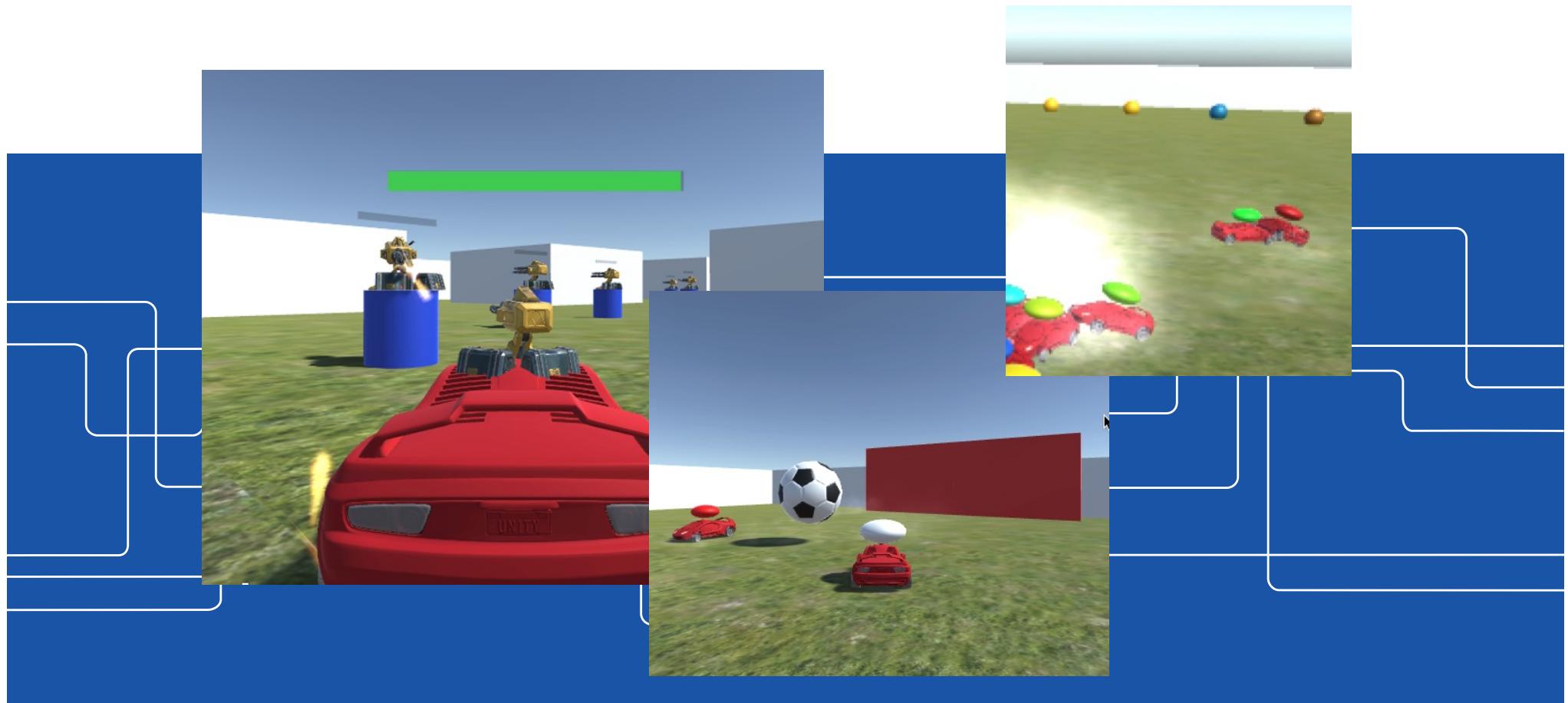




Artificial Intelligence and Multi Agent Systems DD2438

Lecture 2





Pairs for Assignment 1

- By now all pairs should be up and running
- If you or your teammate is dropping the course, please let me know ASAP! ...



Outline of lecture

- Administrative Notes
 - You should be working in the groups now!
 - *Initial Progress* is expected on Tuesday next week
 - Group managers are listed in Canvas (on group page)
 - Todo:
 - Prepare slides
 - Upload/share slides
 - Fill in progress report
 - Peer review slides of others (2 questions)
 - Present slides at meeting
- Motion Planning for the Motion Models ...



Todo for Next Week

- [View Course Stream](#)
- [View Course Calendar](#)
- [View Course Notifications](#)

To Do

- You have to attend the lecture in DD2438 on Tuesday (tomorrow)
DD2438 VT23
Artificial Intelligence and Multi Agent Systems (agent23)
Jan 16 at 3:48pm
- Meeting preparations Week 4 (slides, progress report, peer review)
DD2438 VT23
Artificial Intelligence and Multi Agent Systems (agent23)
Jan 23 at 8pm
- Meeting preparations Week 5 (slides, progress report, peer review)
DD2438 VT23
Artificial Intelligence and Multi Agent Systems (agent23)
Jan 30 at 8pm

A1 Meeting preparations

These instructions are a more detailed version of [the general ones](#).

