

Rigidity of Expectations: Additional Evidence from Density Forecasts of Professionals and Households

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April 1, 2020

Outline

1 Motivation

2 Theory

3 Estimation

- AR(1)
 - SE
 - DE
 - NI
- Stochastic volatility
 - SE
 - DE
 - NI

4 Conclusion

Motivation

- there are various theories on “irrational expectation”
- different theories can be tested using survey data in a comparable manner (Coibion and Gorodnichenko (2012))
- a good theory needs to be (relatively) consistent in predictions across different moments
- higher moments, i.e. uncertainty, brings about one more restriction
- survey also contains information about data generating process itself

What this paper does

- ① time series and cross-sectional pattern of **uncertainty** from **density** forecasts of the inflation
- ② additional reduced-form tests of the full-information rationality null using the uncertainty
- ③ extend Coibion and Gorodnichenko (2012) in two ways
 - ▶ cross-moment estimation for each one of the particular theories on expectation
 - ▶ allowing for stochastic volatility of inflation process

- empirical tests on expectation formation
 - ▶ Mankiw et al. (2003), Carroll (2003), Branch (2004), Malmendier and Nagel (2015), Das et al. (2017), Coibion and Gorodnichenko (2012), Fuhrer (2018)
- density and probabilistic questions in expectation surveys
 - ▶ Manski (2004), Delavande et al. (2011), Manski (2018)
 - ▶ Bertrand and Mullainathan (2001), Van der Klaauw et al. (2008), Delavande (2014)
- different measures of uncertainty
 - ▶ Bachmann et al. (2013), Jurado et al. (2015), Binder (2017), Bloom (2009)

A generic framework

h -period ahead density forecast by agent i at time t based on information set $I_{i,t}$

$$f_{i,t+h|t} \equiv f_{i,t}(y_{t+h}|I_{i,t})$$

- theories of expectation differ in $I_{i,t}$
 - ▶ rational expectation (FIRE): $I_{i,t} = y_{i,t}$
 - ▶ sticky expectation (SE): $I_{i,t} = y_{t-\tau}$, τ being the most recent update date
 - ▶ noisy information (NI): $I_{i,t} = s_{i,t}(y_t)$, where $s_{i,t}$ is a vector of noisy signal(s)
- the process of variable determines the mapping from $I_{i,t}$ to $f_{i,t+h|t}$

Definition and notation

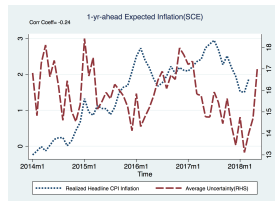
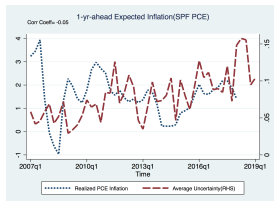
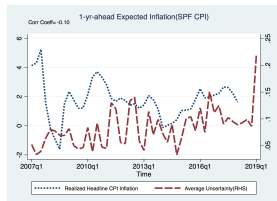
| Individual moments | Population moments |
|--------------------------------|--|
| Mean forecast: $y_{i,t+h t}$ | Average forecast: $\bar{y}_{t+h t}$ |
| Forecast error: $FE_{i,t+h t}$ | Average forecast error: $\overline{FE}_{t+h t}$ |
| Uncertainty: $Var_{i,t+h t}$ | Average uncertainty: $\overline{Var}_{t+h t}$ |
| | Disagreement: $\overline{Disg}_{t+h t}$ |

Data

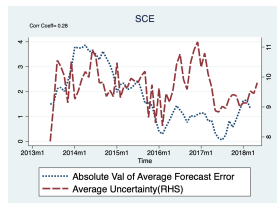
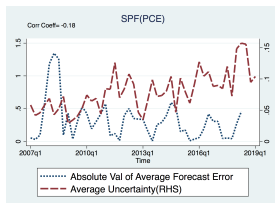
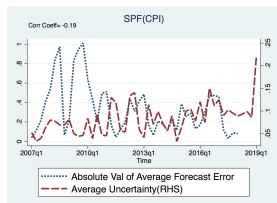
| | SCE | SPF |
|--------------------------|------------------------|-------------------------------------|
| Time period | 2013M6-2018M6 | 2007Q1-2018Q4 |
| Frequency | Monthly | Quarterly |
| Sample Size | 1,300 | 30-50 |
| Aggregate Var in Density | 1-yr-ahead inflation | 1-yr and 3-yr core CPI and core PCE |
| Pannel Structure | stay up to 12 months | average stay for 5 years |
| Demographic Info | Education, Income, Age | Industry |

- density estimation following (Engelberg et al. (2009))
- exclude top and bottom 5% values for forecast errors and uncertainty

Basic patterns: uncertainty and realized inflation

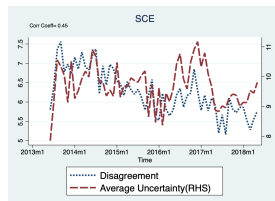
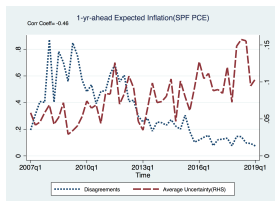
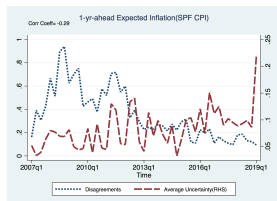


Basic patterns: uncertainty and the size of forecast errors



- no evidence for positive correlation between high ex ante uncertainty and ex post forecast errors.

