

Lab Assignment – 1

Q1. Design a Minimized DFA for the Regular Expression $(a/b)^*abb$ i.e. All strings ending with abb.

```

1  #include <iostream>
2  #include <iomanip>
3  #include <vector>
4  #include <stack>
5  #include <map>
6  #include <cstring>
7  using namespace std;
8  #define COL 5
9  #define _S 30
10
11 // Setting the Global Variables
12 int init[20], fin[20], a = 0, b = 0;
13 string init_dfa[_S], fin_dfa[_S];
14 int _a = 0, _b = 0;
15
16 void initialise(int table_NFA[][COL]) {
17     for(int i = 0; i < 1000; i++)
18         for(int j = 0; j < COL; j++)
19             table_NFA[i][j] = -1;
20 }
21
22 void print_initial_final() {
23     cout << "Initial state/s is/are :- ";
24     for(int i = 0; i < a; i++)
25         cout << init[i] << " ";
26     cout << endl;
27     cout << "Final state/s is/are :- ";
28     for(int i = 0; i < b; i++)
29         cout << fin[i] << " ";
30     cout << endl;
31 }
32
33 void print_initial_final_dfa() {
34     cout << "Initial state/s is/are :- ";
35     for(int i = 0; i < _a; i++)
36         cout << init_dfa[i] << " ";
37     cout << endl;
38     cout << "Final state/s is/are :- ";
39     for(int i = 0; i < _b; i++)
40         cout << fin_dfa[i] << " ";
41     cout << endl << endl;
42     for (int i = 0; i < 60; i++)
43         cout << "-";
44     cout << endl << endl;
45 }
46
47 void reduce_fin(int x) {
48     for(int i = x; i < b - 1; i++)
49         fin[i] = fin[i + 1];
50     b -= 1;
51 }
52
53 // Preprocessor Function
54 string preprocessor(string s) {
55     char x[5000];
56     auto l = s.length();
57     int j = 0;

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58     x[j] = '(';
59     j += 1;
60     for(int i = 0; i < l; i++) {
61         x[j] = s[i];
62         j += 1;
63         if(s[i] >= 97 && s[i] <= 122 && s[i + 1] >= 97 && s[i + 1] <= 122) {
64             x[j] = '.';
65             j += 1;
66         }
67         else if(s[i] == ')' && s[i + 1] == '(') {
68             x[j] = '.';
69             j += 1;
70         }
71         else if(s[i] >= 97 && s[i] <= 122 && s[i + 1] == '(') {
72             x[j] = '.';
73             j += 1;
74         }
75         else if(s[i] == ')' && s[i + 1] >= 97 && s[i + 1] <= 122) {
76             x[j] = '.';
77             j += 1;
78         }
79         else if(s[i] == '*' && (s[i + 1] == '(' || (s[i + 1] >= 97 && s[i + 1] < 122))) {
80             x[j] = '.';
81             j += 1;
82         }
83     }
84     x[j] = ')';
85     j += 1;

```

```

86     string p;
87     for(int i = 0; i < j; i++)
88         p += x[i];
89     return p;
90 }
91
92 // Postfix Function
93 string postfix(string s) {
94     auto l = s.length();
95     char a[5000];
96     stack<char> ch;
97     int j = 0;
98     for(int i = 0; i < l; i++) {
99         char x = s[i];
100        switch(x) {
101            case 'a':
102                a[j] = 'a';
103                j += 1;
104                break;
105
106            case 'b':
107                a[j] = 'b';
108                j += 1;
109                break;
110
111            case '(':
112                ch.push('(');
113                break;

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115     case ')':
116         while(!ch.empty()) {
117             if(ch.top() == '(') {
118                 ch.pop();
119                 break;
120             }
121             else {
122                 a[j] = ch.top();
123                 ch.pop();
124                 j += 1;
125             }
126         }
127         break;
128
129     case '.':
130         if(ch.empty())
131             ch.push('.');
132         else {
133             char temp = ch.top();
134             if(temp == '(')
135                 ch.push('.');
136             else if(temp == '*') {
137                 a[j] = ch.top();
138                 ch.pop();
139                 j += 1;
140                 if(ch.top() == '.') {
141                     a[j] = '.';
142                     j += 1;