On the day before a meeting with an assignment **you need to do the following:**

- Update [progress tables, and best results so far](#)
- Create slides (using Google Slides, [see example](#)) describing your current status
 - Add a [link to your slides here](#)
 - This will be used for peer review and presentation, so make sure everyone with the link can read and comment your work.
 - Upload a [pdf-version of your slides](#) in the corresponding Canvas "assignment"
 - This is used for book-keeping, to check that you met the deadline etc.
- Peer feedback: After the deadline [pick 2 other groups from the list](#) (choose one freely, and one that is right below you in the list) read their slides and provide at least 2 constructive comments or questions to each group (this is done individually, in Google Slides)

When preparing the slides and your presentation consider the following:

- See example slides [here](#).
- Focus on what is **interesting**, do not tell your friends what they already know.
- What did you do, why?
- What are you planning to do, why?
- Do you have any **assumptions, observations** regarding algorithm performance?
- Make the presentation **short**, only a few slides (but plots and videos are interesting)



Template of Slides

https://docs.google.com/presentation/d/1AEhrvdoOA-Nr_5EoMbjozHjY8whdiub3kXRUeMwCLQE/edit#slide=id.g766abca800_0_7



Remember: Ask Questions in Canvas

A screenshot of a Canvas message interface. On the left, there is a user profile icon of a person's head and shoulders. To the right of the icon, the name "Per Andersson" is displayed in blue, followed by the word "Yesterday" in smaller gray text. Below this, a message is shown in a text box:

Hi,
will we know whether there will be diagonal walls or even round corners on the evaluation mazes, or will the mazes be comprised of blocks as the examples are?
Per



Progress Report (link in Canvas)

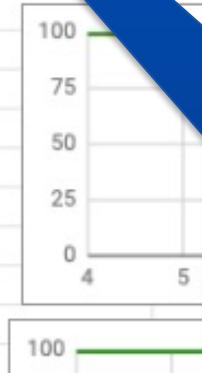
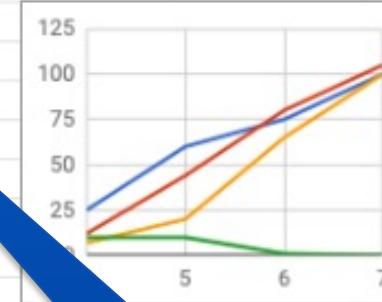
Fill in data
the day
before
each
meeting

Note: Effort is in % out of the 200h (for 2 persons working 2.5 weeks full time)

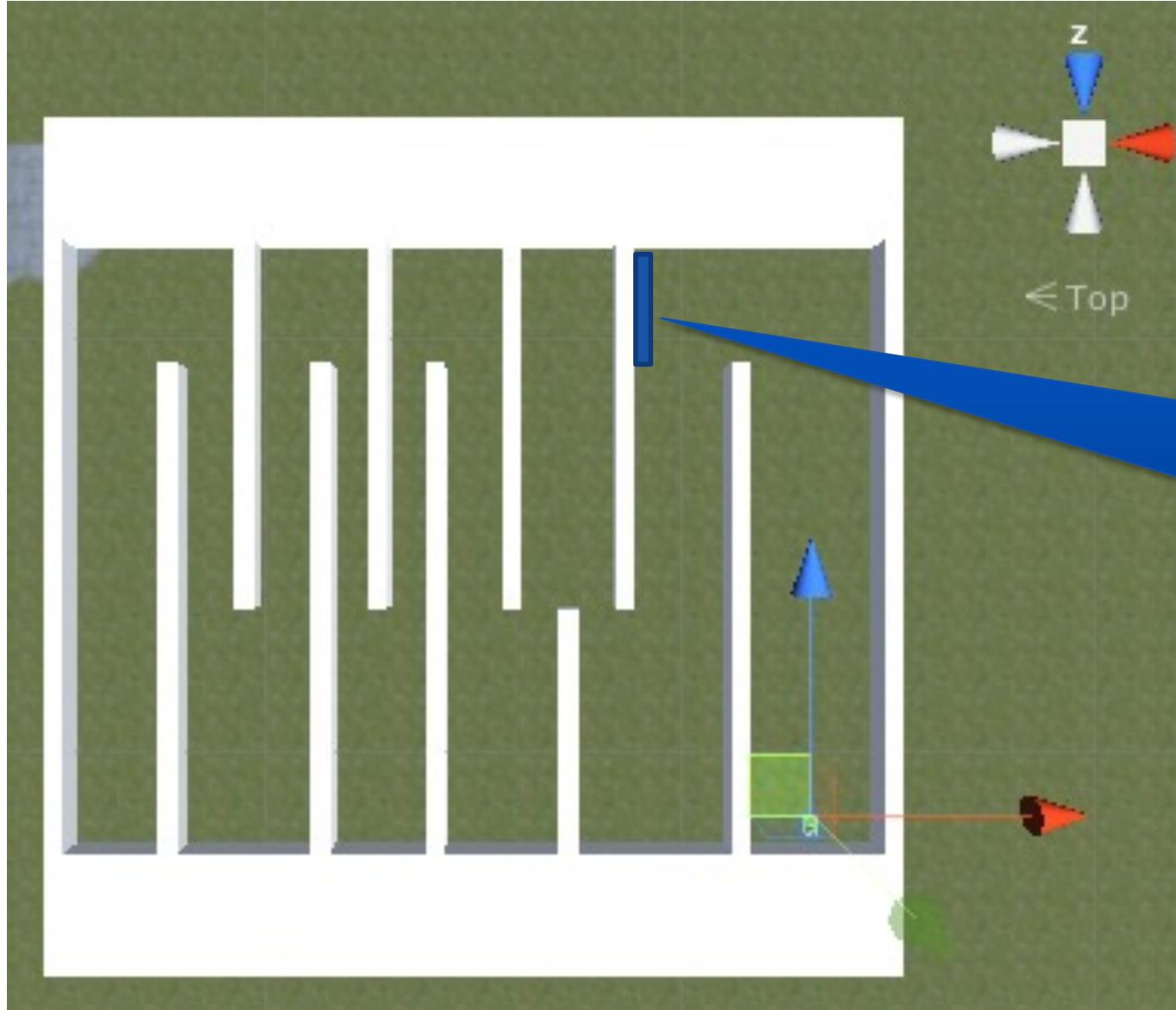
Let the number of each week be given by the effort spent between the meeting in that week and the previous meeting.