Basic patterns: uncertainty and disagreement



- uncertainty are not the same as disagreement for professionals

Basic patterns: summary

- uncertainty varies across time
- uncertainty contains different information from widely proxies such as disagreement and forecast error

AR(1) model of inflation

- **Inflation process**

$$y_t = \rho y_{t-1} + \omega_t$$

$$\omega_t \sim N(0, \sigma_\omega^2)$$

- **Uncertainty**

- ▶ FIRE: time-invariant

$$\overline{Var}_{t+h|t}^* = \sum_{s=1}^h \rho^{2s} \sigma_\omega^2$$

- ▶ SE: time-invariant

$$\overline{Var}_{t+h|t}^{se} = \sum_{\tau=0}^{+\infty} \lambda(1-\lambda)^\tau \overline{Var}_{t+h|t-\tau}^*$$

- ▶ NI: time-variant but quantitatively tiny due to highly efficient Kalman gain

$$\overline{Var}_{t+h|t}^{ni} = \rho^{2h} \overline{Var}_{t|t}^{ni} + \overline{Var}_{t+h|t}^*$$

Stochastic volatility (UCSV) inflation process (Stock and Watson (2007))

- **Inflation process**

$$y_t = \theta_t + \eta_t, \quad \text{where } \eta_t = \sigma_{\eta,t} \xi_{\eta,t}$$

$$\theta_t = \theta_{t-1} + \epsilon_t, \quad \text{where } \epsilon_t = \sigma_{\epsilon,t} \xi_{\epsilon,t}$$

$$\log \sigma_{\eta,t}^2 = \log \sigma_{\eta,t-1}^2 + \mu_{\eta,t}$$

$$\log \sigma_{\epsilon,t}^2 = \log \sigma_{\epsilon,t-1}^2 + \mu_{\epsilon,t}$$

$$\xi_t = [\xi_{\eta,t}, \xi_{\epsilon,t}] \sim N(0, I_2)$$

$$\mu_t = [\mu_{\eta,t}, \mu_{\epsilon,t}]' \sim N(0, \gamma I_2)$$

UCSV inflation process

- **Uncertainty**

- ▶ FIRE: time-varying

$$\overline{Var}_{t+h|t}^* = \sum_{k=1}^h \exp^{-0.5k\gamma_{\eta}} \sigma_{\eta,t}^2 + \exp^{-0.5h\gamma_{\epsilon}} \sigma_{\epsilon,t}^2$$

- ▶ SE: time-varying

$$\overline{Var}_{t+h|t}^{se} = \sum_{\tau=0}^{\infty} (1 - \lambda)^{\tau} \lambda \overline{Var}_{t+h|t-\tau}^*$$

- ▶ NI (1-step-ahead): time-varying

$$\overline{Var}_{t|t-1}^{\theta} = \overline{Var}_{t-1|t-1}^{\theta} + \overline{Var}_{t|t-1}^*(y_t)$$

Simulated method of moment estimation

$$\hat{\Omega} = \underset{\{\Omega \in \Gamma\}}{\operatorname{argmin}} (M_{\text{data}} - F^o(\Omega, Y))' W (M_{\text{data}} - F^o(\Omega, Y))'$$

- Ω : parameters of the particular $o \in \{fire, se, ni, de, seni\} \times \{ar, sv\}$
- Γ : constraints for the parameter.
- M_{data} : data moments
- F : simulated model moments according to a particular theory o , a function of parameters Ω as well as the Y , the real-time data (including history) up till each point of the time t .
 - ▶ unconditional moments, not specific to time
 - ▶ moments selected from average forecast, variance and autocovariance of forecasts, average disagreement, variance and autocovariance of disagreement, average uncertainty, etc.
- W : weight matrix, identity matrix for now

Estimation procedure and algorithm

- 1 for each theory of expectation formation and the inflation process, start with an initial value for the parameter(s) of interest
- 2 simulate individual forecasts for a large enough ($N = 200$) number of forecasters
- 3 compute the average forecast errors, disagreement and average uncertainty across all agents
- 4 compute the time-series moments of the average forecast, disagreement, and uncertainty
- 5 compute the difference between the simulated moments and the data moments
- 6 keep searching the parameter value until reaching below a threshold of the loss

Two-step and joint estimation

- ① two-step estimation: separately estimate inflation process parameters and then parameters of the inflation process
 - ▶ pros: computationally lighter
 - ▶ cons: potential misspecification. does not utilize the expectation data to understand inflation process per se.
- ② joint estimation: targeting both moments of realized inflation series and moments of forecasts to simultaneously estimate both the inflation process and the parameter of expectation formation
 - ▶ pros: additional information gain from expectations data about inflation process itself
 - ▶ cons: more computation burden

