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# Multi-Objective Optimal Power Flow on the IEEE 14-Bus Test System

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#### **Abstract**

This project presents a comprehensive approach to solving the Multi-Objective Optimal Power Flow (MO-OPF) problem of the IEEE 14-bus test system. The optimization framework targets two key objectives: minimizing the total generation cost and enhancing the voltage profile across the network. The generation cost is modeled as a quadratic function of active power, while the voltage profile objective minimizes deviations from the nominal voltage of 1.0 per unit. A weighted sum method is used to combine both objectives into a single formulation, allowing systematic exploration of trade-offs between them.

To enhance flexibility and avoid reliance on arbitrarily fixed weight values, Pareto front analysis is additionally employed across a range of weight combinations. This allows for a more informed and structured selection of operating points that reflect a logical balance between economic efficiency and voltage stability. The approach offers a practical and adaptable framework for real-world power system optimization.

#### 1 Introduction

Power grids are very large, complicated networks designed to deliver electricity both economically and with high reliability. As pressures accumulate—more stringent emission regulations, increased integration of renewables, and higher reliability mandates—grid managers are increasingly reaching for Optimal Power Flow (OPF) techniques.

But modern power grids demand better than cost minimization. The operators must also ensure voltage stability in order to ensure system reliability and power quality. This dual challenge has necessitated Multi-Objective OPF (MO-OPF) methodologies that balance trade-offs between conflicting objectives—like cost minimization versus voltage profile improvement.

This project is addressing two main aims:

- Minimizing overall generation cost (typically expressed as a quadratic function of generator output)
- Improving voltage quality by minimizing deviations from the ideal 1.0 per-unit voltage value

A commonly employed strategy is the weighted sum approach, which pools objectives with adjustable weights. Trade-offs may be manipulated by varying these weights by operators. It is not a straightforward activity to pick the "optimal" weights, though.

Pareto methods overcome this through the provision of a set of optimal trade-offs, referred to as the Pareto front, without predefining weights. Decision-makers may select the ideal solution based on system conditions and priorities thereafter.

This study makes use of the IEEE 14-bus test system to explain the MO-OPF approach. The actual generator mix, lines, and loads of the system are taken as a true testing environment. We make use of both weighted sum and Pareto approaches for demonstrating how efficiently operators can solve the cost–voltage trade-off problem. The structure also remains open for future objectives such as the minimization of emission or loss.

#### 2 Literature Review

#### 2.1 **Review 1:**

Optimal Power Flow (OPF) is a fundamental framework for ensuring power networks operate efficiently and safely. Traditionally, OPF was employed to reduce generation cost under voltage constraints, while recent formulations include objectives like voltage stability, power loss reduction, and emission minimization. Early OPF softwares utilized traditional optimization techniques like linear programming and quadratic programming and Newton-type approaches. Efficient for convex, smooth problems, these struggled with real-world systems not being linear and multimodal, opening the way for heuristic and metaheuristic approaches. They are more versatile but at increased computation and reduced transparency.

Among classical techniques, the weighted sum approach is common in multi-objective OPF (MO-OPF). By summing different objectives into a single function, it allows operators to alter the relative importance given to any goal through weight parameters—helpful in balancing goals like cost reduction and improvement in voltage profile.

In general, MO-OPF is interested in minimizing generation cost (expressed as a quadratic function) and maintaining voltage quality (by minimizing deviation from 1.0 p.u.). The weighted-sum method offers an operational means for investigating the trade-off, although the choice of weights must be determined in terms of system priorities.

Although Pareto-based methods portray the trade-off space in an more explicit manner, the weighted-sum method wins acceptance because it is simple, efficient, and could be readily employed as the starting point for advanced or data-intensive methodologies.

#### 2.2 **Review 2:**

With growing uncertainties caused by renewable integration, market volatility, and climate change, OPF techniques have evolved towards stochastic, robust, and distributionally robust models. While these techniques enhance risk management, they increase complexity as well.

Deterministic MO-OPF remains applicable when system parameters are well established and simplicity is sought. Of them, the weighted-sum technique is widely used for its ability to aggregate multiple objectives into one function, allowing practical trade-off analysis.

