

## Class-02

### Numpy

```
* import numpy as np
from numpy import *
np.addc()
addc()
```

```
* from numpy import *
v = array([1, 2, 3, 4], dtype=float) # 1D Array
print(v)
print(type(v))
```

out :- [1. 2. 3. 4.]

<class 'numpy.ndarray'>  
<class 'list'>

```
x = [1, 2, 3, 4]
print(type(x))
```

```
* from numpy import *
m = array([1, 2, 3], [3, 4, 1], [5, 6, 2], [8, 9, 10]) # 2D array
print(m)
```

\* z = array([1, 2, 3])
z.shape

out (3, 0)

out :- [[1, 2, 3]
[3, 4, 1]
[5, 6, 2]
[8, 9, 10]]]

```
* z = array([[1, 2], [3, 4]])
print(z.shape)
print(z)
```

out : (2, 2)
[[1, 2]
[3, 4]]]

```
* from numpy import *
```

```
z = array([[[1, 2, 3, 7], [3, 8, 4, 5], [5, 9, 9, 0], [9, 9, 9, 9]],
[[1, 2, 7, 0], [0, 3, 4, 8], [8, 7, 9, 2], [1, 2, 9, 8]]])
```

```
Print(z.shape)
Print(z.size)
```

out : (2, 4, 4)

Class-04

Dt. 03/04

## Using array - generating function

arange

$x = \text{arange}(5, 14, 1)$  # out -  $([5, 6, 7, 8, 9, 10, 11, 12, 13])$

linspace & logspace

linear space      logarithmic space

from numpy import \*  
linspace(0, 10, 10)

out: array([0.0, 1.1111111, 2.2222222, 3.3333333, 4.4444444,  
5.5555556, 6.6666667, 7.7777778, 8.8888889, 10.0])

linspace(0, 100, 20)

out: ---

logspace(0, 10, endpoint=True, base=8)

out: array([1.0000000e+00, 1.1111111e+01, ...]).

\*  $x = (1, 2, 3)$

y = array(x, dtype=float)

out: array([1., 2., 3.])

\* from numpy import \*

x, y = mgrid[2:4, 2:1]

-x  
out: array([[[2, 2, 2],  
[3, 3, 3]]])

-y  
out: array([[[2, 3, 4],  
[2, 3, 4]]])

\* z, m=mgrid[2:6, 1:3]

z

out: array([[[2, 2],  
[3, 3],  
[4, 4],  
[5, 5]]])

m

out: array([[[[1, 2],  
[1, 2],  
[1, 2],  
[1, 2]]]])

```
* from numpy import *  
random. random(5, 5)  
out:
```

\* diag (diagonal matrix)

```
diag([1, 2, 3, 4, 5, 6])
```

```
out: array([[1, 0, 0, 0, 0, 0],  
           [0, 2, 0, 0, 0, 0],  
           [0, 0, 3, 0, 0, 0],  
           [0, 0, 0, 4, 0, 0],  
           [0, 0, 0, 0, 5, 0],  
           [0, 0, 0, 0, 0, 6]])
```

```
diag([1, 2, 3])
```

```
array([[1, 0, 0],  
       [0, 2, 0],  
       [0, 0, 3]])
```

\* diag ([1, 2, 3], k=1)

```
out: array([[0, 1, 0, 0],  
            [0, 0, 2, 0],  
            [0, 0, 0, 3],  
            [0, 0, 0, 0]])
```

Class-06

Dt- 05/05/2023

### Zeros and ones

```
* zeros((3, 3))
```

```
out: array([[0., 0., 0.],  
            [0., 0., 0.],  
            [0., 0., 0.]])
```

```
* ones((4, 3))
```

```
out: array([[1., 1., 1.],  
            [1., 1., 1.],  
            [1., 1., 1.],  
            [1., 1., 1.]])
```

