

【研讨论文1】

K. Zhang, W. Zuo, *et al*, Beyond a Gaussian Denoiser: Residual Learning of Deep CNN for Image Denoising,

IEEE TRANSACTIONS ON IMAGE PROCESSING, VOL. 26, NO. 7, JULY 2017:3142-3155

采样图像: y

目标图像: x

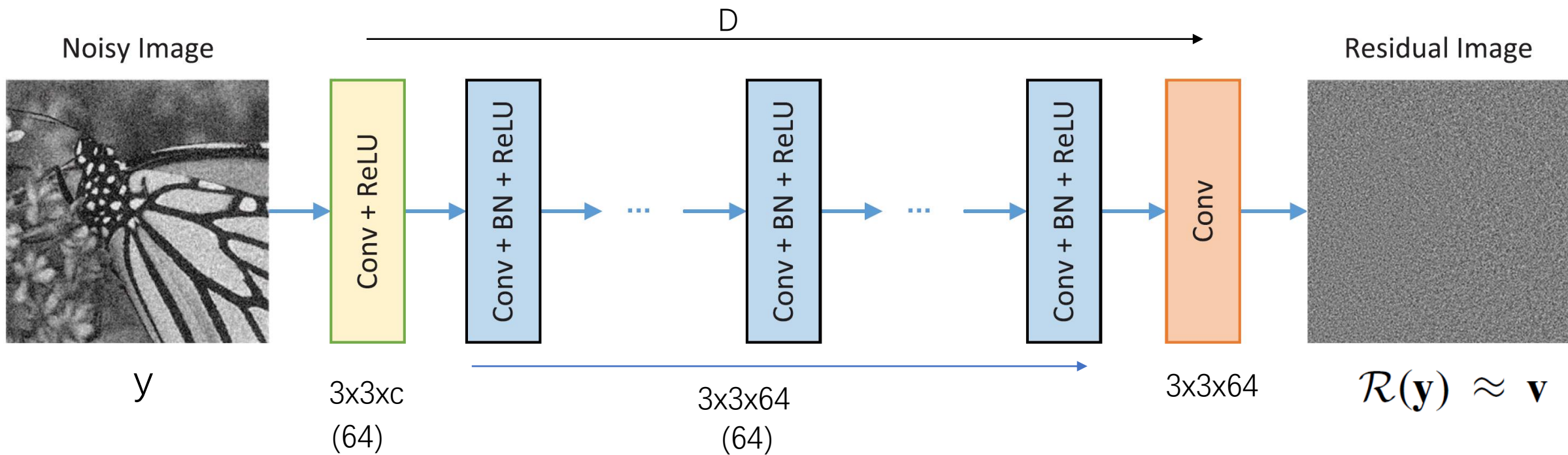
加性白噪声图像: v

(additive white Gaussian noise [AWGN])

$$y = x + v$$

denoising convolutional neural network (DnCNN)

- 训练网络输出噪声图像



$$\mathbf{x} = \mathbf{y} - \mathcal{R}(\mathbf{y})$$

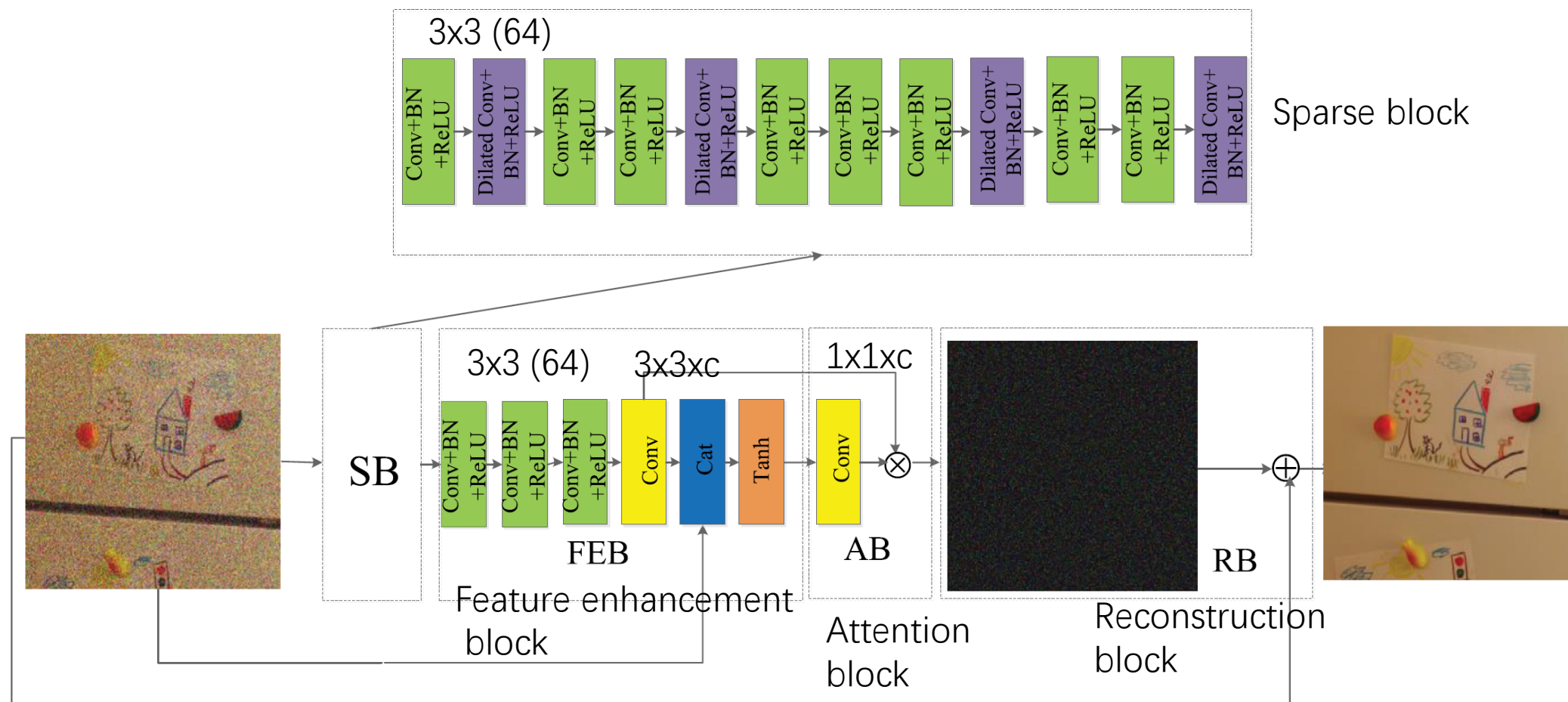
损失函数：

$$\ell(\Theta) = \frac{1}{2N} \sum_{i=1}^N \|\mathcal{R}(\mathbf{y}_i; \Theta) - (\mathbf{y}_i - \mathbf{x}_i)\|_F^2$$