#### 3.1 Notations and Model Parameters

f: Total objective function

 $w_1, w_2$ : Weights for cost and voltage deviation

N<sub>o</sub>: Number of generators

N<sub>b</sub>: Number of buses

a, ,b, ,c; : Cost coefficients for generator i

V<sub>ref</sub>: Reference voltage magnitude (typically 1.0 p.u.)

P<sub>I i</sub>: Real power load at bus i

Q<sub>I,i</sub>: Reactive power load at bus i

Gii: Real part of admittance between bus i and j

 $\boldsymbol{B}_{ij}$ : Imaginary part of admittance between bus i and j

 $S_{ii}^{max}: Maximum \ apparent \ power \ flow \ limit \ on \ line \ i \rightarrow j$ 

#### 3.2 Decision Variables

 $P_{Gi}$ : Real power generated at bus i (MW)

Q<sub>Gi</sub>: Reactive power generated at bus i( MVAr)

V<sub>i</sub>: Voltage magnitude at bus i (p.u.)

 $\theta_i$ : Voltage angle at bus i (radians)

#### 3.3 Multi-Objective Function

We minimize the objective function f to achieve a trade-off between reducing generation cost (first term) and improving voltage profile by minimizing deviations from reference voltages (second term).

$$f = w_1 \cdot \sum_{i=1}^{N_g} \left( a_i P_{Gi}^2 + b_i P_{Gi} + c_i \right) + w_2 \cdot \sum_{j=1}^{N_b} \left( V_j - V_{ref} \right)^2$$

#### 3.4 Constraints

#### **Equality Constraints ( Power Flow Equations)**

1. Active Power Balance: (for all i in Nb)

$$P_{G_i} - P_{L_i} = V_i \sum_{j=1}^{N_b} V_j \left[ G_{ij} cos(\theta_i - \theta_j) + B_{ij} sin(\theta_i - \theta_j) \right]$$

2. Reactive Power Balance: (for all i in Nb)

$$Q_{G_i} - Q_{L_i} = V_i \sum_{j=1}^{N_b} V_j \left[ G_{ij} \sin(\theta_i - \theta_j) - B_{ij} \cos(\theta_i - \theta_j) \right]$$

#### **Inequality Constraints**

1. Generator Operating Limits: (for all i in Nb)

$$\begin{aligned} &P_{G_i}^{min} \leq P_{G_i} \leq P_{G_i}^{max} \\ &Q_{G_i}^{min} \leq Q_{G_i} \leq Q_{G_i}^{max} \end{aligned}$$

2. Voltage Magnitude Limits: (for all i in Nb)

$$V_i^{min} \le V_i \le V_i^{max}$$
 (usually  $0.95 \le V_i \le 1.05 \text{ p.u.}$ )

3. Line Flow Limits: (for all i, j in Nb)

$$S_{ij} = \sqrt{P_{ij}^2 + Q_{ij}^2} \le S_{ij}^{max}$$

4. Slack Bus Constraint:

$$V_1 = 1.0 \text{ p.u. } \theta_1 = 0 \text{ rad}$$

#### 4 Methodology

#### 4.1 **Method 1:**

Optimal power flow (OPF) analysis was performed on the base-case IEEE 14-bus system of MATPOWER's case14 dataset in MATLAB. The generator cost matrix (gencost) was verified and updated to ensure quadratic cost coefficients were defined for all five generators. Major system data—base MVA, bus admittance matrix (Ybus), generator limits, voltage limits, and loads—were extracted. Here, the script also stored the original bus and branch data into two Excel files (bus\_data.xlsx, branch\_data.xlsx)(in Appendix) with load, voltage, and line parameter values for note-taking. The Ybus matrix was divided into real (G) and imaginary (B) components for use in power balance equations, and generator cost coefficients (a, b, c) were utilized to define the cost objective.

Optimization parameters were **Bus Voltage magnitudes**, **Voltage Angles**, and **Real and Reactive power outputs of generators (Pg and Qg).** Initial guesses were specified within feasible limits.

A weighted objective function was formulated based on total generation cost and voltage deviation from 1.0 p.u. and their respective weights as 0.7 and 0.3. Constraints were set to ensure power balance at all buses, apply generator and voltage limits, fix the slack bus angle to 0°, and restrict line flows to below 100 MVA.

