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Indian Institute of Technology Hyderabad

# Quality Aware Generative Adversarial Networks

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- Background
  - Generative Adversarial Network
  - Wasserstein Generative Adversarial Network (WGAN).
  - WGAN-GP
  - Banach WGAN
- Image Quality Assessment
  - Structural Similarity Index (SSIM).
  - Natural Image Quality Evaluator (NIQE)
- Proposed QAGANs
  - QAGAN based on SSIM
  - QAGAN based on NIQE
- References

## Generative Adversarial Network <sup>1</sup>

- Suppose the data points ( $x$ ) are coming from some distribution  $p_{data}(x)$  and  $z$  is the random noise vector drawn from standard Normal distribution  $p_z(z)$ .
- $G(z; \theta_g)$ : Generator with parameters  $\theta_g$ .
- $D(x; \theta_d)$ : Discriminator with parameters  $\theta_d$ .

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<sup>1</sup>I. Goodfellow, J. Pouget-Abadie, M. Mirza, B. Xu, D. Warde-Farley, S. Ozair, A. Courville, and Y. Bengio,

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# Background

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## Objective function

- $D$  and  $G$  play the following two player min-max game with value function  $V(G; D)$ :

$$\min_G \max_D V(D, G) = E_{x \sim p_{data}(x)} [\log(D(x))] + E_{z \sim p_z(z)} [\log(1 - D(G(z)))]$$

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## Wasserstein Generative Adversarial Networks [Arjovsky et al., 2017]

The primal form:  $W(p_r, p_\theta) = \inf_{\gamma \in \Gamma(p_r, p_\theta)} E_{(x,y) \sim \gamma} [\|x - y\|_2]$

$$W(p_r, p_\theta) = \max_{w \in W} E_{x \sim p_r} [D_w(x)] - E_{z \sim p_z} [D_w(g_\theta(z))], \quad w \in [-c, c].$$

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## WGAN-GP [Gulrajani et al., 2017]

$$|D_w(x) - D_w(y)| \leq \|x - y\|_2 \implies \|\nabla D_w(x)\|_2 \leq 1 \quad \forall x \in R^n.$$

$$L = E_{x \sim p_r} [D_w(x)] - E_{z \sim p_z} [D_w(g_\theta(z))] + \lambda E_{\hat{x}} (\|\nabla D_w(\hat{x})\|_2 - 1)^2$$

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## Banach WGAN [Adler and Lunz, 2018]

Generalized the theory of WGAN-GP to Banach spaces.

$$L = \lambda E_{x \sim p_r} [D_w(x)] - E_{z \sim p_z} [D_w(g_\theta(z))] + \lambda E_{\hat{x}} \left( \frac{1}{\gamma} \|\nabla D_w(\hat{x})\|_{B^*} - 1 \right)^2$$

## Challenges in Generative Adversarial Networks:

- **Low visual quality.**
- Mode collapse.
- Generalization.
- Disentanglement.
- Stability in training.



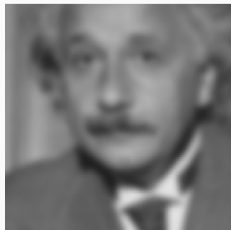
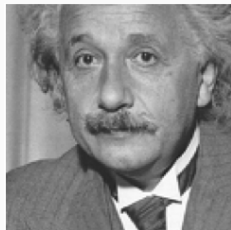
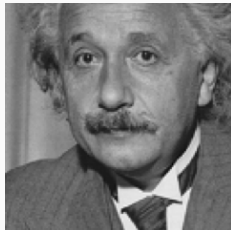
# Major contributions

- We make explicit use of objective image quality assessment (IQA) metrics and their variants for regularizing WGAN with gradient penalty (WGAN-GP), and propose Quality Aware GANs (QAGANs).
- Specifically we have used a full reference image quality assessment algorithm (SSIM) and natural image quality evaluator (NIQE).

