1. Sort a given set of n integer elements using Selection Sort method and compute its time complexity. Run the program for varied values of n> 5000 and record the time taken to sort. Plot a graph of the time taken versus n. The elements can be read from a file or can be generated using the random number generator. Demonstrate using C++/Java how the brute force method works along with its time complexity analysis: worst case, average case and best case.

```
package DAALAB;
import java.util.Arrays;
import java.util.Random;
import java.util.Scanner;
public class selectionSortSmi
static int max = 10000
static void selectionSort(int a[],int n
int min:
for (int i=0; i < n-1; i++)
for (int j=i+1; j<n; j++)</pre>
if (a[j] < a[min])
int temp;
temp = a[min];
a[min] = a[i];
a[i] = temp;
public static void main(String[] args
long start, end;
int n;
Scanner in = new Scanner(System.in);
System.out.println("Enter a value of n");
n=in.nextInt(
int a[]=new int[n];
int ch;
System.out.println("Selection Sort");
System.out.println("1. Best case")
System.out.println("2. Average case");
System.out.println("3. Worst case");
ch=in.nextInt(
System.out.println("Array before sorting");
switch (ch)
```

```
case 1:
for (int i=0;i<n;i++)</pre>
a[i]=i+1;
System.out.print("\t"+a[i]);
break;
case 2
Random random=new Random();
for (int i = 0; i < n; i++)
a[i]=random.nextInt(100);
System.out.print("\t"+a[i]);
break;
case 3:
for (int i=0; i \le n; i++)
System.out.print("\t"+a[i]);
break;
start=System.currentTimeMillis();
selectionSort(a,n)
end=System.currentTimeMillis();
System.out.println("\nThe sorted elements are : ");
for (int i=0; i<n; i++)</pre>
System.out.print("\t"+a[i]);
System.out.println("\nThe time taken to sort is "+(end-start)+"ms");
```

2. Sort a given set of n integer elements using Quick Sort method and compute its time complexity. Run the program for varied values of n> 5000 and record the time taken to sort. The elements can be read from a file or can be generated using the random number generator. Demonstrate using Java how the divide-and-conquer method works along with its time complexity analysis: worst case, average case and best case

```
package p;
import java.util.Random;
import java.util.Scanner;
class quicksort {
static int compari=0;
static int[] arr;
static void guicksort(int low,int high)
if(low<high) {</pre>
compari+=1;
int j=partition(low,high);
quicksort(low,j-1);
quicksort(j+1,high);
}
static int partition(int low,int high) {
int pivot=arr[low];
int i=low, j=high;
while (i<j) {
compari +=1;
while(i<high&&arr[i]<=pivot) {</pre>
compari +=2;
```

```
i=i+1;
}
while(j>low&&arr[j]>=pivot) {
compari+=2;
j=j−1;
}
if(i<j) {
compari +=1;
interchange(i,j);
arr[low] = arr[j];
arr[j]=pivot;
return j;
static void interchange(int i,int j) {
int temp=arr[i];
arr[i]=arr[j];
arr[j]=temp;
}
public static void main(String[]args) {
int n;
Scanner <u>scanner=new Scanner(System.in);</u>
System.out.print("enter value of n:");
n=scanner.nextInt();
arr=new int[n];
System.out.println("quicksort");
System.out.println("1.best/avg case");
```

```
System.out.println("2.worst case");
int ch=scanner.nextInt();
switch(ch) {
case 1:
Random random=new Random(3000);
for (int i=0;i<n;i++) {</pre>
arr[i]=random.nextInt(5000);
}
break;
case 2:
for (int i=0;i<n;i++) {</pre>
arr[i]=i+1;
break;
long start=System.nanoTime();
quicksort(0,n-1);
long end=System.nanoTime();
System.out.println("sorted array");
for (int i=0;i<n;i++) {</pre>
System.out.println(arr[i]);
System.out.println("time taken:"+(end-start));
System.out.println("compari:"+compari);
}
}
```

