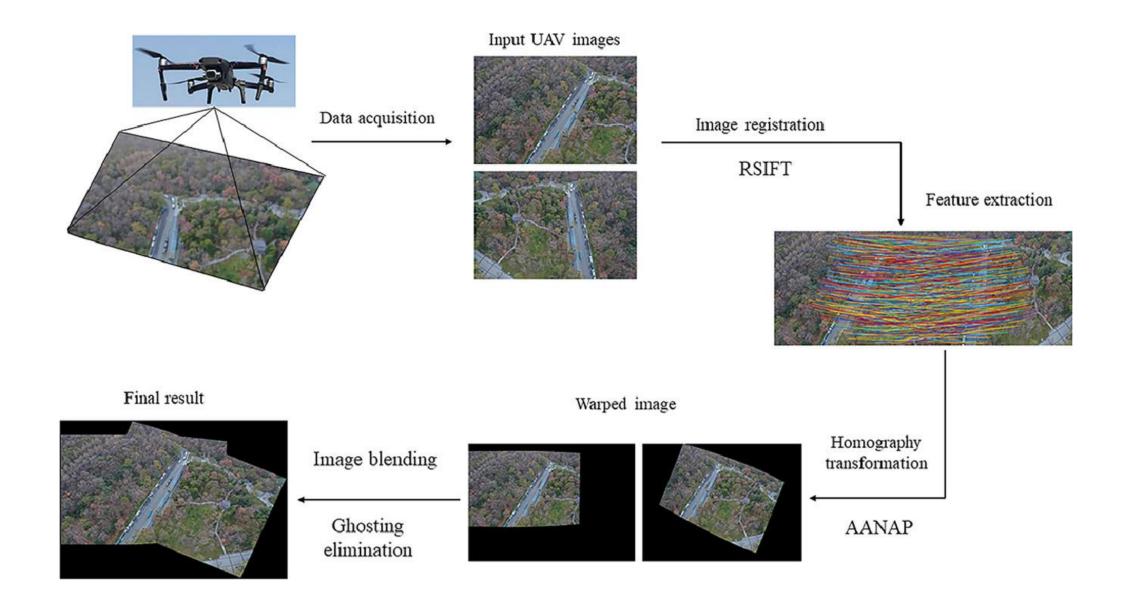
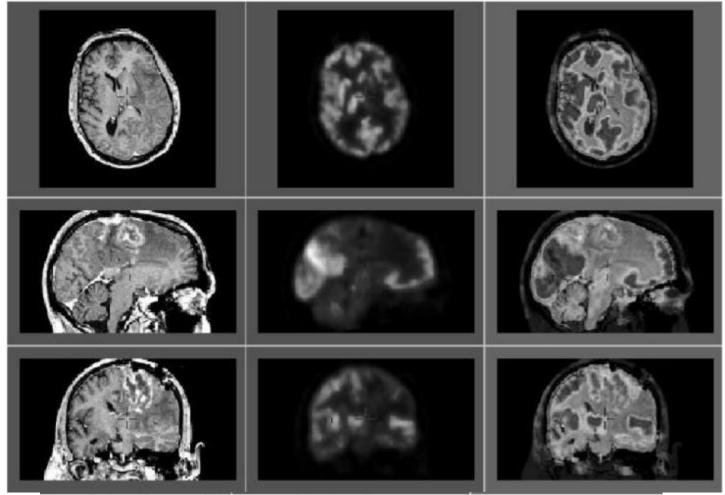
# 图像配准、拼接、融合

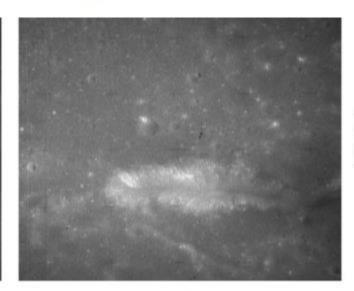
Image Registration, Mosaicing, Fusion



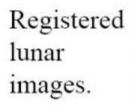


Registration of MR and PET images of the same person.

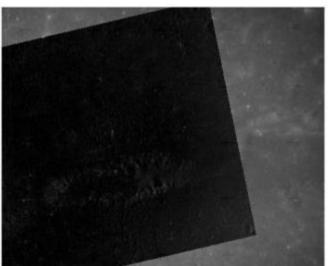
Lunar image 1.



