

# **FINAL LAB REPORT**



**Title: Algorithm I Lab**

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# Searching Algorithm

## Linear Search

### Linear Search

Use of the Algorithm: To Find an element from a list. The list can be sorted or unsorted.

Input of the Algorithm: An Array and a target value.

Output of the Algorithm: Yes, if target value is found, No, if target value is not found.

Complexity :-  $O(N)$ .

① Best case :-  $O(1)$ , Array = {51, 5, 91, 4, 103}, Target = 51

Output :- 1

② Worst case :-  $O(N)$ , Array = {5, 3, 9, 4, 03}, Target = 0

Output 5.

③ Average case :- Array = {51, 3, 91, 4, 03} Target = 91,

Output = 3.  $O(N)$

Basic Workflow :- In this search, a sequential search is performed. Each item is checked.

If a match is found the particular item is returned. Otherwise the search continues until end.

## Source Code:

```
#include<bits/stdc++.h>
using namespace std;
int main()
{
int arr[1001],i,f,n,num,index;
cout<<"\nHow Many Numbers:" ;
cin>>n;
cout<<"\nEnter the Numbers: ";
for(i=0; i<n; i++)
{
cin>>arr[i];
}
cout<<"\nEnter a Number to Search:
";
cin>>num;
for(i=0; i<n; i++)
{
if(arr[i]==num)
{
index = i+1;
f=0;
break;
}
}
```

```
if(f==0)
{
cout<<"\nFound at position :
"<<index;
}
else{cout<<"\nNot Found!!!";}
cout<<endl;
}
```

## Output:

```
C:\Users\USER\Documents\ca.exe

How Many Numbers:4
Enter the Numbers: 1 2 3 4
Enter a Number to Search: 2
Found at position : 2

Process returned 0 (0x0)  execution time : 9.731 s
Press any key to continue.
```

## Binary Search

### Binary Search

use of the Algorithm :- To Find an element from a list. The list should be sorted.

Input of the Algorithm :- An array and a target value.

Output of the Algorithm :- Yes, if target is found. No, if target is not found.

Complexity :-  $O(\log_2 N)$ .

Example :-

(I) Best case :-  $A = \{51, 53, 93\}$ ,  $T = 1$ , output = Yes.

(II) Worst case :-  $A = \{1, 32, 4, 8, 93\}$ ,  $T = 1$ , output = Yes.

(III) Average Case :-  $A = \{1, 4, 8, 12, 9, 73\}$ ,  $T = 4$ , output = Yes.

Basic Workflow of the Algorithm :- The

Search process begins by identifying the mid element of data of the sorted array.

After that the value is compared to the element, then comparison and matching.

searches analyze the value above the mid element.

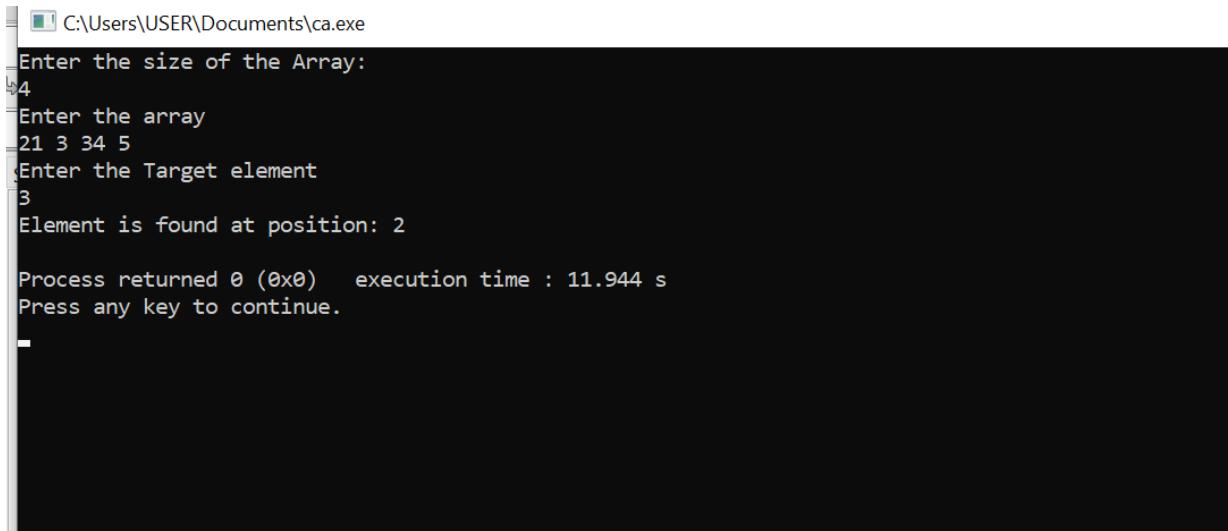
## Source Code:

```
#include <bits/stdc++.h>
using namespace std;

int binarySearch(int array[], int x,
int low, int high)
{
    while (low <= high)
    {
        int mid = low + (high - low) / 2;
        if (array[mid] == x)
            return mid;
        if (array[mid] < x)
            low = mid + 1;
        else
            high = mid - 1;
    }
    return -1;
}

int main() {
    int array[1001],x,n;
    cout<<"Enter the size of the Array:"<<endl;
    cin>>n;
    cout<<"Enter the array"<<endl;
    for(int i=0;i<n;i++)
    {
        cin>>array[i];
    }
    cout<<"Enter the Target element"<<endl;
    cin>>x;
    int result = binarySearch(array, x, 0, n-1);
    if (result == -1)
        cout<<"Not found"<<endl;
    else
        cout<<"Element is found at position: "<<result+1<<endl;
    return 0;
}
```

## Output:



```
C:\Users\USER\Documents\ca.exe
Enter the size of the Array:
4
Enter the array
21 3 34 5
Enter the Target element
3
Element is found at position: 2

Process returned 0 (0x0)  execution time : 11.944 s
Press any key to continue.
-
```

# Sorting Algorithm

## Insertion Sort

### Insertion Sort

use of the Algorithm :- To insert an element from a list of array.