3. Sort a given set of n integer elements using Merge Sort method and compute its time complexity. Run the program for varied values of n> 5000, and record the time taken to sort. The elements can be read from a file or can be generated using the random number generator. Demonstrate using Java how the divide-and-conquer method works along with its time complexity analysis: worst case, average case and best case.

```
package DAALAB;
import java.util.Random;
import java.util.Scanner;
public class MergeSort {
static int a[];
static void mergesort(int low, int high){
if(low<high) {</pre>
int mid=(low+high)/2;
mergesort(low,mid);
mergesort(mid+1,high);
merge(low,mid,high);
static void merge(int low, int mid, int high) {
int n=high-low+1;
int[]temp arr=new int[n];
int i=low, j=mid+1, k=0;
while((i<=mid) && (j<=high)) {
if(a[i]<=a[j]) {
temp arr[k]=a[i];
i++;
}
else {
temp_arr[k]=a[j];
j++;
}
k++;
}
while(i<=mid) {</pre>
temp arr[k]=a[i];
i++;
k++;
while(j<=high) {</pre>
temp arr[k]=a[j];
j++;
k++;
for (k=0; k< n; k++) {
a[low+k]=temp_arr[k];
public static void main(String[] args) {
// TODO Auto-generated method stub
```

```
int n:
Scanner in = new Scanner(System.in);
System.out.println("Enter a value");
n=in.nextInt();
a=new int[n];
int ch;
System.out.println("Merge Sort");
System.out.println("1. Best case");
System.out.println("2. Average case");
System.out.println("3. Worst case");
ch=in.nextInt();
System.out.println("Array before sorting");
switch(ch) {
case 1: for(int i=0;i< n;i++) {
a[i]=i+1;
System.out.print("\t"+a[i]);
break;
case 2: Random random=new Random();
for(int i = 0; i < n; i++) {
a[i]=random.nextInt(100);
System.out.print("\t"+a[i]);
}
break;
case 3: for(int i=0;i< n;i++) {
a[i]=n-i;
System.out.print("\t"+a[i]);
}
break;
}
long start=System.currentTimeMillis();
mergesort(0,n-1);
long end=System.currentTimeMillis();
long timeTaken=end-start;
System.out.println("\nSorted Array");
for(int i=0;i<n;i++) {</pre>
System.out.print("\t"+a[i]);
System.out.println("\nTime taken: " +timeTaken + " ms");
in.close();
}
}
```

Program 4

Write & Execute Java Program. To solve Knapsack problem using Greedy method.

```
package p;
import java.util.Scanner;
public class lab4
{
public static void main(String[] args)
{
int i,j=0,max_qty,m,n;
float sum=0,max;
Scanner <u>sc</u> = new Scanner(System.in);
int array[][]=new int[2][20];
System.out.println("Enter no of items");
n=sc.nextInt();
System.out.println("Enter the weights of each items");
for(i=0;i<n;i++)</pre>
array[0][i]=sc.nextInt();
System.out.println("Enter the values of each items");
for (i=0;i<n;i++)</pre>
array[1][i]=sc.nextInt();
System.out.println("Enter maximum volume of knapsack :");
max_qty=sc.nextInt();
m=max_qty;
while (m>=0)
{
max=0;
for(i=0;i<n;i++)</pre>
{
```

```
if(((float)array[1][i])/((float)array[0][i])>max)
{
max=((float)array[1][i])/((float)array[0][i]);
j=i;
}
}
if(array[0][j]>m)
{
System.out.println("Quantity of item number: "+ (j+1) + " added is " +m);
sum+=m*max;
m=-1;
}
else
{
System.out.println("Quantity of item number: " + (j+1) + " added is " +
array[0][j]);
m-=array[0][j];
sum+=(float)array[1][j];
array[1][j]=0;
}
}
System.out.println("The total profit is " + sum);
sc.close();
}
}
```

```
******** KNAPSACK PROBLEM ******
Enter the total number of items:
Enter the weight of each item:
5
10
20
30
40
Enter the profit of each item:
20
10
90
160
Enter the knapsack capacity:
Information about knapsack problem are
ITEM WEIGHT
                       PROFIT RATIO(PROFIT/WEIGHT)
1
       5.0
               30.0
                       6.0
2
        10.0
               20.0
                       2.0
3
       20.0
               10.0
                       0.5
4
       30.0
               90.0
                       3.0
5
       40.0
               160.0
                      4.0
Capacity = 60
Details after sorting items based on Profit/Weight ratio in descending order:
ITEM WEIGHT
                       PROFIT RATIO (PROFIT/WEIGHT)
        5.0
               30.0
                       6.0
2
       40.0
               160.0
                       4.0
3
        30.0
               90.0
                       3.0
4
        10.0
               20.0
                       2.0
5
       20.0
               10.0
                       0.5
The result is =
        1.0
               1.0
                       0.5
                               0.0
                                       0.0
```