Group 0 (example)		Week number		Final Meeting Report Handin	
		4	5	6	7
Planned Effort (accumulated):		25	60	75	100
Actual Effort (accumulated):		12	44	80	105
Actual Progress:		7	20	65	100
Risk of Failure:		10	10	1	0
Comments on Risk:	(only needed if >5%)				
Comments on Progress:	(only needed if large gaps between first 3 curves)				
Project management:	(what approach are you following and how is it working)				

Group 1 (Name 1)		Week number		Final Meeting Report Handin	
		4	5	6	7
Planned Effort (accumulated):		99	99	99	99
Actual Effort (accumulated):		99	99	99	99
Actual Progress:		99	99	99	99
Risk of Failure:		99	99	99	1
Comments on Risk:					
Comments on Progress:					
Project management:					



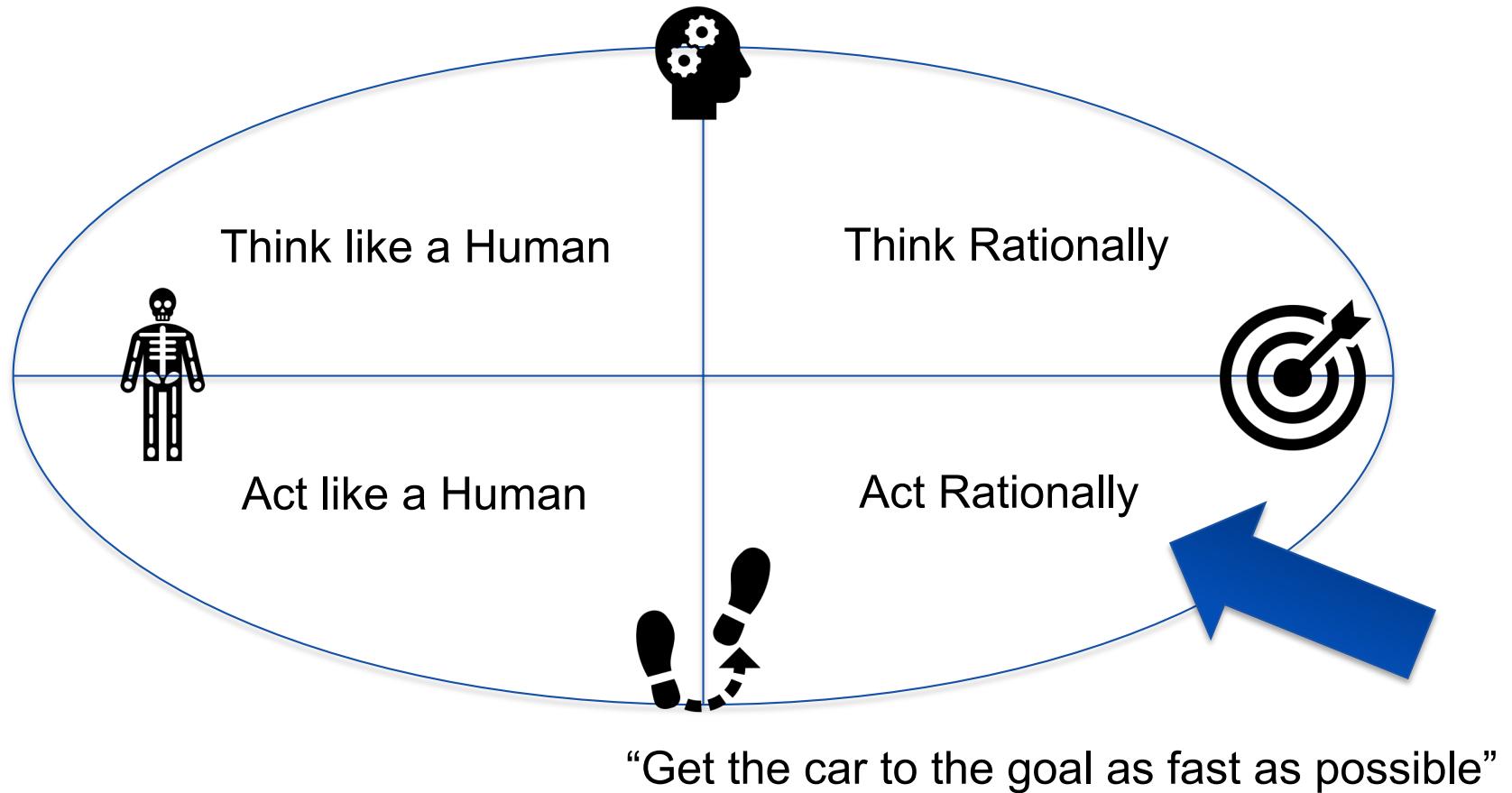
Add data
for “week
between
this and
previous
meeting”



