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ILMENAU

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Submitted by: Author Name

Matriculation Number XXXXX

author-email@tu-ilmenau.de

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I would like to thank ...

Abstract

The English Abstract...

Zusammenfassung

Eine deutsche Zusammenfassung.

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1. Introduction

A correct design for a system is a crucial step to reach a satisfactory result. Building a model is essential to analyze and evaluate the different possibilities in an early stage, or to prove the correctness of the solution in diverse scenarios. For this purpose, there are several models [ZPK00] that can be used, with different expressiveness and properties. If the model is complex enough, an analytical approach may not be possible due to the need of a complete state space exploration and the state explosion limitation [Val98]. To overcome this problem, simulation methods [FJMRM10] can provide an acceptable solution but they introduce a new issue: rare-events [GLFH01, Hee97]. If the simulation needs to evaluate a measure [Haa02] based on an event that is very unlikely to happen (e.g. 10^{-6}), unless special considerations are taken the simulation will rarely go through this event, therefore a good confidence level will be highly time-consuming to achieve. The goal of the current work is to design, implement and evaluate a simulation algorithm, which will be able to overcome the rare-event limitation without requiring a deep understanding of it, nor a high level analysis of the model. Moreover, it introduces a new concept of how to deal with the simulation execution, avoiding random decisions to achieve an execution as close as possible to an analysis...

2. Background Research on Rare-Event Simulation

In this chapter background research on rare-event simulation is reviewed, including the models and the simulation algorithms. First, a descriptive presentation of the different models is conducted, where both Markovian and non-Markovian examples are given...

2.1. Models, Markovian and Non-Markovian

In the current work different types of models are considered, where one of the main classifications is the requirement of memory or not. As introduced, a model without memory requirement is considered Markovian, and by opposition one that requires memory is non-Markovian. A Markovian model is a stochastic model that changes based on a random factor, and the future state depends only on the current one, not on previous states or events leading to it. A non-Markovian model does not fulfill this property, therefore only knowing the current state is not enough to completely describe the current situation. In a non-Markovian model the followed path of states and the events that lead to them are relevant as well.

2.1.1. Markov Chain

A Markov chain model is a static Markovian model, composed of states and transitions, where each state has incoming and outgoing transitions. Each of the outgoing transitions has a probability of being followed, and by definition, this probability only depends on the current state, not on previous visited states. Therefore, if a simulation is run over a Markov chain and at two different points in time the same state is reached, there is no difference between the execution status at those points, and all the following possible paths have the same probability in both scenarios. A simple Markov chain with three states and their transitions is presented in Figure 2.1. The values shown over the transitions correspond to

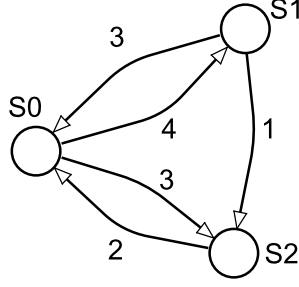


Figure 2.1. – Simple Markov Chain Model

their rates, and the probability is calculated with this value over the sum of all outgoing transitions of the state.

The distribution of the time remaining in a state is memoryless, which is modeled with an exponential distribution: $f(x) = \lambda e^{-\lambda x}$, $F(x) = 1 - e^{-\lambda x}$ ($x \geq 0$) [Haa02]. The average firing time for a transition with rate λ is λ^{-1} . Moreover, in a state with t outgoing transitions the average time spent is:

$$Average\ Time = \frac{1}{\sum_{i=0}^t (rate_i)}$$

In the example presented in Figure 2.1 the transition matrix is:

$$Q = \begin{pmatrix} -7 & 4 & 3 \\ 3 & -4 & 1 \\ 2 & 0 & -2 \end{pmatrix}$$

2.2. Monte Carlo Simulation Algorithm

A Monte Carlo simulation algorithm follows a standard Monte Carlo method [DPK11]. Whenever a decision needs to be made, a random result is generated based on the probability of each of the possible choices. Considering a Markov chain as the underlying model for a simulation executing a Monte Carlo algorithm, given the current state there are some outgoing transitions, each of them with a probability of being executed next...


```
1 // Initialization , set current state to the initial state
2 state *current_state = initial_state;
3
4 // Main simulation loop
5 while ( ! stop_condition_reached() )
6 {
7     int tran , selected_tran;
8     // Array with all the outgoing transitions rates from the current state
9     double trans_rates[] = get_out_transitions_rates( current_state );
10    int trans_count = get_out_transitions_count( current_state );
11
12    // Calculate the sum of all the outgoing transitions rates
13    double total_rates = 0;
14    for( tran = 0; tran < trans_count;  tran++)
15        total_rates += trans_rates[ tran ];
16
17    // Calculate the average time spent in the state
18    double time_spent = 1.0 / total_rates;
19    // Evaluate measures defined over the current state
20    evaluate_measures( current_state , time_spent );
21
22    // Randomly select one outgoing transitions , based on their rates
23    double random_value = generate_random_value( 0, total_rates );
24    for( tran = 0; tran < trans_count;  tran++)
25    {
26        if ( random_value <  trans_rates[ tran ] )
27        {
28            selected_tran = tran;
29            break;
30        }
31        random_value -= trans_rates[ tran ];
32    }
33
34    // Execute the selected transition , and update the current state
35    current_state = fire_transition( current_state , selected_tran );
36 }
37
```