Maximum profit is = 235.0

From a given vertex in a weighted connected graph, find shortest paths to other vertices using Dijkstra's algorithm. Write the program in Java.

```
package p;
import java.util.Scanner;
public class Diji {
      public static void main(String[] args) {
       Scanner scan = new Scanner(System.in);
       System.out.println("Enter Number of Vertices");
       int n = scan.nextInt();
       int adj[][] = new int[n][n];
       System.out.println("Enter Adjacency Matrix");
       for (int i = 0; i < n; i++) {
       for (int j = 0; j < n; j++) {
       adj[i][j] = scan.nextInt();
       }
       System.out.println("Enter Source vertex");
       int src = scan.nextInt();
       int[] dist = dijkstra(adj, src);
       for (int i = 0; i < n; i++) {
       if ((src - 1) == i) {
       continue;
       System.out.println("Shortest Distance from " + src + " to " + (i + 1) +
" is " + dist[i]);
       }
       scan.close();
       }
```

```
static int[] dijkstra(int adj[][], int src) {
int n = adj.length;
int[] dist = new int[n];
boolean[] visited = new boolean[n];
int min_dist, unvis = -1;
for (int i = 0; i < n; i++) {
dist[i] = adj[src - 1][i];
visited[i] = false;
}
visited[src - 1] = true;
for (int i = 1; i < n; i++) {
min_dist = Integer.MAX_VALUE;
for (int j = 0; j < n; j++) {
if (!visited[j] && dist[j] < min_dist) {</pre>
unvis = j;
min dist = dist[j];
visited[unvis] = true;
for (int v = 0; v < n; v++) {
if (!visited[v] && dist[unvis] + adj[unvis][v] < dist[v]) {</pre>
dist[v] = dist[unvis] + adj[unvis][v];
}
return dist;
}
```

}

```
Enter Number of Vertices

5

Enter Adjacency Matrix

0 3 99 7 99

3 0 4 2 99

99 4 0 5 6

5 2 0 4 4

99 99 6 4 0

Enter Source vertex

1

Shortest Distance from 1 to 2 is 3

Shortest Distance from 1 to 3 is 5

Shortest Distance from 1 to 4 is 5

Shortest Distance from 1 to 5 is 9
```

Find Minimum Cost Spanning Tree of a given connected undirected graph using Kruskal's Algorithm. Use Union-Find algorithms in your program.

```
package p;
import java.util.Arrays;
import java.util.Scanner;
class Edge {
int src;
int dest;
int weight;
Edge(int src, int dest, int weight) {
this.src = src;
this.dest = dest;
this.weight = weight;
}
class Kruskal {
public static void main(String[] args) {
Scanner scan = new Scanner(System.in);
System.out.println("Enter number of Vertices");
int n = scan.nextInt();
int adj[][] = new int[n][n];
System.out.println("Enter Adjacency Matrix");
for (int i = 0; i < n; i++) {
for (int j = 0; j < n; j++) {
adj[i][j] = scan.nextInt();
}
```

```
}
scan.close();
// Maximum Edges without any Loops can be ((n * (n - 1)) / 2).
Edge[] edges = new Edge[(n * (n - 1)) / 2];
int k = 0;
for (int i = 0; i < n; i++) {
for (int j = i + 1; j < n; j++) {
edges[k] = new Edge(i, j, adj[i][j]);
k++;
}
}
sort(edges);
// Declare an array of size vertices to keep track of respective leaders of
each element.
int[] parent = new int[n];
// Assign each element of array of with value -1.
Arrays.fill(parent, -1);
int minCost = 0;
System.out.println("Edges: ");
for (int i = 0; i < k; i++) {
// Find the super most of leader of source vertex.
int lsrc = find(parent, edges[i].src);
// Find the super most of leader of destination vertex.
int ldest = find(parent, edges[i].dest);
// If those two leaders are different then they belong to isolated groups.
if (lsrc != ldest) {
System.out.println((edges[i].src + 1) + " <-> " + (edges[i].dest + 1));
minCost += edges[i].weight;
union(parent, lsrc, ldest);
```

```
}
}
System.out.println();
System.out.println("Minimum Cost of Spanning Tree: " + minCost);
}
static void sort(Edge[] edges) {
// Sort Edges according to their weights using Bubble Sort.
for (int i = 1; i < edges.length; i++) {</pre>
for (int j = 0; j < edges.length - i; <math>j++) {
if (edges[j].weight > edges[j + 1].weight) {
Edge temp = edges[j];
edges[j] = edges[j + 1];
edges[j + 1] = temp;
}
}
static int find(int[] parent, int i) {
if (parent[i] == -1) {
// Super Most Leader Element Found.
return i;
}
// Find Above Leader in <a href="recurrsive">recurrsive</a> manner.
return find(parent, parent[i]);
}
static void union(int[] parent, int lsrc, int ldest) {
// Make destination vertex leader of source vertex.
parent[lsrc] = ldest;
```

```
}
}
Output
Enter number of Vertices
Enter Adjacency Matrix
0 3 99 99 6 5
3 0 1 99 99 4
99 1 0 6 99 4
99 99 6 0 8 5
6 99 99 8 0 2
5 4 5 2 2 0
Edges:
2 <-> 3
5 <-> 6
1 <-> 2
2 <-> 6
4 <-> 6
Minimum Cost of Spanning Tree: 15
```