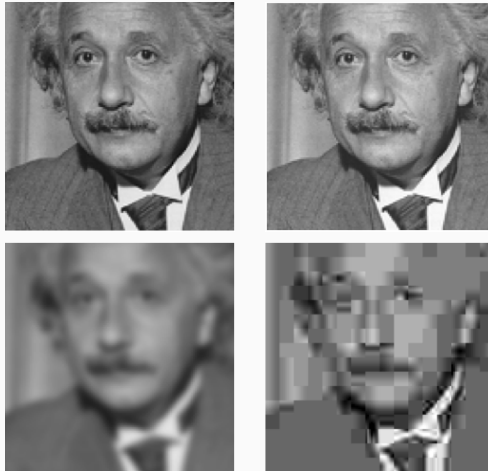
$$(WGAN - GP) + \begin{pmatrix} SSIM' \\ NIQE \end{pmatrix} \Longrightarrow \begin{pmatrix} QAGAN - SSIM \\ QAGAN - NIQE \end{pmatrix}$$

- We demonstrated state-of-the-art performance on CIFAR-10, STL10 and CelebA datasets for non-progressive GANs.

# What is Quality Assessment?



# Why Quality Assessment?



All distorted images have same mean squared error (MSE)!  $L^p$  norms fail! <sup>2</sup>

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<sup>2</sup>Z. Wang, and A. C. Bovik. "Mean squared error: love it or leave it? A new look at signal fidelity measures." *IEEE Signal Processing Magazine* 26.1 (2009): 98-117.

# The Structural Similarity Index (SSIM)<sup>3</sup>

$$\text{SSIM}(P_{(i,j)}, T_{(i,j)}) = L(P_{(i,j)}, T_{(i,j)}) \cdot C(P_{(i,j)}, T_{(i,j)}) \cdot S(P_{(i,j)}, T_{(i,j)}),$$

where  $P$ ,  $T$  refer to the pristine and test image respectively.

$L(P_{(i,j)}, T_{(i,j)})$ ,  $C(P_{(i,j)}, T_{(i,j)})$ ,  $S(P_{(i,j)}, T_{(i,j)})$  are the local luminance, contrast and structure scores at pixel  $(i, j)$  respectively. Further,

$$L(P_{(i,j)}, T_{(i,j)}) = \frac{2\mu_P(i,j)\mu_T(i,j) + C_1}{\mu_P^2(i,j) + \mu_T^2(i,j) + C_1}$$

$$C(P_{(i,j)}, T_{(i,j)}) = \frac{2\sigma_P(i,j)\sigma_T(i,j) + C_2}{\sigma_P^2(i,j) + \sigma_T^2(i,j) + C_2}$$

$$S(P_{(i,j)}, T_{(i,j)}) = \frac{\sigma_{PT}(i,j) + C_3}{\sigma_P(i,j)\sigma_T(i,j) + C_3}$$

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<sup>3</sup> Wang, Z., Bovik, A. C., Sheikh, H. R., and Simoncelli, E. P. (2004). Image quality assessment: from error visibility to structural similarity. IEEE transactions on image processing , 13(4):600–612

The constants  $C_1$ ,  $C_2$ ,  $C_3$  are used to avoid division-by-zero issues. For simplicity,  $C_3 = C_2/2$  in the standard implementation which leads to

$$\text{SSIM}(P_{(i,j)}, T_{(i,j)}) = L(P_{(i,j)}, T_{(i,j)}) \cdot CS(P_{(i,j)}, T_{(i,j)}),$$

where

$$CS(P_{(i,j)}, T_{(i,j)}) = \frac{2\sigma_{PT}(i,j) + C_2}{\sigma_P^2(i,j) + \sigma_T^2(i,j) + C_2}.$$

The valid distance metric can be derived from the components of the SSIM index.

$$d^Q(P_{(i,j)}, T_{(i,j)}) = \sqrt{2 - L(P_{(i,j)}, T_{(i,j)}) - CS(P_{(i,j)}, T_{(i,j)})}$$

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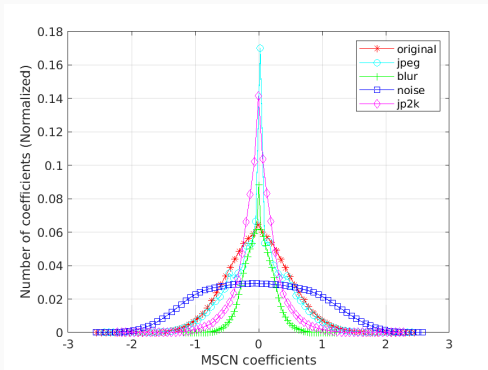
<sup>4</sup> Brunet, Dominique, Edward R. Vrscaj, and Zhou Wang. "On the mathematical properties of the structural similarity index." *IEEE Transactions on Image Processing* 21.4 (2011): 1488-1499

# The statistics of natural images <sup>5</sup>

- Natural images are distinctive because they contain unique statistical signature.