More properties of the numpy arrays

m. itemsize # bytes per element

out: 8

m. nbytes # number of bytes

out: 72

m. ndim # number of dimensions

out: 2

## Manipulating arrays

### Indexing

- \*  $v[0]$  #  $v$  is a vector, and thus has only one dimension, taking one index  
out: 1
- \*  $m[1, 1]$  #  $m$  is a matrix, or a 2 dimensional array, taking two indices  
out: 0.47913739999
- \*  $m$   
out: array([[[0.77872576, 0.40093577, 0.66254019],  
          [0.60410063, 0.4791374, 0.8237106],  
          [0.96856318, 0.15459699, 0.96082399]]])
- \*  $m[1]$  # row, column  
out: array([0.60410063, 0.4791374, 0.8237106])
- \*  $m[1, :]$  # row 1  
out: array([0.60410063, 0.4791374, 0.8237106])
- \*  $m[:, 1]$  # column 1  
out: array([0.40093577, 0.4791374, 0.15459699])
- \*  $m[0, 0] = 2$   
out: array([[[2., 0.40093577, 0.66254019],  
          [0.60410063, 0.4791374, 0.8237106],  
          [0.96856318, 0.15459699, 0.96082399]]])
- \*  $m[1, :] = 0$   
 $m[:, 2] = -1$   
 $m$   
out: array([[[1., 0.40093577, -1.],  
          [0., 0., -1.],  
          [0.96856318, 0.15459699, -1.]]])

## Index Slicing

```
from numpy import *
```

```
A = array([1, 2, 3, 4, 5])
```

```
A  
out: array([1, 2, 3, 4, 5])
```

```
- A[2:6:4]
```

```
out: array([3])
```

```
- A[1:3] = [-2, -3]
```

change

```
A  
out: array([-2, -3, 4, 5])
```

```
- A[:, 1]
```

```
out: array([-2, -3, 4, 5])
```

```
- A[:, 2]
```

```
out: array([-3, 5])
```

```
- A[:, 3]
```

```
out: array([-2, -3])
```

```
- A[:, 4]
```

```
out: array([5])
```

```
* from numpy import *
```

```
A = array([n + m * 10 for n in range(5)]  
          for m in range(5))
```

```
A
```

```
out: array([[0, 1, 2, 3, 4],  
           [10, 11, 12, 13, 14],  
           [20, 21, 22, 23, 24],  
           [30, 31, 32, 33, 34],  
           [40, 41, 42, 43, 44]])
```

\*  $A[1:4, 1:4]$

# a block from the original array

out: array([[[11, 12, 13],  
[21, 22, 23],  
[31, 32, 33]]])

\*  $A[:, ::2, ::2]$

out: array([[[0, 2, 4],  
[20, 22, 24],  
[40, 42, 44]]])

### Fancy indexing

from numpy import \*

B = array([n for n in range(5)])

B

out: array([0, 1, 2, 3, 4])

- row-mask = array([True, True, True, False, False])  
B[row-mask]

out: array([0, 1, 2])

- row-mask = array([1, 1, 1, 0, 0])  
B[row-mask]

out: array([2. 1. 0. 0.])

0 1 2 3 4

10 11 12 13 14

20 21 22 23 24

20 31 32 33 34

0 , 1 4 9 16

100 121 144 169 196

400 441 484 529 576

900 961 1024 1089 1156

\* from numpy import \*

x = arange(0, 10, 0.5)

out: [0, 0.5, 1., 1.5, 2., 2.5, 3., 3.5, 4., 4.5]

\* mask = (5 < x) \* (x < 7.5)

mask  
out = array([False, False, False, False, False, False, False, False, True, True, True, True, True, False, False, False, False], dtype=bool)

\* x[mask]

out = array([5.5, 6., 6.5, 7.])

where

indices = where(mask)

indices

out = (array([11, 12, 13, 14]),)

x[indices]

out = array([5.5, 6., 6.5, 7.])

diag

diag(A)

out: array([0, 11, 22, 33, 44])

diag(A, -1)

out: array([10, 21, 32, 43])

take

\* v2 = arange(-3, 3)

v2

out = array([-3, -2, -1, 0, 1, 2])

\* row\_indices = [1, 3, 5]

v2[row\_indices]

out: array([-2, 0, 2])

\* v2.take(row\_indices)

out = array([-2, 0, 2])

$$A = \begin{bmatrix} 0 & 1 & 2 & 3 & 4 \\ 10 & 11 & 12 & 13 & 14 \\ 20 & 21 & 22 & 23 & 24 \\ 30 & 31 & 32 & 33 & 34 \\ 40 & 41 & 42 & 43 & 44 \end{bmatrix}$$

