

- Alice and Bob need to communicate with encryption
- They have two sets of alphabet, one is the main alphabet that conveys messages and the other is a dummy alphabet

```
L = {a, b, c, d}L2={m, n, o, p}
```

• L2 maps to L

```
L = { a, b, c, d }

t t t t

L2= { m, n, o, p }
```

- Each message they send is an array of strings
- Only some words are meaningful
- They have an agreement for decoding messages
- A string is meaningful if every existing letter from L is mapped/covered by corresponding letter from L2 in proper order.
- The mapping MUST properly follow the sequence of letters.
- A meaningful string MUST have a letter from L.

Proper Nesting of letters is required

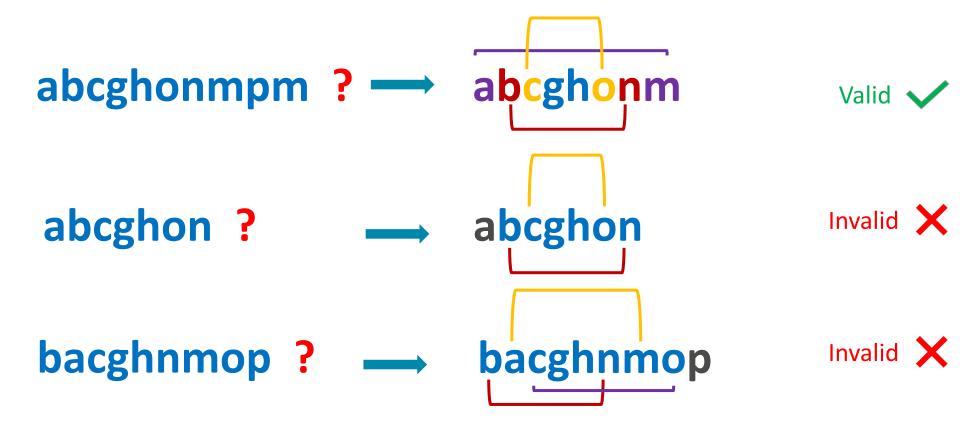
abcghonm? — abcghonm



dcayuom? — dcayuom



Number of letters from L2 = Number of letters from L



Letters from L should occur before letters from L2



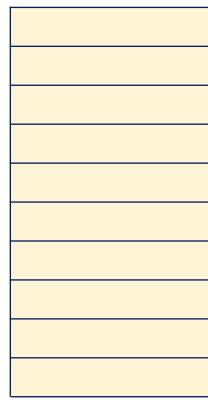


mnotycba? — mnotycba



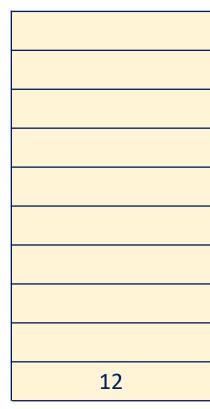
- Stack is a linear data structure that follows the LIFO (Last In First Out) rule
- Think of stacking plates
- The top of stack is always the most recent element that was pushed into the stack
- Stack supports these operations:
 - push() Insert a value on top
 - pop() Remove the value from the top
 - top() return the value of the top element

Operations on stack

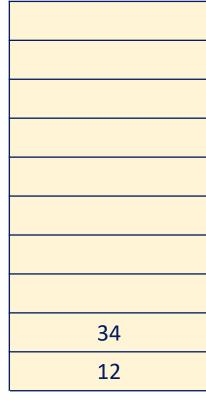


Stack

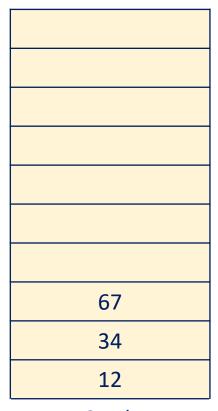
- Operations on stack
 - push(12)



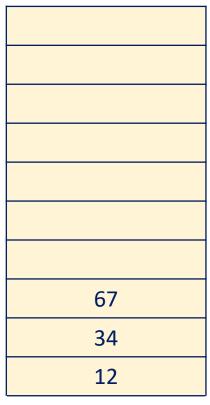
- Operations on stack
 - push(12)
 - push (34)