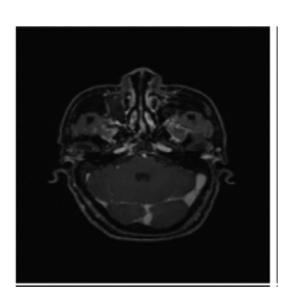
Lunar image 2.

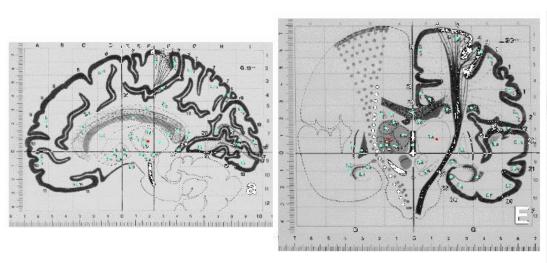


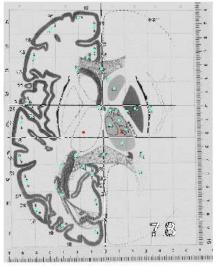




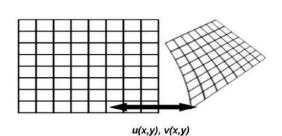
Subtracted images after registration.

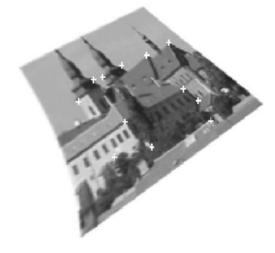


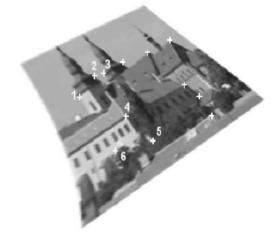














# 图像配准主要步骤

- 1. 特征提取 area based, feature based
- 2. 特征匹配 area based : correlation-like methods
- 3. 坐标映射 浮动图坐标映射到参考图坐标
- 4. 图像几何变换 图像变换到相同坐标系

## **Geometric Transform Models**

# Global mapping models

Bivariate polynomials of low degrees

$$u = \sum_{i=0}^{N} \sum_{j=0}^{N} a_{ij} x^{i} y^{j}$$
$$v = \sum_{i=0}^{N} \sum_{j=0}^{N} b_{ij} x^{i} y^{j}$$

仿射变换(affine transform)

$$\begin{pmatrix} u \\ v \end{pmatrix} = \begin{pmatrix} a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{pmatrix} \begin{pmatrix} x \\ y \\ 1 \end{pmatrix}$$

# 特征匹配 (Feature Matching)

### Area based methods:

Correlation-like methods

$$NCC(u) = \frac{\sum_{i} [I_{1}(x_{i}) - \overline{I_{1}}][I_{2}(x_{i} + u) - \overline{I_{2}}]}{\sqrt{\sum_{i} [I_{1}(x_{i}) - \overline{I_{1}}]^{2}[I_{2}(x_{i} + u) - \overline{I_{2}}]^{2}}} \qquad \overline{I_{1}} = \frac{1}{N} \sum_{i} I_{1}(x_{i})$$