The nonlinear optimization problem was solved by MATLAB's fmincon using the Interior-point algorithm and high iteration and tight tolerance parameters to ensure accuracy. Finally, voltage and angle plots were generated in order to plot the optimal solution.

#### 4.2 **Method 2:**

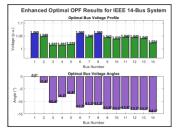
As a continuation of the previous multi-objective OPF solution, a **Pareto front-based** approach was employed to examine generation cost versus voltage deviation trade-offs in a systematic manner. Instead of employing fixed weights, the epsilon-constraint method was used to generate a set of Pareto-optimal solutions by adjusting the permissible voltage deviation over a pre-specified range. For each solution point, the cost was minimized with an upper limit on voltage deviation. A Pareto front was constructed using these solutions for the range of cost-optimal to voltage-optimal operation.

Gradients between nearby Pareto points were utilized to compute equivalent weight pairs ( $w_1$  for cost,  $w_2$  for voltage deviation) per solution. Weights were normalized and expressed to demonstrate balanced trade-offs, dominating objectives, and ideal configurations to aid in making choices. The approach facilitated improved informed decisions among OPF solutions based on system priorities rather than predetermined fixed weightings.

#### 5 Results

#### 5.1 Results for Method 1:

The adjoining graph illustrates a well-controlled voltage and angle profile achieved under the weighted sum optimization for the IEEE 14-bus system. As shown in the bar plots, all bus voltages lie within acceptable operational limits, with generator buses (1, 6, and 8) maintaining the highest



voltage level of 1.060 p.u. and the lowest voltages, approximately 1.015 p.u., observed at Buses 3 and 4. The voltage angles display a smooth and continuous decline from  $0^{\circ}$  at the slack bus (Bus 1) to  $-14.1^{\circ}$  at Bus 14, indicating stable and consistent directional power flow across the network

These trends are also confirmed by the numerical results, which show the effectiveness of the optimization in fulfilling both goals. The **cost of generation** was reduced to a minimum of

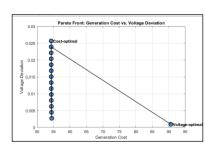
```
Optimal Bus Voltages and Angles:
Bus 1: V = 1.0660 p.u., theta = 0.0000 rad (0.00°)
Bus 2: V = 1.0645 p.u., theta = -0.0423 rad (-2.42°)
Bus 3: V = 1.0148 p.u., theta = -0.1822 rad (-10.44°)
Bus 4: V = 1.0138 p.u., theta = -0.1822 rad (-10.44°)
Bus 5: V = 1.0137 p.u., theta = -0.1828 rad (-6.84°)
Bus 6: V = 1.0177 p.u., theta = -0.1931 rad (-6.84°)
Bus 6: V = 1.0600 p.u., theta = -0.1971 rad (-11.29°)
Bus 7: V = 1.0648 p.u., theta = -0.1971 rad (-11.29°)
Bus 8: V = 1.0649 p.u., theta = -0.2555 rad (-12.92°)
Bus 9: V = 1.0642 p.u., theta = -0.2525 rad (-13.10°)
Bus 10: V = 1.0637 p.u., theta = -0.2252 rad (-13.10°)
Bus 11: V = 1.0487 p.u., theta = -0.2242 rad (-13.18°)
Bus 12: V = 1.0488 p.u., theta = -0.2230 rad (-13.18°)
Bus 13: V = 1.0235 p.u., theta = -0.2312 rad (-13.15°)
Bus 14: V = 1.0235 p.u., theta = -0.2312 rad (-13.25°)
Optimal Generator outputs:
Generator at Bus 1: Fg = 1.3807 p.u. (138.07 MM), Qg = 0.0000 p.u. (0.00 MVAr)
Generator at Bus 3: Fg = 0.0000 p.u. (130.07 MM), Qg = 0.2274 p.u. (22.23 MVAr)
Generator at Bus 8: Fg = 0.0000 p.u. (0.00 MM), Qg = 0.2974 p.u. (22.74 MVAr)
Generator at Bus 8: Fg = 0.0000 p.u. (0.00 MM), Qg = 0.0026 p.u. (8.26 MVAr)
Total Generation cost: $4.2712
Voltage Frofile Metric: 0.025557
```