Input of the Algorithm :- An array of n elements.

output of the Algorithm :- A sorted array.

complexity of the Algorithm :-  $O(N^2)$ .

Example :-

(I) Best case :-  $A = [1, 2, 3, 4]$ ,  $O(N)$ .

(II) Worst case :-  $A = [4, 3, 2, 1]$ ,  $O(N^2)$ .

(III) Average case :-  $A = [2, 1, 3, 4]$ ,  $O(N^2)$ .

Basic workflow of the Algorithm :- Insertion sort works similar to how we play a hand of cards. Array is partially divided into a sorted and an unsorted array. The value is picked from the array and placed in the correct position in the array.

## Source Code:

```
#include <bits/stdc++.h>
using namespace std;
int main()
{
    int ar[1001],n,i,j,k;
    cout<<"Enter the Number of
Index:"<<endl;
    cin>>n;
    cout<<"Enter the Unsorted
Array:"<<endl;
    for(i=0;i<n;i++)
    {
        cin>>ar[i];
    }
    for (i=1;i<n;i++)
    {
        k=ar[i];
        j = i - 1;
        while (j >= 0 && ar[j]>k)
        {
            ar[j + 1] = ar[j];
            j = j - 1;
        }
        ar[j + 1]=k;
    }
}

cout<<"After Sort:"<<endl;
for (int i = 0; i < n; i++)
{
    cout << ar[i] << " ";
}
return 0;
}
```

## Output:

```
C:\Users\USER\Documents\ca.exe
Enter the Number of Index:
4
Enter the Unsorted Array:
12 3 234 33
After Sort:
3 12 33 234
Process returned 0 (0x0) execution time : 10.722 s
Press any key to continue.
```

## Bubble Sort

### +Bubble Sort I

Use of the Algorithm :- To sort element from a list of Array.

Input of the Algorithm :- An array of  $n$  elements.

Output of the Algorithm :- A sorted Array.

Complexity :-  $O(N^2)$

Example :-  $A = [4, 3, 2, 1]$

Best case :-  $A = [1, 2, 3, 4]$ ,  $O(N)$

Average case :-  $A = [4, 3, 2, 1]$ ,  $O(N^2)$

Worst case :-  $A = [4, 3, 2, 1]$ ,  $O(N^2)$

Basic Workflow of the Algorithm :-

Works by repeatedly swapping neighboring elements if they are in the wrong order. This algorithm is not suitable for large data sets because it's worst and average case time complexity is High.

## Source Code:

```
#include <bits/stdc++.h>
using namespace std;
int main()
{
    int a[1001],i,j,n;
    cin>>n;
    for (i=0;i<n;i++)
    {
        cin>>a[i];
    }
    for (i = 0; i < n - 1; i++){
        for (j = 0; j < n - i - 1;
j++){
            if (a[j] > a[j + 1]){
                swap(a[j],a[j + 1]);
}
}
}
cout << "Sorted array: "<<endl;
for (i=0;i<n;i++)
{
    cout<<a[i]<<" ";
}
return 0;
```

## Output:

```
0 C:\Users\USER\Documents\ca.exe
1
2
3
4
5
6
7
8
9
```

4  
re12 2 34 56  
6 Sorted array:  
7 2 12 34 56  
8 Process returned 0 (0x0) execution time : 8.342 s  
9 Press any key to continue.  
0  
1  
2  
3  
4  
5  
6

## Selection Sort

### Selection sort

Use of the Algorithm :- To sort the element from list of array.

Input of the Algorithm :- An array of  $n$  elements

Output of the Algorithm :- A sorted Array.  
complexity :-  $O(N^2)$ .

Example :-

I Best Case :-  $O(N^2)$ ,  $A = \{1, 2, 3, 4\}$

II Worst case :-  $O(N^2)$ ,  $A = \{4, 3, 2, 1\}$

III Average case :-  $O(N^2)$   $A = \{2, 1, 3, 4\}$

Basic Work flow of the Algorithm :- It is an in-place comparison-based algorithm that divide the list into two parts, a left sorted part and a right unsorted part. Initially, the sorted selection is empty, and unsorted contains full list. It is used to sort a short list.

## Source Code:

```
#include <bits/stdc++.h>
using namespace std;
void s_sort(int a[],int n)
{
    int i, j,min_idx;
    for(i=0;i<n-1;i++)
    {
        min_idx = i;
        for (j = i+1; j < n; j++)
            if (a[j] < a[min_idx])
                min_idx = j;
        if(min_idx!=i)
            swap(a[min_idx],a[i]);
    }
}

int main()
{
    int a[1001],n,i;
    cin>>n;
    for(i=0;i<n;i++)
    {
        cin>>a[i];
    }
    s_sort(a,n);
    cout << "Sorted array is: \n";
    for (i=0;i<n;i++)
    {
        cout <<a[i]<< " ";
    }
    return 0;
}
```

## Output:

```
C:\Users\USER\Documents\ca.exe
4
8 12 3 4 2
Sorted array is:
2 3 4 12
Process returned 0 (0x0)  execution time : 16.282 s
fPress any key to continue.

f
```

## Merge Sort

### Merge sort

Use of the Algorithm :- To sort the elements from a list of Array.

Input of the algorithm :- An Array of  $n$  elements.

