1', '2', 'cos', '-', '-', '3', '5', 'cos', '3', 'cos', '3', '/', '2', 'c

Optimized Solution:  
 Best Gene: ['x', '-', '3', '3', 'sin', '2', '3', 'sin', '2', '-', '\*', '+', '1', '5', 'cos', 'sin', '5', '2', '\*', '4', '4', 'x', '3  
 Best Fitness: 0.00112