$$\overline{I_{2}} = \frac{1}{N} \sum_{i} I_{2}(x_{i} + u)$$

Mutual Information methods

$$E(I_1) = -\sum_{g} p_{I_1}(g) \log(p_{I_1}(g))$$

$$MI(I_1, I_2) = E(I_1) + E(I_2) - E(I_1, I_2)$$

$$E(I_1, I_2) = -\sum_{g,h} p_{I_1, I_2}(g, h) \log(p_{I_1, I_2}(g, h))$$

### Feature based methods

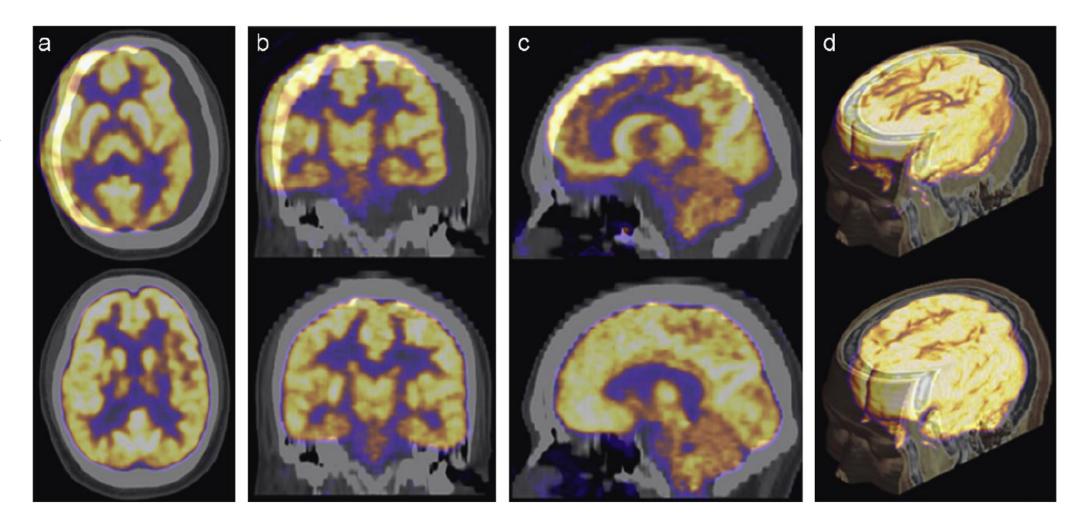
Harris corner detector

$$C = \sum_{i} w(x_i, y_i) \begin{bmatrix} I_{x_i}^2 & I_{x_i} I_{y_i} \\ I_{x_i} I_{y_i} & I_{y_i}^2 \end{bmatrix} \qquad R = Det(C) - \alpha Tr^2(C)$$

$$0.04 \leqslant \alpha \leqslant 0.06$$

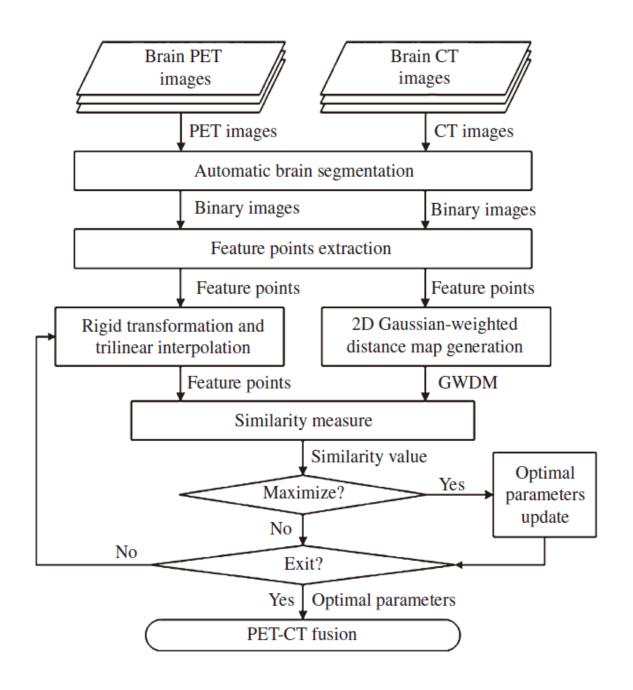
**Graph matching Algorithm** 

H. Lee, J. Lee, *et al*, Robust feature-based registration using a Gaussian-weighted distance map and brain feature points for brain PET/CT images, Computers in Biology and Medicine 38 (2008) 945–961

