BiostatisticsMidterm-tk2886

Problem 1

- a). Assumptions that must be true to use the Poisson Distribution to model the number of infections per month:
 - 1. Events occur one at a time; two or more events cannot occur exactly at the same time and location;
 - 2. The occurrence of an event in a given period is independent of the occurrence of an event in a non-overlapping period;
 - 3. The expected number of events during any period is constant.

b).

b) Suppose the number of infections per month follows a Poisson distribution. What is the probability that in the next month the hospital's patients will have exactly 2 unexplained infections? Include the formula and all the key steps in your calculations. (5 points)

Formula: $P(x=x) = f(x) = \frac{\lambda^x e^{-\lambda}}{x!}$, $\chi = 0, 1, 2, ..., n$ $\chi = 7$, that of unexplained infection among patients per month.

Calculate: $P(\chi=2) = \frac{7^2 e^{-7}}{2!} = 0.0223$

We may use R code to get the same value.

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prob = dpois(2, 7)
prob
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[1] 0.02234111

The probability that in the next month the hospital's patients will have exactly 2 unexplained infections is: 0.0223411.

Problem 2

Formula: Bayes Theorem

$$P(A|B_{i})P(B_{i})$$

$$P(B_{i}|A) = \frac{P(A|B_{i})P(B_{i})+P(A|B_{i})P(B_{i})}{P(A|B_{i})P(B_{i})+P(A|B_{i})P(B_{i})+\dots P(A|B_{i})P(B_{i})}$$

$$D = \text{developed CHD}$$

$$C = |A_{i}+iA| \text{ Serum cholesterol levels above 200}$$

$$P(D) = 0.25, P(D^{c}) = |-0.25 = 0.75$$

$$P(C|D) = 0.60$$

$$P(C|D) = 0.60$$

$$P(C|D^{c}) = 0.16$$
Interested in:
$$P(D^{c}|C^{c}) = \frac{P(D^{c} \cap C^{c})}{P(C^{c})} = \frac{P(C^{c}|D^{c})P(D^{c})}{P(C^{c}|D^{c})+P(C^{c}|D)P(D^{c})}$$

$$P(C^{c}|D^{c}) = |-P(C|D^{c}) = 0.84$$

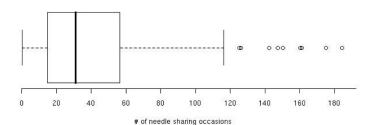
$$P(C^{c}|D) = |-P(C|D) = 0.40$$

$$\frac{(.84)(.75)}{(.84)(.75) + (.40)(.25)} = \frac{.63}{.63 + .1} = 0.8630 \approx 0.86$$

The probability that a random chosen subject will not develop CHD, given that he had an initial serum cholesterol level below or equal 200 is: **0.86**.

Problem 3

Problem 3:



Researchers from New York, studying needle sharing behavior among intravenous drug users, randomly selected 500 patients from the city's two major drug detoxification clinics. At admission, each participant reported the number of their needle sharing occasions in the last year. The researchers summarized the observed data for 'number of needle sharing occasions in the last year' in the box-plot above.

- a) [Circle only one correct answer.] Based on the box-plot of the data, the proportion of subjects whose number of needle sharing occasions is less than the sample average number of needle sharing occasions is:

 (4 points)
 - i. Less than 50%
 - ii. More than 50%
 - iii. Exactly 50%
 - iv. Exactly 100%
- b) [Circle only one correct answer.] What is the probability that the number of needle sharing occasions for a randomly selected patient from the study is smaller than the third quartile (Q3) and larger than the first quartile (Q1)? (4 points)
 - i. About 25%
 - ii. About 50%
 - iii. About 75%
 - iv. About 100%

ii.

- c) [Circle only one correct answer.] In order to report the number of needle sharing occasions per WEEK, the researchers divided all the observed data by 52 and computed new sample statistics. What is the relationship between the sample statistics for ONE WEEK and the sample statistics for ONE YEAR? (4 points)
 - i. The 'one week' mean, median and standard deviation are 52 times larger than the 'yearly' mean, median and standard deviation
 - The 'one week' mean, median and standard deviation are 52 times smaller than the 'yearly' mean, median and standard deviation
 - iii. The 'one week' mean and median are 52 times larger than the 'yearly' mean and median. The standard deviation will stay the same.
 - iv. The ' $\underline{\text{one week}}$ ' mean and median are $\overset{c}{52}$ times smaller than the ' $\underline{\text{yearly}}$ ' mean and median. The standard deviation will stay the same.

Problem 5a

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The variable we're studying in the population is normally distributed.

Placebo group => 40 subjects } n ≥ 30 / Normal /
  · Treatment group => 80 subjects in ≥ 30 / Normal V
  Test Equality of the Vapiances
Since, we have unequal variances, we will use Two Sample Independent +-test: (unequal variance)

Ho: Mp = Mn HA: Mp < My

Placeto Patch Niching Patch Patch Patch
 t = \frac{\overline{\chi_1 - \chi_2}}{\sqrt{\frac{5^2}{n_1} + \frac{5^2}{n_2}}} = \frac{0.222 - 0.125}{\sqrt{\frac{(0.241)^2}{80} + \frac{(1.226)^2}{40}}} = 0.4934
df = \frac{\left(\frac{a_{r}^{2}}{c_{r}^{2}} + \frac{a_{r}^{2}}{c_{r}^{2}}\right)^{2}}{\frac{a_{r}^{2}}{c_{r}^{2}(c_{r}-1)} + \frac{a_{r}^{2}}{c_{r}^{2}(c_{r}-1)}} = 41.2
• Round down to the nearest Integer d^{(1)}: 41
 1七1 4七111,1-受}10.49341 4 2.01954} Fail to Reject
 P-value: pt(.4934,41)=0.6878 70.05} Fail to Reject
Conclusion: We fail to reject the null hypothesis. We do not have enough evidence to reject the null hypothesis that there is no difference of plasma vicotine levels when applying nicotine patch versus applying place of place.
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Problem 5b

b) [Circle only one correct answer.] What is the proper definition of the p-value in the bove hypothesis test?

The probability of rejecting the null hypothesis, assuming that the alternative

The probability of rejecting the null hypothesis, assuming that the null hypothesis is

The probability of obtaining a test statistic as extreme or more extreme than the observed value, assuming that the <u>alternative</u> hypothesis is true. The probability of obtaining a test statistic as extreme or more extreme than the

observed value, assuming that the null hypothesis is true.