【研讨论文2】

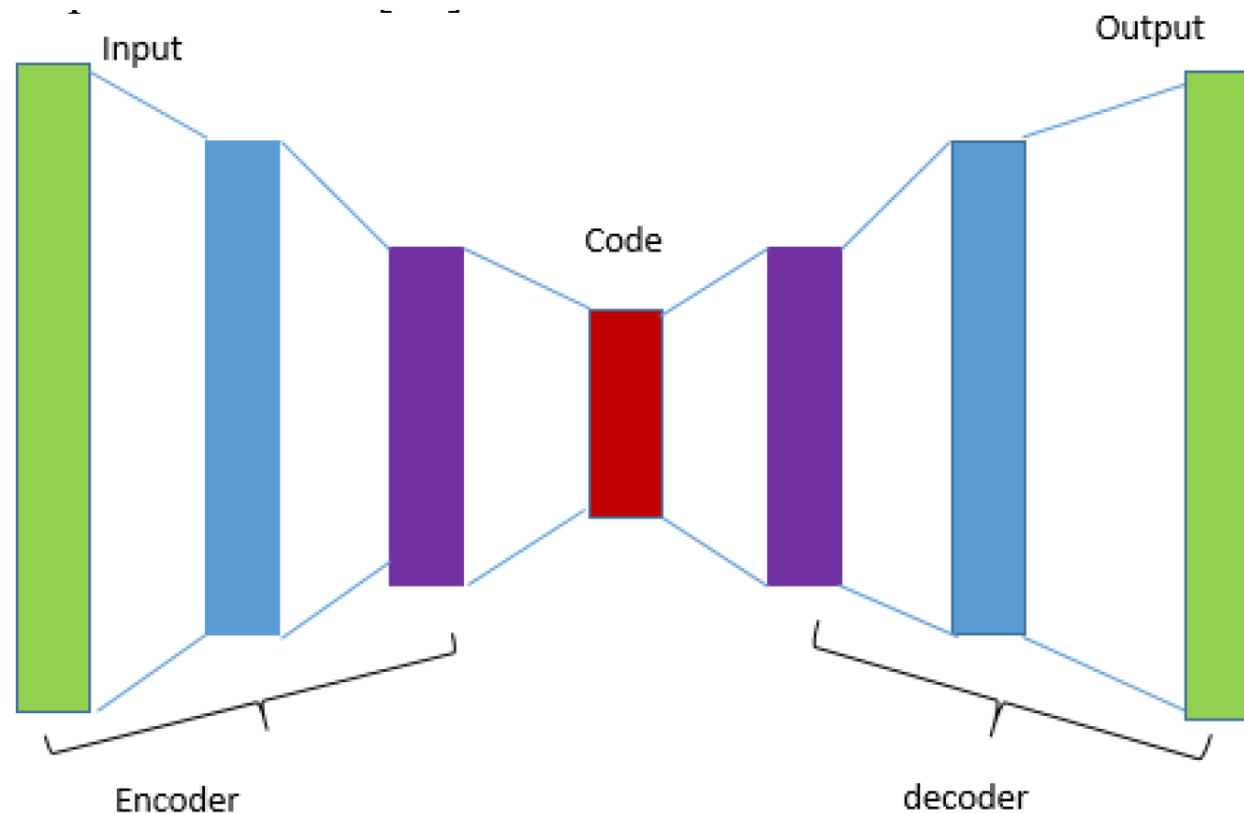
C.Tian, Y.Xu, *et al*, Attention-guided CNN for image denoising,
Neural Networks, 124 (2020): 117-129

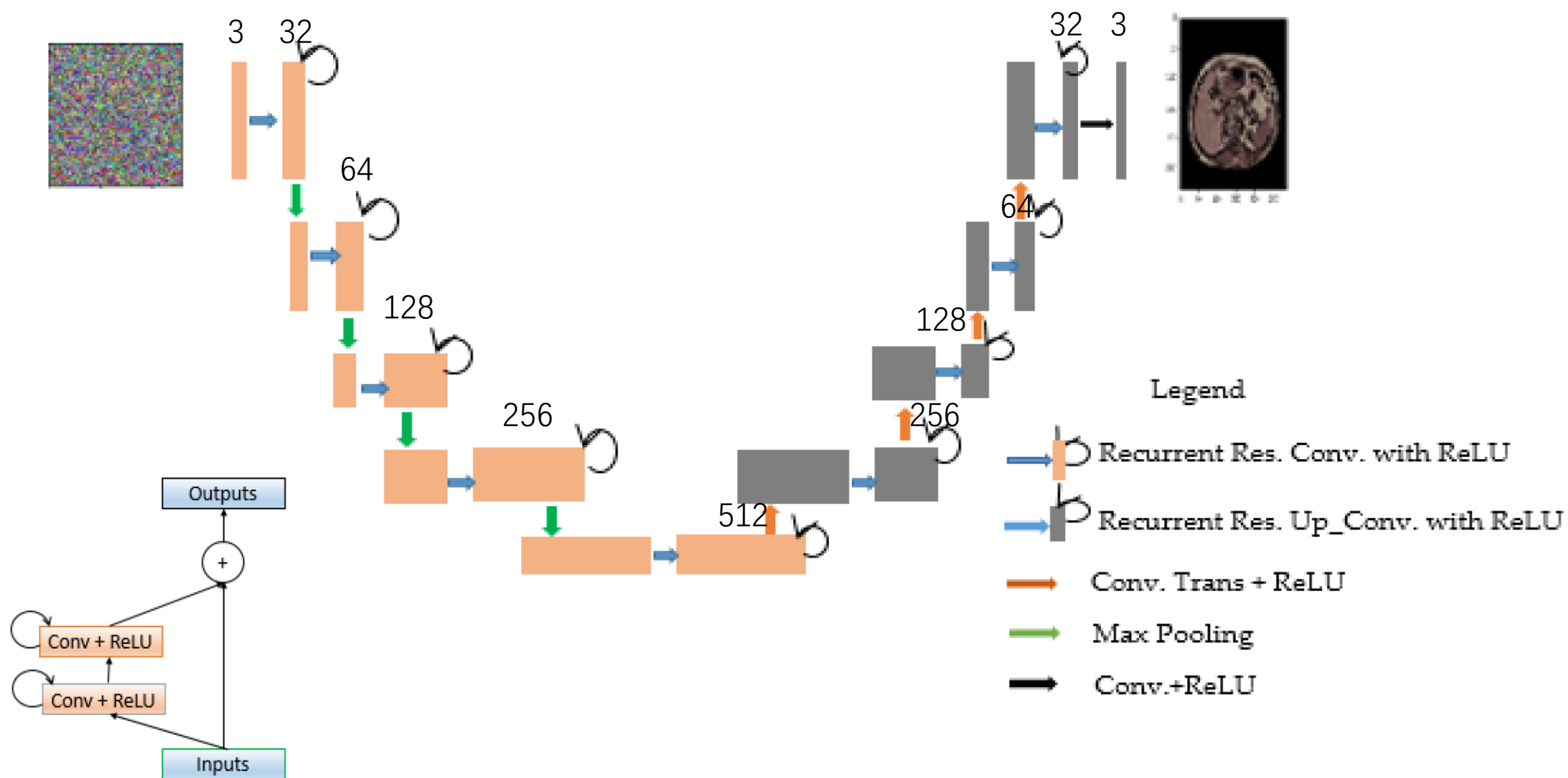
ADNet



【研讨论文3】

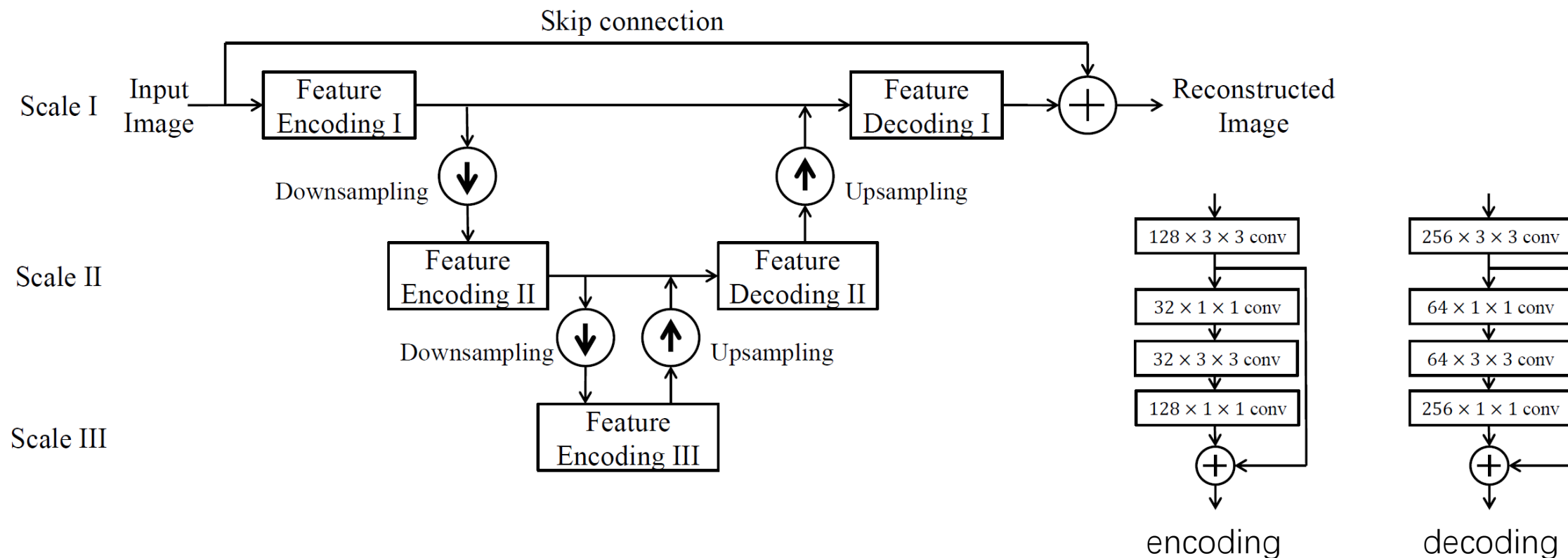
S.Nasrin, Z.Alom, *et al*, Medical image denoising with recurrent residual U-net (R2U-Net) base auto-encoder, Proc. IEEE National Aerospace and Electronics Conf. '2019 : pp 345-350