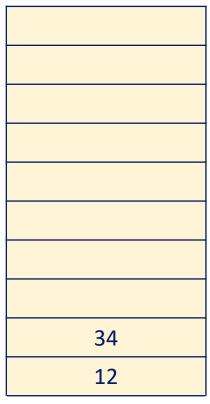
- Operations on stack
 - push(12)
 - push (34)
 - push(67)



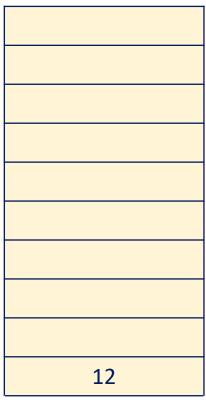
- Operations on stack
 - push(12)
 - push (34)
 - push(67)
 - $top() \rightarrow 67$



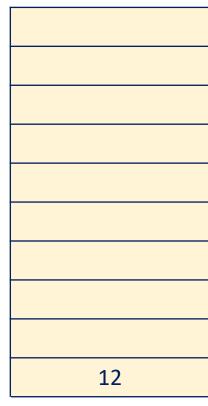
- Operations on stack
 - push(12)
 - push (34)
 - push(67)
 - $top() \rightarrow 67$
 - pop()



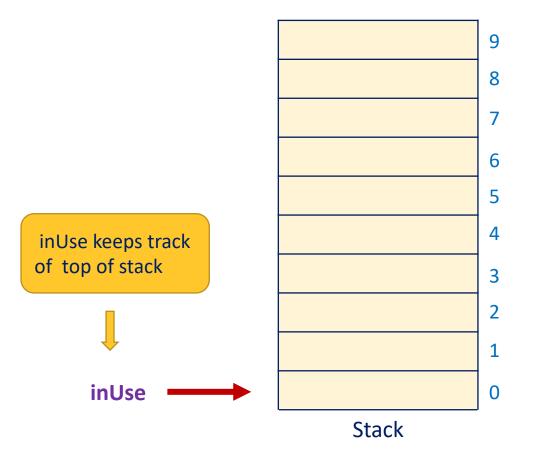
- Operations on stack
 - push(12)
 - push (34)
 - push(67)
 - $top() \rightarrow 67$
 - pop()
 - pop()



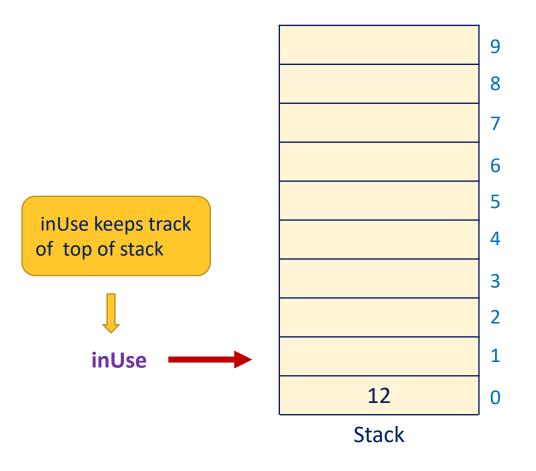
- Operations on stack
 - push(12)
 - push (34)
 - push(67)
 - $top() \rightarrow 67$
 - pop()
 - pop()
 - $top() \rightarrow 12$



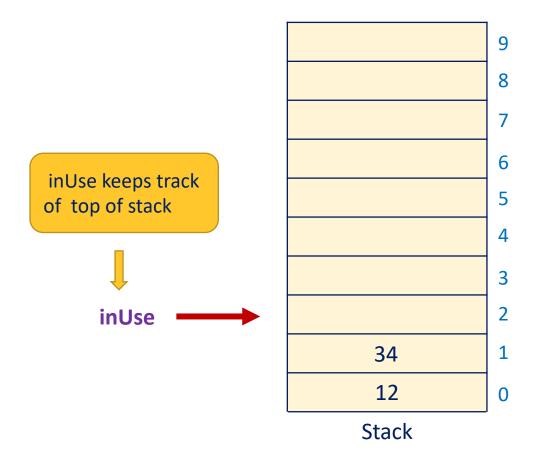
Operations on stack



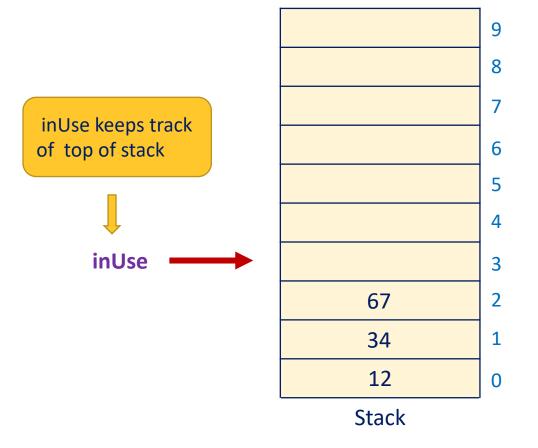
- Operations on stack
 - push (12)