```

```

143             }
144             else
145                 ch.push('.');
146         }
147         else if(temp == '.') {
148             a[j] = ch.top();
149             ch.pop();
150             j += 1;
151             ch.push('.');
152         }
153         else if(temp == '|')
154             ch.push('.');
155     }
156     break;
157
158     case '|':
159         if(ch.empty())
160             ch.push('|');
161         else {
162             char temp = ch.top();
163             if(temp == '(')
164                 ch.push('|');
165             else if(temp == '*') {
166                 a[j] = ch.top();
167                 ch.pop();
168                 j += 1;
169                 ch.push('|');
170             }

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```

171         else if(temp == '.') {
172             a[j] = ch.top();
173             j += 1;
174             ch.pop();
175             ch.push('|');
176         }
177     }
178     break;
179
180     case '*':
181         if(ch.empty())
182             ch.push('*');
183         else {
184             char temp = ch.top();
185             if(temp == '(' || temp == '.' || temp == '|')
186                 ch.push('*');
187             else {
188                 a[j] = ch.top();
189                 ch.pop();
190                 j += 1;
191                 ch.push('*');
192             }
193         }
194         break;
195     }
196 }
197 string p;
198 for(int i = 0; i < j; i++)
199     p += a[i];
200 return p;
201 }
202
203 // Regular Expression to NFA
204 int re_to_nfa(string s, int table_NFA[][COL]) {
205     auto l = s.length();
206     int states = 1;
207     int m, n, j, count;
208     for(int i = 0; i < l; i++) {
209         char x = s[i];
210         switch(x) {
211             case 'a':
212                 table_NFA[states][0] = states;
213                 init[a] = states;
214                 a += 1;
215                 states += 1;
216                 table_NFA[states - 1][1] = states;
217                 fin[b] = states;
218                 b += 1;
219                 table_NFA[states][0] = states;
220                 states += 1;
221                 break;
222             case 'b':
223                 table_NFA[states][0] = states;
224                 init[a] = states;
225                 a += 1;

```

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227         states += 1;
228         table_NFA[states - 1][2] = states;
229         fin[b] = states;
230         b += 1;
231         table_NFA[states][0] = states;
232         states += 1;
233         break;
234
235     case '.':
236         m = fin[b - 2];
237         n = init[a - 1];
238         table_NFA[m][3] = n;
239         reduce_fin(b - 2);
240         a -= 1;
241         break;
242
243     case '|':
244         for(j = a - 1, count = 0; count < 2; count++) {
245             m = init[j - count];
246             table_NFA[states][3 + count] = m;
247         }
248         a = a - 2;
249         init[a] = states;
250         a += 1;
251         table_NFA[states][0] = states;
252         states += 1;
253         for(j = b - 1, count = 0; count < 2; count++) {
254             m = fin[j - count];

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255             table_NFA[m][3] = states;
256         }
257         b = b - 2;
258         fin[b] = states;
259         b += 1;
260         table_NFA[states][0] = states;
261         states += 1;
262         break;
263
264     case '*':
265         m = init[a - 1];
266         table_NFA[states][3] = m;
267         table_NFA[states][0] = states;
268         init[a - 1] = states;
269         states += 1;
270         n = fin[b - 1];
271         table_NFA[n][3] = m;
272         table_NFA[n][4] = states;
273         table_NFA[states - 1][4] = states;
274         fin[b - 1] = states;
275         table_NFA[states][0] = states;
276         states += 1;
277         break;
278     }
279 }
280 return states;
281 }
282

```



