

Recommender Systems

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[Notebook Link Here](#)

Workshop Overview

Prereqs:

- Some basic ML knowledge
- Basic Linear Algebra

Goals:

- Start with basic architectures and build our way up in complexity
 - Basic Models
 - Models currently used in Industry
 - Emerging Architectures
- Implement our own recommendation systems

Workshop Outline

- What are Recommender Systems?
- Motivation
- History Timeline
- Level 1: Basic Models
 - Content Based Filtering (KNN)
 - Collaborative Filtering (Matrix Factorization)
- Level 2: Industry Models
 - Neural Collaborative Filtering
- Level 3: Emerging Architectures
 - Graph Neural Networks
- Notebook
- Useful Resources

What are Recommender Systems?

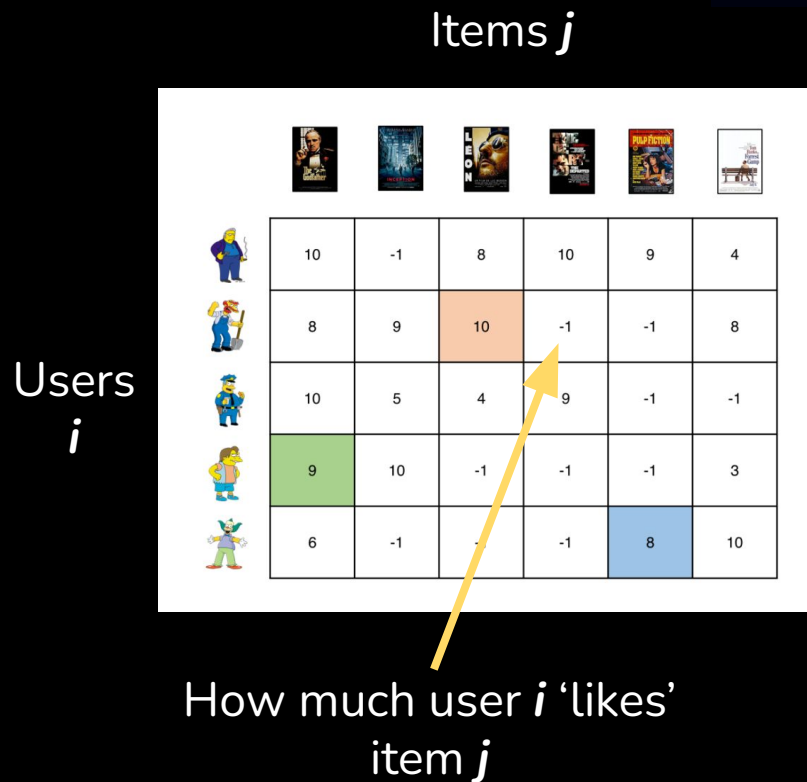
Recommender Systems (Rec Sys) are a class of ML model made to provide personalized recommendations relevant to users

Terminology:

Items - Info about objects being recommended (e.g. movies)

Users - Info about users

Embeddings - Representations of a user/items in a N-dimensional vector



Motivation

- Rec Sys are one of the most relevant ML topics to industry
- They are a core aspect of revenue-generation for many B2C tech companies
- Aim to maximize customer retention

Facts:

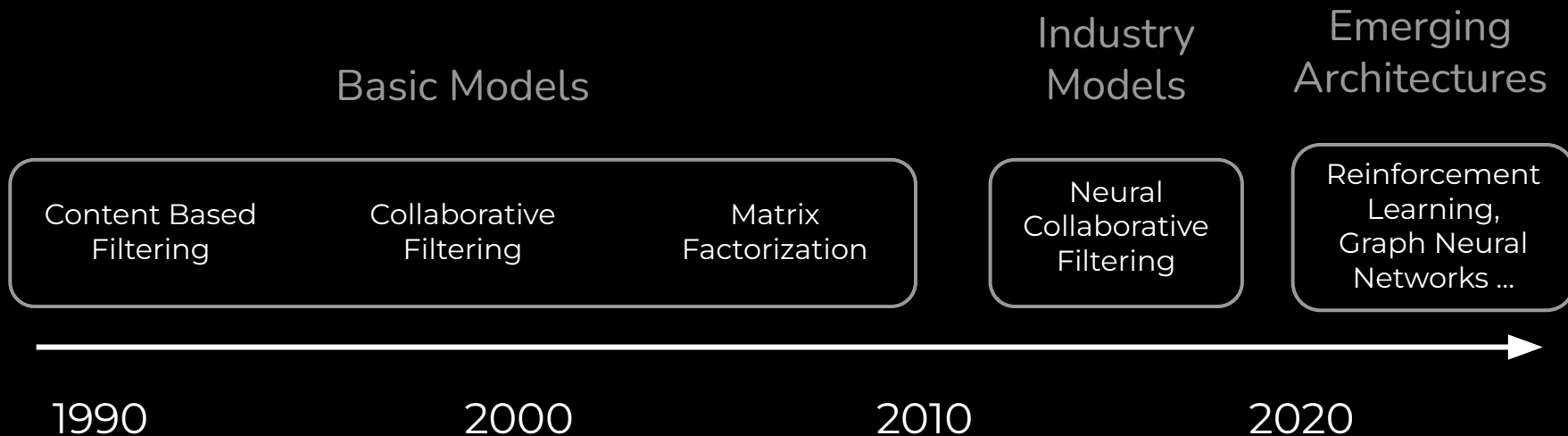
- Rec Sys are responsible for **35%** of Amazon.com's revenue
- **80%** of Netflix stream time comes from its recommendations