## Mean subtracted contrast normalization coefficients (MSCN)

$$\hat{l}(i,j) = \frac{l(i,j) - \mu(i,j)}{\sigma(i,j)}$$



# Natural Image Quality Evaluator (NIQE) <sup>6</sup>

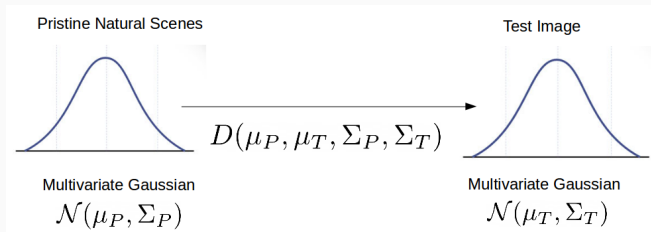
- NIQE builds a statistical model for MSCN coefficients of the class of pristine natural scenes and uses the model's parameters for quality estimation.

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<sup>6</sup>Anish Mittal, Rajiv Soundararajan, and Alan C Bovik. "Making a completely blind image quality analyzer". In: *IEEE Signal Processing Letters* 20.3 (2013), pp. 209–212

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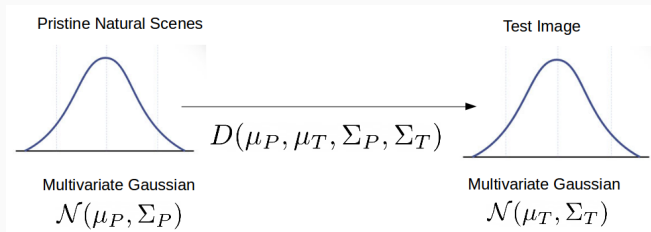


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## Natural Image Quality Evaluator (NIQE)

$$D(\mu_P, \mu_T, \Sigma_P, \Sigma_T) = \sqrt{(\mu_P - \mu_T)^T \left( \frac{\Sigma_P + \Sigma_T}{2} \right)^{-1} (\mu_P - \mu_T)}.$$

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- We propose to use the perceptually correlated SSIM derived metric as the underlying image metric in the wasserstein distance.
- This implies that the discriminator should be lipschitz with respect to SSIM metric ( $d^Q(x, y)$ ).
- As this is a bounded metric between  $0 \leq d^Q(x, y) \leq \sqrt{2}$ .

$$|D(X) - D(Y)| \leq d^Q(X, Y)$$

- SSIM gradient penalty term makes the discriminator quality aware.

$$\text{SSIM GP} = E_{X \sim P_r, Y \sim P_G} \left[ \left( \frac{|D(X) - D(Y)|}{d^Q(X, Y)} \right) - 1 \right]^2.$$

$$L_d = \min_{D \in \mathcal{D}} \left( E_{Z \sim P_z} D(G(z)) - E_{X \sim P_r} D(X) \right) + \lambda_1 E_{\hat{x} \sim P_{\hat{x}}} (\|\nabla_{\hat{x}} D(\hat{x})\|_2 - 1)^2 + \\ \lambda_2 E_{X \sim P_r, G(z) \sim P_G} \left[ \left( \frac{|D(X) - D(G(z))|}{d^Q(X, G(z))} \right) - 1 \right]^2,$$

where  $\lambda_1$  and  $\lambda_2$  are empirically chosen. where  $d^Q(x, y)$  is the metric SSIM, that is