Source Code 2.1 – Abstract Representation - Monte Carlo Algorithm

3. Design of a Multi-Trajectory Simulation Algorithm

This chapter introduces a design for a multi-trajectory simulation algorithm and provides explanations and examples of its main steps. The strength of this algorithm lies in its ability to run simulations within complex models, either with or without the presence of rare-events, and its adaptability to reach a wide coverage of the state space with efficiency in different types of models...

3.1. Introduction to Multi-Trajectory

Multi-trajectory simulation algorithm is based on particles, where a particle represents one possible trajectory of the simulation, and carries a weight that indicates the probability of that trajectory to happen. At any given time there is a collection of particles ready to be executed. Each particle is associated with one state of the model, and the execution of it implies a change in that state by following one or more of its possible transitions.

The core idea of the algorithm can be described as a loop of three steps:

1. Selection of the next particle...
2. Execution of the particle, which consists in choosing between:
 - a) Move: Randomly select...
 - b) Split: Create one new...
3. Insertion of the particle...

Against expectations, after the implementation of these strategies the results obtained by the executions were incorrect. Different attempts were made to overcome this error without success. An analysis of it with a numerical example is presented in Section 2.1.1. Due to this limitation a solution with a fair execution over the particles is chosen, using the definition

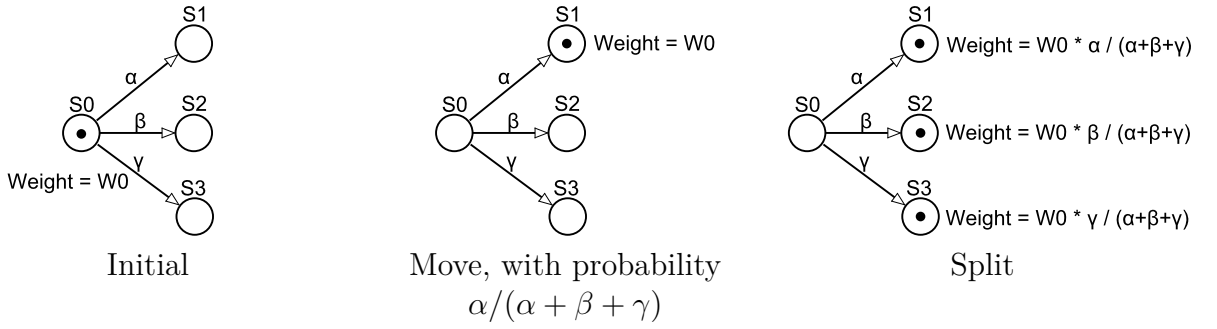


Figure 3.1. – Move or Split Example

of a cycle as the execution of all particles in the pool and the restriction of not execute a particle twice in a cycle.

Only Exponential Transitions Enabled

If there are only exponential transitions enabled, ... and the average time spent in the state is equal to the inverse of the sum of all those weighting factors.

$$Time\ Spent = \frac{1}{\sum_{i=0}^n \left(\frac{enabled_i}{delay_i} \right)}$$

$$Weighting\ Factor[i] = \begin{cases} Immediate\ Transition & = 0 \\ Exponential\ Transition & = \frac{enabled_i}{delay_i} \\ Deterministic\ Transition & = 0 \end{cases}$$

4. Implementation

In this chapter the implementation of a multi-trajectory simulation algorithm is presented...

5. Results and Comparative Analysis

In this chapter an analysis and evaluation of the TimeNET implementation of the multi-trajectory algorithm is presented. First, an analysis of its parameters is conducted and for this purpose a model is designed. Execution of this model with all possible values of different multi-trajectory parameters are shown, and the best combination of parameters is found. Afterwards, a comparative analysis of the implementation with the other three TimeNET implemented simulation algorithms is presented. This analysis is based on a previous research conducted by the author of the current work, *Rare-Event Algorithms Analysis and Simulation* [Can14]. Its goals were to evaluate RESTART TimeNET implementation and the implemented heuristic for its importance function. The multi-trajectory simulation results are compared together with the results obtained from the earlier work, followed by an analysis of how variations of the model properties exert different impact on the execution time of the algorithms. Finally, a non-Markovian model is analyzed and different simulations executed on it are presented.