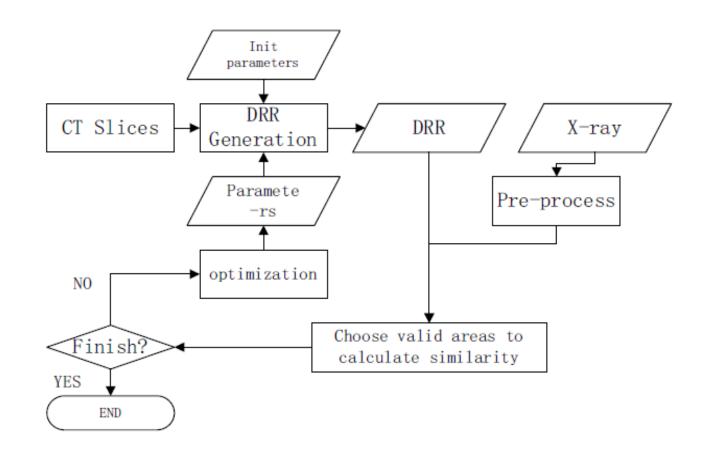


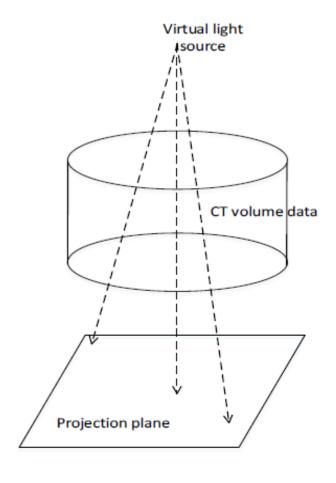
配准前

配准后

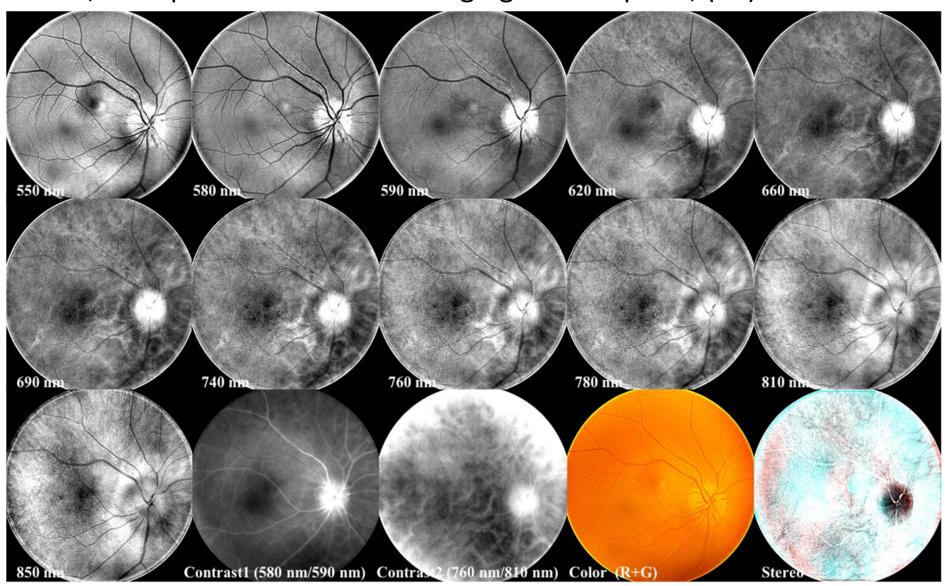


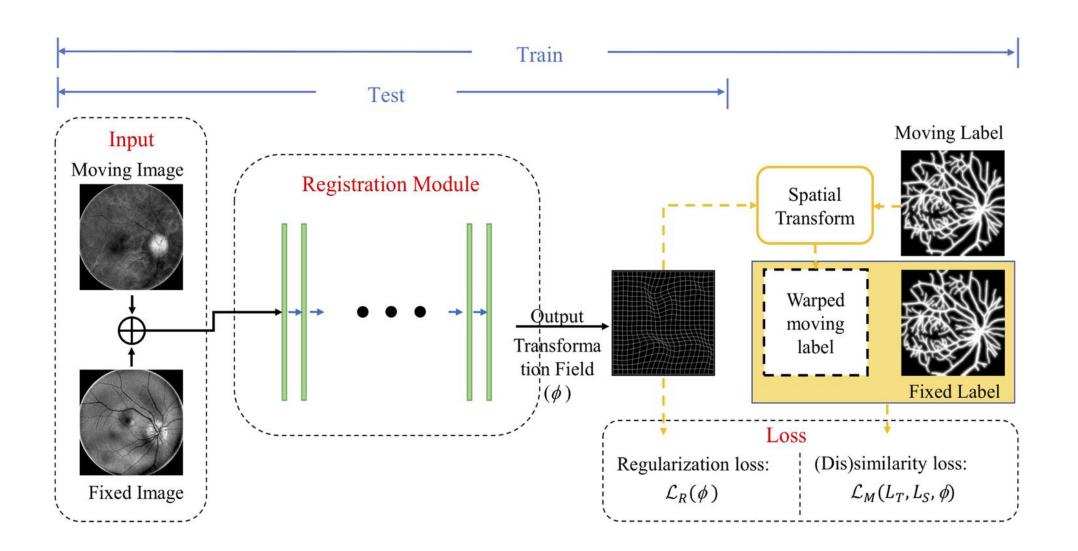
H. Pan, C. Zhou, *et al*, A Fast Registration from 3D CT Images to 2D X-ray Images, Proc. IEEE 3rd International Conference on Big Data Analysis, 2018, pp 351-355