```

283 void print_NFA_table(int table_NFA[][COL], int states) {
284     cout << endl;
285     for(int i = 0; i < 60; i++)
286     |     cout << "*";
287     cout << endl << endl;
288     cout << setw(43) << "TRANSITION TABLE FOR NFA" << endl << endl;
289     cout << setw(10) << "States" << setw(10) << "a" << setw(10) << "b" << setw(10) << "e" << setw(10) << "e" <<
290     for(int i = 0; i < 60; i++)
291     |     cout << "-";
292     cout << endl;
293     for(int i = 1; i < states; i++) {
294     |     for(int j = 0; j < COL; j++) {
295     |         if(table_NFA[i][j] == -1)
296     |         |     cout << setw(10) << "--";
297     |         else
298     |         |     cout << setw(10) << table_NFA[i][j];
299     |     }
300     |     cout << endl;
301     }
302     cout << endl;
303     for(int i = 0; i < 60; i++)
304     |     cout << "*";
305     cout << endl;
306     print_initial_final();
307 }
308
309 void print_DFA_table(string table_DFA[][3], int state) {
310     cout << endl << endl;
311     for(int i = 0; i < 60; i++)

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312     |     cout << "*";
313     cout << endl << endl;
314     cout << setw(43) << "TRANSITION TABLE FOR DFA" << endl << endl;
315     cout << setw(10) << "States" << setw(10) << "a" << setw(10) << "b" << endl;
316     for(int i = 0; i < 60; i++)
317     |     cout << "-";
318     cout << endl;
319     for(int i = 0; i < state; i++){
320     |     for(int j = 0; j < 3; j++)
321     |     |     cout << setw(10) << table_DFA[i][j];
322     |     cout << endl;
323     }
324     cout << endl;
325     for(int i = 0; i < 60; i++)
326     |     cout << "*";
327     cout << endl;
328     print_initial_final_dfa();
329 }
330
331 vector<int> e_closure(int table_NFA[][COL], int x) {
332     stack<int> s;
333     map<int, int> m;
334     vector<int> v;
335     int y;
336     s.push(x);
337     m[x] = 1;
338     while(!s.empty()) {
339     |     y = s.top();

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340         s.pop();
341         if(table_NFA[y][3] == -1)
342             continue;
343         else {
344             s.push(table_NFA[y][3]);
345             m[table_NFA[y][3]] = 1;
346             if (table_NFA[y][4] == -1)
347                 continue;
348             else {
349                 s.push(table_NFA[y][4]);
350                 m[table_NFA[y][4]] = -1;
351             }
352         }
353     }
354     map<int, int>::iterator itr;
355     itr = m.begin();
356     while (itr != m.end()) {
357         v.push_back(itr->first);
358         itr++;
359     }
360     return v;
361 }
362
363 long long int map_it(vector<int> v, int y) {
364     long long int x = 0, m = 1;
365     while(y--)
366         m *= 10;
367     vector<int>::iterator it = v.begin();
368     while(it != v.end()) {
369         x += *it * m;
370         m /= 10;
371         it += 1;
372     }
373     return x / 10;
374 }
375
376 string state_name(int i) {
377     char s = 'q';
378     string p;
379     p += s;
380     if(i == 0) {
381         p += '0';
382         return p;
383     }
384     int a[100];
385     int j = 0;
386     while(i > 0) {
387         int x = i % 10;
388         a[j] = x;
389         j += 1;
390         i = i / 10;
391     }
392     for(int i = j - 1; i >= 0; i--) {
393         int x = a[i];
394         switch(x) {
395             case 0:

```

```
396         p += '0';
397         break;
398
399     case 1:
400         p += '1';
401         break;
402
403     case 2:
404         p += '2';
405         break;
406
407     case 3:
408         p += '3';
409         break;
410
411     case 4:
412         p += '4';
413         break;
414
415     case 5:
416         p += '5';
417         break;
418
419     case 6:
420         p += '6';
421         break;
422
423     case 7:
```