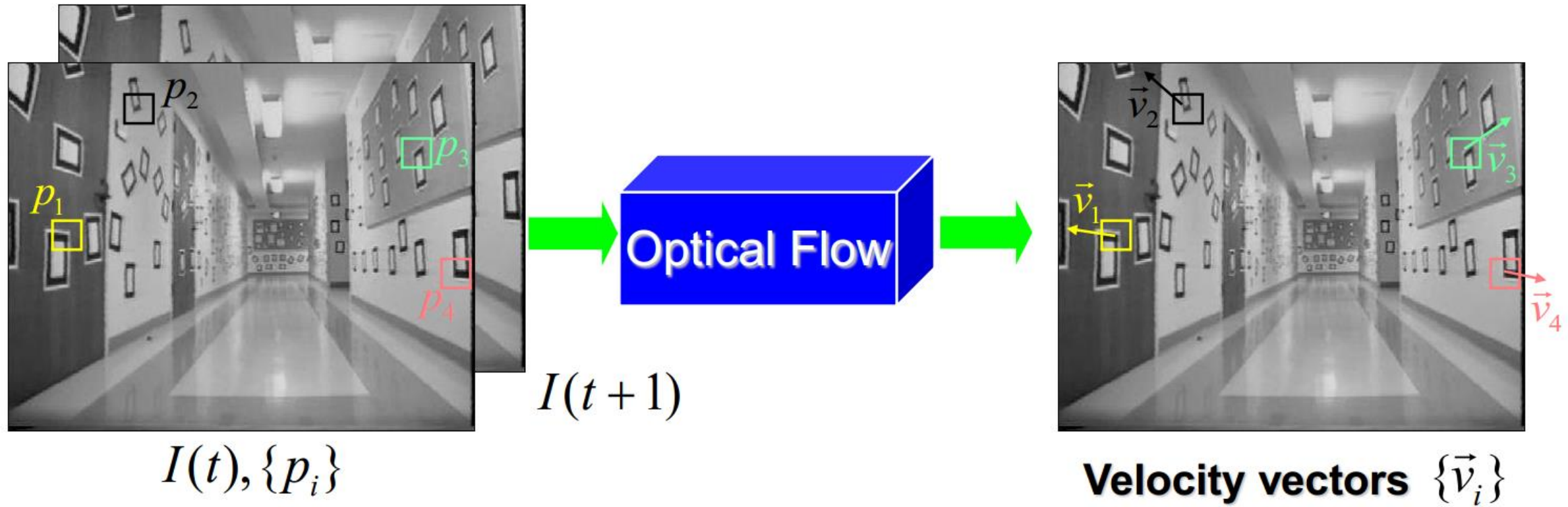


【研讨论文4】

D.Liu, B.Wen, *et al*, When Image Denoising Meets High-Level Vision Tasks: A Deep Learning Approach, Proc. the 27th International Joint Conference on Artificial Intelligence, 2018

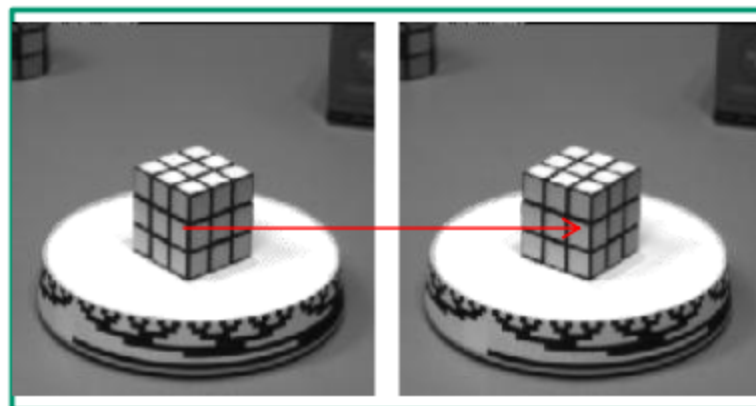


Optical Flow



$$I(p_i, t) = I(p_i + \vec{v}_i, t + 1)$$

Start with an Equation: Brightness Constancy



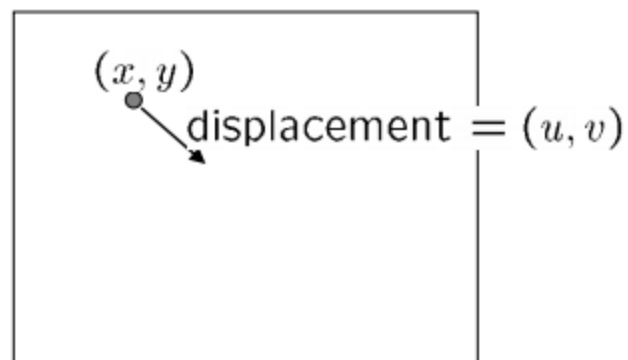
Time: t

Time: $t + dt$

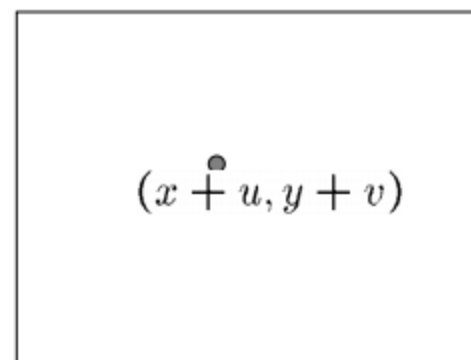
Point moves (small), but its
brightness remains constant:

$$I_{t1}(x, y) = I_{t2}(x + u, y + v)$$

$$I = \text{constant} \rightarrow \frac{dI}{dt} = 0$$



I_1



I_2

Mathematical formulation

$I(x(t), y(t), t)$ = brightness at (x, y) at time t

Brightness constancy assumption (shift of location but brightness stays same):

$$I\left(x + \frac{dx}{dt} \delta t, y + \frac{dy}{dt} \delta t, t + \delta t\right) = I(x, y, t)$$

Optical flow constraint equation (chain rule):

$$\frac{dI}{dt} = \frac{\partial I}{\partial x} \frac{dx}{dt} + \frac{\partial I}{\partial y} \frac{dy}{dt} + \frac{\partial I}{\partial t} = 0$$

The aperture problem

$$u = \frac{dx}{dt}, \quad v = \frac{dy}{dt}$$

$$I_x = \frac{\partial I}{\partial x}, \quad I_y = \frac{\partial I}{\partial y}, \quad I_t = \frac{\partial I}{\partial t}$$

$$I_x u + I_y v + I_t = 0$$

Horn and
Schunck
optical flow
equation

1 equation in 2 unknowns

Optical Flow: 1D Case

Brightness Constancy Assumption:

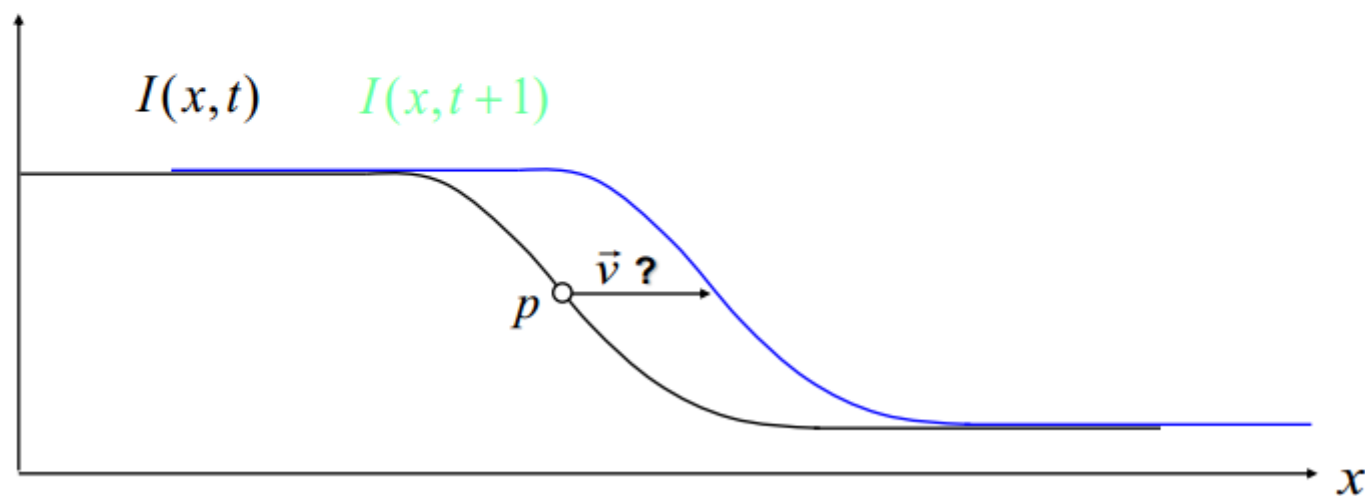
$$f(t) \equiv \underbrace{I(x(t), t)} = I(x(t + dt), t + dt)$$

$$\frac{\partial f(x)}{\partial t} = 0 \quad \text{Because no change in brightness with time}$$

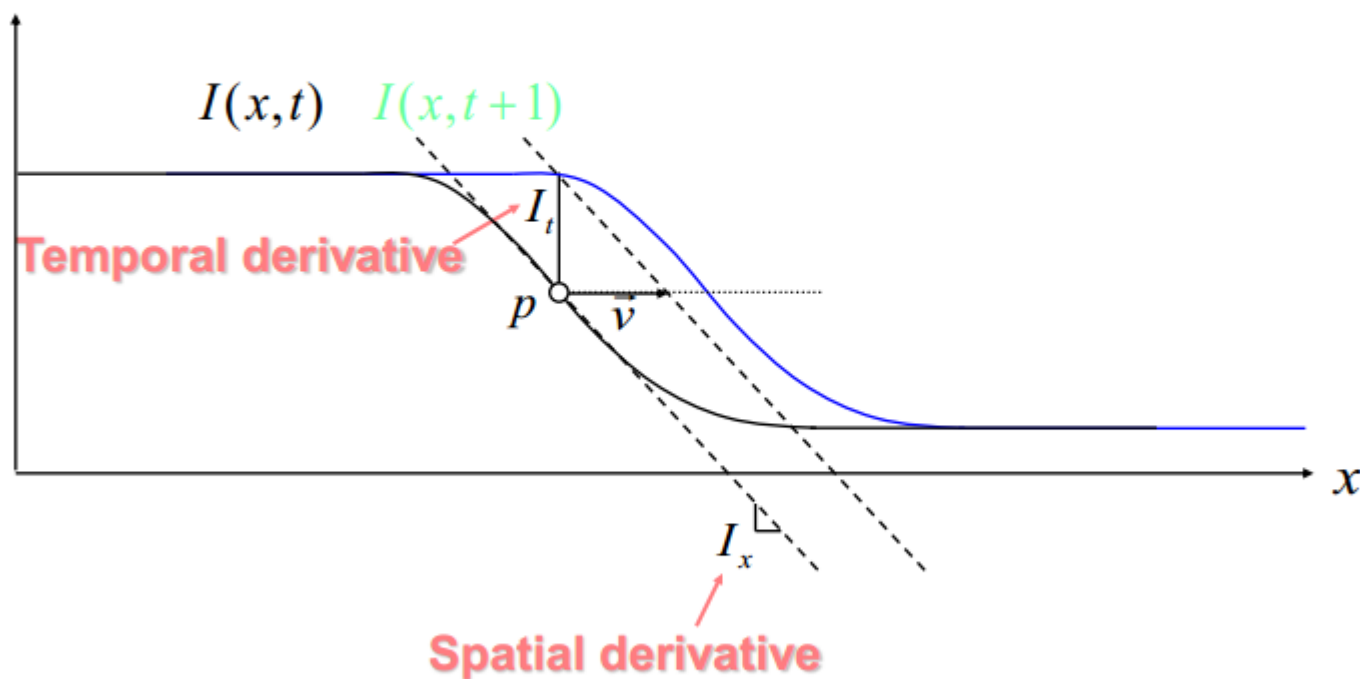
$$\underbrace{\frac{\partial I}{\partial x}}_{I_x} \bigg|_t \left(\underbrace{\frac{\partial x}{\partial t}}_v \right) + \underbrace{\frac{\partial I}{\partial t}}_{I_t} \bigg|_{x(t)} = 0$$

$$\Rightarrow v = - \frac{I_t}{I_x}$$

Tracking in the 1D case:



Tracking in the 1D case:



$$I_x = \left. \frac{\partial I}{\partial x} \right|_t$$

$$I_t = \left. \frac{\partial I}{\partial t} \right|_{x=p}$$



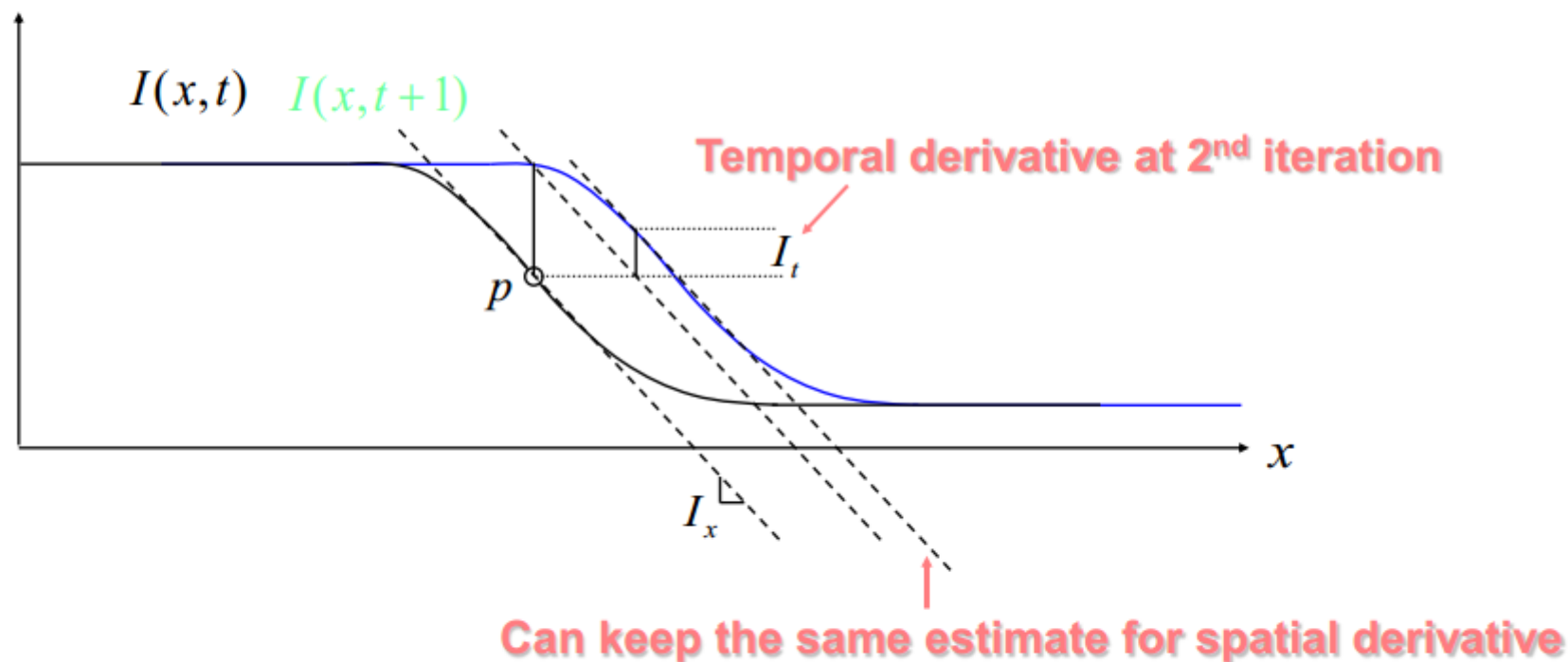
$$\vec{v} \approx -\frac{I_t}{I_x}$$

Assumptions:

- Brightness constancy
- Small motion

Tracking in the 1D case:

Iterating helps refining the velocity vector



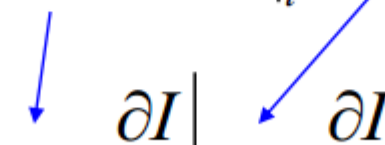
$$\vec{v} \leftarrow \vec{v}_{previous} - \frac{I_t}{I_x}$$

Converges in about 5 iterations

From 1D to 2D tracking

$$\text{1D: } \frac{\partial I}{\partial x} \bigg|_t \left(\frac{\partial x}{\partial t} \right) + \frac{\partial I}{\partial t} \bigg|_{x(t)} = 0$$

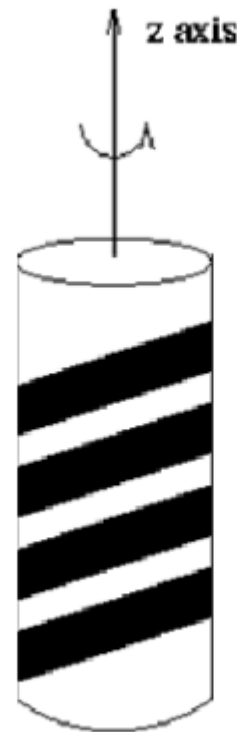
$$\text{2D: } \frac{\partial I}{\partial x} \bigg|_t \left(\frac{\partial x}{\partial t} \right) + \frac{\partial I}{\partial y} \bigg|_t \left(\frac{\partial y}{\partial t} \right) + \frac{\partial I}{\partial t} \bigg|_{x(t)} = 0$$

$$\frac{\partial I}{\partial x} \bigg|_t u + \frac{\partial I}{\partial y} \bigg|_t v + \frac{\partial I}{\partial t} \bigg|_{x(t)} = 0$$


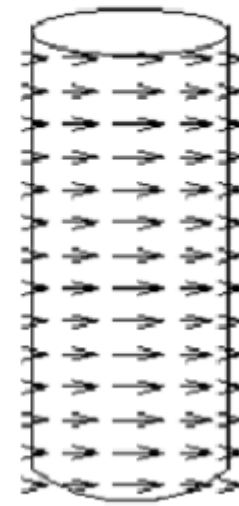
One equation, two velocity (u, v) unknowns...

Optical Flow vs. Motion: Aperture Problem

Barber pole illusion



Barber's pole

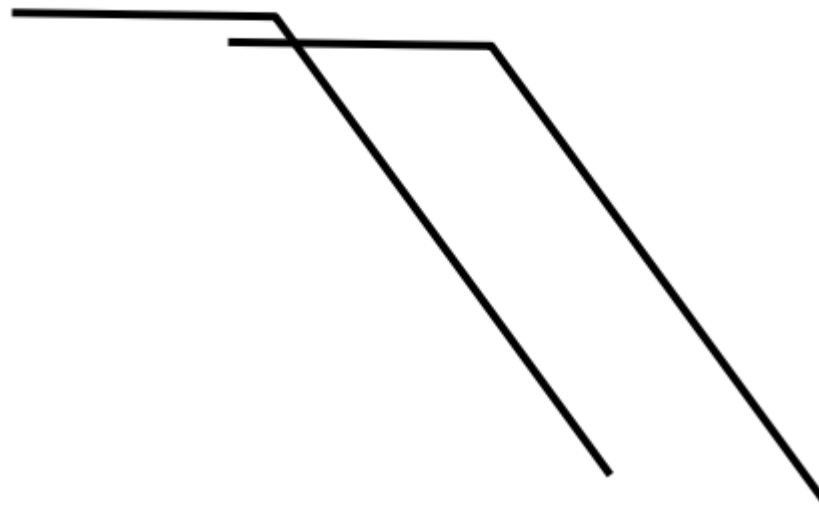
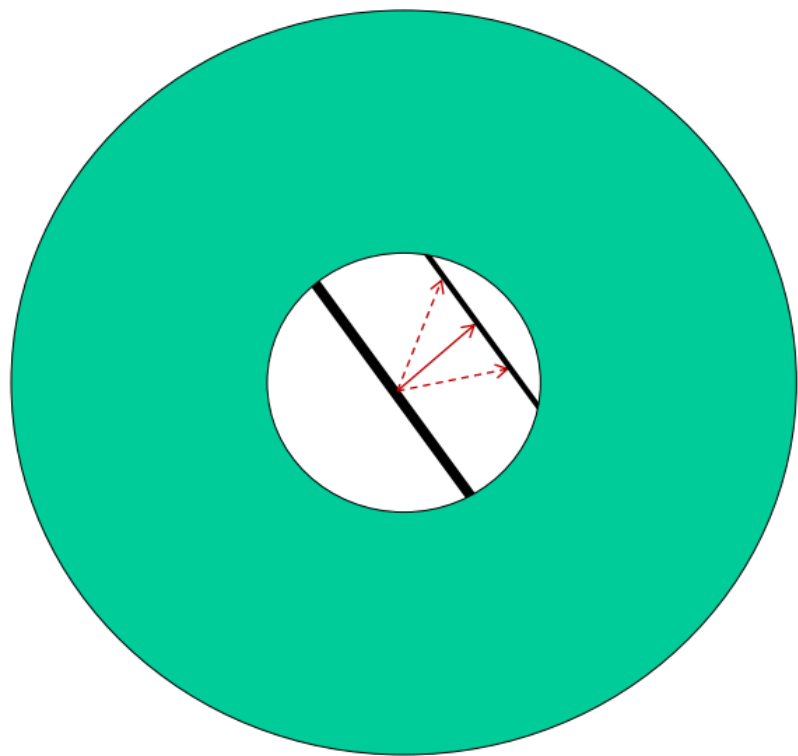