\* take([-3, -2, -1, 0, 1, 2], row-indices)  
out- array([-2, 0, 2])

Choose  
from numpy import \*

which = [1, 0, 0, 1]

Choices = [[-3, -2, -3, -2], [7, 4, 7, 4]]

Choose(which, choices)

out = array([7, -2, -3, 4])

Linear algebra -

Scalar-array Operation :-

from numpy import \*

v1 = arange(0, 5)

out = array([0, 1, 2, 3, 4])

\* print(A)

A \* 2, A / 2

[0 1 2 3 4]  
[10 11 12 13 14]  
[20 21 22 23 24]  
[30 31 32 33 34]  
[40 41 42 43 44]

out = array([[0, 2, 4, 6, 8],  
[20, 22, 24, 26, 28],  
[40, 42, 44, 46, 48],  
[60, 62, 64, 66, 68],  
[80, 82, 84, 86, 88]]),

array([[-2, -1, 0, 1, 2],  
[-9, -8, -7, -6, -5],  
[-18, -19, -20, -21, -22],  
[-28, -29, -30, -31, -32],  
[-39, -38, -37, -36, -35]]))

\* v1 \* 2  
out = array([0, 2, 4, 6, 8])

\* v1 + 2  
out = array([2, 3, 4, 5, 6])

\* A \* A

array([[0, 1, 4, 9, 16],  
[100, 121, 144, 169, 196],  
[400, 441, 484, 529, 576],  
[900, 961, 1024, 1089, 1156],  
[1600, 1681, 1764, 1849, 1936]])

\* print(v1)

v1 \* v1

out- [0, 1, 2, 3, 4]  
array([0, 1, 4, 9, 16])

\* A.shape, v1.shape

((5,5), (5, 1))

\* A \* v1

[0 1 2 3 4]  
[10 11 12 13 14]  
[20 21 22 23 24]  
[30 31 32 33 34]  
[40 41 42 43 44]

[0, 1, 2, 3, 4]

out- array([[[0, 1, 4, 9, 16],  
[0, 11, 24, 39, 56],  
[0, 21, 44, 69, 96],  
[0, 31, 64, 99, 136],  
[0, 41, 84, 129, 176]])

### matrix algebra

\* dot(A, A)

out- array([[[300, 310, 320, 330, 340],  
[1300, 1360, 1420, 1420, 1490],  
[2300, 2410, 2520, 2630, 2740],  
[3300, 3460, 3620, 3780, 3940],  
[4300, 4510, 4720, 4930, 5140]]])

\* dot(A, v1)

out- array([30, 130, 230, 330, 430])

\* M = matrix(A)

print(M)

v = matrix(v1).T

\* c = matrix([1, 2, 3, 4, 5])

c.T

out- matrix([[[1],  
[2],  
[3],  
[4],  
[5]]])

out- [[1 -2 -3 4 5]]

matrix([[0],  
[1],  
[2],  
[3],  
[4]])

Class - 08

Dt - 07/05

### Array / Matrix transformation

c = matrix  $\left( \begin{bmatrix} 1 - 1.3j, 5 + 2j \\ 3j, 7 + 4j \end{bmatrix} \right)$  real  $\frac{1-3j}{2}$  imag

c  
out - matrix  $\left( \begin{bmatrix} 1 - 1.3j, 5 + 2j \\ 0 + 3j, 7 + 4j \end{bmatrix} \right)$  #  $a+jb \rightarrow$  imaginary part  
a  $\rightarrow$  real part a  
a, b  $\rightarrow$  real number

### \* Conjugate(c)

out - matrix  $\left( \begin{bmatrix} 1 + 1.3j, 5 - 2j \\ 0 - 3j, 7 - 4j \end{bmatrix} \right)$  #  $1 + ij \rightarrow 1 - ij$   
 $3 + 3j \rightarrow 3 - 3j$   
 $j \rightarrow -j$

### \* C.H

out - matrix  $\left( \begin{bmatrix} 0 - 1j, 0 - 3j \\ 0 - 2j, 0 - 4j \end{bmatrix} \right)$