Find Minimum Cost Spanning Tree of a given connected undirected graph using Prim's algorithm

```
package p;
import java.util.Scanner;
class Prim {
public static void main(String[] args) {
Scanner scan = new Scanner(System.in);
System.out.println("Enter Number of Vertices");
int n = scan.nextInt();
int[][] costMatrix = new int[n][n];
boolean[] visited = new boolean[n];
System.out.println("Enter Cost Adjacency Matrix");
for (int i = 0; i < n; i++)
for (int j = 0; j < n; j++)
costMatrix[i][j] = scan.nextInt();
for (int i = 0; i < n; i++)
visited[i] = false;
System.out.println("Enter Source Vertex");
int srcVertex = scan.nextInt();
scan.close();
visited[srcVertex - 1] = true;
int source = 0, cost = 0, target = 0;
System.out.print("Edges: ");
for (int i = 1; i < n; i++) {
int min = Integer.MAX VALUE;
for (int j = 0; j < n; j++) {
if (visited[j]) {
```

```
for (int k = 0; k < n; k++) {
if (!visited[k] && min > costMatrix[j][k]) {
min = costMatrix[j][k];
source = j;
target = k;
}
}
visited[target] = true;
System.out.print("(" + (source + 1) + "," + (target + 1) + ")");
cost += min;
System.out.println("\nMinimum cost of Spanning Tree: " + cost);
}
}
Output
Enter Number of Vertices
Enter Cost Adjacency Matrix
0 3 99 99 6 5
3 0 1 99 99 4
99 1 0 6 99 4
99 99 6 0 8 5
6 99 99 8 0 2
6 4 5 2 2 0
```

Enter Source Vertex

1

Edges: (1,2)(2,3)(2,6)(6,4)(6,5)