5.1. Multi-Trajectory Results

In this section the results from the multi-trajectory simulations are compared with the results from the previous work. The multi-trajectory algorithm has been executed with the default parameters over all variations of the models, but only the most significant results are presented here.

5. Results and Comparative Analysis

Model Variations					Standard Simulation Results			
Mod	Pla	Tok	Del	Math Res	CPU Time	Overall T.	Value	Error
1	5	1	10	9.00E-05	0:00:13	0:00:03	9.20E-05	2.22%
1	5	1	100	9.90E-09	2:41:08	0:28:59	9.19E-09	7.17%
1	5	1	1000	9.99E-13		» 24 hs		
1	5	3	10	2.70E-04	0:00:11	0:00:03	2.71E-04	0.37%
1	5	3	100	2.97E-08	2:45:31	0:29:44	2.83E-08	4.71%
1	5	3	1000	3.00E-12		» 24 hs		
1	5	10	10	9.00E-04	0:00:29	0:00:06	9.23E-04	2.56%
1	5	10	100	9.90E-08	2:48:56	0:32:47	9.67E-08	2.32%
1	5	10	1000	9.99E-12		» 24 hs		
2	5	1	10	6.83E-05	0:00:30	0:00:06	6.92E-05	1.32%
2	5	1	100	9.61E-09	2:41:24	0:28:34	8.95E-09	6.87%
2	5	1	1000	9.96E-13		» 24 hs		
2	5	3	10	2.05E-04	0:00:11	0:00:03	2.04E-04	0.49%
2	5	3	100	2.88E-08	2:49:14	0:29:59	2.63E-08	8.68%
2	5	3	1000	2.99E-12		» 24 hs		
2	5	10	10	6.83E-04	0:00:17	0:00:04	6.79E-04	0.59%
2	5	10	100	9.61E-08	3:09:25	0:34:05	9.32E-08	3.02%
2	5	10	1000	9.96E-12		» 24 hs		

Table 5.1. – Standard Simulation Results [Can14]

Model Variations					RESTART Simulation Results			
Mod	Pla	Tok	Del	Math Res	CPU Time	Overall T.	Value	Error
1	5	1	10	9.00E-05	0:00:15	0:00:04	8.87E-05	1.44%
1	5	1	100	9.90E-09	0:02:20	0:00:25	9.74E-09	1.62%
1	5	1	1000	9.99E-13	0:47:54	0:08:01	1.10E-12	10.11%
1	5	3	10	2.70E-04	0:00:17	0:00:05	3.45E-04	27.78%
1	5	3	100	2.97E-08	0:03:27	0:00:35	3.06E-08	3.03%
1	5	3	1000	3.00E-12	0:59:34	0:11:24	3.00E-12	0.00%
1	5	10	10	9.00E-04	0:00:22	0:00:04	1.06E-03	17.78%
1	5	10	100	9.90E-08	0:13:53	0:02:21	1.17E-07	18.18%
1	5	10	1000	9.99E-12	2:20:50	0:23:54	9.84E-12	1.50%
2	5	1	10	6.83E-05	0:00:17	0:00:05	6.74E-05	1.32%
2	5	1	100	9.61E-09	0:00:35	0:00:07	9.75E-09	1.46%
2	5	1	1000	9.96E-13	0:21:25	0:03:38	9.52E-13	4.42%
2	5	3	10	2.05E-04	0:00:17	0:00:04	2.14E-04	4.39%
2	5	3	100	2.88E-08	0:00:47	0:00:10	3.05E-08	5.90%
2	5	3	1000	2.99E-12	0:36:54	0:06:19	3.49E-12	16.72%
2	5	10	10	6.83E-04	0:00:17	0:00:04	7.18E-04	5.12%
2	5	10	100	9.61E-08	0:01:15	0:00:13	9.51E-08	1.04%
2	5	10	1000	9.96E-12	2:16:35	0:23:21	9.69E-12	2.71%

Table 5.2. – RESTART Simulation Results [Can14]

6. Conclusions and Further Work

The goal of the current work was to design, implement and evaluate a new simulation algorithm capable of ...

A. Appendix

This appendix presents the details of the stationary analysis and multi-trajectory simulation executions of the model introduced in Figure 3.1 (Section 3.1, page 6).

Interconnected Model Analysis Output

Interconnected Model Analysis Output

Analysis Output:

STEADY STATE SOLUTION OF NET Interconnected_Model

STRUCTURAL ANALYSIS ...

GENERATING THE REDUCED REACHABILITY GRAPH USING TIME EFFICIENT ALGORITHM ...