### \* real(c)

out - matrix  $\left( \begin{bmatrix} 1, 5 \\ 0, 7 \end{bmatrix} \right)$

### \* imag(c)

matrix  $\left( \begin{bmatrix} -1.3, 2 \\ 3, 4 \end{bmatrix} \right)$

### Matrix Computations

#### Inverse

### \* linAlg. inv(c)

out - matrix  $\left( \begin{bmatrix} 0.2 + j, 0 - 1j \\ 0 - 1.5j, 0 + 0.5j \end{bmatrix} \right)$

### \* C.I \* C

out - matrix  $\left( \begin{bmatrix} 1.0000000e+00 + 0.j, 4.69089290e-16 + 0.j \\ 0.0000000e+00 + 0.j, 1.0000000e+00 + 0.j \end{bmatrix} \right)$

## Determinant

Linalg. det(c)

$$\text{out} = \left( 2.0000000000000004 + 0j \right)$$

Wnaly - det (C-I )

$$\text{out} = \left( 0.5000000000000001, 1 + 0j \right)$$

Mode  $\rightarrow$  3

4 1 3 6 2 3

$$\text{Mean} \rightarrow 19/6 \rightarrow 3.33$$

Median  $\rightarrow 3 + 3 / 2 \rightarrow 3$

\* mean(data[:3])

out- 6.197096947515859

## Standard deviation and variance

`std_(data[:, 3]), var_(data[:, 3])`

out - ( 8.2822 . . . , 68.596023 . . . )

mix and max

```
data[:, 3].mean()
```

```
data[:,3].max()
```

out - 29.300000000000004

## Class-09

Dt - 10/10

Reshaping, resizing & stacking

\* A

[out]

```
from numpy import *
```

A

```
[out] array([0, 1, 2, 3, 4],  
           [10, 11, 12, 13, 14],  
           [20, 21, 22, 23, 24],  
           [30, 31, 32, 33, 34],  
           [40, 41, 42, 43, 44]))
```

\* n, m = A.shape

\* B = A.reshape ((1, n\*3))

B

```
[out] array([[0, 1, 2, 3, 4, 10, 11, 12, 13, 14, 20, 21, 22, 23, 24, 30,  
            31, 32, 33, 34, 40, 41, 42, 43, 44]])
```

\* C = arange (0, 12)

C

```
d = c.reshape (4, 3)
```

d

```
[out] array([[0, 1, 2],  
           [3, 4, 5],  
           [6, 7, 8],  
           [9, 10, 11]]))
```

\* from numpy import \*

```
b = random.rand (3, 3)
```

```
b[0, 0] = 12
```

```
print (b)
```

```
[out] [[12.          0.80467401   0.86135114]  
       [0.26140153  0.61689014   0.01410927]  
       [0.64319837  0.85647648   0.35020965]]
```

\* B[0, 0:5] = 5

B

```
out = array ([[5, 5, 5, 5, 5, 10, 11, 12, 13, 14, 20, 21, 22, 23, 24, 30, 41,  
             32, 33, 34, 40, 41, 42, 43, 44]]))
```

\* A # and the original variable is also changed.

[out] array ([[5, 5, 5, 5, 5],  
[10, 11, 12, 13, 14],  
[20, 21, 22, 23, 24],  
[30, 31, 32, 33, 34],  
[40, 41, 42, 43, 44]])

\* B = A.flatten()

[out] <sup>B</sup> array ([5, 5, 5, 5, 10, 11, 12, 13, 14, 20, 21, 23, 24, 30,  
31, 32, 33, 34, 40, 41, 42, 43, 44])

\* B[0:5] = 10

[out] <sup>B</sup> array ([10, 10, 10, 10, 10, 10, 11, 12, 13, 14, 20, 21, 22, 23, 24,  
30, 31, 32, 33, 34, 40, 41, 42, 43, 44])

\* A # now A has not changed, because B's data is  
a copy of A's.