Note that
grid sizes
can be
smaller
than the
car

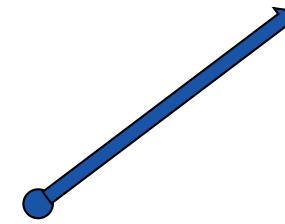
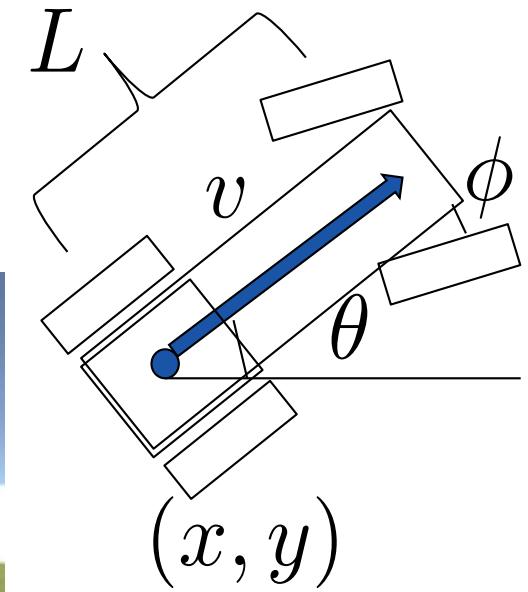
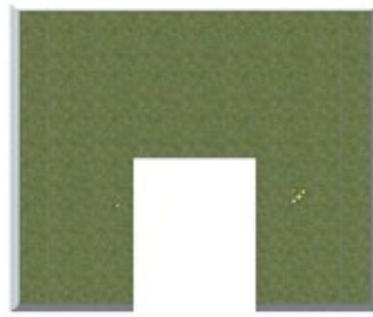
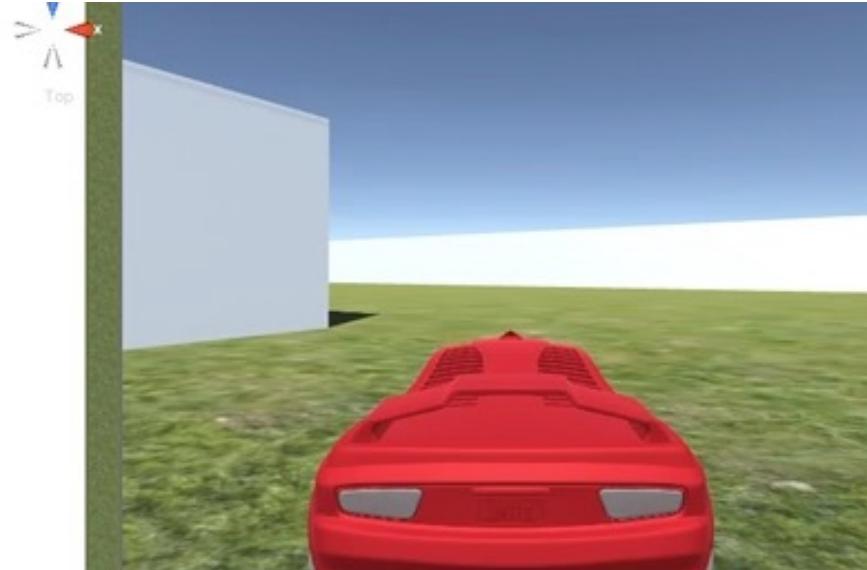
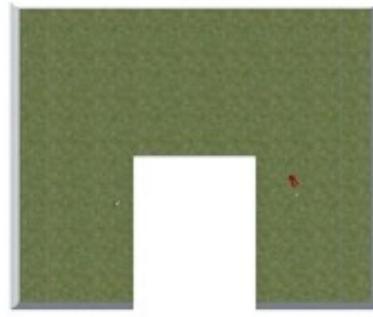