Scoring card for a theory of expectation formation

To look if the parameter and goodness of fit is robust to

- ① use of different moments in estimation
- ② alternative assumption about the underlying process
- ③ two-step estimation or joint-estimation
- ④ relatively fit with professionals and households

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SE parameter estimate

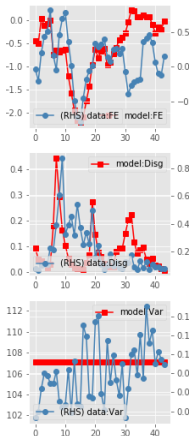
Table: SMM Estimates of SE

| 0 | 1 | 2 | 3 | | SE: $\hat{\lambda}_{SPF}(Q)$ | SE: $\hat{\lambda}_{SPF}(Q)$ | SE: ρ | SE: σ | SE: $\hat{\lambda}_{SCE}(M)$ | SE: $\hat{\lambda}_{SCE}(M)$ | SE: ρ | SE: σ |
|-------|---------|---------|---------|-----|------------------------------|------------------------------|------------|--------------|------------------------------|------------------------------|------------|--------------|
| FEVar | FEATV | | | | 0.47 | 0.36 | 1 | 0.08 | 0.2 | 0.5 | 0.84 | 0.25 |
| FEVar | DisgATV | DisgVar | | | 0.47 | 0.38 | 1 | 0.1 | 0.21 | 0.54 | 0.92 | 0.18 |
| FEVar | FEATV | DisgVar | DisgATV | Var | 0.47 | 0.36 | 1 | 0.08 | 0.21 | 0.5 | 0.84 | 0.25 |

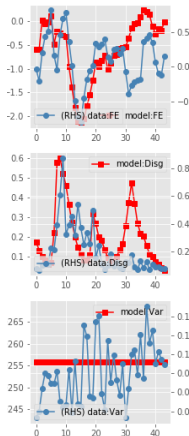
- λ : update rate in SE

Professionals and SEAR

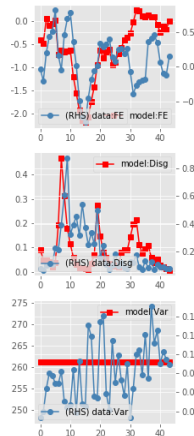
(a) FE



(b) Disg

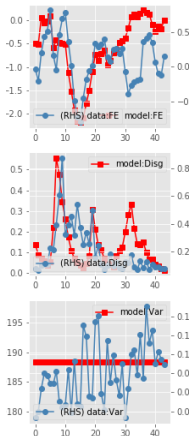


(c) FE/Disg

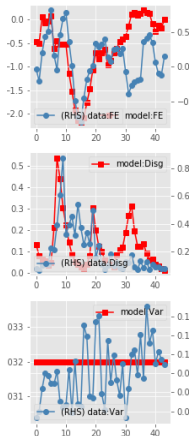


Professionals and SEAR: joint estimation

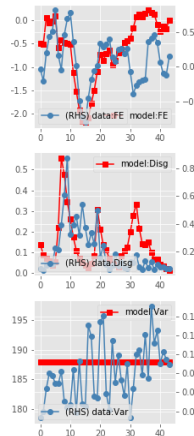
(a) FE



(b) Disg

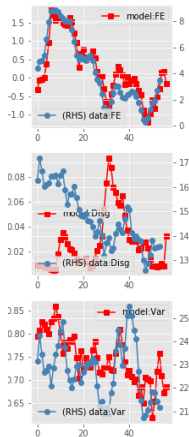


(c) FE/Disg

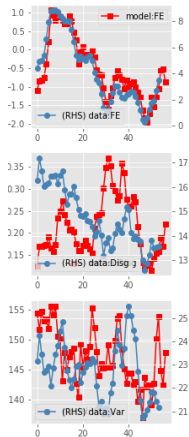


Households and SEAR

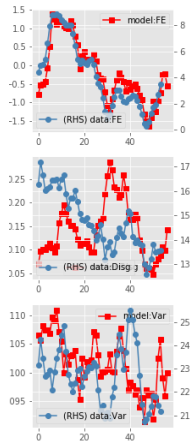
(a) FE



(b) Disg

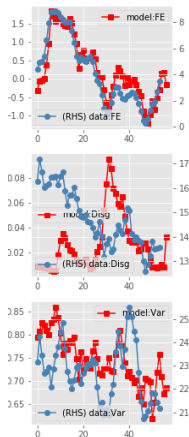


(c) FE/Disg

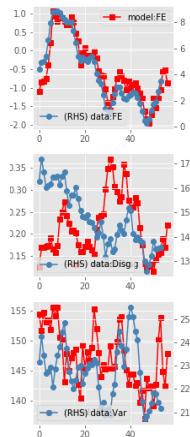


Households and SEAR: joint estimates

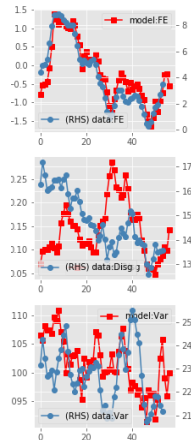
(a) FE



(b) Disg



(c) FE/Disg



DE parameter estimate

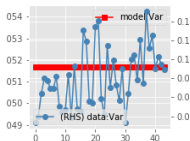
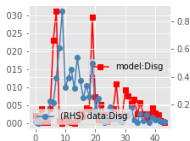
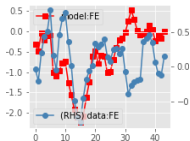
Table: SMM Estimates of DE