The reduced reachability graph of this eDSPN
cannot be generated because of lacking main memory.

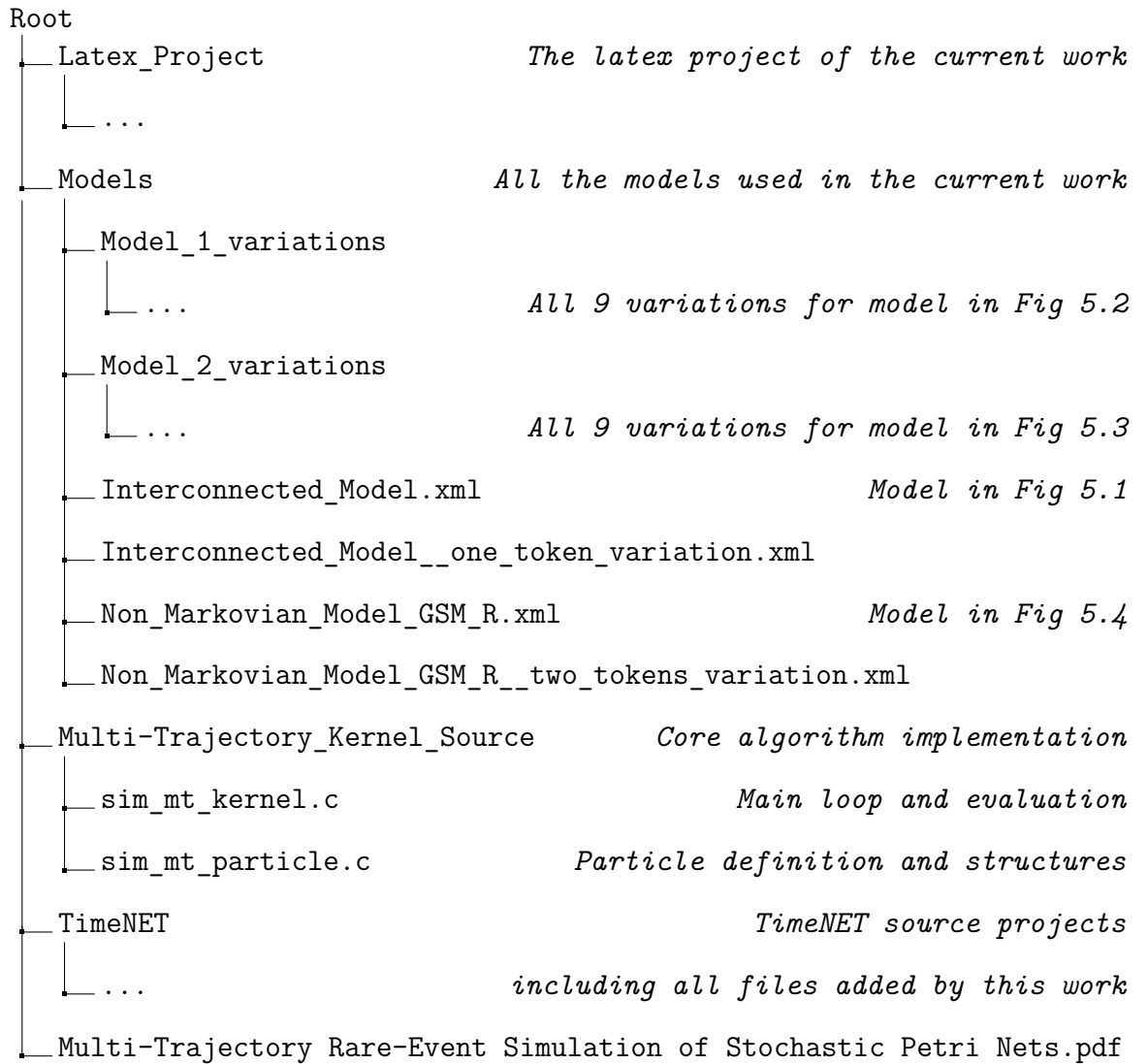
ERROR occurred while derive_SMC execution.
SOLUTION OF MODEL Interconnected_Model FAILED.

Removing temporary files.

Analysis error, see above.

CD Structure

A soft version of the current work is submitted. Following, the CD structure is presented.



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Declaration Of Authorship

I, Author Name, Matriculation Number XXXXX, hereby declare that my Master Thesis with the Title

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was produced by me, independently and without using any other references than those mentioned. This work is submitted in completion of the requirements for the Master Degree Research in Computer and Systems Engineering in Ilmenau University of Technology, and I did not publish nor submit this thesis to another university examination board.

Ilmenau, XX.XX.20XX

AUTHOR NAME