

Control Flow in Programs

(Part I: Sequential and Conditional control)

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Outline

Programs and Control Flow

Control Flow Graphs

Executions

Conditionals

Conclusion

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Programs and Control Flow

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Conclusion

What is a Program?

- **Program:** A sequence **instructions** interleaved with **locations**

```
0
  a = 3
1
  b = read()
2
  c = a // b
3
  d = c - a
4
  # end
```

What is Control flow?

```
0
  a = 3
1
  b = read()
2
  c = a // b
3
  d = c - a
4
  # end
```

What is control flow analysis?

```
0
a = 3
1
b = read()
2
c = a // b
3
d = c - a
4
# end
```

- Control Flow analysis is the examination of possible paths a program can take when it runs. These paths are called **executions**.
- Control Flow analysis is done **without** running the program, i.e., statically.

Structural Abstraction

Program

```
0
  a = 3
1
  b = read()
2
  c = a // b
3
  d = c - a
4
  # end
```

Structural Abstraction

Program

```
0
  a = 3
1
  b = read()
2
  c = a // b
3
  d = c - a
4
  # end
```

Structural Abstraction

```
0
  expression assignment
1
  expression assignment
2
  expression assignment
3
  expression assignment
4
  # end
```


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Control Transfer Functions

Structural Abstraction

Control Transfer Functions

```
0  expression assignment
1  expression assignment
2  expression assignment
3  expression assignment
4  # end
```

Control Transfer Functions

Structural Abstraction

```

0      expression assignment
1      expression assignment
2      expression assignment
3      expression assignment
4      # end
    
```

Control Transfer Functions

i	next	error
0	1	4
1	2	4
2	3	4
3	4	4
4		

Control Flow Graph

Control Flow Graph

Control Transfer Functions

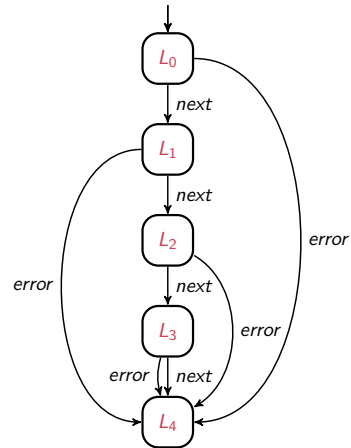
i	next	error
0	1	4
1	2	4
2	3	4
3	4	4
4		

Control Flow Graph

Control Transfer Functions

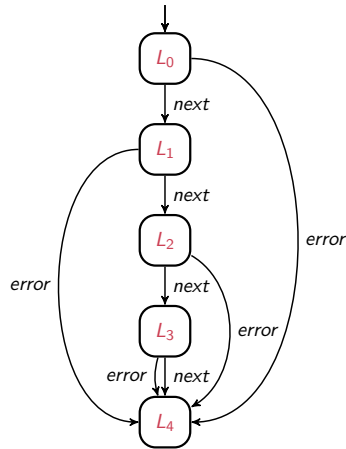
i	next	error
0	1	4
1	2	4
2	3	4
3	4	4
4		

Control Flow Graph

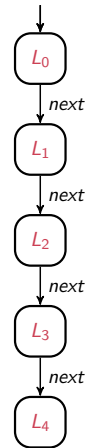


Implicit Error edges

Control Flow Graph



Control Flow Graph with
error edges implicit



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Programs and Control Flow

Control Flow Graphs

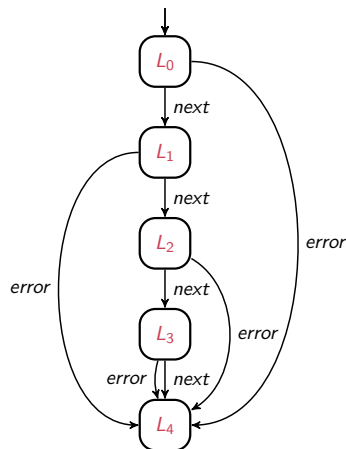
Executions

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What is an execution?

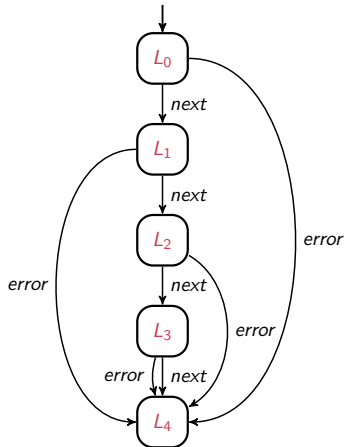
Control Flow Graph



An execution is a labelled path in the Control Flow graph starting from L_0 and ending at the last location L_N .

