

Analytics & Machine Learning in Data Systems (Part 4)

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Taxonomy of Machine Learning

Labeled Data

Indirect
(reward)

Unlabeled Data

Supervised
Learning

Reinforcement
& Bandit
Learning

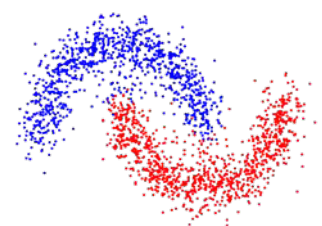
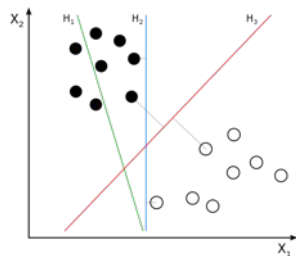
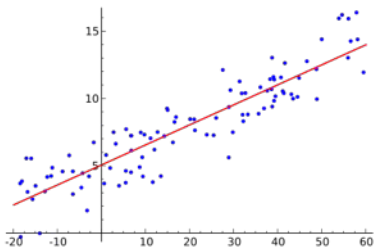
Unsupervised
Learning

Regression

Classification

Dimensionality
Reduction

Clustering




Spam Classification

- **Goal:** given the **text in an** email **predict** whether it is **spam**
- **Training Data:**

Content	Is Spam
Viagra & Cialas half-off today...	SPAM
Class is Cancelled today	NOT SPAM
Deals on new Autos	SPAM
Receipt from Ritual Coffee ...	NOT SPAM

```
def predSpam(doc):  
    if "Viagra" in doc:  
        return True  
    elif "Cialas" in doc:  
        return True  
    elif "Class" in doc:  
        return False  
    elif "Deals" in doc:  
        return True  
    else:  
        return False
```

- **First best solution?** 
 - What is wrong with this?
- **Why is Spam Classification Hard?**
 - Easy for humans to **recognize**
 - **Difficult** to formally describe (as an algorithm)
 - **Personal:** different people have different tastes in Spam
 - Good candidate for Machine Learning, the second best solution

Spam Classification

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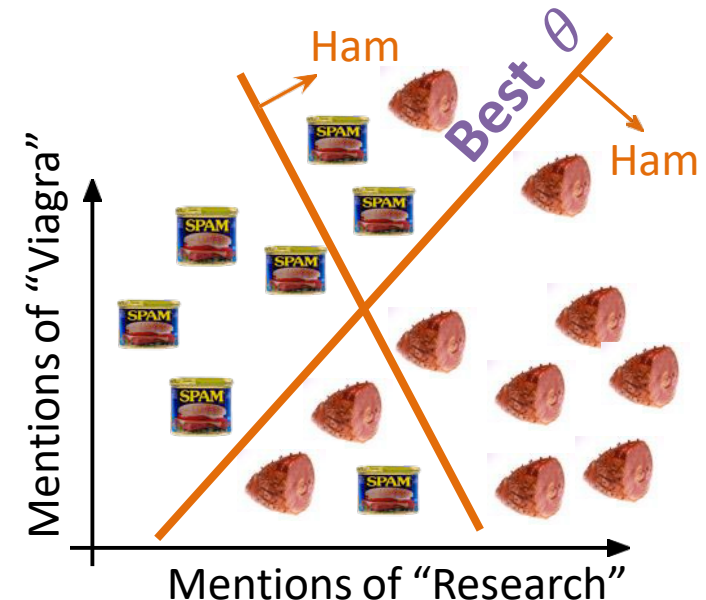
- **Machine Learning:**

- Learn a function that generalizes the relation:

$$\mathbf{F}(\text{Content}; \theta) \rightarrow \text{isSpam}$$

- \mathbf{F} : is the model type
- θ : are the model parameters

- Machine learning alg. search for the “best” θ



Basic Classification Models

- Most models predict the probability
 - Why would probability be helpful?
- **Logistic Regression:** *widely used*
 - Similar to least squares regression but for classification

- **Model form:**

$$\mathbf{P}(\text{isSpam} \mid \text{Words})$$

- **Naïve Bayes:** *occasionally used*
 - Classic model based on Bayes Rule
 - assumes words are independent given
 - **Model form:**

$$\mathbf{P}(\text{isSpam} \mid \text{Words}) \propto \mathbf{P}(\text{isSpam}) \prod_{\text{Words}} \mathbf{P}(\text{Word} \mid \text{isSpam})$$

- Which should I use?
 - try both ...