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | DE: θ_{SPF} | DE: $\sigma_{\theta, SPF}$ | DE: θ_{SPE} | DE: $\sigma_{\theta, SPE}$ | DE: ρ | DE: σ | DE: θ_{SCE} | DE: $\sigma_{\theta, SCE}$ | DE: θ_{SCE} | DE: $\sigma_{\theta, SCE}$ | DE: ρ | DE: σ |
|----|-------|-------|------|---------|---------|-----|--------------------|----------------------------|--------------------|----------------------------|------------|--------------|--------------------|----------------------------|--------------------|----------------------------|------------|--------------|
| FE | FEVar | FEATV | | | | | -0.23 | 0.22 | NA | NA | NA | NA | 9.35 | 10.65 | 0.82 | 0.85 | 1 | 0 |
| FE | FEVar | FEATV | Disg | DisgVar | DisgATV | | -0.26 | 1.41 | -0.14 | 1.44 | 0.99 | 0.16 | 8.2 | 9.52 | 4.79 | 4.59 | 0.58 | 0.55 |
| FE | FEVar | FEATV | Disg | DisgVar | DisgATV | Var | -0.24 | 1.43 | -0.17 | 1.44 | 0.99 | 0.16 | 4.78 | 3.01 | NA | NA | NA | NA |

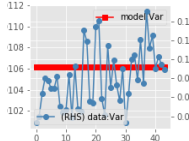
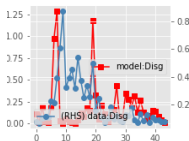
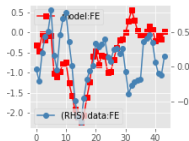
- θ : representativeness parameter, $\theta > 0$ according to DE.
- σ_{θ} : dispersion of representativeness across population

Professionals and DEAR

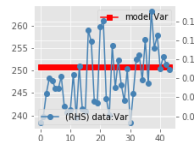
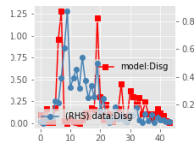
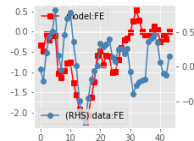
(a) FE



(b) Disg



(c) FE/Disg



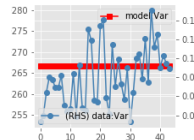
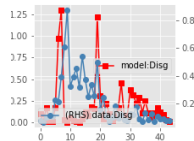
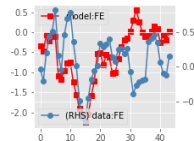
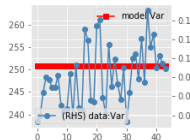
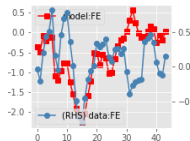
Professionals and DEAR: joint estimate