[out] array ([[5, 5, 5, 5, 5],  
[10, 11, 12, 13, 14],  
[20, 21, 22, 23, 24],  
[30, 31, 32, 33, 34],  
[40, 41, 42, 43, 44]])

Adding a new dimension: newaxis

\* v = array ([1, 2, 3])

[out] <sup>v</sup> array ([1, 2, 3])

\* shape (v)

[out] (3, )

\* v[:, newaxis]

[out] array([[1],  
[2],  
[3]])

\*  $\nabla[:, \text{newaxis}].shape$

out - (3, 1)

\*  $\nabla[\text{newaxis}, :].shape$

out: (1, 3)

tile and repeat

\*  $a = \text{array}([[[1, 2], [3, 4]]])$

[out]  $a = \text{array}([[[1, 2], [3, 4]]])$

\* repeat(a, 3)

out - array([1, 1, 1, 2, 2, 2, 3, 3, 3, 4, 4, 4])

\* tile(a, 3)

[out]  $\text{array}([[[1, 2, 1, 2, 1, 2], [3, 4, 3, 4, 3, 4]]])$

Concatenate

\*  $b = \text{array}([[5, 6]])$

b.T

[out]  $- \text{array}([[5], [6]])$

\* Concatenate((a, b), axis=0)

out - array ([[1, 2],  
[3, 4],  
[5, 6]])

\* Concatenate((a, b.T), axis=1)

[out]  $\text{array}([[1, 2, 5], [3, 4, 6]])$

\* b

out - array ([[5, 6]])

## hstack & vstack

\* vstack ((a, b))

[out] array ([[1, 2],  
[3, 4],  
[5, 6]])

\* hstack ((a, b.T))

[out] array ([[1, 2, 5],  
[3, 4, 6]])

## Copy and "deep copy"

\* A = array ([[1, 2], [3, 4]])

[out] <sup>A</sup> array ([[1, 2],  
[3, 4]])

\* B = A

\* B[0, 0] = 10

[out]: array ([[10, 2],  
[3, 4]])

\* A

[out] array ([[10, 2],  
[2, 4]])

\* B = copy(A)

\* B[0, 0] = -5

[out] <sup>B</sup> array ([[−5, 2],  
[3, 4]])

\* A

[out] array ([[10, 2],  
[3, 4]])

## Class-10

Dt - 12/07/2021

- \*  $v = \text{array}([1, 2, 3, 4])$   
for  $i$  in  $v$ :                    out:  $\begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix}$   
    print( $i$ )
- \*  $M = \text{array}([[1, 2, 3], [4, 5, 6]])$   
for row in  $M$ :                    out: row  $[1 2 3]$   
    print("row", row)  
    for element in row:  
        print(element)
- \* for row-idx, row in enumerate( $M$ ):  
    print("row-idx", row-idx, "row", row)  $\{3, 4\}$   
    for col-idx, element in enumerate(row):  
        print("col-idx", col-idx, "element", element)  
        # update the matrix  $M$ : square each element  
         $M[row-idx, col-idx] = \text{element}^{**2}$

**out:**  $\{$ 

- ('row-idx', 0, 'row', array([1, 2]))
- ('col-idx', 0, 'element', 1)
- ('col-idx', 1, 'element', 2)
- ('row-idx', 0, 'row', array([3, 4]))
- ('col-idx', 0, 'element', 3)
- ('col-idx', 1, 'element', 4)

 $\}$

\*  $M$   
**out:** array  $([[1, 4], [9, 16]])$

from  
x = 0  
y = 0  
x+y  
**out:**  
\* free  
x = 0  
y  
x+y  
**out:**

\* from numpy import \*  
 x = array([5, 8, 9, 10, 0]) # Broadcasting operation on  
 y = array([5, 3, 2, 1, 9]) case of numpy arrays  
 x+y

[out]- array([10, 11, 11, 11, 9])

\* from numpy import \*  
 x = array([[0, 0, 0], [10, 10, 10], [50, 50, 50], [70, 70, 70], dtype=int)  
 y = array([[3.0, 4.0, 5.0]])  
 x+y

[out] array([[3., 4., 5.],  
           [13., 14., 15.],  
           [53., 54., 55.],  
           [73., 74., 75.]])