54.2712, showcasing economic effectiveness, and the voltage profile metric reduced to 0.025657, signifying low deviation from nominal voltage. Only Buses 1 and 2 produced real power with generations of 138.07 MW and 130.74 MW, respectively. Reactive support was given by Buses 3, 6, and 8. Overall, the outcomes verify that

the weighted sum approach effectively balances cost reduction with voltage stability throughout the network.

#### 5.2 Results for Method 2:

The Pareto front achieved by the epsilon-constraint method shows the trade-off relationship

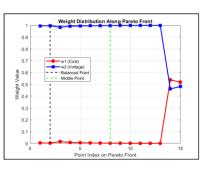


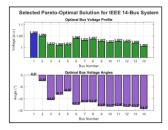
between voltage deviation and generation cost. The curve shows that reducing generation cost leads to larger voltage deviations, and the reverse. This reverse relationship illustrates the nature of multi-objective optimization—where the improvement in one objective normally sacrifices another. The smooth continuity of points along the front reveals a well-behaved

optimization process and a well-balanced range of feasible solutions.

In the adjoining figure, discrete Pareto-optimal solutions are plotted for selected values of the

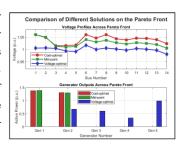
epsilon constraint. Each point represents an optimal solution obtained for a fixed upper bound on voltage deviation. The graph illustrates how the generation cost decreases gradually as the permissible deviation increases. This confirms that the cost function responds effectively to variations in the constraint and enables a range of optimal trade-off solutions to be explored based on operational priorities.





The bar chart shows how generation cost decreases with increasing epsilon values. As the voltage deviation constraint is relaxed, the cost drops steadily, highlighting the benefit of allowing slight flexibility. This supports earlier findings and offers a clearer comparison across discrete scenarios for informed cost optimization.

This figure corroborates the cost analysis by showing the respective voltage deviation profile for each epsilon value. An increasing deviation trend is apparent, which exactly replicates the cost savings seen earlier. This verifies the expected trade-off pattern, as more relaxed deviation limits allow the system to be more cost-effective but with poorer voltage quality.



Detailed Results for Fareto Solution:
Generation Cost: \$4.2961, Voltage Deviation: 0.013311

Optimal Bus Voltages and Angles:
Bus 1: V = 1.0000 p.u., theta = 0.0000 rad (0.00")
Bus 2: V = 1.0095 p.u., theta = -0.0433 rad (-2.48")
Bus 3: V = 1.01225 p.u., theta = -0.1421 rad (-6.14")
Bus 3: V = 1.01225 p.u., theta = -0.1421 rad (-6.14")
Bus 5: V = 1.0120 p.u., theta = -0.1421 rad (-6.78")
Bus 5: V = 1.0309 p.u., theta = -0.2135 rad (-12.35")
Bus 7: V = 1.0306 p.u., theta = -0.2135 rad (-13.37")
Bus 8: V = 1.0345 p.u., theta = -0.1979 rad (-11.34")
Bus 9: V = 1.0231 p.u., theta = -0.2306 rad (-13.21")
Bus 11: V = 1.0231 p.u., theta = -0.2312 rad (-13.23")
Bus 11: V = 1.0231 p.u., theta = -0.2312 rad (-13.23")
Bus 12: V = 1.0246 p.u., theta = -0.2312 rad (-13.23")
Bus 13: V = 1.0199 p.u., theta = -0.2482 rad (-13.23")
Bus 14: V = 1.0054 p.u., theta = -0.2482 rad (-14.22")