(a) FE

(b) Disg

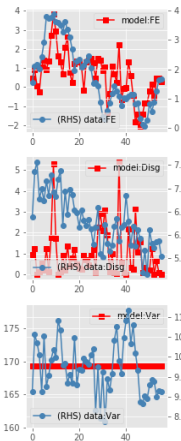
(c) FE/Disg

figuresDraft/spf_de_est.png

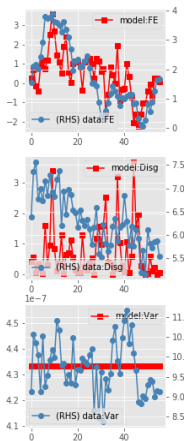


Households and DEAR

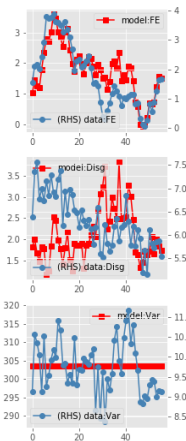
(a) FE



(b) FE/Disg

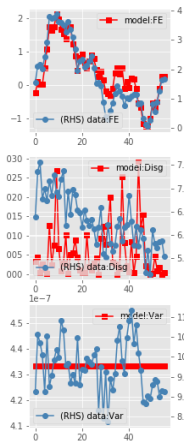


(c) FE/Disg/Var

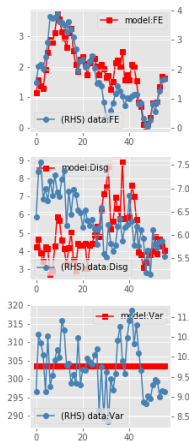


Households and DEAR: joint estimates

(a) FE



(b) FE/Disg



(c) FE/Disg/Var

figuresDraft/

NIAR parameters

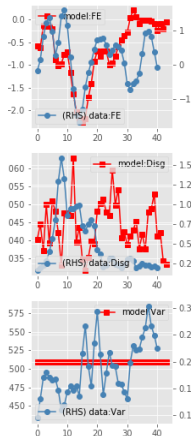
Table: SMM Estimates of NI

| 0 | 1 | 2 | 3 | 4 | NI: $\hat{\sigma}_{pb,SPF}$ | $\hat{\sigma}_{pr,SPF}$ | NI: $\hat{\sigma}_{pb,SPF}$ | $\hat{\sigma}_{pr,SPF}$ | NI: ρ | NI: σ | NI: $\hat{\sigma}_{pb,SCE}$ | $\hat{\sigma}_{pr,SCE}$ | NI: $\hat{\sigma}_{pb,SCE}$ | $\hat{\sigma}_{pr,SCE}$ | NI: ρ | NI: σ |
|-------|-------|---------|---------|-----|-----------------------------|-------------------------|-----------------------------|-------------------------|------------|--------------|-----------------------------|-------------------------|-----------------------------|-------------------------|------------|--------------|
| FEVar | FEATV | | | | 0.09 | 2.77 | 0.093 | 1.408 | 0.911 | 0.422 | 3.4 | 15.4 | 3.397 | 15.395 | 0.997 | 0.027 |
| FEVar | FEATV | DisgVar | DisgATV | | 0.09 | 2.77 | 0.093 | 1.408 | 0.911 | 0.422 | 3.4 | 15.4 | 3.397 | 15.395 | 0.997 | 0.027 |
| FEVar | FEATV | DisgVar | DisgATV | Var | 0.14 | 3.85 | 0.133 | 1.359 | 0.911 | 0.422 | 4.9 | 22.4 | 4.860 | 22.367 | 0.997 | 0.027 |

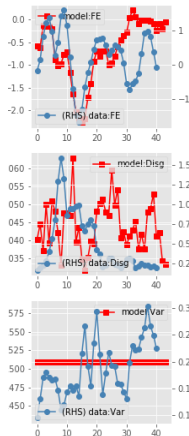
- σ_{pb} : noisiness of public signals in NI
- σ_{pr} : noisiness of private signals in NI

