1-1.5-32

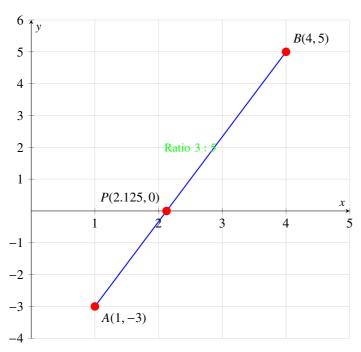
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Question:

Find the ratio in which the line segment joining the points (1, -3) and (4, 5) is divided by X axis.

Solution:



1. **Equation of the Line Segment:** The line segment joining A = (1, -3) and B = (4, 5) can be expressed parametrically as:

$$\frac{x - x_1}{x_2 - x_1} = \frac{y - y_1}{y_2 - y_1}$$

where $(x_1, y_1) = (1, -3)$ and $(x_2, y_2) = (4, 5)$. So,

$$\frac{x-1}{4-1} = \frac{y+3}{5+3}$$

Simplify to:

$$\frac{x-1}{3} = \frac{y+3}{8}$$

2. Finding Intersection with the x-Axis:

The intersection with the x-axis occurs when y = 0. Substitute y = 0 into the parametric equation:

$$\frac{x-1}{3} = \frac{0+3}{8}$$

Simplify:

$$\frac{x-1}{3} = \frac{3}{8}$$

Solving for x:

$$x-1=\frac{3\cdot 3}{8}=\frac{9}{8}$$

$$x = 1 + \frac{9}{8} = \frac{8+9}{8} = \frac{17}{8}$$

Therefore, the point of intersection with the x-axis is $\left(\frac{17}{8},0\right)$.

3. Using Section Formula to Find Ratio:

Let this point $\left(\frac{17}{8},0\right)$ divide the segment AB in the ratio k:1. The section formula for a point dividing a line segment in the ratio k:1 is given by:

$$\left(\frac{kx_2 + x_1}{k+1}, \frac{ky_2 + y_1}{k+1}\right)$$

Here, substituting the coordinates A = (1, -3) and B = (4, 5):

$$\left(\frac{k\cdot 4+1}{k+1}, \frac{k\cdot 5-3}{k+1}\right) = \left(\frac{17}{8}, 0\right)$$

Equate the *y*-coordinates:

$$\frac{k \cdot 5 - 3}{k + 1} = 0$$

$$k \cdot 5 - 3 = 0$$

$$k = \frac{3}{5}$$

Now, we need to verify the x-coordinate:

$$\frac{\frac{3}{5} \cdot 4 + 1}{\frac{3}{5} + 1} = \frac{\frac{12}{5} + 1}{\frac{8}{5}} = \frac{\frac{12+5}{5}}{\frac{8}{5}} = \frac{\frac{17}{5}}{\frac{8}{5}} = \frac{17}{8}$$

This confirms that our ratio $k = \frac{3}{5}$ is correct.

Hence, the ratio in which the line segment joining the points (1, -3) and (4, 5) is divided by the *x*-axis is 3:5.

Ratio =
$$\frac{3}{5}$$
: 1 = 3:5