Artificial Intelligence





The two vehicle models: Car and Drone

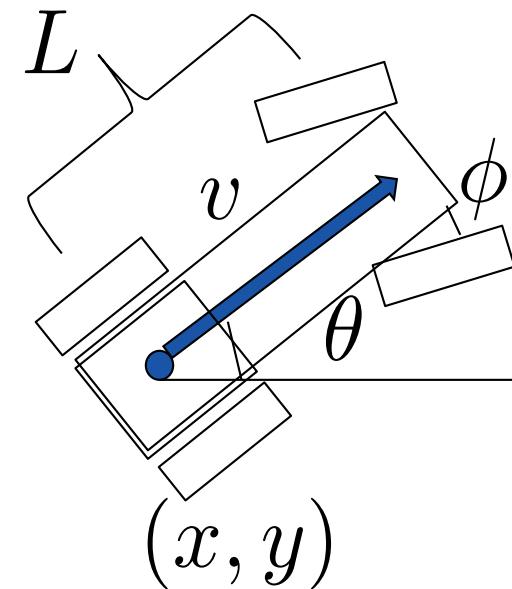


(x, y)

Summary of vehicle models

Complexity

- Discrete state space
- Kinematic point model
- Dynamic point model
- Differential drive
- Car model
- More detailed models



$$\begin{aligned}\dot{x} &= v \cos \theta, \\ \dot{y} &= v \sin \theta, \\ \dot{\theta} &= \frac{v}{L} \tan \phi.\end{aligned}$$



Short overview of Path Planning Algorithms

Initial Note:

- These slides are meant to give you **a rough idea** of how the different algorithms work
- You are **not** expected to be able to solve the assignment by just reading the slides
- You are expected to
 - Search for information (even beyond listed references)
 - Combine and modify ideas
 - Do problem solving
 - Discuss at meetings





References can be found here...

The screenshot shows a course management system interface. On the left is a sidebar with icons for Account, Dashboard, Courses, Calendar, Inbox (with 20 notifications), History, Commons, and Help. The main content area has a title "Project reporting" and a list of reporting requirements. It also includes a "Links" section with a list of research papers and a "Module 1: Agent Models and Path Planning" section with an "Assignment 1 description".

Project reporting

Project reporting will be carried out in the following form:

- Before the meeting (see deadline) each week:
 - Upload slides
 - Update progress report on Google Sheet ([link ↗](#))
 - Be prepared to give a short presentation at each meeting
- At the final meeting
 - Solve example problems similar to A,B,C
- In a report, in the form of a scientific paper, one week after each final meeting

Details regarding all of these can be found [here](#).

Links

Links to possibly (you decide) interesting material

- [Delayed D*](#) ↗
- [Hybrid A*](#) ↗
- [Hybrid A* in Darpa Urban Challenge](#) ↗
- [RRT](#) ↗
- [Visibility Graph](#) ↗
- [Voronoi diagram](#) ↗
- [RRT*](#) ↗
- [Kinodynamic RRT*](#) ↗
- [Urban Challenge approach](#) ↗
- [Obstacle Distances for Car-like robots](#) ↗
- [Informed RRT](#) ↗
- [Balancing Exploration and Exploitation in Sampling-Based Motion Planning](#) ↗
- [Optimal Motion Planning with the Half-Car Dynamical Model for Autonomous High-Speed Driving](#) ↗
- [Trajectory Tracking of a Car-Trailer System](#) ↗
- [Control of Mobile platforms using a virtual vehicle approach](#) ↗
- [Application of Hybrid A* to an Autonomous Mobile Robot for Path Planning in Unstructured Outdoor Environments](#) ↗
- [Plan and transform](#) ↗

[◀ Previous](#) [Next ▶](#)

A separate window for Google Scholar is shown, featuring the "Google Scholar" logo and a search bar with the placeholder "your text here...".

... but searching on your own is encouraged ...