Output of the Algoirthm :- A sorted Array.

complexity :-  $O(N \log N)$

Example :-

① Best case :-  $O(N \log N)$ ,  $A = \{1, 4, 8, 10\}$

② Worst case :-  $O(N \log N)$ ,  $A = \{4, 3, 2, 1\}$

③ Average case :-  $O(N \log N)$ ,  $A = \{2, 1, 1, 3, 2\}$

Basic Workflow of the Algorithm :- We divide a

array in sub array until reach a stage where

we try to perform Mergeform on a sub array.

After that the merge function comes into play and combine the sorted arrays into larger arrays until the whole array is merge.

## Source Code:

```
#include<bits/stdc++.h>
using namespace std;
int ar[10] = {11, 19, 13, 96, 14,
12, 28, 47};
vector<int>v;
void Partition(int l, int r)
{
    if(l==r) return;
    int mid = (l+r)/2;
    Partition(l,mid);
    Partition(mid+1,r);
    v.clear();
    int i=l, j=mid+1;
    while(i<=mid || j<=r)
    {
        if(i<=mid &&
j<=r)
        {
            if(ar[i]<ar[j])
            {
                v.push_back(ar[i]);
                i++;
            }
            else
            {
                v.push_back(ar[j]);
                j++;
            }
        }
        else if(i<=mid)
        {
            v.push_back(ar[i]);
        }
    }
}
int main()
{
    int i = 0;
    Partition(0,7);
    cout<<"After sorting:
"<<endl;
    while(i<8)
    {
        cout << ar[i] <<
" ";
        i++;
    }
    return 0;
}
```

## **Output:**

---

```
[1] "C:\Users\USER\Downloads\388 (1).exe"
After sorting:
11 12 13 14 19 28 47 96
Process returned 0 (0x0) execution time : 0.247 s
Press any key to continue.
[1]
```

## Quick Sort

### Quick Sort

Use of the Algorithm :- To sort the element from a list.

Input of the Algorithm :- An Array of  $n$  elements.

Output of the Algorithm :- A sorted Array.

complexity :-  $O(N \log N)$ .

Example :-

(I) Best case :-  $A = \{4, 3, 2, 1\}$  ;  $O(N \log N)$ .

(II) Worst case :-  $A = \{1, 2, 3, 4\}$  ,  $O(N \log N)$ .

(III) Average case :-  $A = \{2, 1, 1, 3, 3, 1\}$   $O(N^2)$ .

Basic Work flow of the Algorithm :-

(I) An array is divided into subarray by selecting a pivot element.

(II) The left and right subarrays are also divided into the same approach until it contains a single element.

(III) The approach is the pivot element should be positioned in such a way that elements less than pivot are kept on the left side and elements greater than pivot are on the right side of the pivot.

(IV) At this point, the elements are already sorted.

## Source Code:

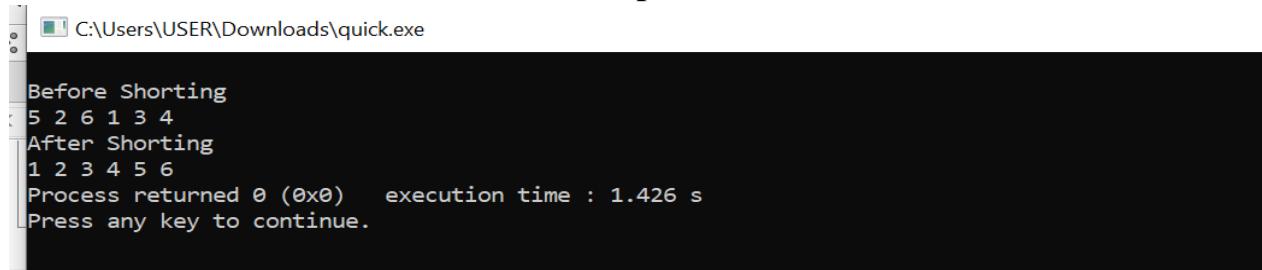
```
#include <bits/stdc++.h>
#include<iostream>
using namespace std;
int a[]={5,2,6,1,3,4};
int par(int l, int r)
{
    int pivotindex=l;
    while(l!=r)
    {
        if(pivotindex==l)
        {

if(a[pivotindex]<a[r])
            {
                r--;
            }
            else
            {
swap(a[pivotindex],a[r]);
                pivotindex=r;
            }
        }
        else
        {
            if(a[l]<a[pivotindex])
            {
                l++;
            }
            else
            {

swap(a[pivotindex],a[l]);
                pivotindex=l;
            }
        }
    }
}

return 1;
}
void qs(int l, int r)
{
    if(l>=r) return;
    int mid=par(l,r);
    qs(l,mid-1);
    qs(mid+1,r);
}
int main()
{
    cout<<endl<<"Before
Shorting"<<endl;
    for(int i=0;i<6;i++)
    {
        cout<<a[i]<<" ";
    }
    cout<<endl<<"After
Shorting"<<endl;
    qs(0,5);
    for(int i=0;i<6;i++)
    {
        cout<<a[i]<<" ";
    }
    return 0;
}
```

## Output:



```
C:\Users\USER\Downloads\quick.exe

Before Shorting
5 2 6 1 3 4
After Shorting
1 2 3 4 5 6
Process returned 0 (0x0)  execution time : 1.426 s
Press any key to continue.
```

## Heap Sort

### Heap Sort

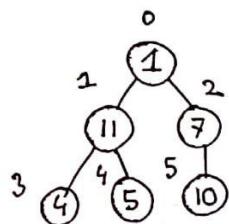
Use of the Algorithm :- To sort the elements from a tree nodes.