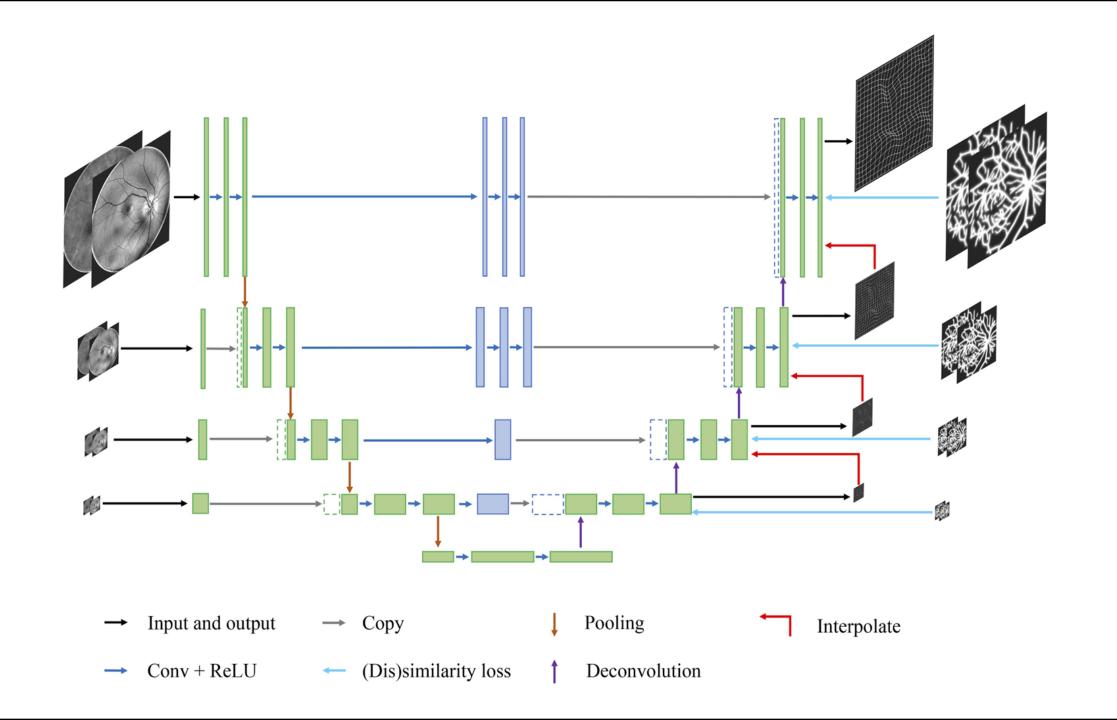




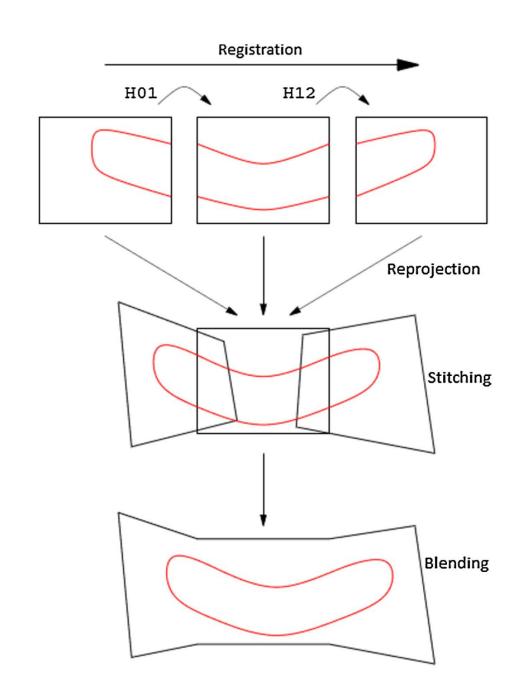
X. Sui, Y. Zheng, et al, Deep multispectral image registration network, Computerized Medical Imaging and Graphics, (87) 2021