Professionals and NIAR

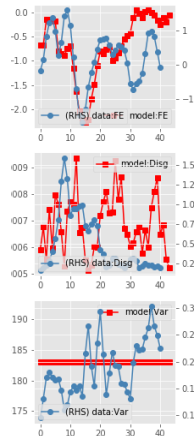
(a) FE



(b) Disg

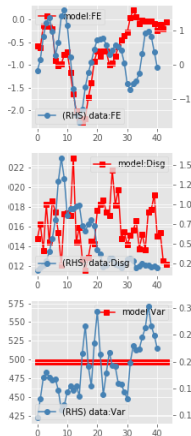


(c) FE/Disg/Var

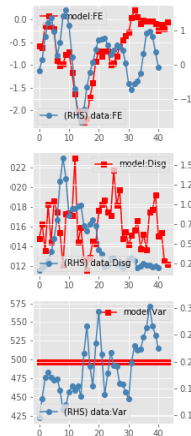


Professionals and NIAR: joint estimates

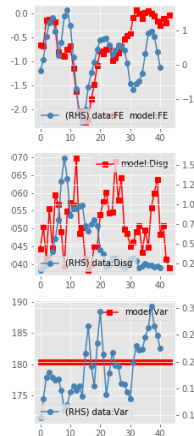
(a) FE



(b) Disg

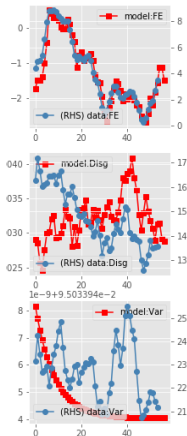


(c) FE/Disg

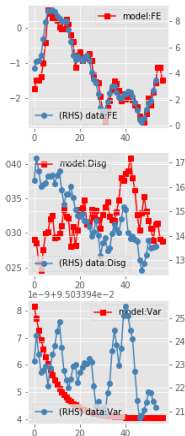


Households and NIAR

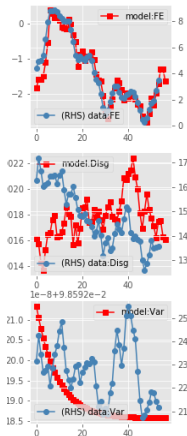
(a) FE



(b) FE/Disg

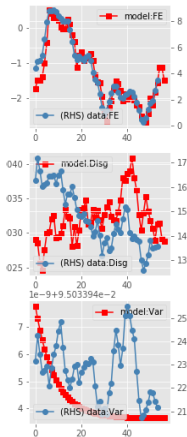


(c) FE/Disg/Var

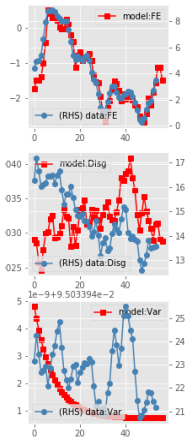


Households and NIAR: joint estimates

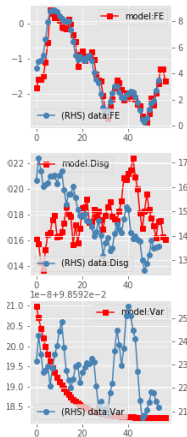
(a) FE



(b) FE/Disg



(c) FE/Disg/Var



Outline

1 Motivation

2 Theory

3 Estimation

- AR(1)
 - SE
 - DE
 - NI
- Stochastic volatility
 - SE
 - DE
 - NI

4 Conclusion

SESV parameters

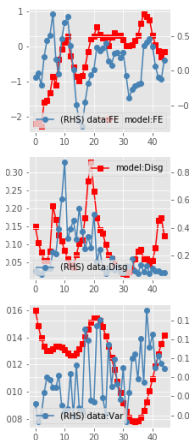
Table: SMM Estimates of Parameters of SESV

| 0 | 1 | 2 | 3 | SE: $\hat{\lambda}_{SPF}(Q)$ | SE: $\hat{\lambda}_{SPF}(Q)$ | SE: γ | SE: $\hat{\lambda}_{SCE}(M)$ | SE: $\hat{\lambda}_{SCE}(M)$ | SE: γ |
|---------|---------|---------|-----|------------------------------|------------------------------|--------------|------------------------------|------------------------------|--------------|
| DisgATV | Var | | | 0.3 | 0.46 | 2.52 | 0.09 | 0.09 | 0.7 |
| FEATV | DisgVar | DisgATV | | 0.3 | 0.46 | 2.53 | 0.07 | 0.07 | 0.26 |
| FEATV | DisgVar | DisgATV | Var | 0.3 | 0.46 | 1.26 | 0.07 | 0.07 | 0.26 |

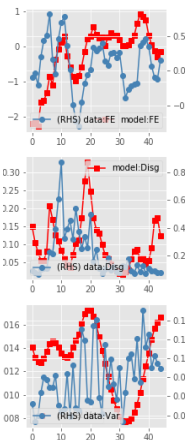
- λ : update rate in SE
- γ : size of the innovation to volatility