```

424         p += '7';
425         break;
426
427         case 8:
428             p += '8';
429             break;
430
431         case 9:
432             p += '9';
433             break;
434     }
435 }
436 return p;
437 }
438
439 void init_CHECK(vector<int> v, string s) {
440     for(int i = 0; i < v.size(); i++) {
441         if(v[i] == init[0]) {
442             init_dfa[_a] = s;
443             _a += 1;
444         }
445     }
446 }
447
448 void fin_CHECK(vector<int> v, string s) {
449     for(int i = 0; i < v.size(); i++) {
450         if(v[i] == fin[0]) {
451             fin_dfa[_b] = s;
452             _b += 1;
453         }
454     }
455 }
456
457 bool valid_CHECK(string word) {
458     auto len = word.length();
459     int i = 0;
460     for(i = 0; i < len; i++) {
461         if(word[i] == 'a' || word[i] == 'b')
462             continue;
463         else
464             return false;
465     }
466     if(i == len)
467         return true;
468     return false;
469 }
470
471 int NFA_to_DFA(int table_NFA[][COL], int states, string table_DFA[][3]) {
472     bool flag[states];
473     memset(flag, true, sizeof(flag));
474     int state = 0, j = 0;
475     map<vector<int>, string> m_STATE;
476     vector<int> v, v1, v2, v3, v4;
477     v = e_closure(table_NFA, init[0]);
478     flag[init[a]] = false;
479     m_STATE[v] = state_name(j++);

```

```

480 init_CHECK(v, m_STATE[v]);
481 fin_CHECK(v, m_STATE[v]);
482 stack<vector<int> > st;
483 st.push(v);
484 int count = 0;
485 while(true) {
486     while(!st.empty()) {
487         vector<int> v;
488         v = st.top();
489         st.pop();
490         count += 1;
491         table_DFA[state][0] = m_STATE[v];
492         for(int i = 0; i < v.size(); i++) {
493             flag[v[i]] = false;
494             int temp = table_NFA[v[i]][1];
495             int temp1 = table_NFA[v[i]][2];
496             if (temp >= 0)
497                 v1.push_back(temp);
498             if (temp1 >= 0)
499                 v3.push_back(temp1);
500         }
501         map<int, int> map_temp, map_temp1;
502         map<int, int>::iterator it;
503         for(int i = 0; i < v1.size(); i++) {
504             v2 = e_closure(table_NFA, v1[i]);
505             for(int j = 0; j < v2.size(); j++)
506                 map_temp[v2[j]] = 1;
507             v2.clear();

```

```

508         }
509         for(int i = 0; i < v3.size(); i++) {
510             v4 = e_closure(table_NFA, v3[i]);
511             for(int j = 0; j < v4.size(); j++)
512                 map_temp1[v4[j]] = 1;
513             v4.clear();
514         }
515         for(it = map_temp.begin(); it != map_temp.end(); it++) {
516             v2.push_back(it->first);
517             flag[it->first] = false;
518         }
519         for(it = map_temp1.begin(); it != map_temp1.end(); it++) {
520             v4.push_back(it->first);
521             flag[it->first] = false;
522         }
523         if(v2.empty())
524             table_DFA[state][1] = "--";
525         else {
526             string t = m_STATE[v2];
527             char flagg = t[0];
528             if(flagg == 'q')
529                 table_DFA[state][1] = m_STATE[v2];
530             else {
531                 table_DFA[state][1] = state_name(j++);
532                 m_STATE[v2] = table_DFA[state][1];
533                 init_CHECK(v2, m_STATE[v2]);
534                 fin_CHECK(v2, m_STATE[v2]);
535                 st.push(v2);

```

```

536     }
537 }
538 if(v4.empty())
539     table_DFA[state][2] = "--";
540 else {
541     string t = m_STATE[v4];
542     char flagg = t[0];
543     if(flagg == 'q')
544         table_DFA[state][2] = m_STATE[v4];
545     else {
546         table_DFA[state][2] = state_name(j++);
547         m_STATE[v4] = table_DFA[state][2];
548         init_CHECK(v4, m_STATE[v4]);
549         fin_CHECK(v4, m_STATE[v4]);
550         st.push(v4);
551     }
552 }
553 v1.clear();
554 v2.clear();
555 v3.clear();
556 v4.clear();
557 state += 1;
558 }
559 int k = 1;
560 for(k = 1; k < states; k++) {
561     if(flag[k]) {
562         v = e_closure(table_NFA, k);
563         m_STATE[v] = state_name(j++);

```