$$d^Q(X, Y) = \sqrt{2 - L(X, Y) - CS(X, Y)}$$

# Motivation to impose Quality aware gradient penalty

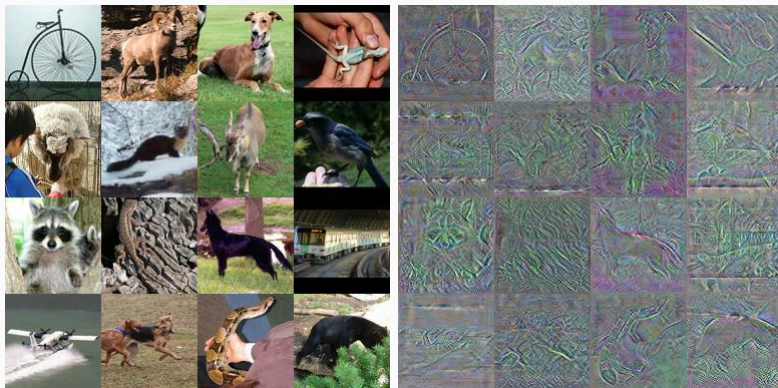
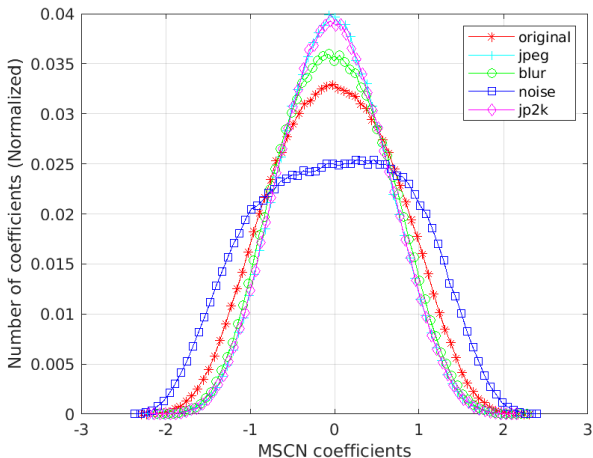


Figure: Real images and their corresponding discriminator gradient maps

# Motivation to impose Quality aware gradient penalty



MSCN coefficients of the discriminator gradient maps.

## Estimating the pristine model:

- The core idea of enforcing statistical signature onto the discriminator gradient map remains the same as the gradient maps are computed from the smooth function.
- The reference model parameters  $\mu_P, \Sigma_P$  are estimated from the real discriminator gradient maps.

## The naturalness of a test discriminator gradient map ( $T$ )

$$\|(T|\mu_P, \Sigma_P)\|_{\text{NIQE}} := \sqrt{(\mu_P - \mu_T)^T \left( \frac{\Sigma_P + \Sigma_T}{2} \right)^{-1} (\mu_P - \mu_T)},$$

where  $\mu_T, \Sigma_T$  are the model parameters of the test image's multivariate gaussian model.

## Discriminator Loss Function

$$L_d = \min_{D \in \mathcal{D}} \left( E_{Z \sim P_Z} D(G(Z)) - E_{X \sim P_r} D(X) \right) + \lambda_1 E_{\hat{x} \sim P_{\hat{x}}} (\|\nabla_{\hat{x}} D(\hat{x})\|_2 - 1)^2 + \\ \lambda_2 E_{\hat{x} \sim P_{\hat{x}}} (\|( \nabla_{\hat{x}} D(\hat{x}) | \mu_P, \Sigma_P )\|_{\text{NIQE}}),$$

where  $\lambda_1$  and  $\lambda_2$  are hyper parameters chosen empirically. As before,  $\hat{x}$  is sampled from a line joining the real and fake image distributions.

Table1: FID scores on the **CelebA** dataset ( $64 \times 64$ ).

Model	FID
Real Faces (CelebA)	1.09
WGAN-GP	12.89
Banach WGAN	10.5
MMD GAN-rep-b	6.79
<b>QAGAN (SSIM)</b>	<b>6.421</b>
<b>QAGAN (NIQE)</b>	<b>6.504</b>



# Qualitative Results

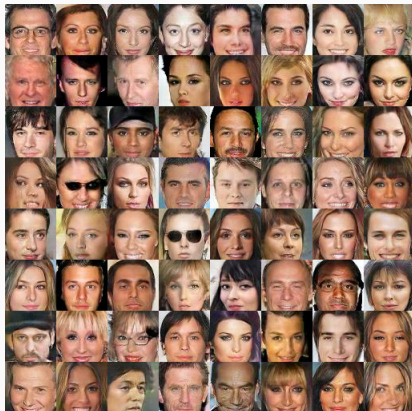


Figure: Randomly sampled images generated using QAGAN(SSIM) for CelebA dataset ( $64 \times 64$ ).

# Qualitative Results



Figure: Randomly sampled images generated using QAGAN(NIQE) for CelebA dataset ( $64 \times 64$ ).

Table2: IS and FID on the **STL-10** dataset ( $48 \times 48$ ).