\* x = arange(0, 100, 5)  
 x = x.reshape(4, 5)

Print(x)

z = x.T

Print(z)

for i in z:

    for j in i:

        print(j)

[out]: [[0 5 10 15 20]  
       [25 30 35 40 45]  
       [50 55 60 65 70]  
       [75 80 85 90 95]]

[[0 25 50 75]  
   [5 30 55 80]  
   [10 35 60 85]  
   [15 40 65 90]  
   [20 45 70 95]]

0	60
25	85
50	15
75	40
5	65
30	90
55	20
80	45
10	70
35	95

\* for i in range(0, 4):

Print(x[i, 0:4])

[out]

[0 5 10 15]  
[25 30 35 40]  
[50 55 60 65]  
[75 80 85 90]

\* x = arange(8). reshape(2, 4)

Print(x)

x.flatten(order = 'F')

[out]

- [[0, 1, 2, 3],  
[4, 5, 6, 7]]

array([0, 1, 2, 3, 4, 5, 6, 7])

\* x.flat[5]

[out] - 5

\* y = arange(4). reshape(1, 4, 1)

Print(y)

rollaxis(y, 0, 2)

[out] - [[[0]]

[1]  
[2]  
[3]]]

array([[ [0],  
[1],  
[2],  
[3]]])

\* from numpy import \*

y = arange(8). reshape(2, 2, 2)

Print(y)

rollaxis(y, 2, 2)

[out] - [[[0, 1],  
[2, 3]],  
[[4, 5],  
[6, 7]]]

array([[[0, 1],  
[2, 3]],

[[[4, 5],  
[6, 7]]]])

```
* from numpy import *
z = arange(12)
print(z)
y = split(z, 4)
x = split(z, [0, 6])
x
```

**Out** - [ 0 1 2 3 4 5 6 7 8 9 10 11 ]  
 $\text{array}([ ], \text{dtype}=$   
 $\text{array}([0, 1, 2]), \text{array}([3, 4, 5]), \text{array}([6, 7, 8, 9, 10, 11])]$

```
* z = arange(32). reshape(8, 4)
print(z)
y = split(z, 8)
y
```

**Out** - [[ 0 1 2 3],  
 $\text{array}([0, 1, 2, 3]),$   
 $\text{array}([4, 5, 6, 7]),$   
 $\text{array}([8, 9, 10, 11]),$   
 $\text{array}([12, 13, 14, 15]),$   
 $\text{array}([16, 17, 18, 19]),$   
 $\text{array}([20, 21, 22, 23]),$   
 $\text{array}([24, 25, 26, 27]),$   
 $\text{array}([28, 29, 30, 31])]$

$\text{array}([4, 5, 6, 7]),$   
 $\text{array}([8, 9, 10, 11]),$   
 $\text{array}([12, 13, 14, 15]),$   
 $\text{array}([16, 17, 18, 19]),$   
 $\text{array}([20, 21, 22, 23]),$   
 $\text{array}([24, 25, 26, 27]),$   
 $\text{array}([28, 29, 30, 31])]$

```
* right_shift(8, 2)
```

**Out** - 2

```
* z = array([0, 30, 8, 45, 60.2, 90])
cos(z*pi/180)
```

$\tan(z * \pi / 180)$

```
array([0.00000000e+00, 5.98119690e-01, 1.00000000e+00,
       1.74609143e+00, 1.63312399e+16])
```

- \*  $z = 9.2$   
parent( $\text{ceil}(z)$ )  
float( $z$ )  
**out** - 8.0  
9.0
- \* reciprocal( $z$ )  
**out** - 0.233092009923308
- \*  $z = \text{array}([0, 30.8, 45, 60.2, 90])$   
y = array([0, -30.8, 45, 60.8, 90])  
 $\text{mod}(z, y)$   
**out** - array([nan, -0, 0., 60.2, 0.])
- \* power( $z, 2$ )  
**out** - array([0., 948.64, 2025., 2624.04, 8100.])
- \*  $z = \text{array}([[6, 8, 2], [7, 3, 9], [2, 0, 7]])$   
**out** - array([[6, 8, 2],  
[7, 3, 9],  
[2, 0, 7]])
- \* amax( $z, \text{axis}=1$ )  
**out** - array([2, 3, 0])
- \* amax( $z, \text{axis}=0$ )  
**out** - array([2, 0, 2])
- \* amax( $z$ )  
**out** - 9
- \* median( $z$ )  
median( $z, 0$ )  
median( $z, 1$ )  
mean( $z$ )  
mean( $z, 1$ )  
mean( $z, 0$ )  
std( $z$ )