Common Classification Models

- Most models predict the probability
 - Why would probability be helpful?
- **Nearest Neighbor:** *works embarrassingly well*
 - return the label of the nearest training point to the query point
- **Logistic Regression:** *widely used and simple*
 - Similar to least squares regression but for classification
- **Naïve Bayes:** *occasionally used*
 - Classic model based on Bayes Rule
- **Support Vector Machines:** *kernel methods*
 - Capable of automatically growing model size with data
- **Deep Learning:** *more on this soon ...*

Logistic Regression

□ Basic Model:

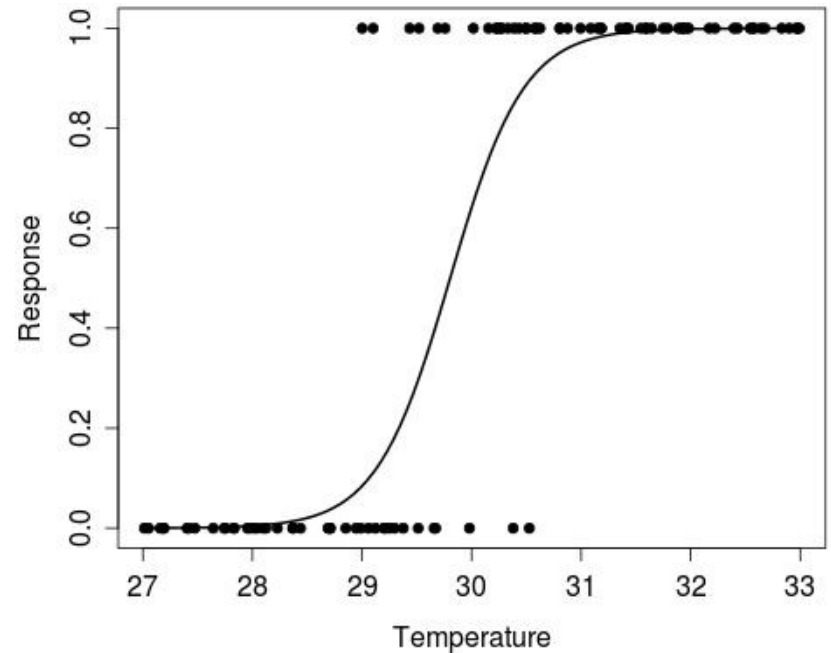
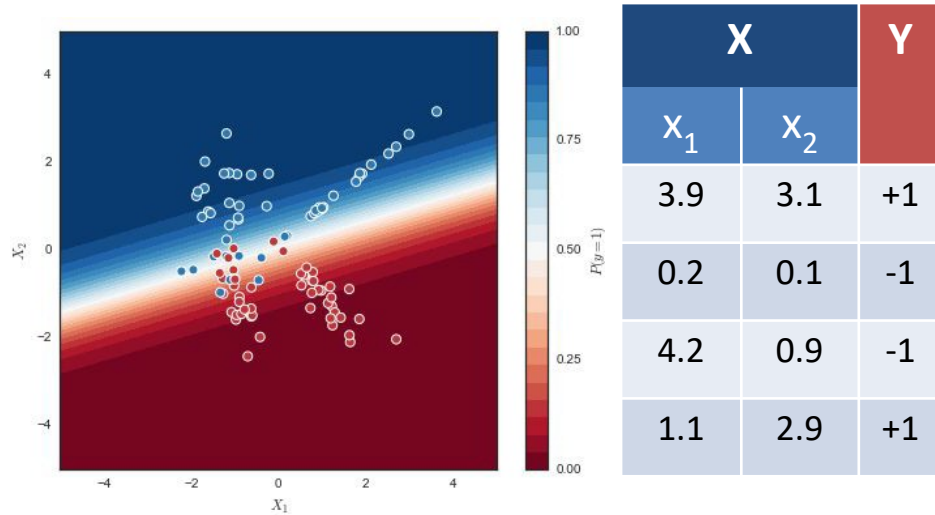
$$\mathbf{P}(y|x, \theta) = \frac{\sigma(y(\theta^T x))}{1 + \exp(-y(\theta^T x))}$$

$$= \frac{1}{1 + \exp(-y(\theta^T x))}$$

Note that y is either +1 or -1

□ Logistic Function:

$$\sigma(z) = \frac{1}{1 + \exp(-z)}$$



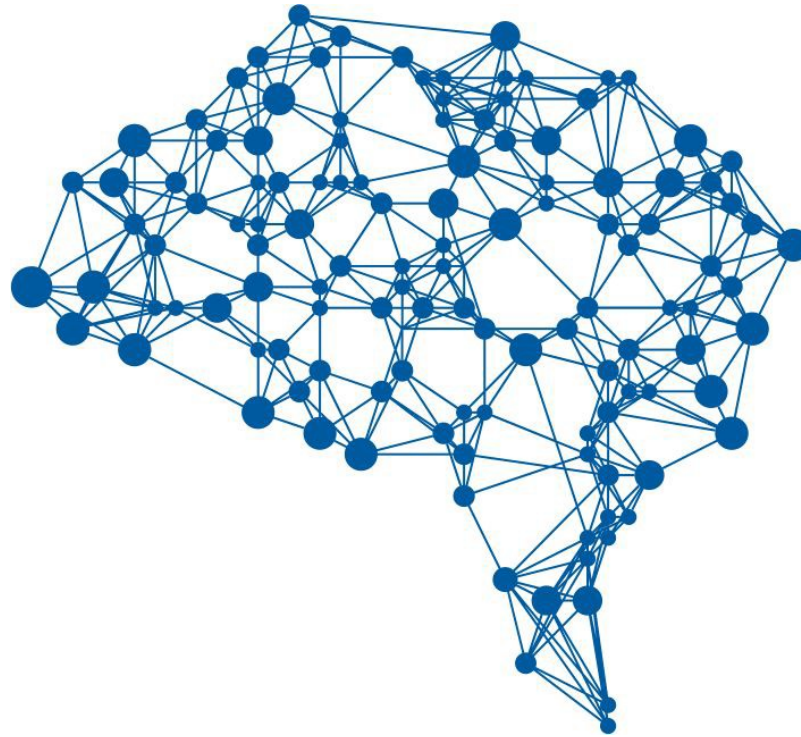
Learning the Logistic Regression Model

- How do we fit the Logistic Regression model?
 - method of maximum likelihood
- Select the best θ by maximizing prob. of data
 - Solve the following **convex** optimization problem

$$\hat{\theta} = \arg \min_{\theta \in \mathbb{R}^p} \quad \frac{1}{n} \sum_{i=1}^n \log (1 + \exp (-y_i(\theta^T x_i))) + \lambda R(\theta)$$

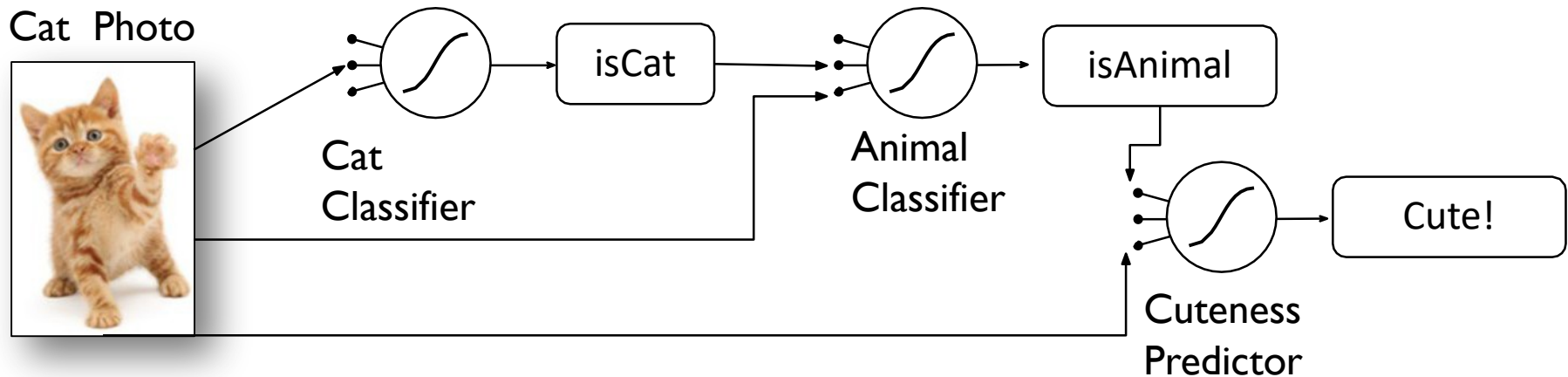
- Regularized using same techniques as regression
- Optimized using numerical methods
 - **SGD**: Stochastic Gradient Descent