These graphs are confirmed by the numerical results, which show the effectiveness of using the Pareto front analysis for optimization in fulfilling both goals. The **cost of** 

```
Optimal Generator Outputs:

Generator at Bus 1: Pg = 1.3900 p.u. (139.00 MW), gg = 0.0000 p.u. (0.00 MVAr)

Generator at Bus 2: Pg = 1.2955 p.u. (129.95 MW), gg = 0.3453 p.u. (14.93 MVAr

Generator at Bus 3: Pg = 0.0000 p.u. (0.00 MW), gg = 0.3395 p.u. (30.39 MVAR

Generator at Bus 6: Pg = 0.0000 p.u. (0.00 MW), gg = 0.0349 p.u. (3.49 MVAr)

Generator at Bus 8: Pg = 0.0000 p.u. (0.00 MW), gg = 0.0349 p.u. (3.49 MVAr)
```

generation was reduced to a minimum of 54.2961, and the voltage profile metric reduced to 0.013311, signifying low deviation

from nominal voltage. Buses 1 and 2 produced real power with generations of 139.00 MW and 129.95 MW, respectively. Reactive support was given by Buses 3, 6, and 8. Overall, the outcomes show that the Pareto front analysis is a logical and effective way to deal with real-life multi-objective functions.

#### 6 Conclusion

This project achieves a technique of solving the Multi-Objective Optimal Power Flow (MO-OPF) problem using the IEEE 14-bus test system. By applying dual goals of reducing total generation cost and enhancing voltage profile, the research gives a practicable framework for solving economic and stability concerns in power system operation. Though the weighted sum approach proved effective to combine the cost and voltage objectives into one function, Pareto front analysis was employed to generate a collection of optimal, non-dominated solutions that offer a broader perspective of the balance of cost and voltage. The approach is devoid of the limitations of relying on a single set of pre-specified weights and allows operators to select best-suited solutions according to available system conditions.

The application of both techniques in the MO-OPF framework equips power system operators with enhanced decision-making capacities to deal with the advanced and dynamic requirements of modern power systems, enabling wiser and robust operating strategies.

#### 7 References

Reference 1: Ebeed, M., Kamel, S., & Jurado, F. (2018). Optimal Power Flow Using Recent Optimization Techniques. In Classical and Recent Aspects of Power System Optimization (Chapter 7, pp. 157-183). Academic Press.

Reference 2: Roald, L. A., Pozo, D., Papavassiliou, A., Molzahn, D. K., Kazempour, J., & Conejo, A. (2023). Power systems optimization under uncertainty: A review of methods and applications. Electric Power Systems Research, 214, 108725. https://www.elsevier.com/locate/epsr

#### 8 Appendix

#### Method 1:

```
1 function analyze opf case14()
2 % Load MATPOMER's 14-bus case and define constants mpc = case14;
4 define_constants;
6 define_constants;
                                                                                                                  MX Extract System Parameters baseMA = mpc.baseMA = mpc.ba
                                                                                                      nl = size(mpc.branch, 1); % Namber of branches slack_bus = find(mpc.bus(; BUS_TYPE) == 3);

% Admittance matrix
[Ybus, -, -] = make*Dus(base*NA, mpc.bus, mpc.branch);
d = real("Nub2);
d = inmq("Nub2);
d = inmq(
                                                                                                      end
disp('Optimal Generator Outputs:');
for i = 1:ng
```

```
fprintf('Generator at Bus %2d: Pg = %.4F p.u. (%.2f MM), Qg = %.4F p.u. (%.2f MMAr)\n', ...
gen_buses(i), Pg_opt(i), Pg_opt(i)*baseMA, Qg_opt(i), Qg_opt(i)*baseMA);
                                                                                                                                           rprintf University of Book 202 by - 3.47 p.U. (b. 7. mb), (g. 2.48 p.U. (k.2.7 ced)

end

of the second of the sec
                                                                                                                                  end
grid on;
stabel('Bus Number');
ylabel('Woltage (p.u.'));
title('Gyitala Bus Woltage Profile');
ylias(insiN_opt)-0.05, max('opt)-0.5);
xticks(1:equif('opt));
% Amostate each the with its voltage value
text(k, V.opt(k)-0.005, spriatf('%.5F, V.opt(k)), ...
text(k, V.opt(k)-0.005, spriatf('%.5F, V.opt(k)), ...
'HorizontalAlignment', 'center', 'FontSize', 9, 'FontSeight', 'bold');
end
                                                                                                                              end

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end

NX Nonlinear Contraints

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                                                                                                                                      end

% Power balance equations for each bus
Pbalance = zeros(nb, 1);
(Dalance = zeros(nb, 1);
(For i = 1:nb)

P_unj = 0;
(Jin) = 0;

                                                                                                                                                            end

Pbalance(i) = Pg_bus(i) - Pd(i) - P_inj;

Qbalance(i) = Qg_bus(i) - Qd(i) - Q_inj;
                                                                                                                              end
% Line flow constraints
line_flow = [];
if -isempty(Snamy && Smax(1) --- 999
line_flow = computetineFlows(V, theta, mb, nl, G, B, Smax);
end
```