Minimum cost of Spanning Tree: 12

Write Java programs to Implement All-Pairs Shortest Paths problem using Floyd's algorithm.

```
package p;
import java.util.Scanner;
class Floyd {
public static void main(String[] args) {
Scanner scan = new Scanner(System.in);
System.out.println("Enter Number of Vertices");
int n = scan.nextInt();
int[][] D = new int[10][10];
System.out.println("Enter Distance Matrix");
for (int i = 1; i \le n; i++) {
for (int j = 1; j \le n; j++) {
D[i][j] = scan.nextInt();
}
}
scan.close();
for (int k = 1; k \le n; k++) {
for (int i = 1; i <= n; i++) {
for (int j = 1; j \le n; j++) {
D[i][j] = Math.min(D[i][j], D[i][k] + D[k][j]);
}
}
}
System.out.println("Shortest Distance Matrix");
for (int i = 1; i <= n; i++) {
for (int j = 1; j \le n; j++) {
```

```
System.out.print(D[i][j] + " ");
System.out.println();
}
}
}
Output
Enter Number of Vertices
Enter Distance Matrix
0 99 3 99
2 0 99 99
99 7 0 7
6 99 99 0
Shortest Distance Matrix
0 10 3 10
2 0 5 12
9 7 0 7
6 16 9 0
```

```
Program 9
Solve Travelling Sales Person problem using Dynamic programming
package jj;
import java.util.Scanner;
public class TravSalesPerson
static int MAX = 100;
static final int infinity = 999;
public static void main(String args[])
int cost = infinity;
int c[][] = new int[MAX][MAX]; // cost matrix
int tour[] = new int[MAX]; // optimal tour
int n; // max. cities
System.out.println("Travelling Salesman Problem using Dynamic Programming\n");
System.out.println("Enter number of cities: ");
Scanner scanner = new Scanner(System.in);
n = scanner.nextInt();
System.out.println("Enter Cost matrix:\n");
for (int i = 0; i < n; i++)
for (int j = 0; j < n; j++)
c[i][j] = scanner.nextInt();
if(c[i][j] == 0)
c[i][j] = 999;
}
for (int i = 0; i < n; i++)
tour[i] = i;
```

```
cost = tspdp(c, tour, 0, n);
// print tour cost and tour
System.out.println("Minimum Tour Cost: " + cost);
System.out.println("\nTour:");
for (int i = 0; i < n; i++)
System.out.print(tour[i] + " -> ");
}
System.out.println(tour[0] + "\n");
scanner.close();
}
static int tspdp(int c[][], int tour[], int start, int n)
int i, j, k;
int temp[] = new int[MAX];
int mintour[] = new int[MAX];
int mincost;
int cost;
if (start == n - 2)
return c[tour[n - 2]][tour[n - 1]] + c[tour[n - 1]][0];
mincost = infinity;
for (i = start + 1; i < n; i++)
for (j = 0; j < n; j++)
temp[j] = tour[j];
temp[start + 1] = tour[i];
temp[i] = tour[start + 1];
if (c[tour[start]][tour[i]] + (cost = tspdp(c, temp, start + 1, n)) < mincost)
```

```
mincost = c[tour[start]][tour[i]] + cost;
for (k = 0; k < n; k++)
mintour[k] = temp[k];
}
}
for (i = 0; i < n; i++)
tour[i] = mintour[i];
return mincost;
}
}
Output
Travelling Salesman Problem using Dynamic Programming
Enter number of cities:
Enter Cost matrix:
0 1 2 4
1 0 999 1
2 999 0 1
4 1 1 0
Minimum Tour Cost: 5
Tour:
0 -> 1 -> 3 -> 2 -> 0
```

Implement in Java, the 0/1 Knapsack problem using Dynamic Programming method.

```
package jj;
import java.util.Scanner;
class Knapsack {
int[] weight, profit;
int capacity, n;
Knapsack() { //constructor automatically called
Scanner scan = new Scanner(System.in);
System.out.println("Enter Number of Items");
n = scan.nextInt();
weight = new int[n];
profit = new int[n];
System.out.println("Enter Weights of Items");
for (int i = 0; i < n; i++) {
weight[i] = scan.nextInt();
}
System.out.println("Enter Profits of Items");
for (int i = 0; i < n; i++) {
profit[i] = scan.nextInt();
}
System.out.println("Enter Capacity of Knapsack");
capacity = scan.nextInt();
scan.close();
void fill() {
int[][] K = new int[n + 1][capacity + 1];
```

```
for (int i = 0; i \le n; i++) {
for (int j = 0; j \le capacity; j++) {
if (i == 0 || j == 0) {
K[i][j] = 0;
} else if (j < weight[i - 1]) {</pre>
K[i][j] = K[i - 1][j];
} else {
K[i][j] = Math.max(K[i - 1][j], profit[i - 1] + K[i - 1][j - weight[i - 1]]);
}
}
}
System.out.println("Maximum Profit: " + (K[n][capacity]));
System.out.print("Items Considered: ");
int i = n, j = capacity;
while (i > 0 \&\& j > 0) {
if (K[i][j] != K[i - 1][j]) {
System.out.print(i + " ");
j -= weight[i - 1];
}
i -= 1;
System.out.println();
public static void main(String[] args) {
Knapsack knapsack = new Knapsack();
knapsack.fill();
}
}
```

```
Program 11
Find a subset of a given set S = \{s1, s2, \ldots, sn\} of n positive integers whose sum is
equal to a given positive integer d. For example, if S = \{1, 2, 5, 6, 8\} and d = 9
there are two solutions{1,2,6}and{1,8}.A suitable message is to be displayed if the
given problem instance doesn't have a solution.
package p;
import java.util.Scanner;
class Subset {
static int[] arr;
static int count;
public static void main(String[] args) {
Scanner scan = new Scanner(System.in);
System.out.println("Enter n value");
int n = scan.nextInt();
arr = new int[n];
System.out.println("Enter Elements of Set");
for (int i = 0; i < n; i++) {
arr[i] = scan.nextInt();
System.out.println("Enter Total Sum value");
int total = scan.nextInt();
scan.close();
subSet(total, n - 1, new boolean[n]);
if (count == 0) {
System.out.println("No solution");
}
}
static void subSet(int total, int index, boolean[] solution) {
if (total == 0) {
printSolution(solution);
```

```
} else if (total < 0 || index < 0) {</pre>
return;
} else {
boolean[] tempSolution = solution.clone();
tempSolution[index] = false;
subSet(total, index - 1, tempSolution);
tempSolution[index] = true;
subSet(total - arr[index], index - 1, tempSolution);
}
}
static void printSolution(boolean[] solution) {
count += 1;
System.out.print("Solution: ");
for (int i = 0; i < solution.length; i++) {</pre>
if (solution[i]) {
System.out.print(arr[i] + " ");
}
}
System.out.println();
}
}
Output
Enter n value
5
Enter Elements of Set
1 2 5 6 8
```