Deep Learning



Intuition

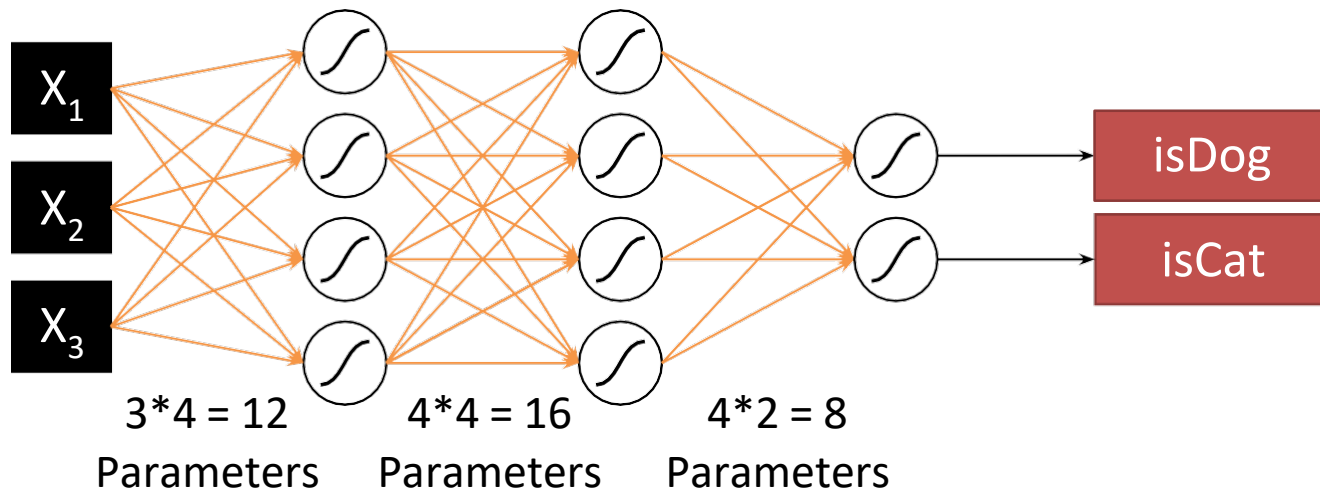
□ Model Composition



- Predictions from one model → features for another
- Why not train the entire pipeline of models?

Going a Little Deeper

- **Basic idea:** stacking **logistic regression** models

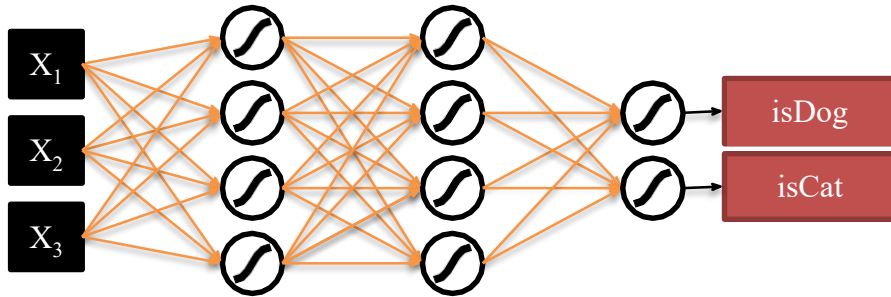
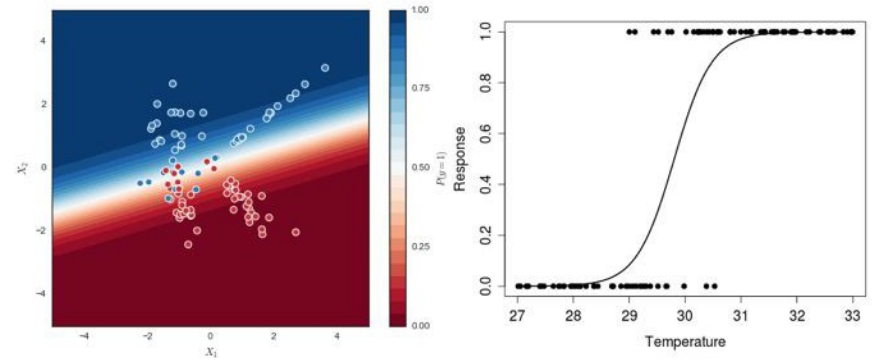
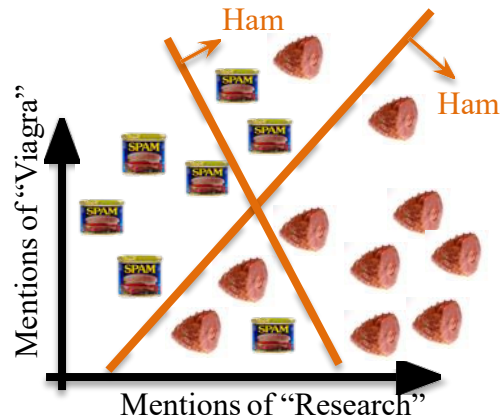


- Many parameters θ (36 in the above model)
 - millions of parameters fits complex functions
 - Requires substantial training data to prevent over-fitting
- Tricky & slow to train
 - Specialized training algorithms and GPU acceleration

Deep Learning the Big Shift in ML

- Recent **big** trend in machine learning
- State of the art results in
 - **Computer Vision**: exceeding human abilities
 - **Speech Recognition**: at the core of all commercial speech recognition systems
 - **AI + Search**: Google's AlphaGo
- Companies investing heavily in Deep Learning:
 - Facebook, Google, Baidu, Nvidia, & Intel have very large Deep Learning groups
 - New software and hardware
- **Hype**: Still requires substantial amounts of data and expertise to train and deploy ...
 - Many applications still use other techniques
 - AI winter is coming ...?