#### Method 2:

```
| Note |
```

```
fprintf('Rin Cost Solution: Cost = X.6f, Voltage Deviation = X.6f\n', fiel_cost, voltage_dev_st_cost_opt);

% Then, optimize for voltage profile only
objfun_voltage = (0) of_voltage_dejective(v, mb, Verf);
objfun_voltage_optimelresults

& Extract voltage-optimelresults

cost_st_volt_opt = opf_cost_objective(v_volt, mb, mg, gen_buses, a, b, c);
fprintf('Rin Voltage Deviation Solution: Cost = X.6f\n', Voltage_Deviation = X.6f\n', cost_st_volt_opt, fval_volt);

% Define the range of epillon values

if voltage_dev_at_cost_opt > ral_volt

epillon_values = lineace(Fal_volt, voltage_dev_at_cost_opt, mm_points);

depellon_values = lineace(Fal_volt, voltage_dev_at_cost_opt, mm_points);

depellon_values = lineace(Fal_volt, voltage_dev_at_cost_opt, mm_points);
equilon_values = linspace(fval_volt, voltage_dev_at_cost_opt, mom_points);

else
equilon_values = linspace(fval_volt, 2*voltage_dev_at_cost_opt, mom_points);

develor_array to sture Parch front results
Foretar_cost = rerea(mom_points, 1);
pareta_solutions = call(mom_points, 1);
pareta_solutions = call(mom_points, 1);
pareta_solutions = call(mom_points, 1);
$ store cost-optical_solution
pareta_voltage_dev(1) = voltage_dev_at_cost_opt;
pareta_voltage_dev(nom_points) = call(mom_points, 1);
$ store voltage_optical_solution
$ store voltage_dev(nom_points) = call(mom_points);
$ store voltage_dev(nom_points) = call(mom_points) = call(mom_p
                                                                                                                   med and a continue = (mid_solutions, parent_solutions(1));
and

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scatter(unit Cont, valid well, 10);
figne("bms', "Parent Freet OFF Initi-Objective", "Color", [1 11));
plant(unit_cont, valid_valt_n);
plant(unit_cont, valid_valt_n);
plant(unit_cont);
plant(unit_con
                                                                                                                            gen_boss(1), Pg_opt(1), Pg_opt(1)) hasnebh, Gut(1), Qg_opt(1) hasnebh, Gut(1), Gut(1
                                                                                                                   end
grid on; box on;
xlabel('Bus Number');
ylabel('Voltage (p.u.)');
title('Optimal Bus Voltage Profile');
```

```
"meriontabligment', 'center', 'manum', 'sector', 'manum', 'sector', 'sector'
                                                                                                                 text(, (theta.px(c)/200/ple)5, sprant('c.ir', toms.govic.')
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```
# Epsilon constraint on voixnom.
V = X(limb);
voltage_dev = sum((V - Vref).^2);
c_eps = voltage_dev = epsilon;
% Combine constraint;
c = [c_reg; c_eps];
| 122 | 123 | 124 | 125 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 | 126 
                                                                                                                                   $ contac contraints

de = {c(reg);

SX Compute Line Flower
incritin c = competitionFlower(v, theta, rb, nl, 6, 8, Snasc)

Illen_count = 0;

for i = 1:nb;

f
                                                                                                do = norm_nubt(i=1) - norm_nubt(i=1);
end

$ calculate predictor (lope of tampent line)
if calculate predictor (lope of tampent line)
if eq. |
uf = 0;
                                                                                                                                                                                                                                                                                                 w2 = gradlent / (1 + gradient)
end

% Normalize weights to sum to 1
sum_u = w1 + w2;
w2 = w2 / sum_w;
v2 = w2 / sum_w;
f = w2 < sim_w;
f = w2 < sim_w;
f = w2 < sim_w;
else
ratio = w1/w2;
end
                                                                                                                                                                                                                                                                                                          retus - m...

end X Print results

fprintf('Mad | X10.4F | X10.4F | X10.4F | X12.4F | X10.4F 
                                                                                                                                                                                                                           i, valid_cost(); valid_cost(); valid_cost(); val_cost(); value_cost(); value_cost(); value_cost(); value_cost(); value_cost(); value_cost()); illength(valid_cost)))); value_cost(); val
                                                                                                                                                                                                                                    il/(sear_cost(ed_ide/)nor_cost(ed_ide)), ed_ide);

ester (1/2. Nddde Ferter point: d = %.6/, 2d = %.6/ (point %d))n', ...

1/(sear_cost(ed_ide/)nor_cost(ed_ide)), ...

ed 
introduce cost(ed_ide/)nor_cost(ed_ide), ...

ed 
introduce cost(ed_ide/)nor_cost(ed_ide), ...

finin_ma_dar_cost(ed_ide/)nor_cost(ed_ide), ...

1/(sear_cost(ed_ide/)nor_cost(ed_ide/)nor_cost(ed_ide/), ...

1/(sear_cost(ed_ide/)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_ide,)nor_cost(ed_id
                                                                                                                                                                                                                           If (!mom.cort(ein.pun_ido)/mom.cort(ein.pun_ido)), min.sum_ido);

[[apper(]unn', 'upin_ido) fisticitation lang parto front', 'color', [1 ] ]];

ut_values = zeros(lempt(valid_cost), 1);

of = [ = limenth(valid_cost), 1);

of = [ = limenth(valid_cost), 1);

of = = limenth(valid_cost), or = [ = limenth(valid_cost), 1);

of = = non_unit(i) - non_unit(i);

of = non_
                                                                                                                                                                                                                                                                                                                                                      dc = norm_cost(i+1) - norm_cost(i-1);
dv = norm_volt(i+1) - norm_volt(i-1);
end
                                                                                                                                                                                                                                                                                else

gradient = -dv/dc;

M1_values(i) = 1 / (1 + gradient);

M2_values(i) = gradient / (1 + gradient);
```