Structurally Feasible Executions

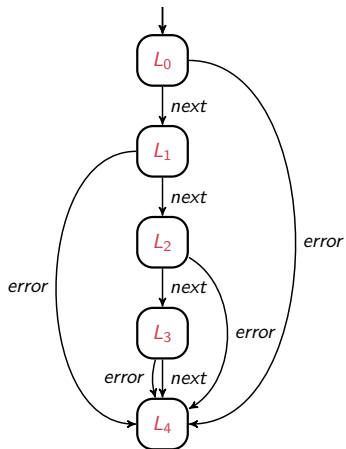
Control Flow Graph



Structurally Feasible Executions:

Structurally Feasible Executions

Control Flow Graph



Structurally feasible executions:

1.

$$L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{next}} L_2 \xrightarrow{\text{next}} L_3 \xrightarrow{\text{next}} L_4$$

2. All error executions (executions containing an error edge).

Logically Feasible Executions

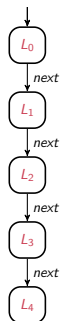
Logically feasible executions:

Sequential Flow Program:

```

0      a = 3
1      b = read()
2      c = a // b
3      d = c - a
4      # end
    
```

CFG:



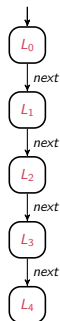
Logically Feasible Executions

Program:

```

0  a = 3
1  b = read()
2  c = a // b
3  d = c - a
4  # end
    
```

Control Flow Graph:



Logically feasible executions:

- b is a number not equal to 0:
 $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{next}} L_2 \xrightarrow{\text{next}} L_3 \xrightarrow{\text{next}} L_4$
- $b = 0$:
 $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{next}} L_2 \xrightarrow{\text{error}} L_4$
- b is not a number:
 $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{next}} L_2 \xrightarrow{\text{error}} L_4$

Actual Execution

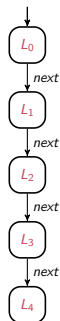
Actual execution given that $b = 5$:

Program:

```

0  a = 3
1  b = read()
2  c = a // b
3  d = c - a
4  # end
    
```

Corresponding CFG:

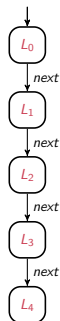


Actual Execution

Program:

```
0  a = 3
1  b = read()
2  c = a // b
3  d = c - a
4  # end
```

Corresponding CFG:



Actual execution given that $b = 5$:

$$L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{next}} L_2 \xrightarrow{\text{next}} L_3 \xrightarrow{\text{next}} L_4$$

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Conditional Control Flow

```
0  a = read()
1  if a < 5:
2      b = 7
3  else:
4      b = 2 * a
5  c = a + b
6  # end
```

1. A block is a sequence of instructions.
2. An If-else statement ($L_1 - L_4$) has three parts:
 - A 'test' expression (L_1)
 - A 'then' block ($L_2 - L_2$)
 - An 'else' block ($L_4 - L_4$)
 - The 'else' keyword (L_3) is punctuation.
3. In the concrete syntax, the then and else blocks are indented.

Structural Abstraction

Program

```
0      a = read()
1
2      if a < 5:
3          b = 7
4      else:
5          b = 2 * a
6      c = a + b
7      # end
```

Structural Abstraction

```
0      expression assignment
1
2      if:
3          expression assignment
4      else:
5          expression assignment
6      expression assignment
7      # end
```

Control Transfer Functions

Structural Abstraction

Control Transfer Functions

```
0      expression assignment
1
2      if:
3          expression assignment
4      else:
5          expression assignment
6      expression assignment
7      # end
```

Control Transfer Functions

Structural Abstraction

```

0      expression assignment
1
2      if:
3          expression assignment
4      else:
5          expression assignment
6      expression assignment
7      # end
    
```

Control Transfer Functions

i	next	true	false	error
0	1			6
1		2	3	6
2	5			6
3	4			
4	5			6
5	6			6
6				

Control Flow Graph

Control Transfer Functions

Control Flow Graph with
Error edges implicit

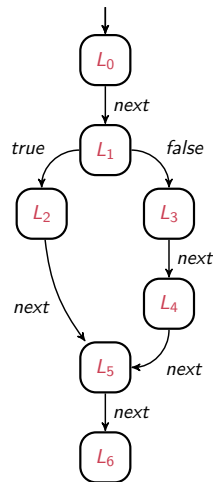
i	next	true	false	error
0	1			6
1		2	3	6
2	5			6
3	4			
4	5			6
5	6			6
6				

Control Flow Graph

Control Transfer Functions

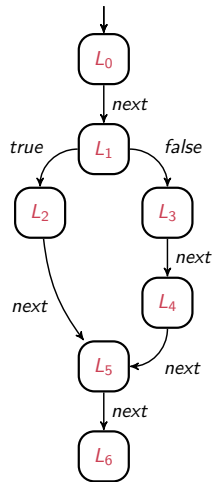
i	next	true	false	error
0	1			6
1		2	3	6
2	5			6
3	4			
4	5			6
5	6			6
6				