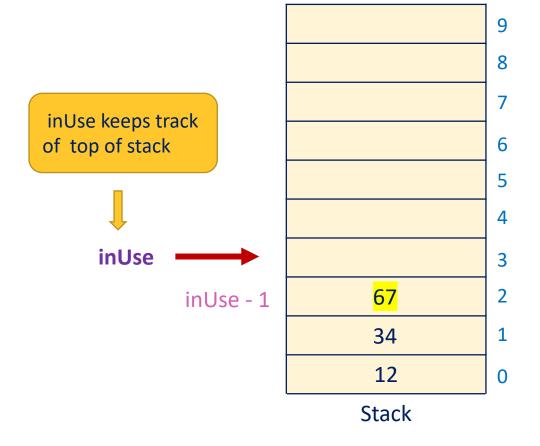
- Operations on stack
 - push (12)
 - push (34)



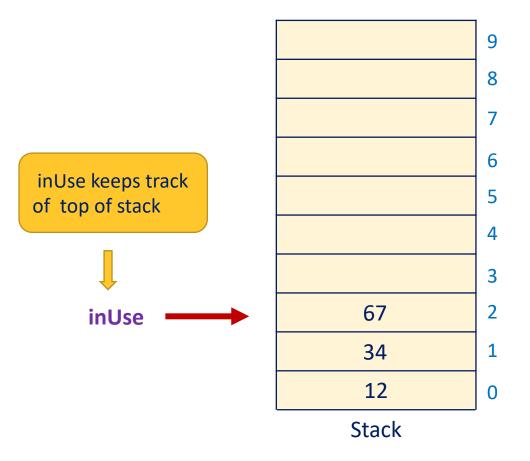
- Operations on stack
 - push (12)
 - push (34)
 - push (67)



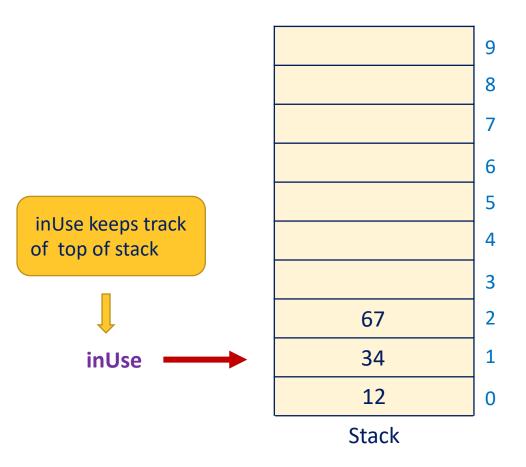
- Operations on stack
 - push (12)
 - push (34)
 - push (67)
 - top() => inUse-1 => 67



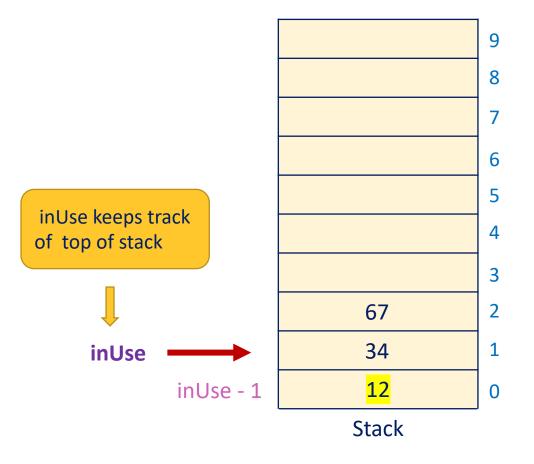
- Operations on stack
 - push (12)
 - push (34)
 - push (67)
 - top() => inUse-1 => 67
 - pop ()