```

564         init_CHECK(v, m_STATE[v]);
565         fin_CHECK(v, m_STATE[v]);
566         cout << endl << m_STATE[v] << " represents :- ";
567         for(int i = 0; i < v.size(); i++)
568             cout << v[i] << " ";
569         cout << endl;
570         st.push(v);
571         break;
572     }
573 }
574 if(k == states)
575     break;
576 }
577 print_DFA_table(table_DFA, state);
578 return state;
579 }
580
581 void simulator(string table_DFA[][3], string word, int state) {
582     auto len = word.length();
583     string temp = init_dfa[0];
584     bool check = valid_CHECK(word);
585     if(!check)
586         temp = "--";
587     int i = 0;
588     for(i = 0; i < len; i++) {
589         if(temp == "--") {
590             cout << endl << "String does not belong to given RE." << endl << endl << endl;
591             break;

```

```

592     }
593     else {
594         int j = 0;
595         for(j = 0; j < state; j++)
596             if(temp == table_DFA[j][0])
597                 break;
598         if(word[i] == 'a')
599             temp = table_DFA[j][1];
600         else if(word[i] == 'b')
601             temp = table_DFA[j][2];
602     }
603 }
604 if(i == len) {
605     int j = 0;
606     for(j = 0; j < _b; j++) {
607         if(temp == fin_dfa[j]) {
608             cout << endl << "String belongs to given RE." << endl << endl;
609             break;
610         }
611     }
612     if(j == _b)
613         cout << endl << "String does not belongs to given RE." << endl << endl;
614 }
615 }
616
617 int main() {
618     int table_NFA[1000][COL];
619     initialise(table_NFA);
620
621     int states = 0;
622     cout << "Regular Expression to DFA:" << endl;
623     cout << "Enter a regular expression like (a|b)*abb: ";
624     string s;
625     cin >> s;
626     s = preprocessor(s);
627     s = postfix(s);
628
629     // Thompson's Construction
630     states = re_to_nfa(s, table_NFA);
631     print_NFA_table(table_NFA, states);
632
633     // Subset Construction
634     string table_DFA[1000][3]; // Adjust the size if necessary
635     int State_DFA = NFA_to_DFA(table_NFA, states, table_DFA);
636
637     while(true) {
638         string word;
639         cout << "Enter the string" << endl;
640         cout << "Press 1 to exit" << endl;
641         cout << "Enter String: ";
642         cin >> word;
643         if(word == "1")
644             break;
645         simulator(table_DFA, word, State_DFA);
646     }
647     return 0;

```

OUTPUT:


```

● PS C:\Users\GARG> cd 'c:\Users\GARG\AppData\Local\Microsoft\Windows\INetCache\IE\Z0RM3TPE\output'
○ PS C:\Users\GARG\AppData\Local\Microsoft\Windows\INetCache\IE\Z0RM3TPE\output> & .\'Assignment-1\'[1``].exe'
Regular Expression to DFA:
Enter a regular expression like (a|b)*abb: (a|b)*abb

```

```

*****

```

TRANSITION TABLE FOR NFA

States	a	b	e	e

1	2	--	--	--
2	--	--	6	--
3	--	4	--	--
4	--	--	6	--
5	--	--	3	1
6	--	--	5	8
7	--	--	5	8
8	--	--	9	--
9	10	--	--	--
10	--	--	11	--
11	--	12	--	--
12	--	--	13	--
13	--	14	--	--
14	--	--	--	--

```

*****

```

```

*****

```

```

Initial state/s is/are :- 7
Final state/s is/are :- 14

```

```

*****

```

TRANSITION TABLE FOR DFA

States	a	b

q0	q1	q2
q2	q1	q2
q1	q1	q3
q3	q1	q4
q4	q1	q2

```

*****

```

```

Initial state/s is/are :- q0
Final state/s is/are :- q4

```

```

-----

```

```

Enter the string
Press 1 to exit
Enter String: 1

```

```

○ PS C:\Users\GARG\AppData\Local\Microsoft\Windows\INetCache\IE\Z0RM3TPE\output> 

```

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