Examples in Industry:

- Amazon.com Products
- Netflix Movies
- Youtube Home page
- Instagram Explore Page
- Steam Explore Page

And so on ...

History Timeline



Level 1 - Content Based Filtering

Defn: Recommending **similar items** to what the user likes

Ex - Video Game Recommendations

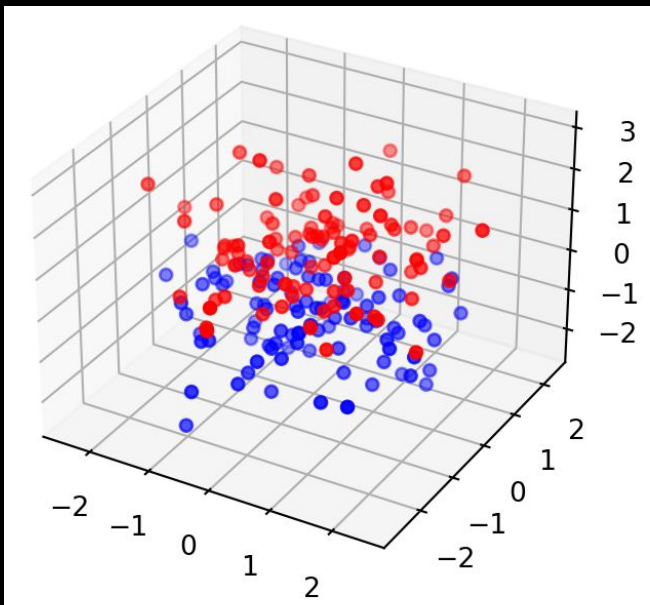
	Features		
	F1	F2	F3
User 1	0	4	9
User 2	6	2	1
User 3	7	3	5

	Features		
	F1	F2	F3
Item 1	5	5	2
Item 2	9	7	9
Item 3	0	3	8

Feature Labels:
F1 - FPS
F2 - Adventure
F3 - Sports

Level 1 - Content Based Filtering

Given the user + item embeddings we can represent them in a N dimensional space:



Red Points - Users

Blue Points - Items

The Rec Sys has to find the most similar items for user i using a **similarity metric** that measures distance between embeddings/points

Level 1 - Content Based Filtering

Similarity Metric: Euclidean Distance

$$d(x, y) = \sqrt{\sum_{i=1}^n (y_i - x_i)^2}$$

Magnitude of a straight line between two points in a N-dimensional space

Find Similar Points: K-Nearest Neighbors (KNN)

- Initialize value of K
- For every item embedding:
 - Calculate distance between item and user i
- Find the K smallest calculated distances
- The corresponding items are your “similar items”

Precision @ K:

(# of relevant items at K)

K

Level 1 - Content Based Filtering

Pros	Cons
Easy to understand + High interpretability	Needs hand-engineered features beforehand
Scalable for lots of users (since users treated independently)	Needs information for each user and item beforehand (expensive & infeasible)