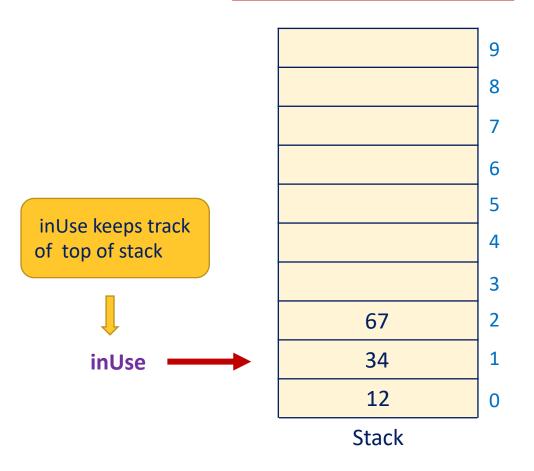
- Operations on stack
 - push (12)
 - push (34)
 - push (67)
 - top() => inUse-1 => 67
 - pop()
 - pop()



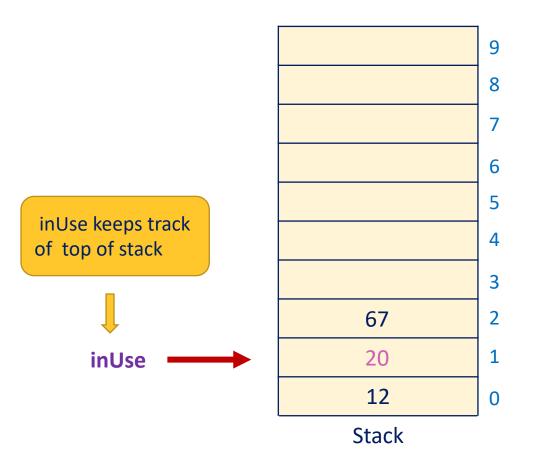
- Operations on stack
 - push (12)
 - push (34)
 - push (67)
 - top() => inUse-1 => 67
 - pop()
 - pop()
 - top() => inUse-1 => 12



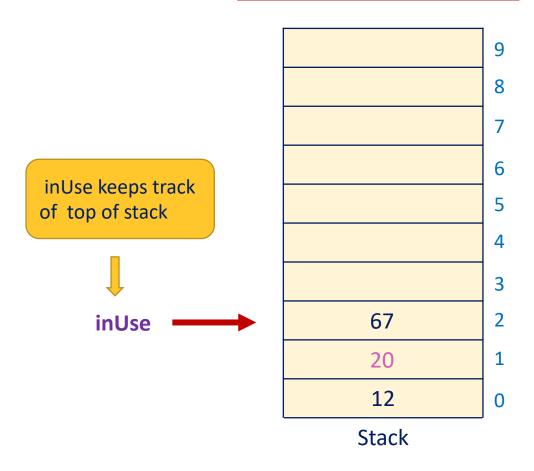
- Operations on stack
 - push (12)
 - push (34)
 - push (67)
 - top() => inUse-1 => 67
 - pop()
 - pop()
 - top() => inUse-1 => 12
 - push(20)



- Operations on stack
 - push (12)
 - push (34)
 - push (67)
 - top() => inUse-1 => 67
 - pop()
 - pop()
 - top() => inUse-1 => 12
 - push(20)



- Operations on stack
 - push (12)
 - push (34)
 - push (67)
 - top() => inUse-1 => 67
 - pop()
 - pop()
 - top() => inUse-1 => 12
 - push(20)



General Algorithm

If your current character is a member of L:

push the character into the stack

If your current character is a member of L2:

- Verify the top of the stack contains the matching letter from L2
- pop/remove the letter from L from the stack

When you encounter the end of the string

Verify the stack is empty => String is meaningful and part of the message

Ignore any other symbols contained in the expression

General Algorithm

You check for invalid string when:

Your current character is a member of L2:

- The stack is empty => you have extra letters from L2
- The top of stack letter is not a correct match

When you encounter the end of the string

If the stack is not empty => you have extra letters from L that are not mapped

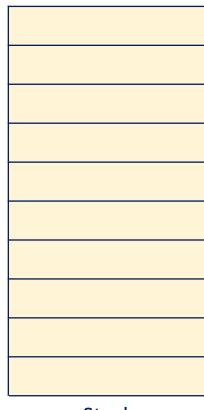
If a string is invalid, you can move to the next string in the message