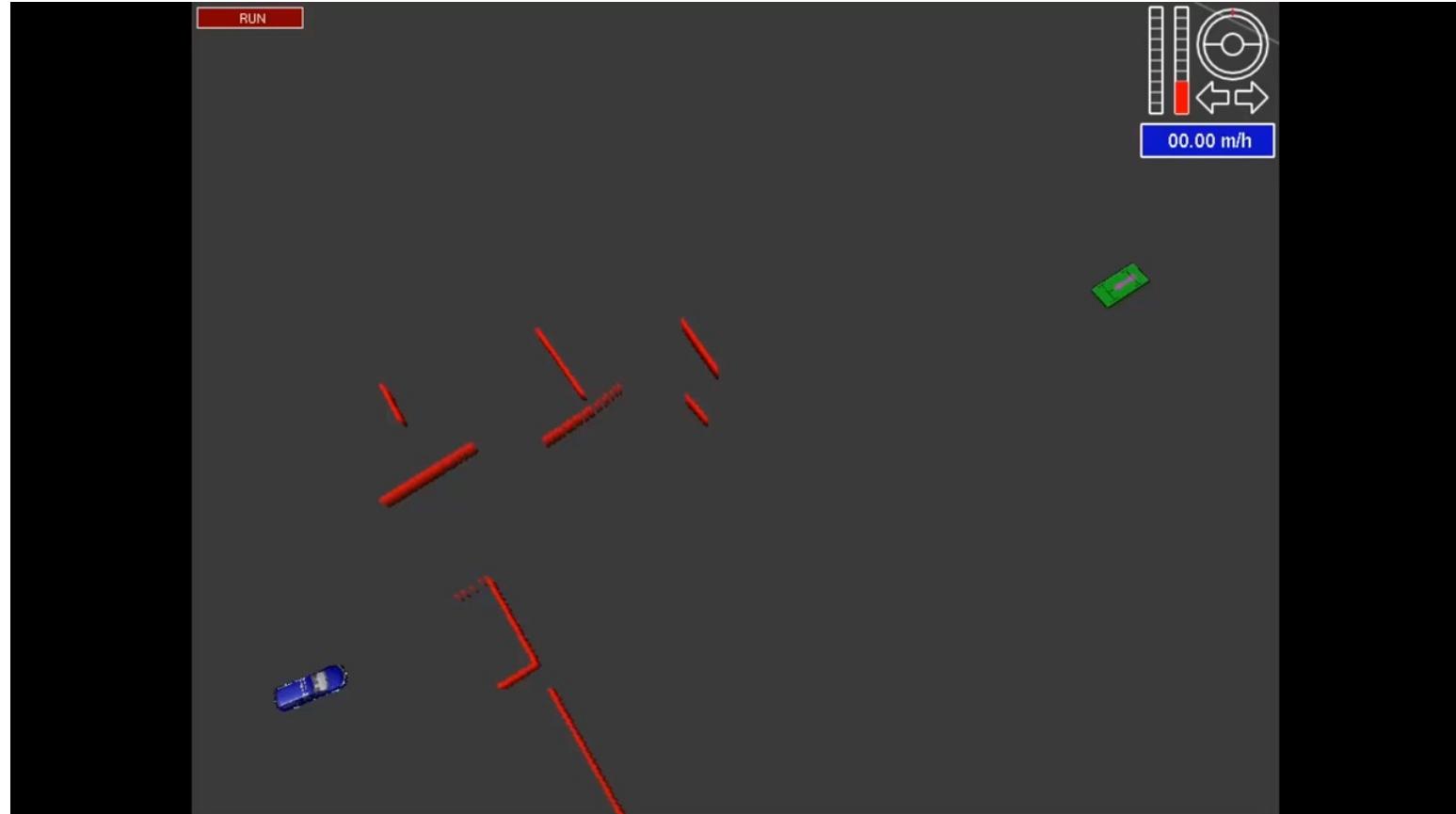


In general: Path planning is hard

- A complete algorithm finds a path if one exists and reports no path exists otherwise.
- Several variants of the path planning problem have been proven to be NP-hard.
- A complete algorithm may take exponential time.