Input of the Algorithm :- An array of  $n$  elements.

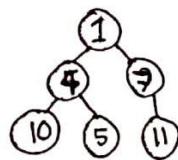
Output of the Algorithm :- An array of  $n$  elements.

Complexity :-  $O(N \log N)$ .

Example :-



1	11	7	4	5	10
---	----	---	---	---	----



1	9	5	7	10	11
---	---	---	---	----	----

Min heap

Basic Workflow of the Algorithm :-

- ① Construct min heap and the min item stored in the root.
- ② Remove the root element and put at the end of the array, put the last item

of the tree at the Vacant palace.

④ Reduce the size of heap by 1. Heapify the root element again so that we have lowest element at root. The process is repeated until all the items of the list are sorted.

## Source Code:

```
#include <iostream>
using namespace std;
void heapify(int arr[], int n, int i)
{
    int largest = i;
    int l = 2 * i + 1;
    int r = 2 * i + 2;
    if (l < n && arr[l] > arr[largest])
        largest = l;
    if (r < n && arr[r] > arr[largest])
        largest = r;
    if (largest != i)
    {
        swap(arr[i], arr[largest]);
        heapify(arr, n, largest);
    }
    heapify(arr, i, 0);
}

void heapSort(int arr[], int n)
{
    for (int i = n / 2 - 1; i >= 0; i--)
        heapify(arr, n, i);
    for (int i = n - 1; i >= 0; i--)
    {
        swap(arr[0], arr[i]);
        heapify(arr, i, 0);
    }
}
int main()
{
    int arr[] = {511, 14, 73, 92, 21};
    int n = sizeof(arr) /
    sizeof(arr[0]);
    heapSort(arr, n);
    cout << "Sorted array is \n";
    for (int i = 0; i < n; ++i)
        cout << arr[i] << " ";
    cout << "\n";
}
```

## Output:

```
C:\Users\USER\Downloads\quick.exe
Sorted array is
14 21 73 92 511

Process returned 0 (0x0)  execution time : 6.588 s
Press any key to continue.
```

## Greedy Algorithms

### Activity Selection Problem

#### Activity Selection problem

##### Use of the algorithm:-

It is use to find the number of maximum non overlapping activities that can be perform. It is also known as Interval partitioning. We can find largest compatible set of works by this.

##### Input of the algorithm:-

The input of the Algorithm is a array which contain starting time and ending time.

##### Output of the Algorithm:-

largest number of compatible work result in array.

complexity:-  $O(N \log N)$

##### Basic work flow:-

- ① Take a structure which contains Start & Finish time.

- II Short the Activity According to their finish time.

III The selected first element of the array will be printed. After get the first activity from the array. Then start time is updated to the next activity's start time. If the next activity's start time is greater or equal to the finish time of the previous selected activity then print it and update it to the next activity's start time. Repeat this process until the value of it is less than or equal to the destination.

IV Now the iterative process continues until the destination is reached after minimum of steps.

Example: • *principles of marketing*

## Activities → 8

Activities		$\rightarrow$	8
1	3	-	Output :-
0	4	-	$(1,2), (3,5), (5,8)$
1	2	fitting	trips
9	6	visiting	gymn
2	9	odds	skate
5	8	visiting	swim
3	5	gymn	skate
4	5	swim	gymn

## Source Code:

```
#include<bits/stdc++.h>
using namespace std;
struct Activity_selection{
int begin_;
int finish ;
Activity_selection()
{
}
Activity_selection(int initia_, int end_)
{
begin_ = initia_;
finish = end_;
}
Activity_selection A[101];
bool com(Activity_selection a,
Activity_selection b)
{
if(a.finish<b.finish)
return true;
return false;
}

int main()
{
int N;
scanf("%d", &N);
for(int i=0; i<N; i++)
{
scanf("%d%d", &A[i].begin_,
&A[i].finish);
}
sort(A,A+N,com);
cout << "-----Selected
activities-----\n";
int i = 0;
cout << "(" <<
A[i].begin_<< "," <<
A[i].finish << ")";
for(int j=1; j<N; j++)
{
if(A[j].begin_>=A[i].finish)
{
cout << "(" <<
A[j].begin_<< "," <<
A[j].finish << ")";
i = j;
}
}
return 0;
}
```

## Output:

```
C:\Users\USER\Documents\200_202200\activity.exe
8
1 3
0 4
1 2
4 6
2 9
5 8
3 5
4 5
-----Selected activities-----
(1,2)(3,5)(5,8)
Process returned 0 (0x0)  execution time : 2.413 s
Press any key to continue.
```

## Optimal Caching

### Optimal Caching

Use of the Algorithm :- Cache is the fast, small memory which hold a certain amount. It is use for reduces the number of each miss to a minimum possible number. Rather than it is use for minimize the number of each miss.

Input of the Algorithm :- Two strings.

Output of the Algorithm :- Total number of cache miss and total number of cache hit.

complexity :- ~~O(n^2)~~ O(n.m)

$$O(n.m)$$

Example :-

$$K=2$$

Initial cash = ab

Request = a, b, c, b, c, a, a, b

Ans.

2 cache miss

## Basic Workflow of the Algorithm :-

- Step I:- First we get two input of strings.
- It's frame consists of block size. We need to perform all counting of size of each medium memory location so it can be done.
- II Two variables one for request size and for cash memory.
- III A loop i=0 to n and if  $r[i]$  is in cash memory then hit else miss.
- For all  $j=0-m$  find the furthest req to request in memory. Replace it with request and return the number of each miss and hit.