Level 1 - Collaborative Filtering

Defn: Recommending items based on what **similar users** like

Feedback Matrix $A_{M \times N}$

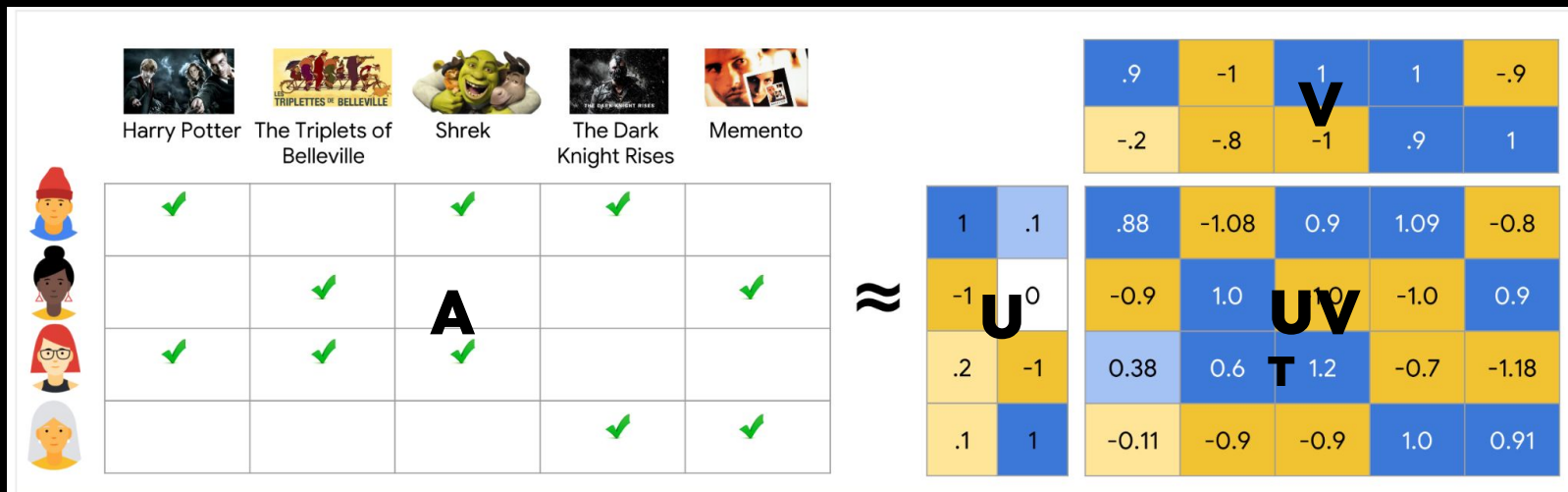
	 Harry Potter	 The Triplets of Belleville	 Shrek	 The Dark Knight Rises	 Memento
	✓		✓	✓	
		✓			✓
	✓	✓	✓		
				✓	✓

$A_{i,j} = 1 \rightarrow$ User i interested in item j

$A_{i,j} = 0 \rightarrow$ User i not interested in item j (or unobserved)

Level 1 - Collaborative Filtering

Item Embedding
Matrix



Feedback Matrix

User Embedding
Matrix

Level 1 - Collaborative Filtering

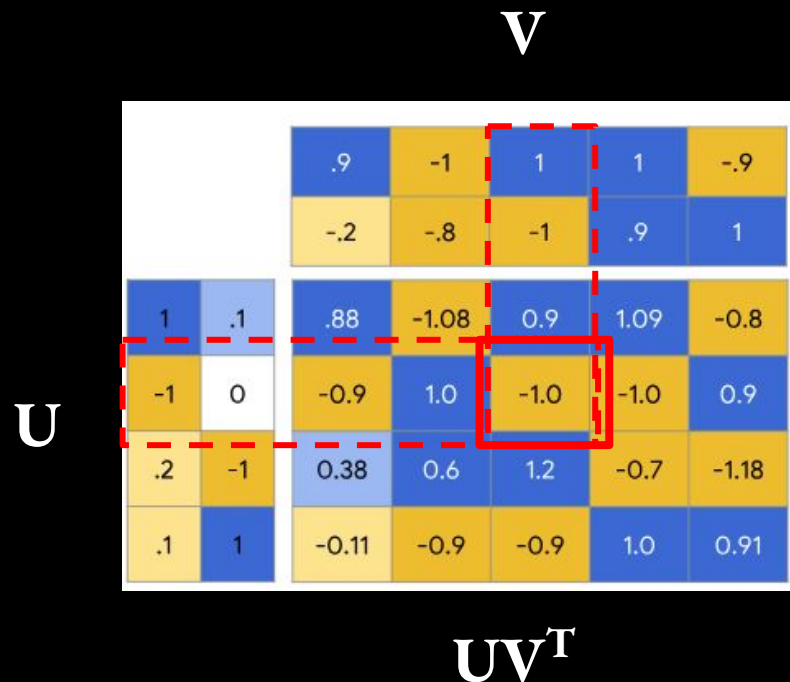
Matrix Factorization:

Finds user matrix U and item matrix V that minimizes the function

$$\min_{U \in \mathbb{R}^{m \times d}, V \in \mathbb{R}^{n \times d}} \|A - UV^T\|_F^2.$$