Motion field



Optical flow

Aperture Problem



Normal Flow

Notation

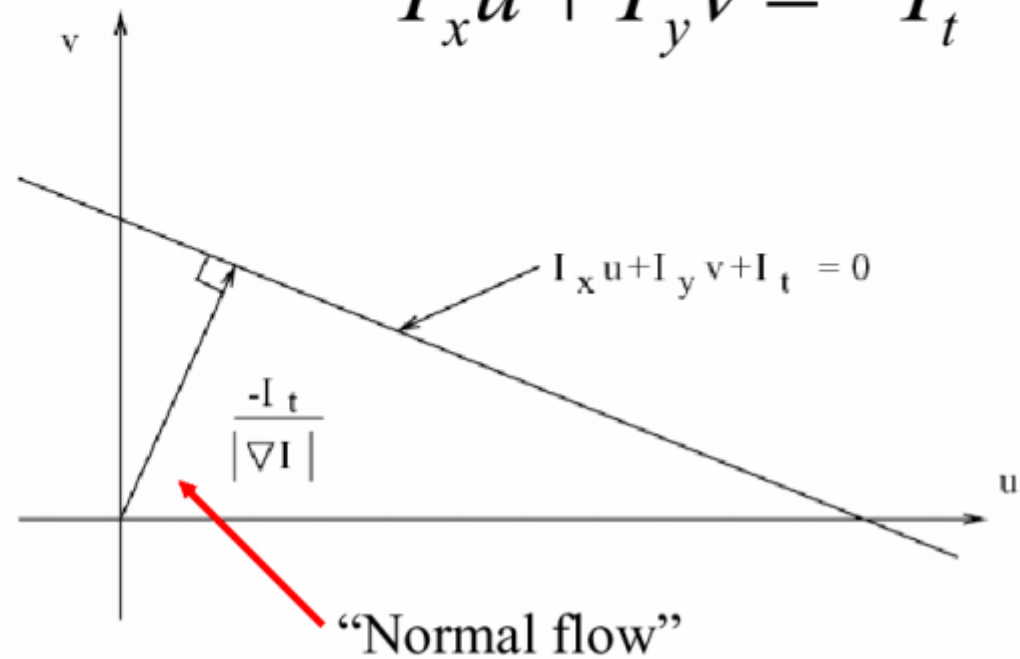
$$I_x u + I_y v + I_t = 0$$

$$\nabla I^T \mathbf{u} = -I_t$$

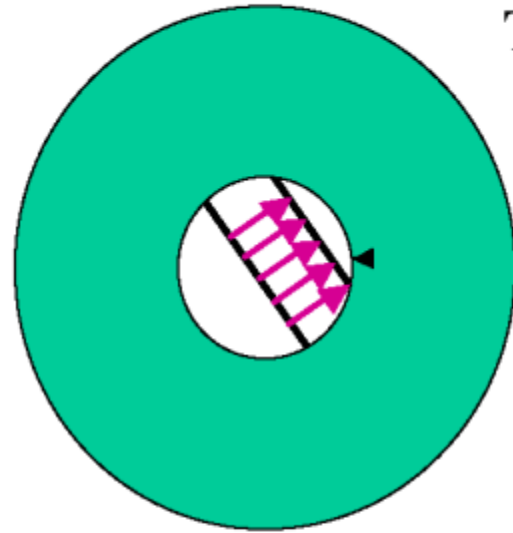
$$\mathbf{u} = \begin{bmatrix} u \\ v \end{bmatrix} \quad \nabla I = \begin{bmatrix} I_x \\ I_y \end{bmatrix}$$

At a single image pixel, we get a line:

$$I_x u + I_y v = -I_t$$



Aperture Problem and Normal Flow



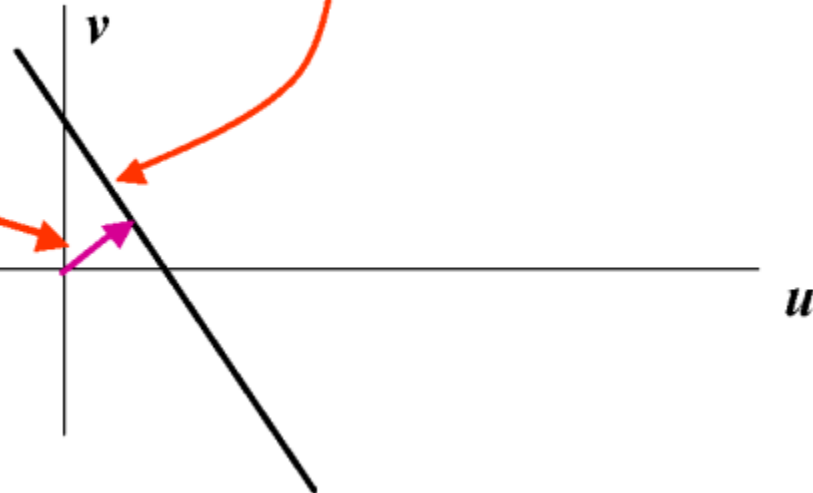
The gradient constraint:

$$\begin{aligned} I_x u + I_y v + I_t &= 0 \\ \nabla I \bullet \vec{U} &= 0 \end{aligned}$$

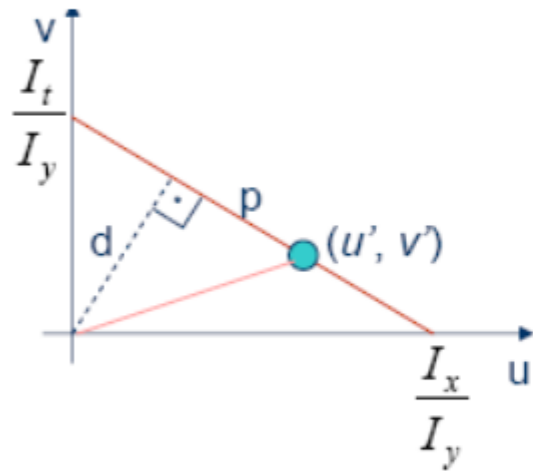
Defines a line in the (u, v) space

Normal Flow:

$$u_{\perp} = -\frac{I_t}{|\nabla I|} \frac{\nabla I}{|\nabla I|}$$



Aperture Problem and Normal Flow



$$v = u \frac{I_x}{I_y} + \frac{I_t}{I_y}$$

- Let (u', v') be true flow
- True flow has two components
 - Normal flow: d
 - Parallel flow: p
- Normal flow **can be** computed
- Parallel flow **cannot**

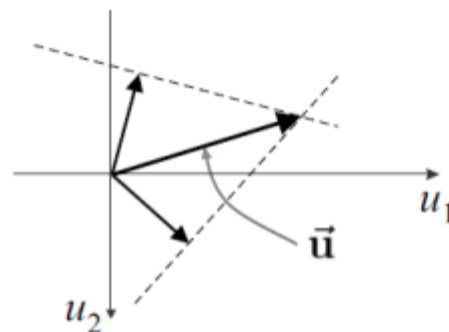
Possible Solution: Neighbors

Two adjacent pixels which are part of the same rigid object:

- we can calculate normal flows \mathbf{v}_{n1} and \mathbf{v}_{n2}
- Two OF equations for 2 parameters of flow: $\bar{\mathbf{v}} = \begin{pmatrix} v \\ u \end{pmatrix}$

$$\nabla I_1 \cdot \bar{\mathbf{v}} - I_{t1} = 0$$

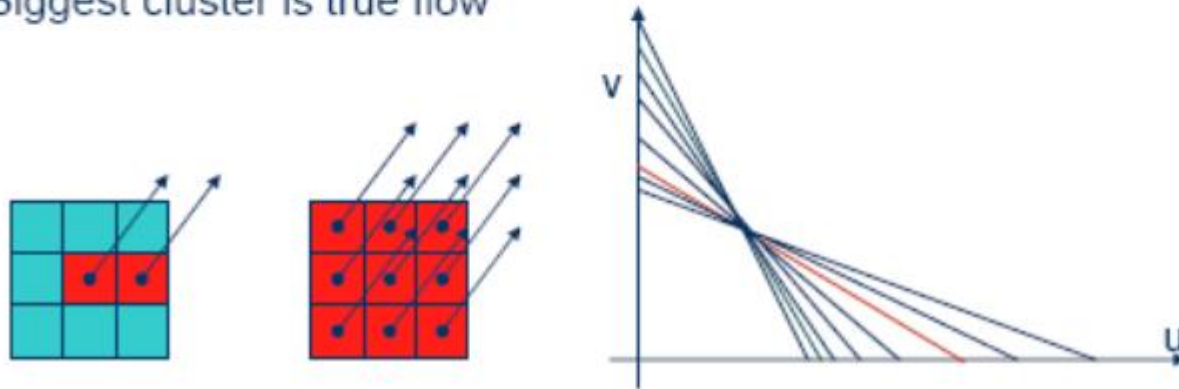
$$\nabla I_2 \cdot \bar{\mathbf{v}} - I_{t2} = 0$$



Considering Neighbor Pixels

Schunck

- If two neighboring pixels move with same velocity
 - Corresponding flow equations intersect at a point in (u,v) space
 - Find the intersection point of lines
 - If more than 1 intersection points find clusters
 - Biggest cluster is true flow



Horn & Schunck algorithm

Horn and Schunck's approach — Regularization

Two terms are defined as follows:

- Departure from smoothness

$$e_s = \int \int_{\Omega} ((u_x^2 + u_y^2) + (v_x^2 + v_y^2)) dx dy$$

- Error in optical flow constraint equation

$$e_c = \int \int_{\Omega} (E_x u + E_y v + E_t)^2 dx dy$$

The formulation is to minimize the linear combination of e_s and e_c ,

$$e_s + \lambda e_c$$

where λ is a parameter.