Enter Total Sum value

9

Solution: 1 2 6

Solution: 1 8

```
Design and implement in Java to find all Hamiltonian Cycles in a connected
undirected Graph G of n vertices using backtracking principle
package jj;
import java.util.Scanner;
class Hamiltonian {
static int[][] graph;
static int[] soln;
static int n, count = 0;
public static void main(String[] args) {
Scanner scan = new Scanner(System.in);
System.out.println("Enter Number of Vertices");
n = scan.nextInt();
// Read Adjacency Matrix in Graph array(1 Indexed)
graph = new int[n + 1][n + 1];
System.out.println("Enter Adjacency Matrix");
for (int i = 1; i \le n; i++) {
for (int j = 1; j \le n; j++) {
graph[i][j] = scan.nextInt();
}
ŀ
scan.close();
// Instatiate Solution array(1 Indexed), (Default Value is 0)
soln = new int[n + 1];
System.out.println("Hamiltonian Cycle are");
// In a cycle source vertex doesn't matter // Assign Starting Point to prevent repetitions
soln[1] = 1;
```

// Call Hamiltonian function to start backtracking from vertex 2

```
hamiltonian(2);
if (count == 0) {
System.out.println("No Hamiltonian Cycle");
}
}
static void hamiltonian(int k) {
while (true) {
nextValue(k);
// No next vertex so return
if (soln[k] == 0) {
return;
}
// if cycle is complete then print it else find next vertex
if (k == n) {
printArray();
} else {
hamiltonian(k + 1);
}
}
static void nextValue(int k) {
// Finds next feasible value
while (true) {
soln[k] = (soln[k] + 1) % (n + 1);
// If no next vertex is left, then return
if (soln[k] == 0) {
return;
}
```

```
// If there exists an edge
if (graph[soln[k - 1]][soln[k]] != 0) {
int j;
// Check if the vertex is not repeated
for (j = 1; j < k; j++) {
if (soln[j] == soln[k]) {
break;
}
// If vertex is not repeated
if (j == k) {
// If the vertex is not the last vertex or it completes the cycle then return
if (k < n \mid | (k == n \&\& graph[soln[n]][soln[1]] != 0)) {
return;
}
}
}
static void printArray() {
count += 1;
// Print Solution Array
for (int i = 1; i \le n; i++) {
System.out.print(soln[i] + " ");
}
System.out.println(soln[1]);
}
}
```

Output

Enter Number of Vertices

6

Enter Adjacency Matrix

0 1 1 1 0 0

1 0 1 0 0 1

1 1 0 1 1 0

1 0 1 0 1 0

0 0 1 1 0 1

0 1 0 0 1 0

Hamiltonian Cycle are

1 2 6 5 3 4 1

1 2 6 5 4 3 1

1 3 2 6 5 4 1

1 3 4 5 6 2 1

1 4 3 5 6 2 1

1 4 5 6 2 3 1