Ways to solve

- Singular Value Decomposition (too slow)
- Stochastic Gradient Descent



Level 1 - Collaborative Filtering

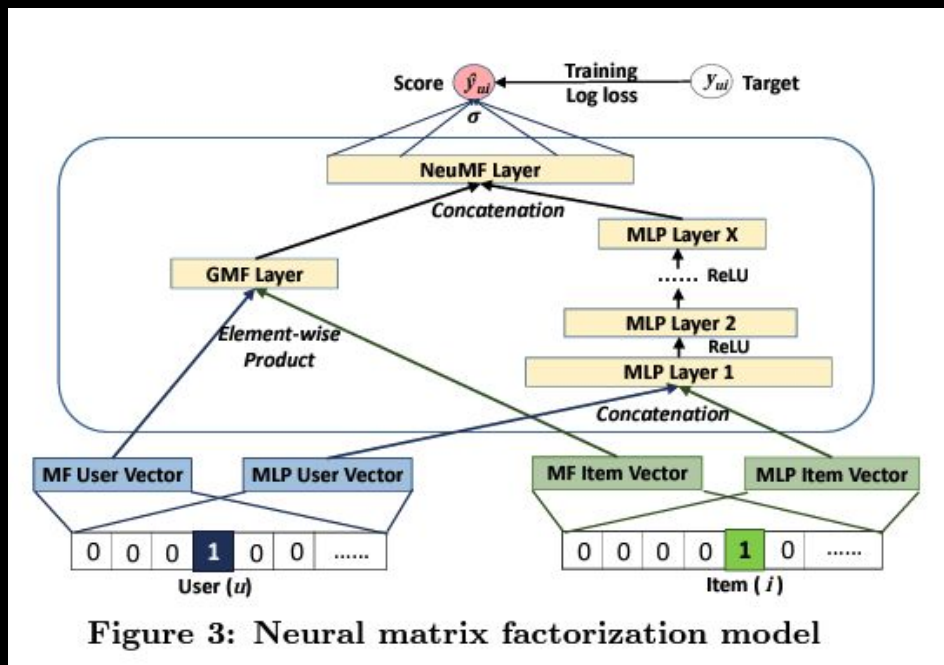
Pros	Cons
Don't need to specify features beforehand	Unable to capture non-linear relationships between users and items
No domain knowledge required	(Since UV^T is made up of weighted sums)
Makes use of all data available for predictions	

Level 2 - Neural Collaborative Filtering

Was the next breakthrough in RecSys in 2017

Kickstarted the use of Deep Learning (Neural Networks) in Rec Sys.

Made the upgrade from the previous industry standard: Matrix Factorization

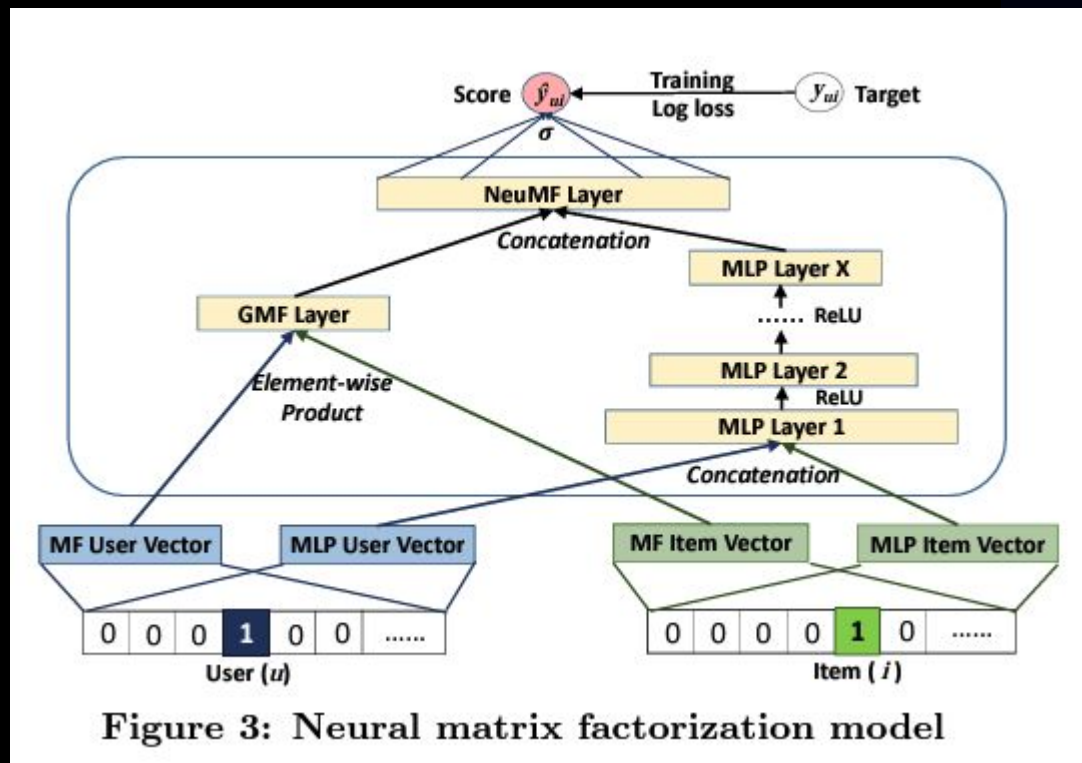


Level 2 - Neural Collaborative Filtering

Purpose:

Model predicts interaction score between **user u** and **item j**

Predicted score is denoted \hat{y}_{ui}



Level 2 - Neural Collaborative Filtering

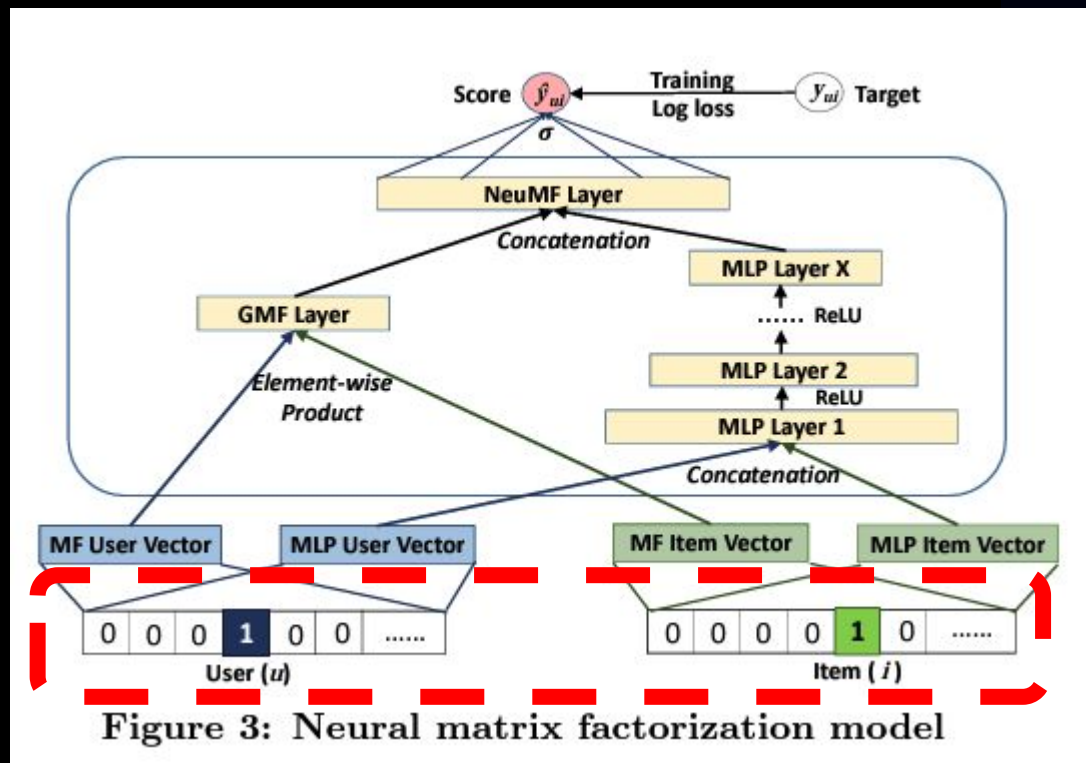
Input Layer:

IDs of (user, item) pair in sparse one hot encoded form

Ex:

4 \rightarrow [0,0,0,1,0,0, ...]

5 \rightarrow [0,0,0,0,1,0, ...]



Level 2 - Neural Collaborative Filtering

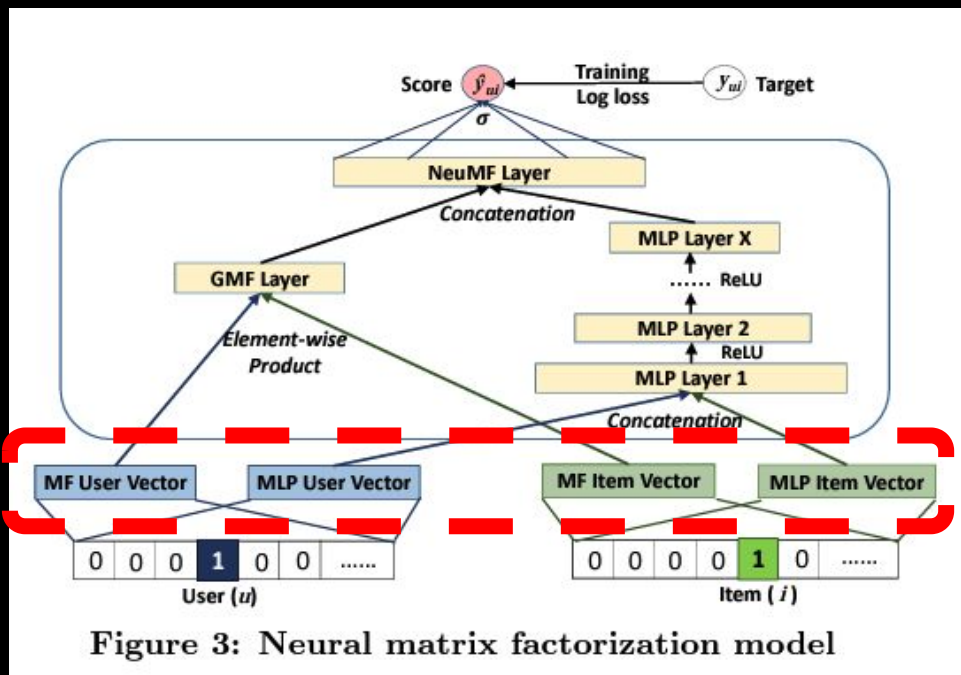
Embedding Layer:

The inputs converted to their corresponding embeddings from matrix factorization model

Embedding of user ID 3 below

		.9	-1	1	1	-.9
		-.2	-.8	-1	.9	1
1	.1	.88	-1.08	0.9	1.09	-0.8
-1	0	-0.9	1.0	-1.0	-1.0	0.9
.2	-1	0.38	0.6	1.2	-0.7	-1.18
.1	1	-0.11	-0.9	-0.9	1.0	0.91

Matrix factorization model representation: U (User Embeddings), V (Item Embeddings), and UV^T (Predicted Ratings).