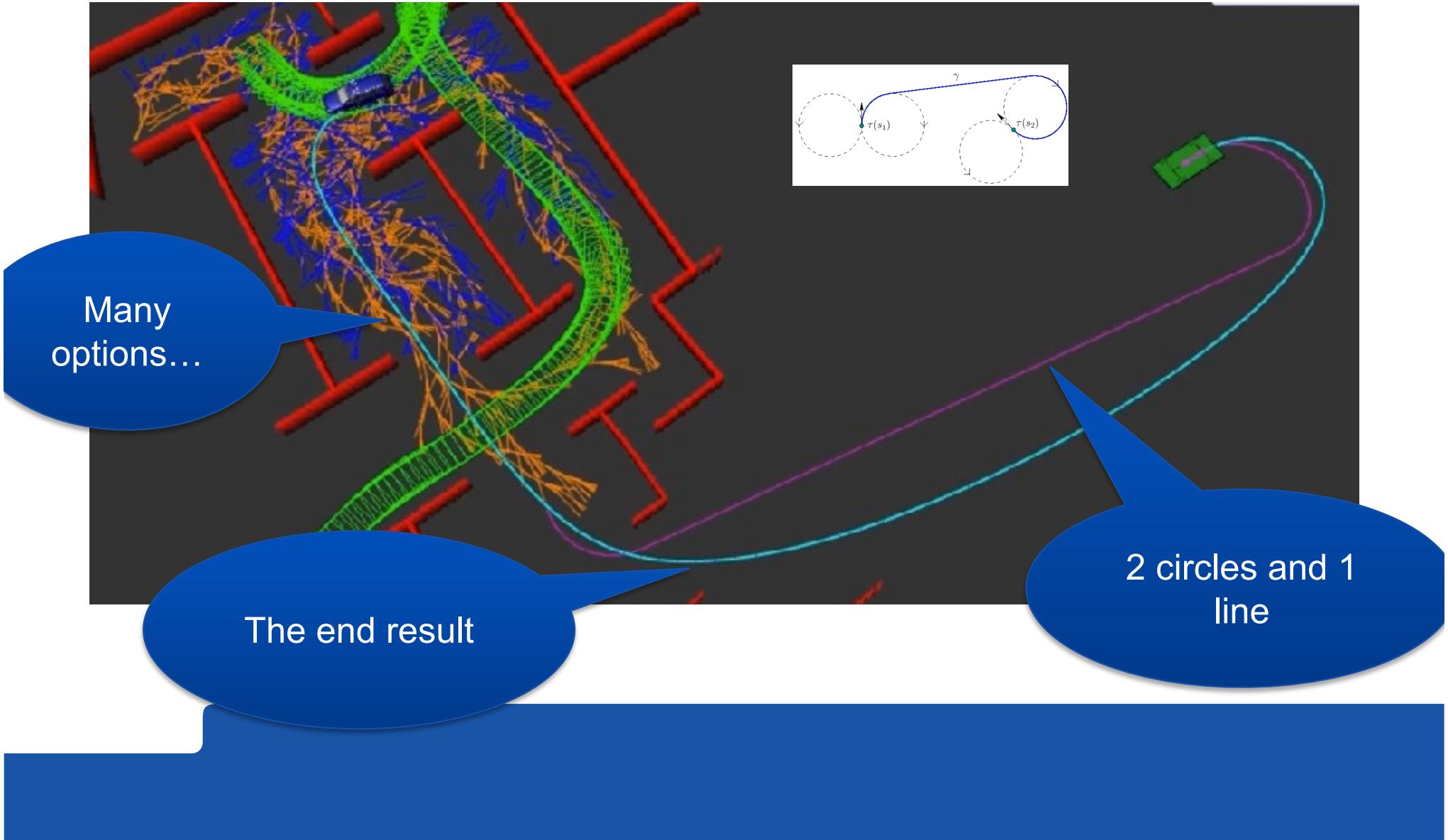


Planning for Autonomous Driving



How is this done?

Some observations



The foundation for many planning algorithms

Shortest Path in a Graph

A Graph $G=(V,E)$

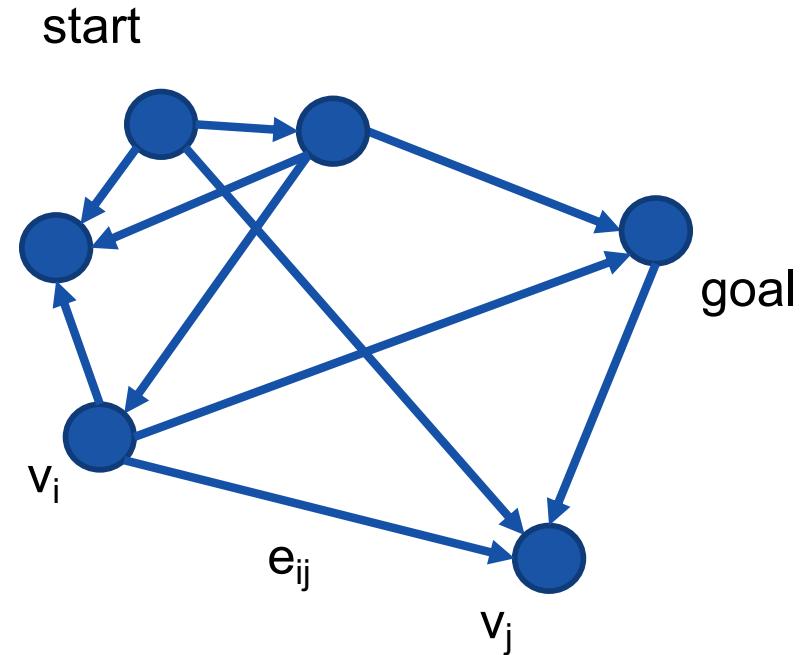
Vertices (v_i)