Note: In this formulation, u and v are functions of x and y . Physically, u is the x -component of the motion, and v is the y -component of the motion.

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Horn & Schunck

The Euler-Lagrange equations :

$$F_u - \frac{\partial}{\partial x} F_{u_x} - \frac{\partial}{\partial y} F_{u_y} = 0$$

$$F_v - \frac{\partial}{\partial x} F_{v_x} - \frac{\partial}{\partial y} F_{v_y} = 0$$

In our case ,

$$F = (u_x^2 + u_y^2) + (v_x^2 + v_y^2) + \lambda(I_x u + I_y v + I_t)^2,$$

so the Euler-Lagrange equations are

$$\Delta u = \lambda(I_x u + I_y v + I_t)I_x,$$

$$\Delta v = \lambda(I_x u + I_y v + I_t)I_y,$$

$$\Delta = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \quad \text{is the Laplacian operator}$$

Horn & Schunck

Remarks :

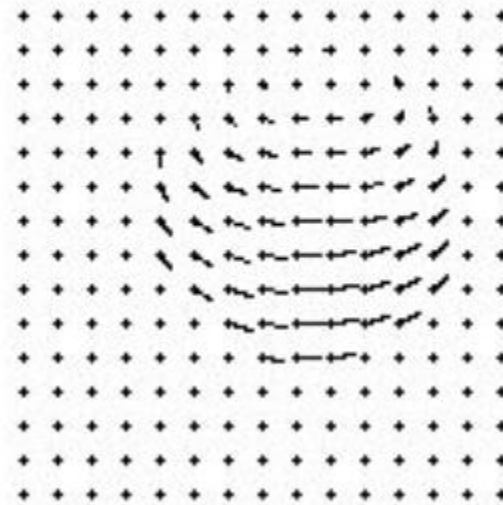
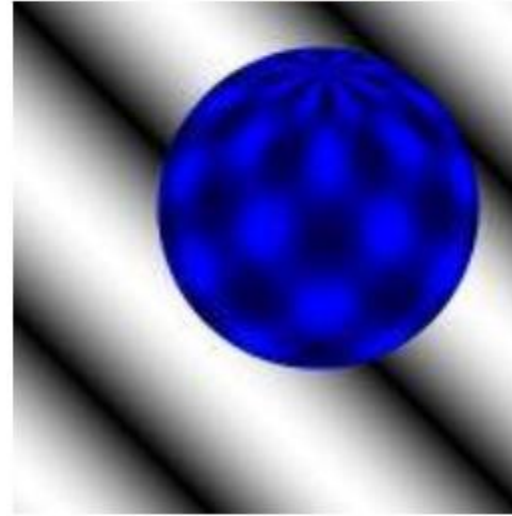
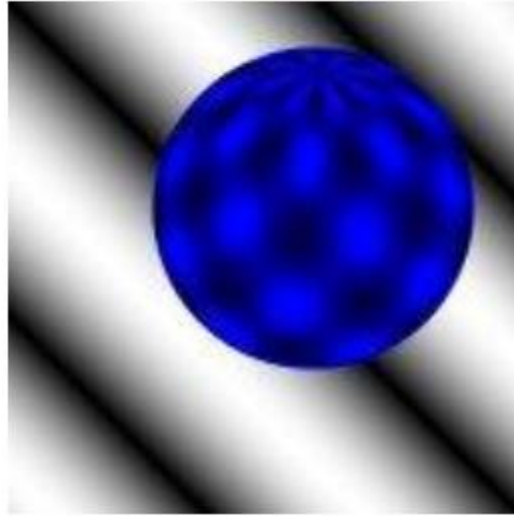
1. Coupled PDEs solved using iterative methods and finite differences

$$\frac{\partial u}{\partial t} = \Delta u - \lambda(I_x u + I_y v + I_t)I_x,$$

$$\frac{\partial v}{\partial t} = \Delta v - \lambda(I_x u + I_y v + I_t)I_y,$$

2. More than two frames allow a better estimation of I_t
3. Information spreads from corner-type patterns

Example



超分辨率图像重建 (superresolution)