Level 2 - Neural Collaborative Filtering

Generalized Matrix Factorization Layer:

$$\mathbf{x} = \mathbf{p}_u \odot \mathbf{q}_i$$
$$\hat{y}_{ui} = \alpha(\mathbf{h}^\top \mathbf{x}),$$

\mathbf{p}_u = embedding for user u

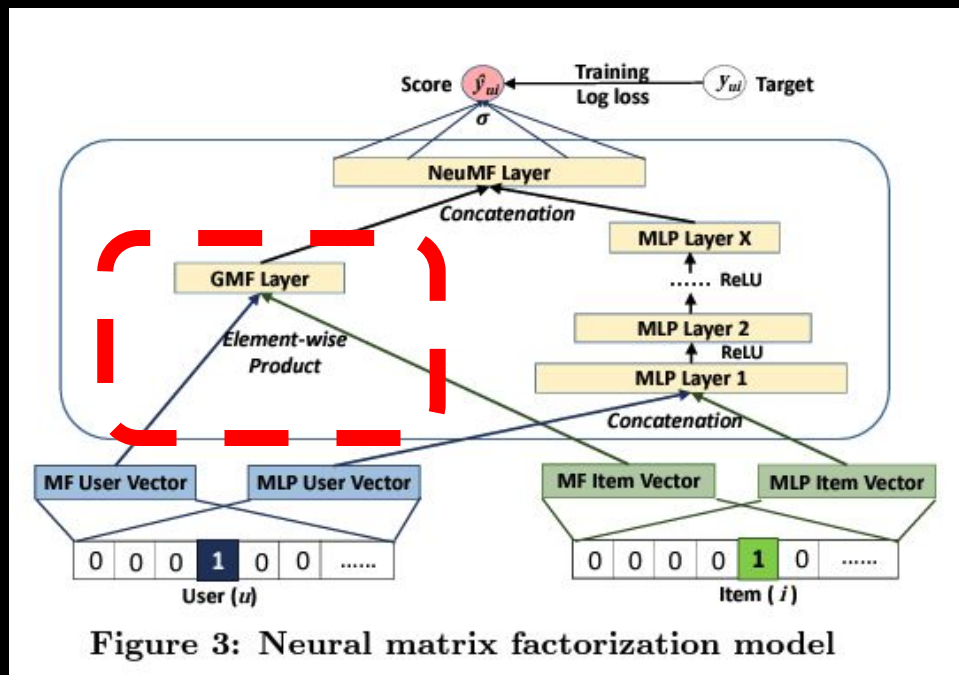
\mathbf{q}_i = embedding for item i

\mathbf{x} = resulting input vector

α = activation function of NN

\mathbf{h} = weights of NN

\hat{y}_{ui} = prediction for user u , item i



Level 2 - Neural Collaborative Filtering

Multi-Layer Perceptron Layer:

Responsible for capturing the non-linear patterns

$$\begin{aligned}z^{(1)} &= \phi_1(\mathbf{U}_u, \mathbf{V}_i) = [\mathbf{U}_u, \mathbf{V}_i] \\ \phi^{(2)}(z^{(1)}) &= \alpha^1(\mathbf{W}^{(2)}z^{(1)} + b^{(2)}) \\ &\vdots \\ \phi^{(L)}(z^{(L-1)}) &= \alpha^L(\mathbf{W}^{(L)}z^{(L-1)} + b^{(L)}) \\ \hat{y}_{ui} &= \alpha(\mathbf{h}^\top \phi(z^{(L-1)}))\end{aligned}$$