String: a b c g o n m

Current Character: At start of Expression

Character Type: Nothing yet

Task: Clear stack



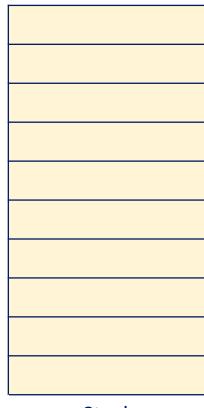
String: a b c g o n m

Λ

Current character: a

Character Type: Belongs to L

Task: push onto stack



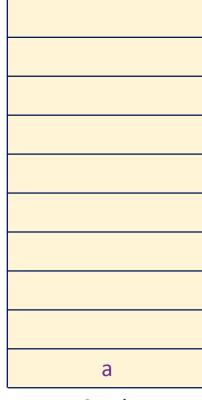
String: a b c g o n m

Λ

Current character: a

Character Type: Belongs to L

Task: push onto stack



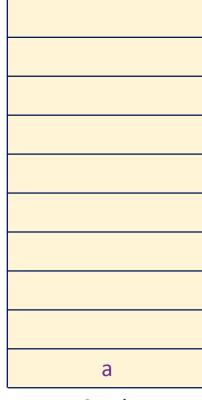
String: a b c g o n m

Λ

Current character: b

Character Type: Belongs to L

Task: push onto stack



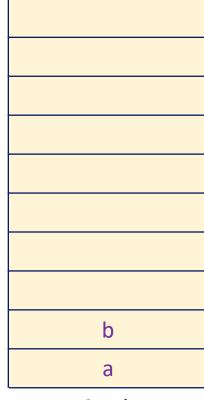
String: a b c g o n m

Λ

Current character: b

Character Type: Belongs to L

Task: push onto stack



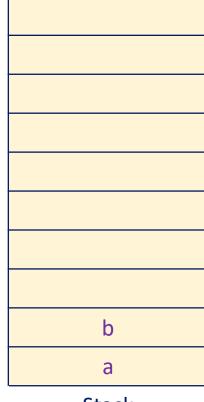
String: a b c g o n m

Λ

Current character: c

Character Type: Belongs to L

Task: push onto stack



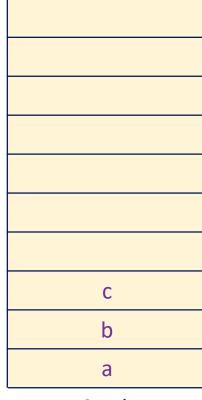
String: a b c g o n m

Λ

Current character: c

Character Type: Belongs to L

Task: push onto stack



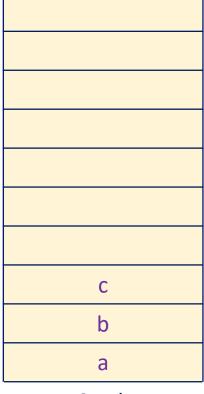
String: a b c g o n m

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Current character: g

Character Type: Not in *L* or *L2*

Task: ignore



String: abcgonm

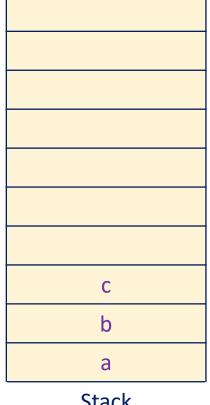
Λ

Current character:

Character Type: Belongs to **L2**

Task: Verify if it is mapping top of stack

character, if so pop the stack



String: a b c g o n m

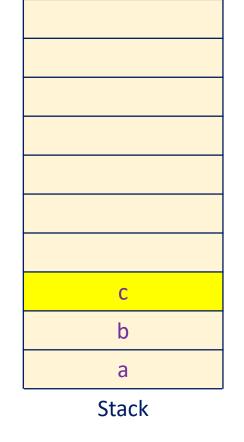
Λ

Current character: o

Character Type: Belongs to *L2*

Task: Verify if it is mapping top of stack

character, if so pop the stack



o maps to c

 $L = \{ a, b, c, d \}$ $\downarrow \downarrow \downarrow \downarrow \downarrow$ $L_{2} = \{ m, n, o, p \}$

String: a b c g o n m

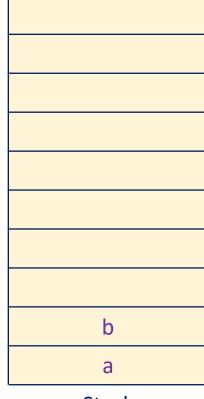
Λ

Current character: o

Character Type: Belongs to *L2*

Task: Verify if it is mapping top of stack

character, if so pop the stack



String: abcgonm

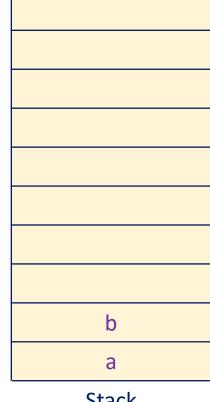
Λ

Current character:

Character Type: Belongs to **L2**

Task: Verify if it is mapping top of stack

character, if so pop the stack



 $L = \{a, b, c, d\}$

String: abcgonm

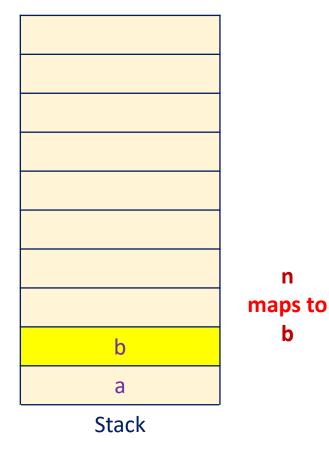
Λ

Current character:

Character Type: Belongs to **L2**

Task: Verify if it is mapping top of stack

character, if so pop the stack



n

b

String: a b c g o n m

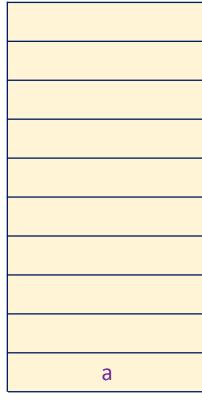
Λ

Current character: n

Character Type: Belongs to *L2*

Task: Verify if it is mapping top of stack

character, if so pop the stack



String: abcgonm

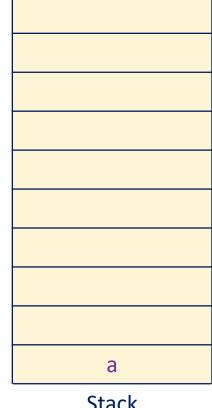
Λ

Current character: m

Character Type: Belongs to **L2**

Task: Verify if it is mapping top of stack

character, if so pop the stack



String: a b c g o n m

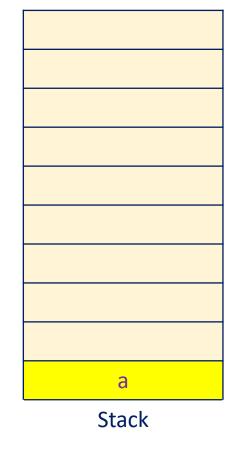
Λ

Current character: m

Character Type: Belongs to *L2*

Task: Verify if it is mapping top of stack

character, if so pop the stack



m maps to

 $L = \{ a, b, c, d \}$ $\downarrow \downarrow \downarrow \downarrow$ $L_2 = \{ m, n, o, p \}$

String: a b c g o n m

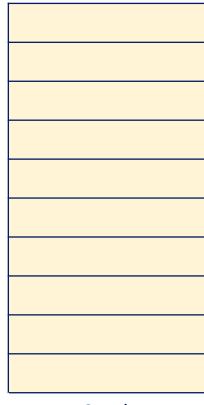
Λ

Current character: m

Character Type: Belongs to *L2*

Task: Verify if it is mapping top of stack

character, if so pop the stack



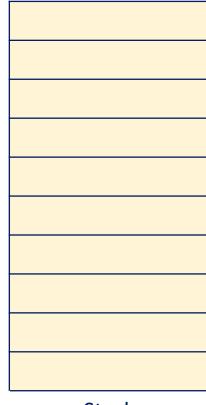
String: a b c g o n m

Λ

Current character: '/0'

Character Type: End of string

Task: Verify stack is Empty



String: a b c g o n m

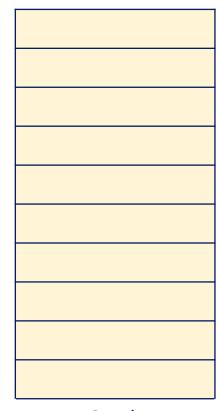
Λ

Current character: '/0'

Character Type: End of string

Task: Verify stack is Empty

Stack is empty so our word is meaningful



String: a b c g o n m

Decoding Status: Meaningful

Next Step: Call RemoveExtraLetters ()

Removing Extra Letters

Input String: a b c g o n m

Output String: abc

Add the reduced string to your decoded message