Model	IS	FID
Real Data ( $48 \times 48$ )	$26.08 \pm 0.26$	7.9
WGAN-GP	$9.05 \pm 0.12$	$55.1 \pm 0.0$
SNGAN	$9.10 \pm 0.04$	$40.10 \pm 0.50$
MMD GAN-rep	$9.36 \pm 0.0$	$36.67 \pm 0.0$
<b>QAGAN (SSIM)</b>	<b><math>9.29 \pm 0.05</math></b>	<b><math>19.77 \pm 0.0091</math></b>
<b>QAGAN (NIQE)</b>	<b><math>9.1720 \pm 0.08</math></b>	<b><math>19.45 \pm 0.0013</math></b>

# Qualitative Results

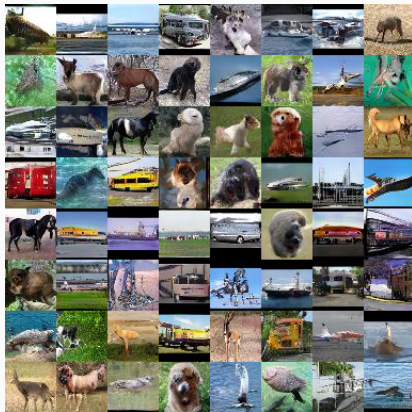


Figure: Randomly sampled images generated using QAGAN(SSIM) for STL10 dataset ( $64 \times 64$ ).

# Qualitative Results

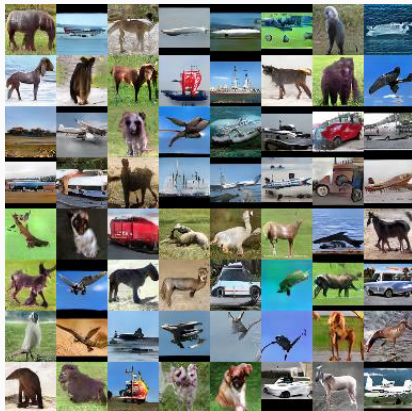


Figure: Randomly sampled images generated using QAGAN(NIQE) for STL10 dataset ( $64 \times 64$ ).

## Results - CIFAR-10 dataset

Table1: Inception Score (IS) and Fréchet Inception Distance (FID) computed from 50,000 samples of the **CIFAR-10** dataset ( $32 \times 32$ ). Scores that are unavailable are marked with a '-'.

Model	IS	FID
Real data	$11.24 \pm 0.12$	7.80
DCGAN	$6.16 \pm 0.07$	-
WGAN-GP	$7.86 \pm 0.10$	$40.2 \pm 0.0$
CTGAN	$8.12 \pm 0.12$	-
SNGAN	$8.12 \pm 0.12$	$21.5 \pm 0.21$
$W^{-\frac{3}{2},2}$ - Banach WGAN	$8.26 \pm 0.07$	-
$L^{10}$ - Banach WGAN	$8.31 \pm 0.07$	-
MMD GAN-rep-b	$8.29 \pm 0.0$	$16.21 \pm 0,0$
<b>QAGAN (SSIM)</b>	<b><math>8.37 \pm 0.04</math></b>	<b><math>13.91 \pm 0.105</math></b>
<b>QAGAN (NIQE)</b>	<b><math>7.87 \pm 0.027</math></b>	<b><math>12.4697 \pm 0.068</math></b>

# Qualitative Results



Figure: Randomly sampled images generated using QAGAN(SSIM) for CIFAR10 dataset ( $32 \times 32$ ).

# Qualitative Results

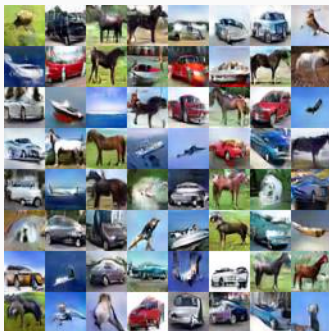


Figure: Randomly sampled images generated using QAGAN(NIQE) for CIFAR10 dataset ( $32 \times 32$ ).



- Based on insights from both FR and NR IQA metrics, we have proposed two novel regularization approaches for the WGAN-GP framework.
- The key takeaway from our work is that the unique local structural and statistical signature of pristine natural images must be preserved in the generated images.
- We believe that this work opens up new and exciting directions in image and video generative modeling, given the plethora of excellent QA metrics.

- code : <https://www.iith.ac.in/lfovia/downloads.html>
- P. Kancharla, S. S. Channappayya, Quality Aware Generative Adversarial Networks, accepted to the Thirty-third Conference on Neural Information Processing Systems (NeurIPS) 2019, Vancouver, Canada.



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