## Source Code:

```
#include<bits/stdc++.h>
using namespace std;
string F,R;
int main()
{
    int FS;
    scanf("%d",&FS);
    cout<<"Frame:";
    cin>>F;
    cout<<"Request:";
    cin>>R;
    int count=0;
    int f_s=F.size();
```

```
else{
    cout<<"\t miss \t\t ";
    for(int j=0;j<f_s;j++){
        int dis=INT_MAX;
        for(int k=i+1;k<r_s;k++){
            if(F[j]==R[k]){
                dis=k-i;
                break;
            }
        }
    }
}
```

```

int r_s=R.size();
cout<<"\nRequest \t hit/miss \t
replaced by \t present cache\n";
for(int i=0;i<r_s;i++){
cout<<R[i]<< " \t";
bool hit=false;
for(int j=0;j<f_s;j++){
if(R[i]==F[j]){
hit=true;
break;
}
}
int repl_ind,mx_dist=0;
if(hit)
{
cout<<"\t hit \t\t none
\t\t";
}
cout<<"\n";
}
}
if(mx_dist<dis)
{
mx_dist=dis;
repl_ind=j;
}
}
}
if(!hit)
{
count++;
cout<<F[repl_ind]<<"\t\t";
F[repl_ind]=R[i];
}
for(int
j=0;j<f_s;j++)cout<<F[j];
cout<<"\n";
}
cout<<"Minimum miss number:
"<<count<<"\n";
return 0;
}

```

## Output:

```
C:\Users\USER\Documents\388_202200\optimalcashing.exe
2
Frame:ab
Request:a b c b c a a b

Request          hit/miss          replaced by      present cache
a                  hit            none           ab
Minimum miss number: 0

Process returned 0 (0x0)  execution time : 31.219 s
Press any key to continue.
```

## Minimize Maximum Lateness

### Mimimizing Maximum Lateness

- ④ Minimum Latness Algorithm is used, ~~efor to find~~ ↳ prilod latitga  
the maximum lateness.
- ④ The input of the Algorithm is structure ↳ imitator of libA  
[user define data type]. ↳ addgant latitwtt
- ④ The output is integer number. ↳ prilod math
- ④ Complexity is  $N \log N$ .

### Workflow

- ① User define data type Event to get duration & deadline
- ② Shoot the event.
- ③  $\text{lateness} = \max(0, k - d)$
- ④ Shoot the lateness.
- ⑤ Output is the final index of lateness.

## Source Code:

```
#include<bits/stdc++.h>
#include<bits/stdc++.h>
using namespace std;
struct Event
{
    int duration;
    int deadline;
    Event(){}
    Event(int du, int de)
    {
        duration =du;
        deadline =de;
    }
    void print()
    {
        printf("Duration = %d,
Deadline=%d\n",duration,deadline);
    }
};
Event E[100];
bool com(Event a, Event b)
{
    if(a.deadline<b.deadline)
        return true;
    return false;
}
int main()
{
    int N;
    cout<<"Enter values\n";
    cin>>N;
    for(int i=0;i<N;i++)
    {
        scanf("%d%d",&E[i].duration,&E[i].deadline);
    }
    for(int i=0;i<N;i++)
    {
        E[i].print();
    }
    sort(E,E+N,com);
    cout<<"\n";
    cout<<"After Sorting\n\n";
    for(int i=0;i<N;i++)
    {
        E[i].print();
    }
    int l[1001];
    for(int i=0;i<N;i++)
    {
        int k;
        k=k+E[i].duration;
        int d=E[i].deadline;
        l[i]=max(0,k-d);
    }
    sort(l,l+N);
    cout<<"\n";
    cout<<"Maximum Lateness is :
"<<l[N-1];
    cout<<"\n";
    return 0;
}
```

## Output:

```
C:\Users\USER\Documents\388_202200\MinimizeMaximumLateness.exe
```

```
Enter values
```

```
6
```

```
3 6
```

```
2 8
```

```
1 9
```

```
4 9
```

```
3 14
```

```
2 15
```

```
Duration = 3, Deadline=6
```

```
Duration = 2, Deadline=8
```

```
Duration = 1, Deadline=9
```

```
Duration = 4, Deadline=9
```

```
Duration = 3, Deadline=14
```

```
Duration = 2, Deadline=15
```

```
After Sorting
```

```
Duration = 3, Deadline=6
```

```
Duration = 2, Deadline=8
```

```
Duration = 1, Deadline=9
```

```
Duration = 4, Deadline=9
```

```
Duration = 3, Deadline=14
```

```
Duration = 2, Deadline=15
```

```
Maximum Lateness is : 1
```

```
Process returned 0 (0x0) execution time : 25.503 s
```

```
Press any key to continue.
```

## Fractional Knapsack

start of problem

**Fractional Knapsack**

End

(1)

Use of the Algorithm :-

When a set of items each with a weight and a value, if subset of items has to choose such that total weight of the items is less than or equal to the size of the knapsack and the profit is maximum. It is

use to maximize the total value of knapsack by breaking items.

$\leftarrow$  positive

Inputs of the Algorithm :-

An array contain weight and profit.

The knapsack size also.

Q 1

F 0

S P

C L

B E

-

Output :- Output is maximum profit of the chosen items.

Complexity :-  $O(N \log N)$

Example :-

$$\text{Profit} = \{12, 32, 40, 30, 50\}$$

$$\text{Weight} = \{4, 8, 2, 6, 2\}$$

$$\text{Maximum profit} = 124$$

Basic work flow :-

- (I) Need a user define data type to contain profit and weight.
- (II) Then the ratio of value and weight calculation for each item.
- (III) Sort all the items in decreasing order. From the ration we get.
- (IV) If weight of current item is less or equal to remaining capacity then sum the value into the result or break the item add the profit on the final value.