### branch\_data.xlsx

1	From_Bus	To_Bus	G_pu	B_pu	S_max_MVA
2	1	2	4.999131601	-15.26308652	0
3	1	5	1.025897455	-4.234983682	0
4	2	3	1.135019192	-4.781863152	0
5	2	4	1.686033151	-5.115838326	0
6	2	5	1.701139667	-5.193927398	0
7	3	4	1.98597571	-5.068816978	0
8	4	5	6.840980661	-21.57855398	0
9	4	7	0	-4.781943382	0
10	4	9	0	-1.797979072	0
11	5	6	0	-3.967939052	0
12	6	11	1.955028563	-4.094074344	0
13	6	12	1.52596744	-3.175963965	0
14	6	13	3.098927404	-6.102755448	0
15	7	8	0	-5.676979847	0
16	7	9	0	-9.09008272	0
17	9	10	3.902049552	-10.36539413	0
18	9	14	1.424005487	-3.029050457	0
19	10	11	1.880884754	-4.402943749	0
20	12	13	2.489024587	-2.251974626	0
21	13	14	1.136994158	-2.314963475	0

### bus\_data.xlsx

1	Bus	P_Load_MW	Q_Load_MVAr	V_ref_pu
2	1	0	0	1.06
3	2	21.7	12.7	1.045
4	3	94.2	19	1.01
5	4	47.8	-3.9	1.019
6	5	7.6	1.6	1.02
7	6	11.2	7.5	1.07
8	7	0	0	1.062
9	8	0	0	1.09
10	9	29.5	16.6	1.056
11	10	9	5.8	1.051
12	11	3.5	1.8	1.057
13	12	6.1	1.6	1.055
14	13	13.5	5.8	1.05
15	14	14.9	5	1.036

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