Professionals and SESV

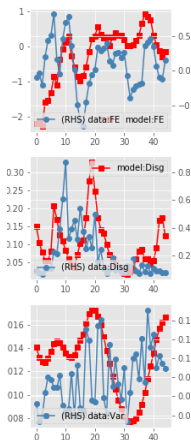
(a) FE



(b) Disg

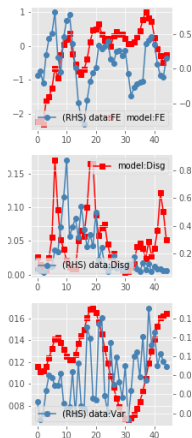


(c) FE/Disg

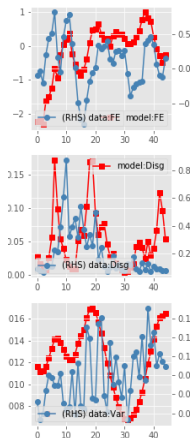


Professionals and SESV: joint estimates

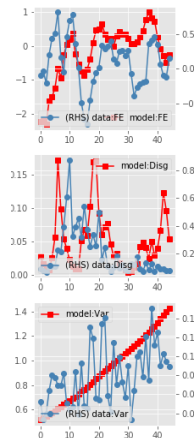
(a) FE



(b) Disg

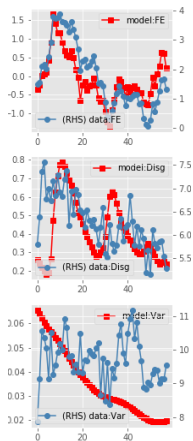


(c) Disg

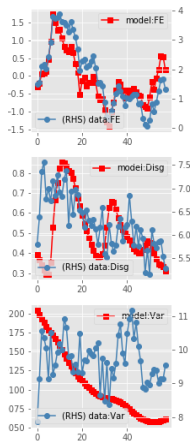


Households and SESV

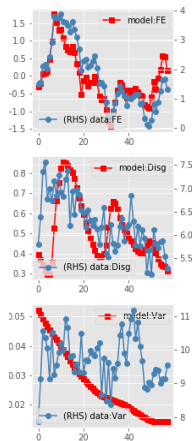
(a) Disg/Var



(b) FE/Disg

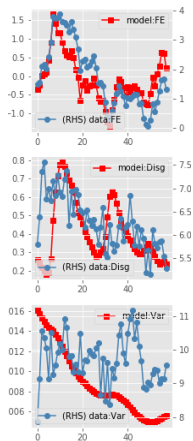


(c) FE/Disg/Var

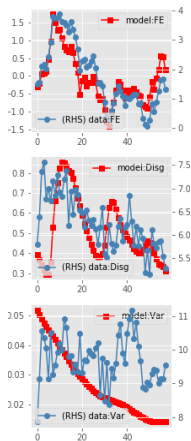


Households and SESV: joint estimates

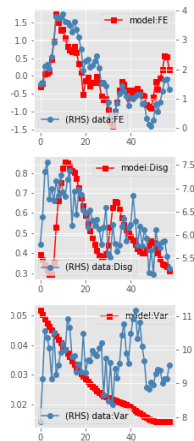
(a) Disg/Var



(b) FE/Disg



(c) FE/Disg/Var



DESV parameters

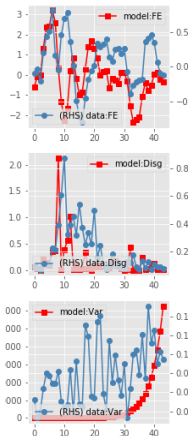
Table: SMM Estimates of Parameters of DESV

| 0 | 1 | 2 | 3 | 4 | DE: θ | σ_θ | DE: θ | σ_θ | γ | DE: θ | σ_θ | DE: θ | σ_θ | γ |
|-------|-------|---------|---------|-----|--------------|-----------------|--------------|-----------------|----------|--------------|-----------------|--------------|-----------------|----------|
| FE | FEVar | FEATV | | | -0.44 | 0.36 | -0.43 | 1.03 | 0.13 | 7.81 | 4.39 | 7.81 | 2.99 | 0.7 |
| FEVar | FEATV | DisgVar | DisgATV | | -0.44 | 0.27 | -0.44 | 0.27 | 0.3 | 7.64 | 6.46 | 7.64 | 6.46 | 0.7 |
| FEVar | FEATV | DisgVar | DisgATV | Var | -0.43 | 0.26 | -0.43 | 0.26 | 0.14 | 1.03 | 0 | 1.03 | 0 | 0.2 |

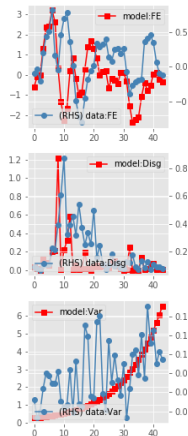
- θ : representativeness parameter
- σ_θ : dispersion of representativeness across population
- γ : size of the innovation to volatility

Professionals and DESV

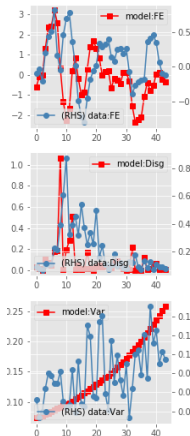
(a) FE



(b) FE/Disg

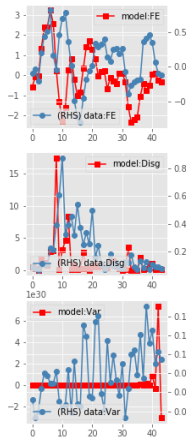


(c) FE/Disg/Var

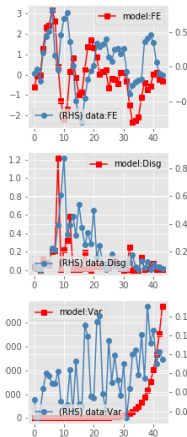


Professionals and DESV: joint estimates

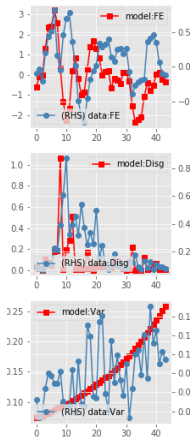
(a) FE



(b) FE/Disg

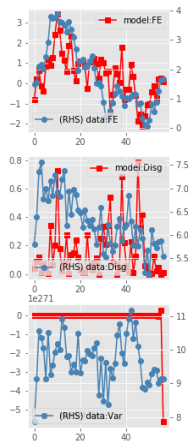


(c) FE/Disg/Var

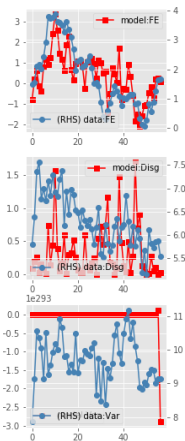


Households and DESV

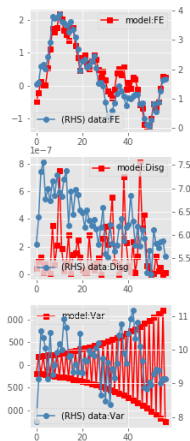
(a) FE



(b) FE/Disg

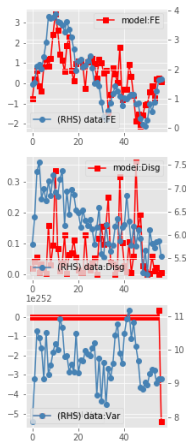


(c) FE/Disg

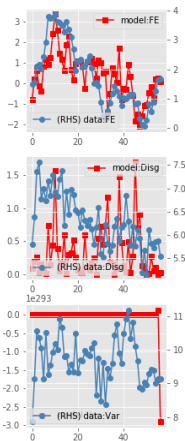


Households and DESV: joint estimates

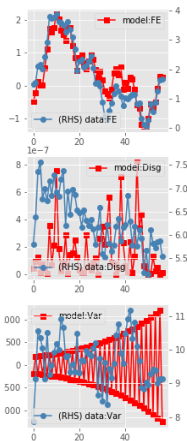
(a) FE



(b) FE/Disg



(c) FE/Disg/Var



NISV parameters

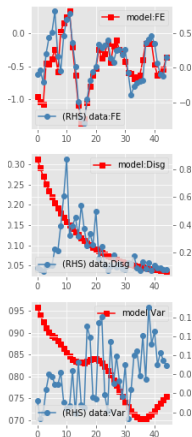
Table: SMM Estimates of Parameters of NISV