Summary of Classification:



Big
Data





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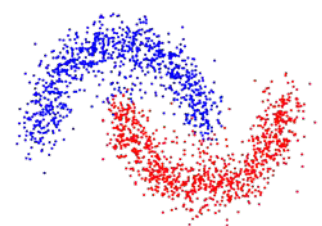
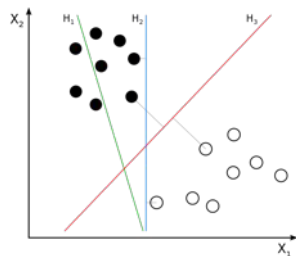
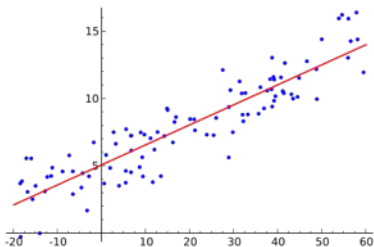
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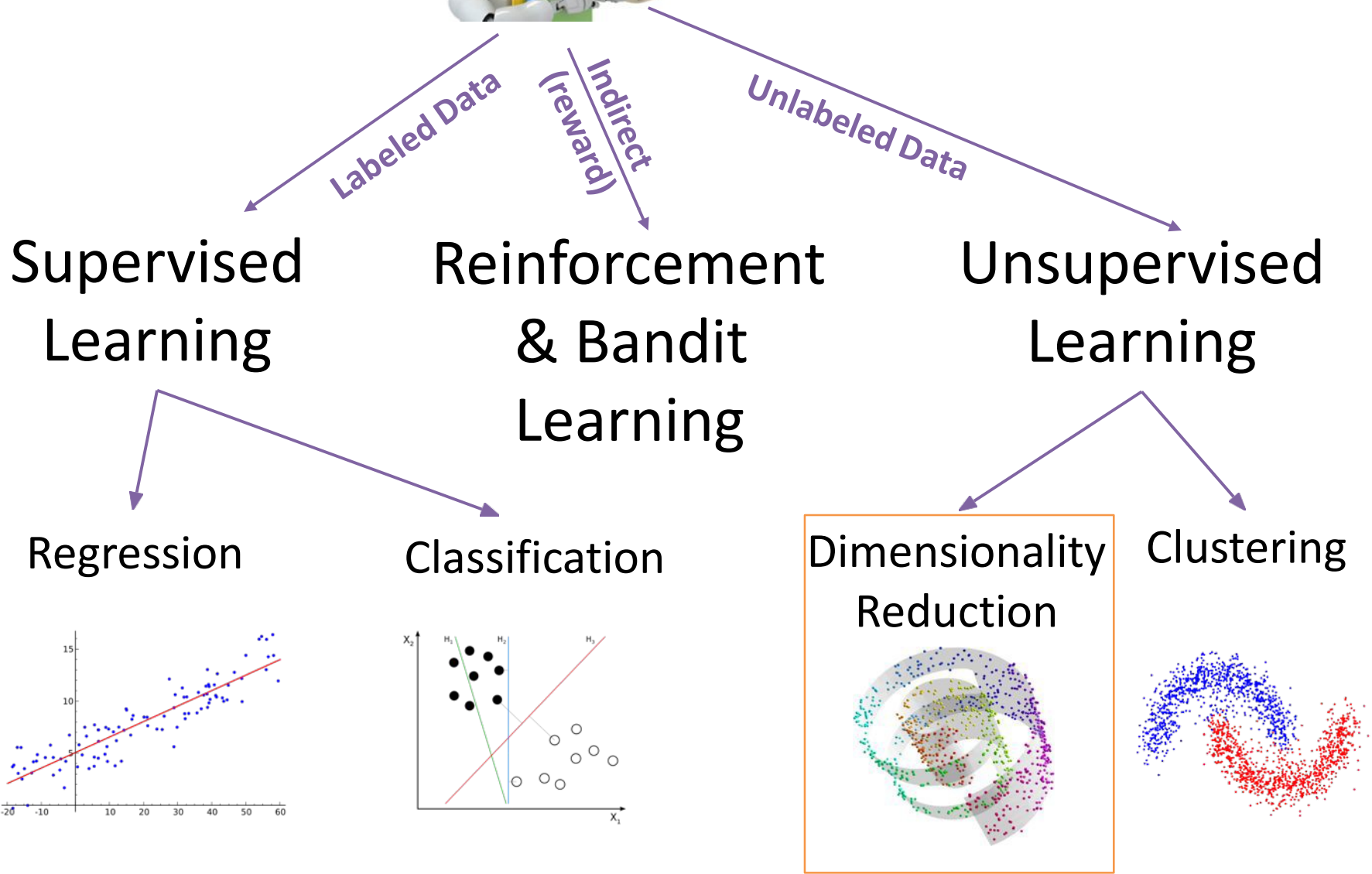
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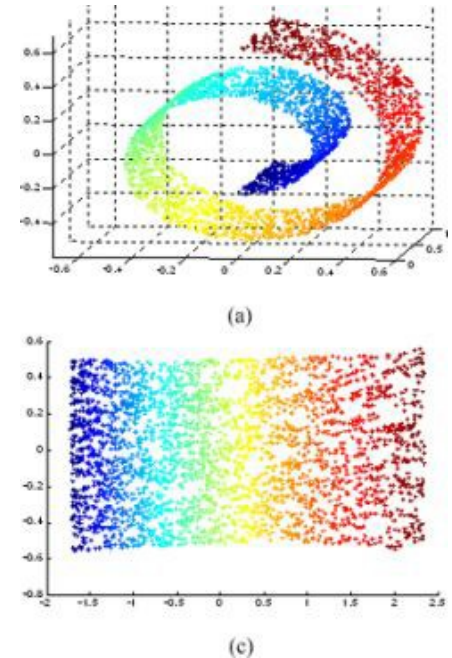
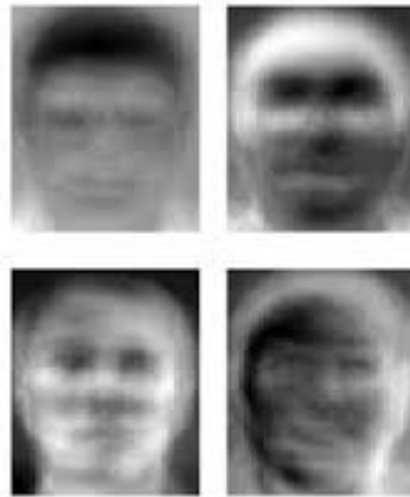
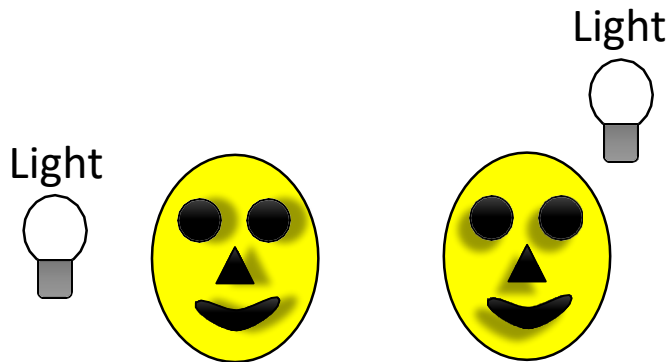