### Source Code:

```
#include <bits/stdc++.h>
using namespace std;
struct item
{
    int value, weight;
    item(){}
    item(int v, int w)
        : value(v), weight(w)
    {
    }
};

int knapsack(const vector<item>& arr, int W)
{
    int n = arr.size();
    vector<int> dp(W + 1, 0);
    for (int i = 0; i < n; ++i) {
        for (int w = W; w >= arr[i].weight; --w) {
            if (arr[i].weight > w)
                continue;
            dp[w] = max(dp[w], dp[w - arr[i].weight] + arr[i].value);
        }
    }
    return dp[W];
}
```

```

{
value = v;
weight = w;
}
};

item arr[101];
bool cmp(item a,item b)
{
double f1 = (double)a.value /
(double)a.weight;
double f2 = (double)b.value /
(double)b.weight;
return f1 > f2;
}

double frac_Knap(int W,item arr[], int N)
{
sort(arr, arr + N, cmp);
double finalvalue = 0.0;
for (int i = 0; i < N; i++)
{
if (arr[i].weight <= W)
{
W -= arr[i].weight;
break;
}
finalvalue += arr[i].value;
}
return finalvalue;
}

int main()
{
int W,N;
cout<<"Enter the number of items\n";
cin>>N;
cout<<"Enter the weight of Knapsack\n";
cin>>W;
cout<<"Enter the item Values:\n";
for(int i=0;i<N;i++)
{
cin>>arr[i].value;
cin>>arr[i].weight;
}
cout << "Maximum value = "
<< frac_Knap(W, arr,
N);
return 0;
}

```

## Output:

```

C:\Users\USER\Documents\388_202200\FractionalKnapsac.exe
Enter the number of items
5
Enter the weight of Knapsack
10
Enter the item Values:
12 4
32 8
40 2
30 6
50 1
Maximum value = 124
Process returned 0 (0x0) execution time : 35.024 s
Press any key to continue.

```

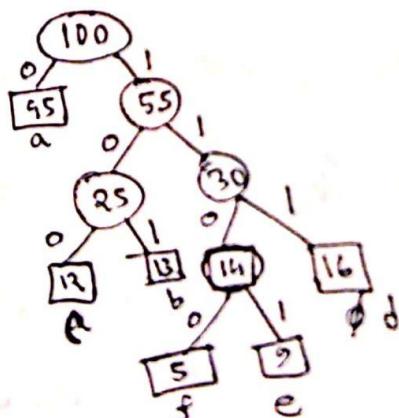
## Huffman Coding

### Huffman Coding

#### Use of the Algorithm :-

- Huffman coding is a method of data compression that is independent of data type.
- It reduces the overall size of file.
- Input :- Pair of integer and string.
- Output :- Length and codeword.
- complexity :-  $O(n \log n)$ .

#### Example :-



codeword	frequency
a	0
b	101
c	100
d	111
e	1101
f	1100

## Basic workflow

- ① We take map and pair, Priority queue for take input.
- ② Constructed graph of Tree and mark the left & Right child.
- ③ Get the codeword and print.

## Source Code:

```
#include <bits/stdc++.h>
using namespace std;
#define N '\n'
#define ll long long
map<pair<int, string>, int> M;
pair<int, string> node[100];
vector<int> G[100];
priority_queue<pair<int, string>, vector<pair<int, string>>, greater<pair<int, string>> PQ;
void cpy(int n, string code)
{
if(G[n].size() > 1)
{
cpy(G[n][0], code + "0");
cpy(G[n][1], code + "1");
}
else
{
cout << node[n].second << ": Length = "
" << code.size() << " Codeword = "
" << code << N;
}
while(PQ.size() > 1)
{
pair<int, string> a, b, c;
a = PQ.top();
PQ.pop();
b = PQ.top();
PQ.pop();
c.first = a.first + b.first;
c.second = a.second + b.second;
PQ.push(c);
cnt++;
M[c] = cnt;
node[cnt] = c;
int x, y, z;
x = M[a];
y = M[b];
z = M[c];
G[z].push_back(x);
G[z].push_back(y);
}
int p = M[PQ.top()];
cpy(p, " ");
}
int main()
```

```

}
}

void huffman(int number)
{
ll cnt=0;
for(ll i=0; i<number; i++)
{
string s;
int k;
cin>>s;
cin>>k;
pair<int,string>
A=make_pair(k,s);
M[A]=i+1;
node[i+1]=A;
PQ.push(A);
cnt++;
}

```

```

{
cout<<"-----"
-----"<<N;
cout<<"Enter total number of
charecter"<<N;
ll number;
cin>>number;
cout<<"-----"
-----"<<N;
cout<<"Enter the character
and frequency"<<N;
huffman(number);
return 0;
}

```

## Output:

```

C:\Users\USER\Documents\388_202200\Huffman.exe
-----
Enter total number of charecter
6
-----
Enter the character and frequency
a 45
b 13
c 12
d 16
e 9
f 5
a: Length = 2 Codeword =  0
c: Length = 4 Codeword =  100
b: Length = 4 Codeword =  101
f: Length = 5 Codeword =  11001
e: Length = 5 Codeword =  1101
d: Length = 4 Codeword =  111

Process returned 0 (0x0)  execution time : 105.430 s
Press any key to continue.

```

## Dynamic programming

### Longest Increasing Subsequence

#### Longest Increasing Subsequence

Use of the Algorithm :- To Find the length of long increasing subsequence of a given sequence.

Input of the Algorithm :- An Array.

Output of the Algorithm :- Length of the subsequence.

Complexity :-  $O(N^2)$ .