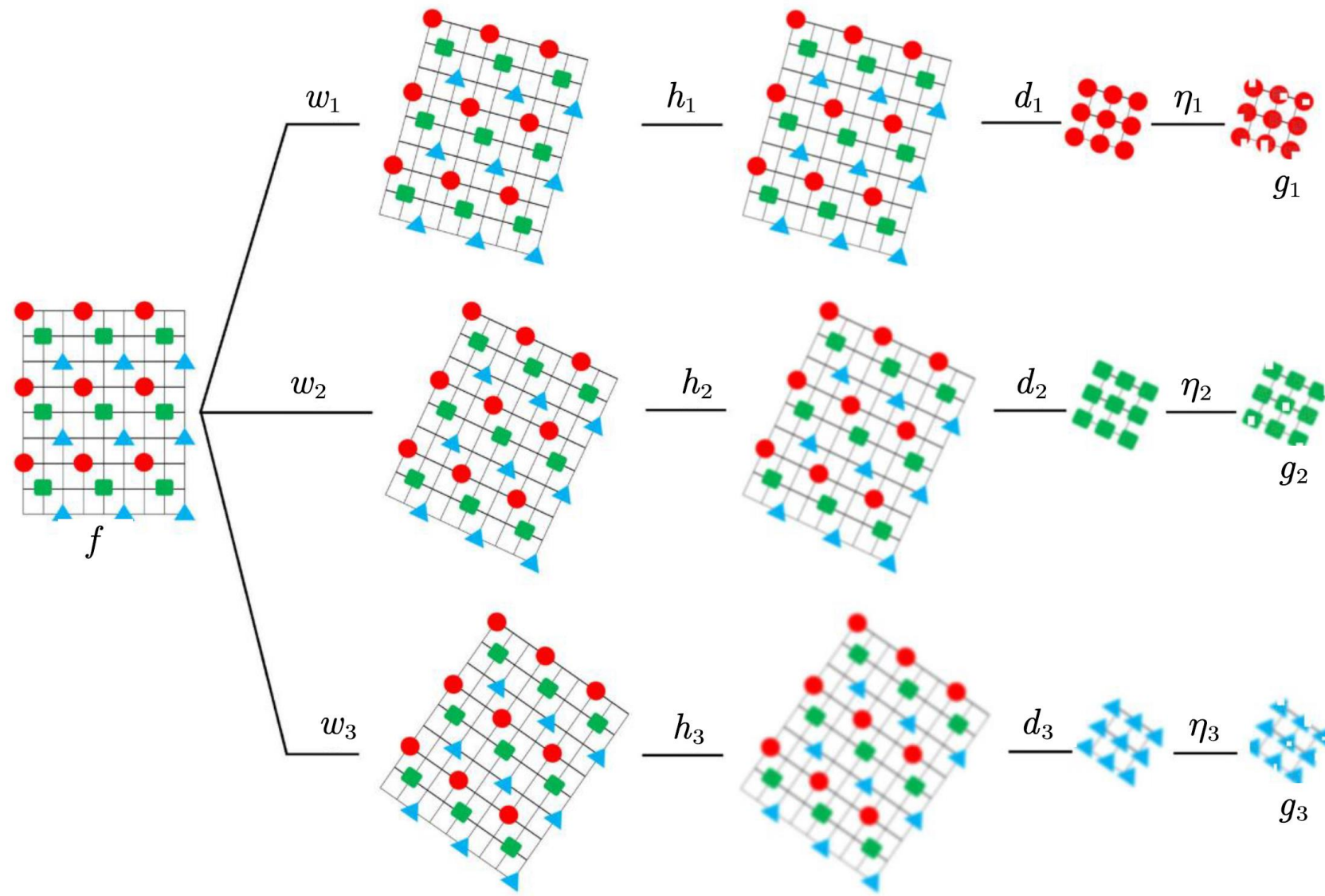
高分辨(HR)场景图像 $f(x,y)$

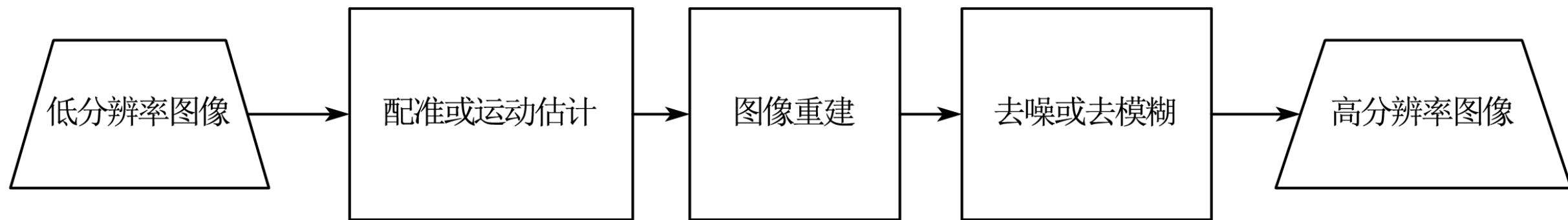
低分辨率(LR)场景图像 $g(m,n)$

$$g(m,n) = d \left(h \left(w(f(x,y)) \right) \right) + \eta(m,n)$$

$d()$: 降采样, $h()$: 模糊算子, $w()$: 形变矩阵

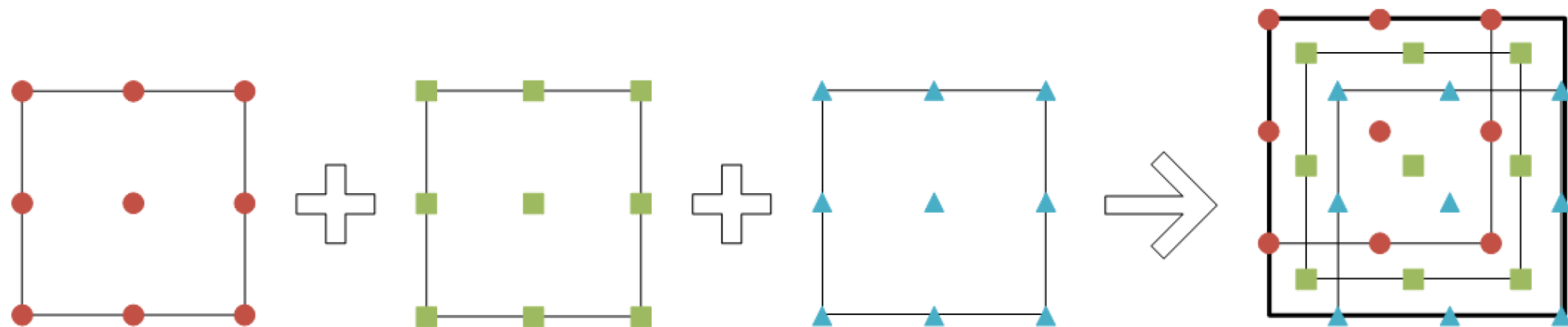
$$g = Af + \eta$$





单图像超分辨率 → 根据经验（模型）估计HR图像

多图像超分辨率 → 图像之间的亚像素位移补充HL图像中缺失的高频信息

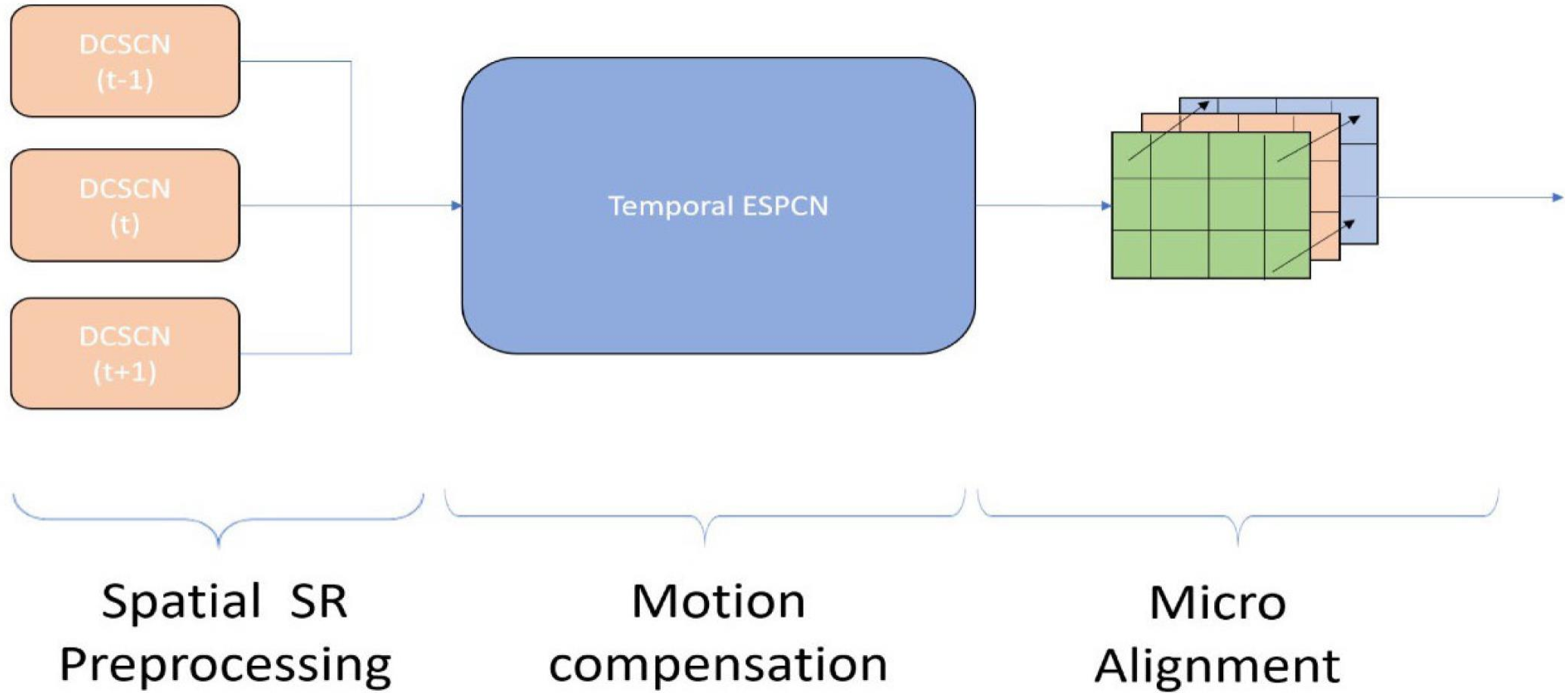


位移估计：光流场估计

$$I(\vec{x}, t) = I(\vec{x} + \vec{u}, t + 1)$$

$$\frac{d}{dt}I(\vec{x}(t), t) = \frac{\partial I}{\partial x} \frac{\partial x}{\partial t} + \frac{\partial I}{\partial y} \frac{\partial y}{\partial t} + \frac{\partial I}{\partial t} \frac{\partial t}{\partial t} = \nabla I \cdot \vec{u} + I_t = 0$$

J.Mojoo, M.Sabri, T.Kurita, Video Super Resolution with Estimation of Motion Information by Using Higher Resolution Images Obtained by Single Image Super Resolution, Proc. International Joint Conference on Neural Networks, 2019



【研讨论文5】

S.Savvin, A.Sirota, **An Algorithm for Multi-Fame Image Super-Resolution Under Applicative Noise Based on a Convolutional Neural Network**, proc. international conf. on Control Systems, Mathematical Modeling, Automation and Energy Efficiency, 2020, pp 422-424