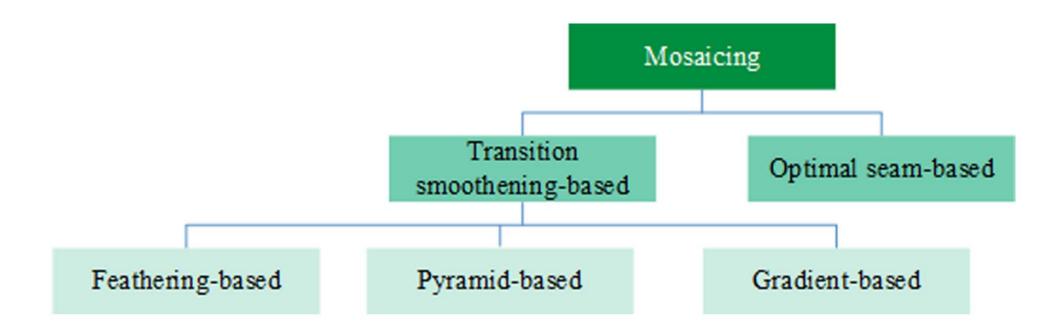




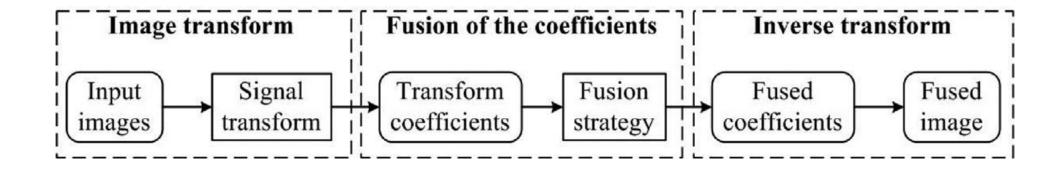
图像拼接 (Image Mosaicing)