Basic Workflow of the Algorithm :- By using Dynamic programming this type of problem can be solved.

Hence we can get overlapping sub problems.

By Dynamic programming technique we can memoize this and apply on need. By Tabular

format technique we can memorize it. LIS is longest increasing of an array. We can

take the input and performing dynamic programming technique on it.

## Source Code:

```
#include <iostream>
using namespace std;
int _lis(int arr[], int n, int*
max_ref)
{
    if (n == 1)
        return 1;
    int res, max_ending_here = 1;
    for (int i = 1; i < n; i++) {
        res = _lis(arr, i,
max_ref);
        if (arr[i - 1] < arr[n - 1]
            && res + 1 >
max_ending_here)
            max_ending_here =
res + 1;
        if (*max_ref < max_ending_here)
            *max_ref =
max_ending_here;
    }
    return max_ending_here;
}
```

```
#include <iostream>
using namespace std;
int _lis(int arr[], int n, int*
max_ref)
{
    if (n == 1)
        return 1;
    int res, max_ending_here = 1;
    for (int i = 1; i < n; i++) {
        res = _lis(arr, i,
max_ref);
        if (arr[i - 1] < arr[n - 1]
            && res + 1 >
max_ending_here)
            max_ending_here =
res + 1;
        if (*max_ref <
max_ending_here)
            *max_ref =
max_ending_here;
    }
    return max_ending_here;
}
```

## Output:

```
C:\Users\USER\Documents\ca.exe
Length of LIS is 6
Process returned 0 (0x0) execution time : 0.141 s
Press any key to continue.
```

## Longest Common Subsequence

### Longest Common Subsequence

Use of the Algorithm :- Find the longest common subsequence between two strings.

Input of the algorithm :- Two string.

Output of the Algorithm :- Longest common subsequence and it's Length.

Complexity :-  $O(N^2)$ .

Basic Workflow :- By doing tabular format this kind of problem can be solved. If  $s_1$  and  $s_2$  are two given sequences then  $\pi$  is the common subsequence of both  $s_1$  &  $s_2$ . The method of dynamic programming reduces the number of function calls. It stores the result of each function call so that it can be used in future call.

## Source Code:

<pre>#include&lt;bits/stdc++.h&gt; using namespace std; int lcs(string str1, string str2, int len1, int len2) {     int i, j;     int LCS[len1+1][len2+1];     for(i=0; i&lt;=len1; i++)         LCS[i][0]=0;     for(j=0; j&lt;=len2; j++)         LCS[0][j]=0;     for(i=1; i&lt;=len1; i++)     {         for(j=1; j&lt;=len2; j++)         {             if(str1[i-1]==str2[j-1])             {                 LCS[i][j]=1+LCS[i-1][j-1];             }             else             {                 LCS[i][j]=max(LCS[i-1][j],LCS[i][j-1]);             }         }     }     return LCS[len1][len2]; }</pre>	<pre>int main() {     string str1,str2;     cout&lt;&lt;"Enter first string   ";     getline(cin, str1);     cout&lt;&lt;"Enter second string  ";     getline(cin, str2);     int len1=str1.length();     int len2=str2.length();     cout&lt;&lt;"Length of longest common subsequence is "&lt;&lt;lcs(str1,str2,len1,len2);     cout&lt;&lt;endl;     return 0; }</pre>
---	---

## Output:

The screenshot shows a terminal window with the following output:

```
C:\Users\USER\Documents\ca.exe
Enter first string  BACABACB
Enter second string ACBAABAC
Length of longest common subsequence is 6

Process returned 0 (0x0)  execution time : 29.574 s
Press any key to continue.
```

## 0/1 knapsack Problem

### 0/1 Knapsack

Use of the algorithm :- By filling the knapsack of size  $N$ , we have to maximize the profit.

Input of the algorithm :- Weight of the items, Values of the item, size of the knapsack.

Output of the Algorithm :- Maximum profit.

Complexity :-  $O(N \cdot W)$ .

Basic Workflow :- By DP[][] table let's consider all the possible weights from 1 to " $W$ " as the columns and weights can be kept in the rows. The state  $DP[i][j]$  will denote maximum value of  $j$  weight considering all values from 1 to  $i$ th. By using tabular format technique we can solve this kind of problem. By sequentially Do this we can get the maximum profit.

## Source Code:

```
#include <bits/stdc++.h>
using namespace std;
int max(int a, int b)
{
    return (a > b) ? a : b;
}
int knapSack(int W, int wt[], int val[], int n)
{
    int i, w;
    vector<vector<int>> K(n + 1,
vector<int>(W + 1));
    for(i = 0; i <= n; i++)
    {
        for(w = 0; w <= W; w++)
        {
            if (i == 0 || w ==
0)
                K[i][w] = 0;
            else if (wt[i - 1]
<= w)
                K[i][w] =
max(val[i - 1] +
K[i - 1][w - wt[i - 1]],
K[i - 1][w]);
            else
                K[i][w] = K[i
- 1][w];
        }
    }
    return K[n][W];
}

int main()
{
    int val[] = {12,10,9,6};
    int wt[] = {2,4,3,1};
    int W =6;
    int n = sizeof(val) /
sizeof(val[0]));

    cout << knapSack(W, wt, val,
n);

    return 0;
}
```

## Output:

```
C:\Users\USER\Documents\ca.exe
27
Process returned 0 (0x0)  execution time : 2.437 s
Press any key to continue.
```

## Graph Algorithms

### Breadth First search (BFS)

BFS

Use of the Algorithm :- To visit all the node of the graph.

Input of the graph :- Vertices and Edges of Graph.