| 0 | 1 | 2 | 3 | 4 | NI: $\hat{\sigma}_{pb,SPF}$ | $\hat{\sigma}_{pr,SPF}$ | NI: $\hat{\sigma}_{pb,SPF}$ | $\hat{\sigma}_{pr,SPF}$ | γ | NI: $\hat{\sigma}_{pb,SCE}$ | $\hat{\sigma}_{pr,SCE}$ |
|-------|-------|---------|---------|-----|-----------------------------|-------------------------|-----------------------------|-------------------------|----------|-----------------------------|-------------------------|
| FEVar | FEATV | Var | | | 2.35 | 2 | 2.04 | 23.01 | 2.53 | 2.00014E+14 | 3.63 |
| FEVar | FEATV | DisgVar | DisgATV | Var | 3.33 | 1.71 | 2.04 | 22.96 | 2.53 | 1.09884E+13 | 3.63 |

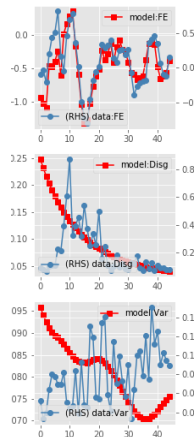
- σ_{pb} : noisiness of public signals in NI
- σ_{pr} : noisiness of private signals in NI
- γ : size of the innovation to volatility

Professionals and NISV

(a) FE/Var

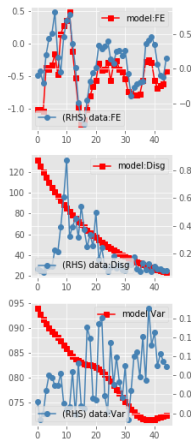


(b) FE/Disg/Var

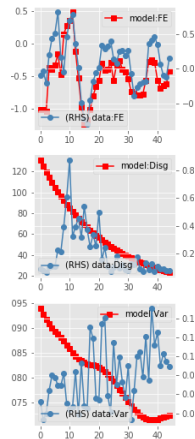


Professionals and NISV: joint estimates

(a) FE/Var

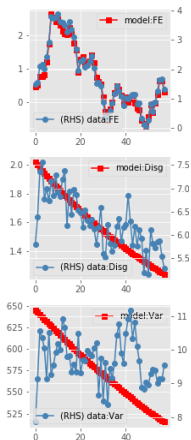


(b) FE/Disg/Var

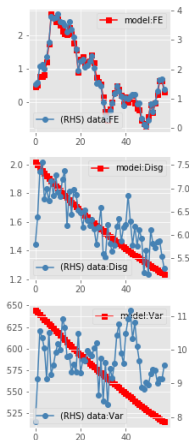


Households and NISV

(a) FE/Var

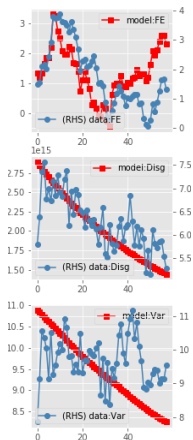


(b) FE/Disg/Var

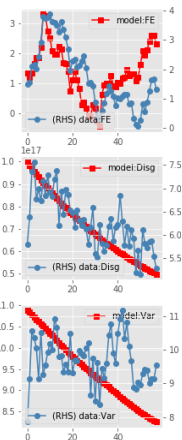


Households and NISV: joint estimates

(a) FE/Var



(b) FE/Disg/Var



Taking stock

Table: A scoring card of different theory

| Criteria | SE | NI | DE |
|---|--------|-----|--------|
| Sensitive to moments used for estimation? | No | No | No |
| Sensitive to the assumed inflation process? | No | Yes | No |
| Sensitive to a two-step or joint estimate? | No | Yes | No |
| Sensitive to the type of agents? | Yes | Yes | Yes |
| Matching with FE | Yes | Yes | Yes |
| Matching with disagreement | Yes | No | Unsure |
| Matching with uncertainty | Unsure | No | No |

Conclusion

- Sticky expectation (SE) augmented with stochastic volatility of inflation process matches data of inflation and expectations better than other theories for both professionals and households.
- Within each model, households are more inconsistent compared to professionals
- Incorporating higher moments, i.e. uncertainty, helps “discipline” theories on expectation formation
- Higher moments from surveys also contain useful information about the inflation dynamics itself

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