# Image Blending



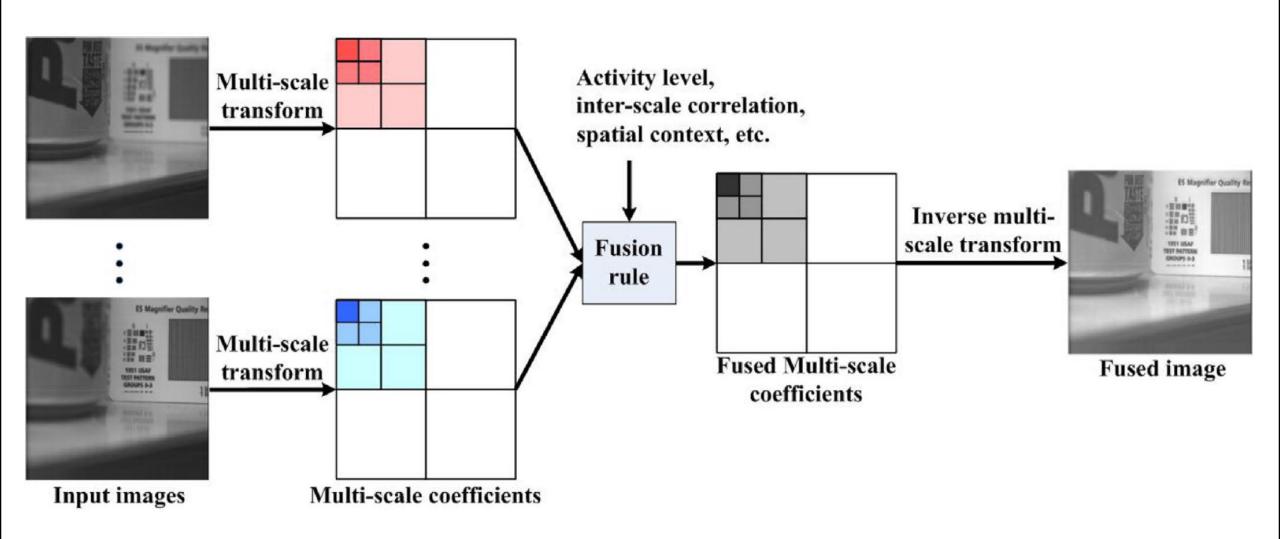
# Pixel based image fusion



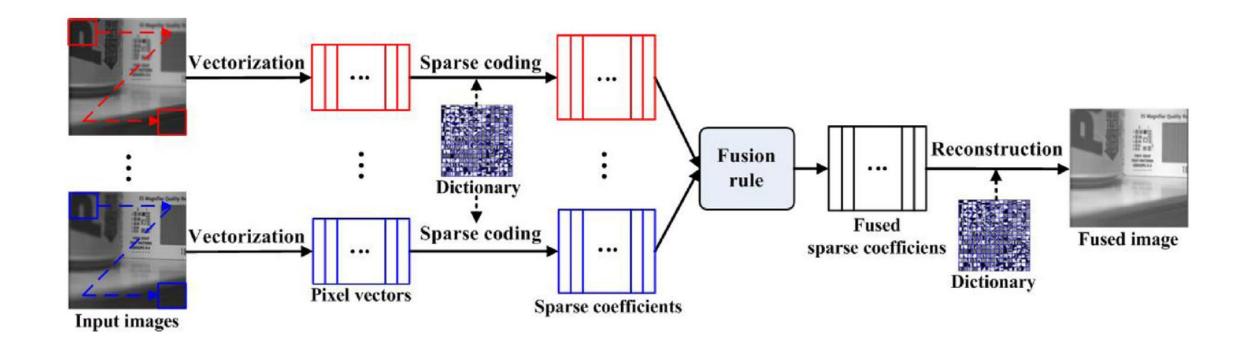
Multi-scale decomposition

Sparse representation (SR)

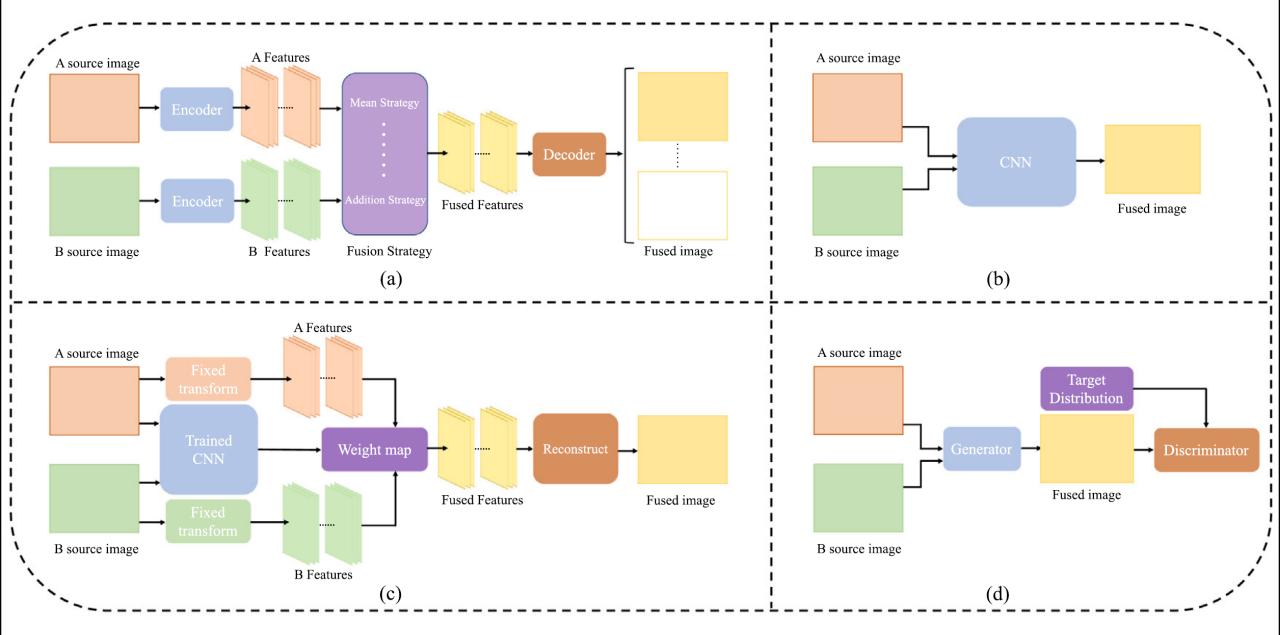
Methods in other domains



Multi-scale based image fusion



Sparsity based image fusion



deep architectures for image fusion.