Output of the Algorithm :- All visited node of the graph.

complexity :-  $O(V+E)$

Basic Work flow of the Algorithm :-

- ① Declare a queue and insert the starting vertex.
- ② Initialize a visited array and mark the starting vertex as visited.
- ③ By following below process until the queue becomes empty:-
  - ① Remove the first vertex of the queue.
  - ② Mark that vertex as visited.
  - ③ Insert all the unvisited neighbour of the vertex into the queue.

## Source Code:

```
#include<bits/stdc++.h>
using namespace std;
vector<int>G[1000];
bool visited[100];
void dfs(int src)
{
    cout<<src<<" ";
    visited[src]=true;
    for(auto it:G[src])
    {
        if(!visited[it])
        {
            visited[it]=true;
            dfs(it);
        }
    }
}

int main()
{
    int edge,vertex,i,v,u;
    cout<<"Enter the vertices and
edge:";

    cin>>edge>>vertex;
    cout<<"Enter the edge:\n";
    for(i=0;i<edge;i++)
    {
        cin>>u>>v;
        G[u].push_back(v);
        G[v].push_back(u);
    }
    cout<<"\nThe node is after
traversing(DFS):";
    dfs(1);
    return 0;
}
```

## Output:

```
C:\Users\USER\Downloads\quick.exe
Enter the vertices and edge:5 6
Enter the vertices and edge:
s
1 5
5 2
5 3
1 4
4 3

The node is after traversing(DFS):1 5 2 3 4
Process returned 0 (0x0) execution time : 75.272 s
Press any key to continue.
```

## Depth First search (DFS)

[DFS]

use of the algorithm :- To traverse all the nodes of a graph.

Input of the Algorithm :- Vertices and edges of a graph.

Output of the Algorithm :- All visited vertex of the graph.

complexity :-  $O(V+E)$

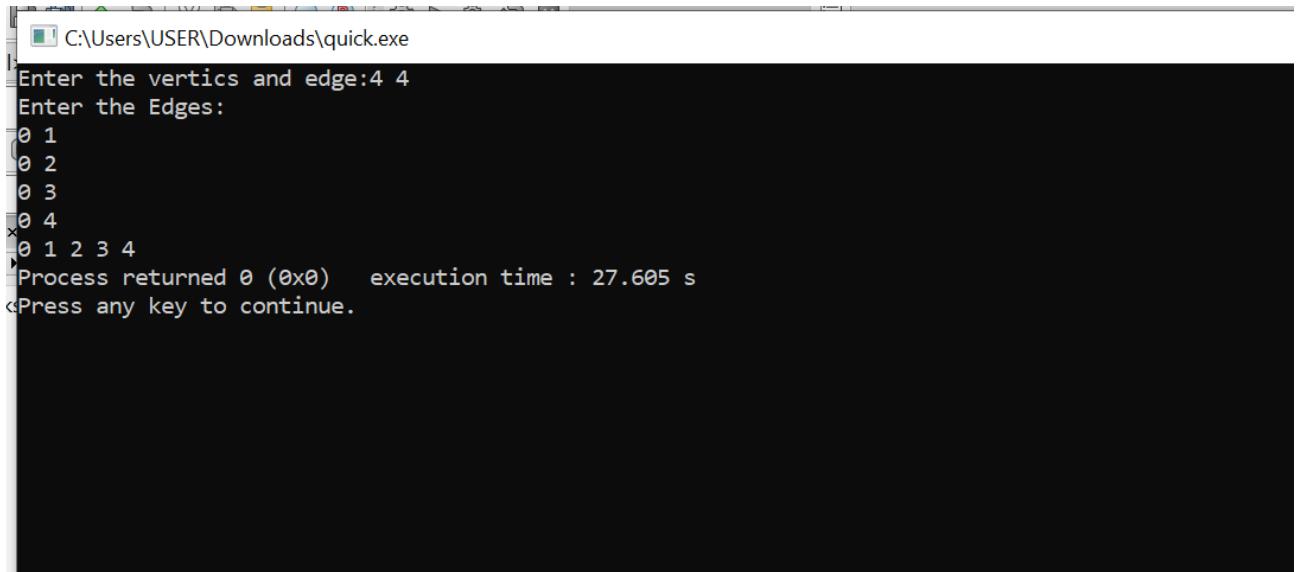
Basic Workflow :-

- ① First put any of the node of the graph at the top of a stack.
- ② Takeout the top most item of the stack and add it to visited list.
- ③ Create a list of that vertex adjacent nodes. Add the one's which aren't in the visited list to the top of the stack.
- ④ Keep Repeating step 2 & 3 untill the stack is empty.

## Source Code:

```
#include<iostream>
#include<bits/stdc++.h>
using namespace std;
vector<int>G[100];
bool visited[1000];
int main()
{
    int vertex,edge,i,u,v;
    cout<<"Enter the vertices and
edge:";
    cin>>vertex>>edge;
    cout<<"Enter the Edges:\n";
    for(i=0;i<edge;i++)
    {
        cin>>u>>v;
        G[u].push_back(v);
        G[v].push_back(u);
    }
}
queue<int>q;
q.push(0);
visited[0]=true;
while(!q.empty())
{
    int x = q.front();
    q.pop();
    cout<<x<<" ";
    for(auto it:G[x])
    {
        if(!visited[it])
        {
            q.push(it);
            visited[it]=true;
        }
    }
}
return 0;
```

## Output:



```
C:\Users\USER\Downloads\quick.exe
Enter the vertices and edge:4 4
Enter the Edges:
0 1
0 2
0 3
0 4
0 1 2 3 4
Process returned 0 (0x0)  execution time : 27.605 s
Press any key to continue.
```