\mathbf{W} - weight matrix

b - bias vector

α - activation function

Φ - function of labelled layer

z - output of labelled layer

\hat{y}_{ui} = prediction for user u , item i

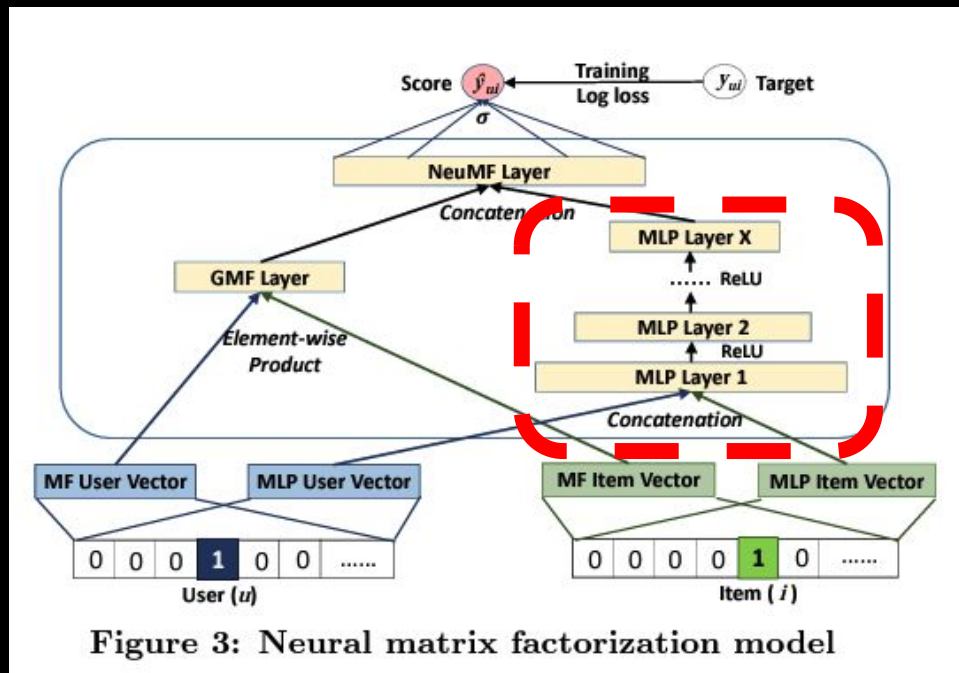


Figure 3: Neural matrix factorization model

Level 2 - Neural Collaborative Filtering

NeuMF Layer:

Combines results both networks

Concatenates the second last layers of the GMF and MLP networks to get:

$$\hat{y}_{ui} = \sigma(\mathbf{h}^\top [\mathbf{x}, \phi^L(z^{(L-1)})]).$$

σ - sigmoid activation function

\mathbf{h} - projection matrix

\hat{y}_{ui} = prediction for user u , item i

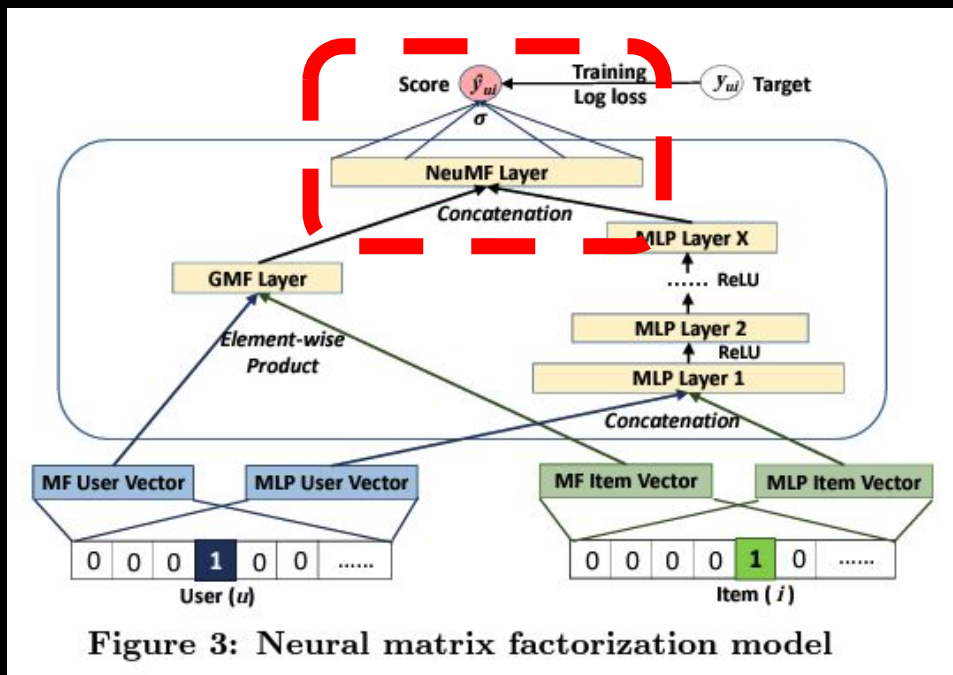


Figure 3: Neural matrix factorization model

Level 2 - Neural Collaborative Filtering

Loss Score:

Neural Collaborative Filtering uses pointwise loss:

$$L_{sqsr} = \sum_{(u,i) \in \mathcal{Y} \cup \mathcal{Y}^-} w_{ui} (y_{ui} - \hat{y}_{ui})^2,$$