Control Flow Graph with error edges implicit



Structurally Feasible Executions

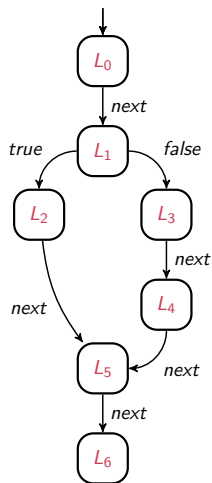
CFG:



Structurally Feasible Executions:

Structurally Feasible Executions

CFG:



Structurally Feasible Executions:

1. $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{true}} L_2 \xrightarrow{\text{next}} L_5 \xrightarrow{\text{next}} L_6$
2. $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{false}} L_3 \xrightarrow{\text{next}} L_4 \xrightarrow{\text{next}} L_5 \xrightarrow{\text{next}} L_6$
3. All error executions.

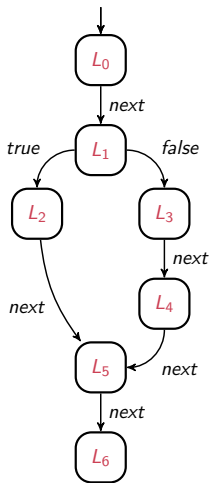
Logically Feasible Executions

Program:

```

0  a = read()
1  if a < 5:
2      b = 7
3
4  else:
5      b = 2 * a
6
# end
    
```

CFG:



Logically Feasible Executions:

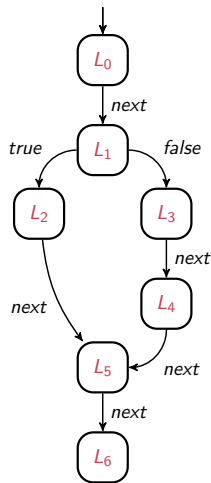
Logically Feasible Executions

Program:

```

0      a = read()
1      if a < 5:
2          b = 7
3      else:
4          b = 2 * a
5      c = a + b
6      # end
    
```

CFG:



Logically Feasible Executions:

- $a < 5$:
 $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{true}} L_2 \xrightarrow{\text{next}} L_5 \xrightarrow{\text{next}} L_6$
- $a \geq 5$:
 $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{false}} L_3 \xrightarrow{\text{next}} L_4 \xrightarrow{\text{next}} L_5 \xrightarrow{\text{next}} L_6$
- a is not a number:
 $L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{error}} L_6$

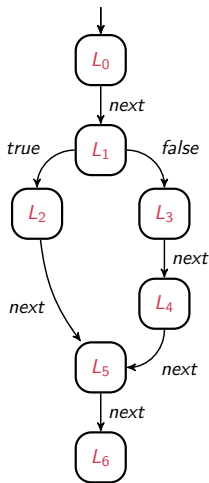
Actual Execution

Program:

```

0  a = read()
1  if a < 5:
2      b = 7
3
4  else:
5      b = 2 * a
6
# end
    
```

CFG:



Actual execution given that value read at L_0 is the number 3.

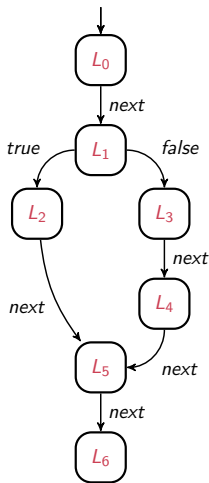
Actual execution

Program:

```

0  a = read()
1  if a < 5:
2      b = 7
3
4  else:
5      b = 2 * a
6
7  c = a + b
8
9  # end
    
```

CFG:



Actual execution, given that value read at L_0 is the number 3.

$L_0 \xrightarrow{\text{next}} L_1 \xrightarrow{\text{true}} L_2 \xrightarrow{\text{next}} L_5 \xrightarrow{\text{next}} L_6$

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Program and its structural abstraction

1. **Location:** a natural number between 0 and N
2. **Instruction:** A basic executorial unit of a program
3. **Program:** A map from $[0..N - 1]$ to instructions
4. **Structural abstraction of an instruction:** Expression assignment, if or else
5. **Structural abstraction of a program:** structural abstractions of all its instructions

Control transfer functions and CFG

1. **Control Transfer Functions:** partial functions from locations to locations
2. **next, error, true and false:** control transfer functions
3. **Control Flow Graph:** A diagram representing the control transfer functions
4. **Control Flow Graph with implicit error edges:** error edges suppressed to reduce clutter