Taxonomy of Machine Learning



Dimensionality Reduction: Eigen Faces

Given images under different lighting construct images under any light lighting



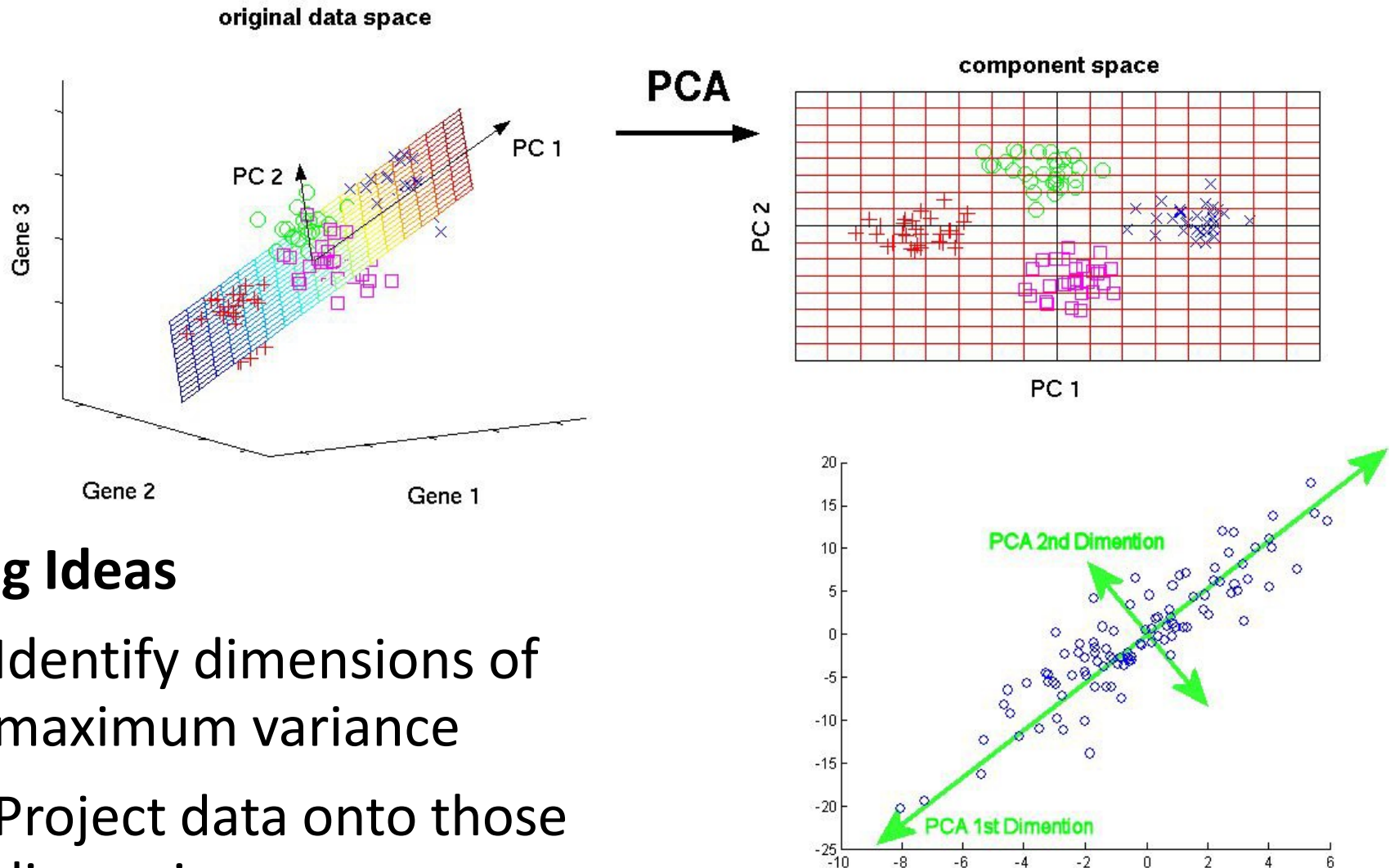
□ Machine Learning Approach:

$$\text{Embedding}(\text{Image}; \theta) \rightarrow \{x_1, x_2, x_3, x_4\}$$

$$\text{Recovery}(\{x_1, x_2, x_3, x_4\}; \theta) \rightarrow \text{Reconstructed Image}$$

□ Use common structure in data to identify embedding

Principal Component Analysis



Big Ideas

- ❑ Identify dimensions of maximum variance
- ❑ Project data onto those dimensions

Scaling Principal Component Analysis

□ PCA Algorithm

- Computes eigenvectors of covariance matrix

$$\mathbf{Cov}(X) = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(x_i - \bar{x})^T = \frac{1}{n} X^T X - \bar{x} \bar{x}^T$$

- The covariance matrix $d \times d$ is generally smaller than X ($n \times d$)
 - For high dimensional data consider dist. Lanczos ...

□ We therefore only need to compute:

$$X^T X = \begin{matrix} d & \boxed{\times} & n \end{matrix} \begin{matrix} d \\ \boxed{X} \\ n \end{matrix} = \begin{matrix} d \\ \boxed{X^T X} & d \end{matrix} = \sum_{i=1}^n x_i x_i^T$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i = \begin{matrix} | & d \end{matrix}$$

- In summation form
- Only one pass required!

PCA for Anomaly Detection

- Run PCA and get top k eigenvectors: $V_{(k)}$

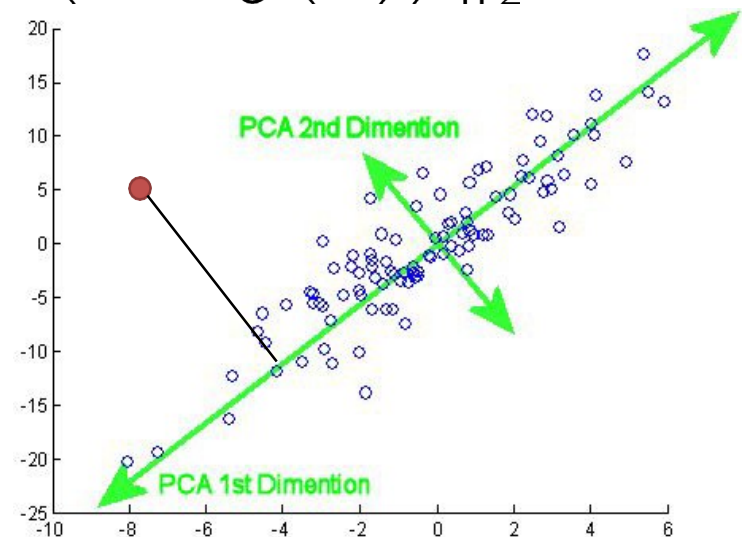
$$\mathbf{Proj}(x) = V_{(k)}^T (x - \bar{x})$$

$$\mathbf{Recv}(q) = V_{(k)} q + \bar{x}$$

- Compute the error in approximate recovery:

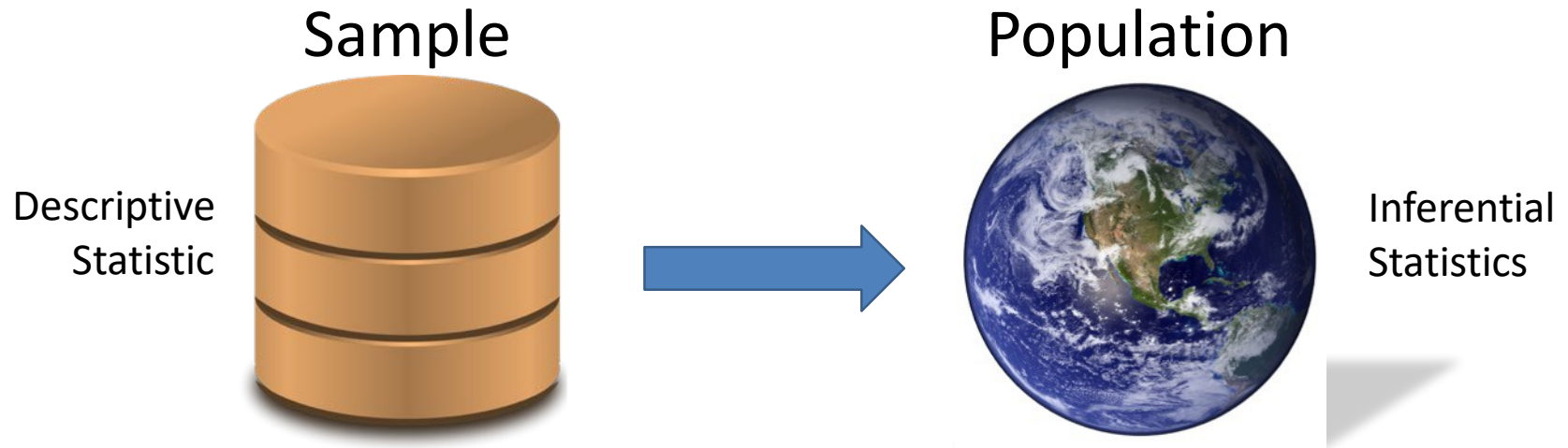
$$\mathbf{Error}(x) = \|x - \mathbf{Recv}(\mathbf{Proj}(x))\|_2^2$$

- Outliers are those points far from their embedding



Knowledge Discovery in Databases (KDD)

- Process of extracting ***knowledge*** from a ***data***



- **Descriptive Statistics:** *describe* the sample data
 - Can be **measured directly** from the database
- **Inferential Statistics:** *estimate* the population
 - May be **estimated** using descriptive statistics

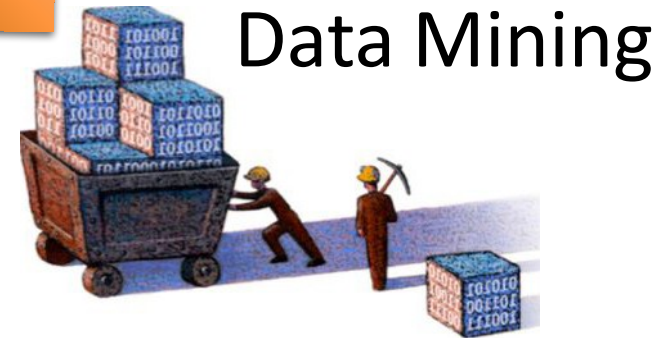
The Knowledge Discovery Process

- **Data Selection:** *What data do I need for a given task?*
 - If data was already collected, how was the data collected?

- **Data Cleaning:** *Preparing the data for a given task*
 - Typically most challenging (time consuming) part.
 - Why might ETL not be enough?

- **Data Mining & ML:** *Running algorithms to infer patterns*
 - The fun part! Many tools, many options, complex tradeoffs.

- **Evaluation:** *Verifying that patterns are significant*
 - Algorithms will typically find patterns especially when none exist.



Data Mining



Machine Learning