\mathcal{Y} - set of observed interactions

\mathcal{Y}^- - set of unobserved interactions

w_{ui} - weight hyperparameter

y_{ui} - target

\hat{y}_{ui} - prediction

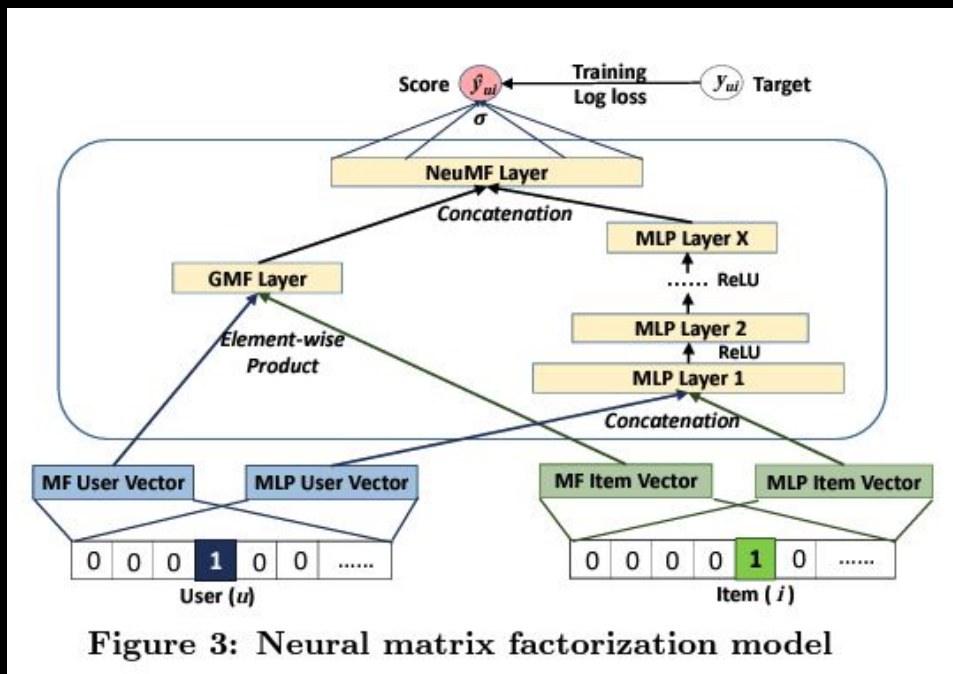


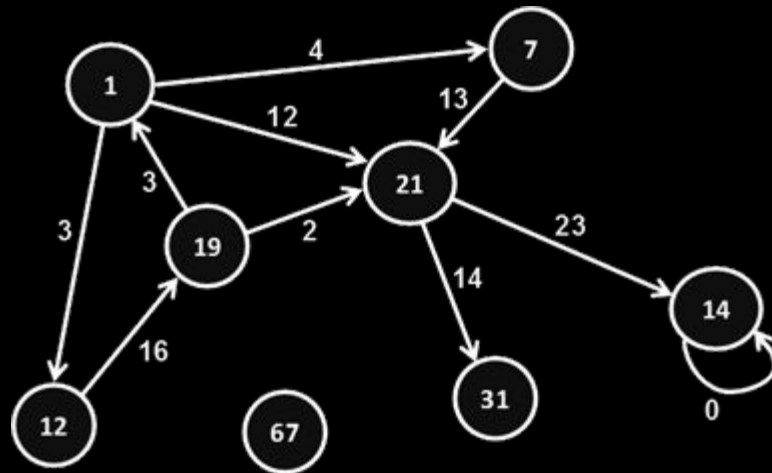
Figure 3: Neural matrix factorization model

Level 3 - Graph Neural Networks

Graph Based methods help capture **more complex relational dependencies** in the data, and have been gaining popularity since 2020

Work well for data with relational dependencies

- Social Media networks (mutual friends)
- Large Knowledge Graphs
- Citation Networks



Level 3 - Graph Neural Networks

Amazon - “Using graph neural networks to recommend related products”

- Using GNNs to model asymmetric product relationships leading to 30-160% performance improvements

Snap Inc - “Graph Neural Networks for Friend Ranking in Large-scale Social Platforms”

- Propose GNN model that uses messages, likes, & other interactions to generate higher quality user representations

Google Maps - “ETA Prediction with Graph Neural Networks in Google Maps”

- Use GNN to model connectivity of road networks to reduce inaccuracies of ETA calculations by more than 50%

We will show how to implement basic recommender systems based on the ideas covered today

1. Content-Based Filtering (KNN method)
2. Collaborative Filtering (Matrix Factorization method)
3. Neural Collaborative Filtering

Useful Resources

Datasets:

- [Recommender System Datasets](#)
- [Stanford Graph/Recommendation Datasets](#)
- [Netflix \\$1M Prize Competition Dataset](#)

Architectures:

- [Intro to Content-Based Filtering](#)
- [Intro to Collaborative Filtering](#)
- [Neural Collaborative Filtering Paper \(2017\)](#)

Future of Recommendation Systems:

- [Amazon Science: GNNs for related products](#)
- [Snap Inc: GNNs for Large Scale Friend Ranking](#)
- [Google Maps: ETA Prediction using GNNs](#)