Edges $e_{ij}=(v_i, v_j)$

Costs c_{ij}

Solved by

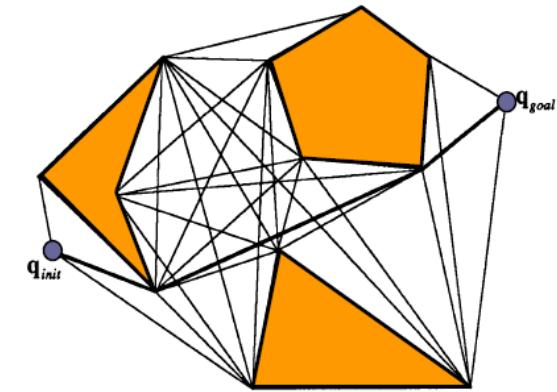
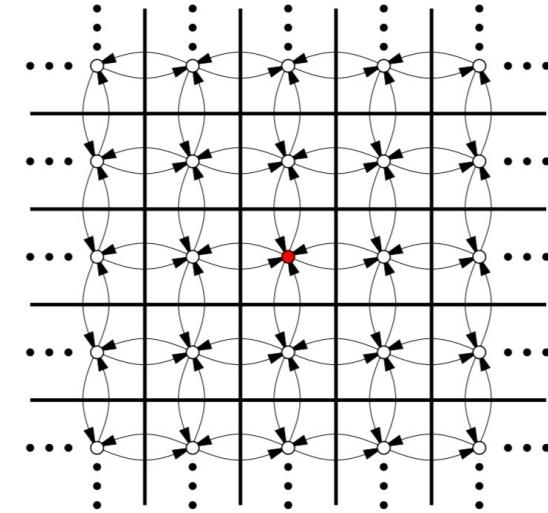
- Dijkstras algorithm
- A*





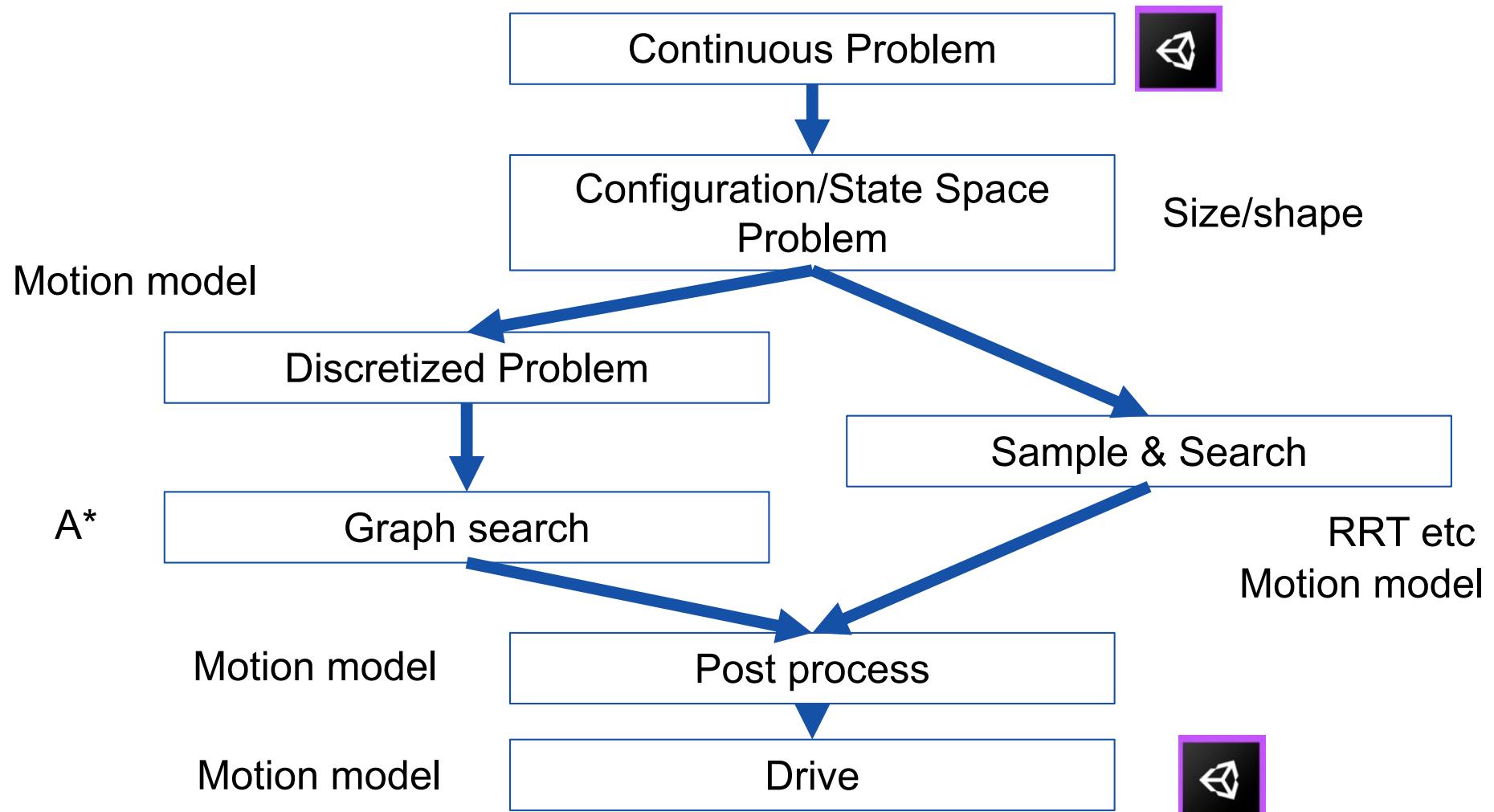
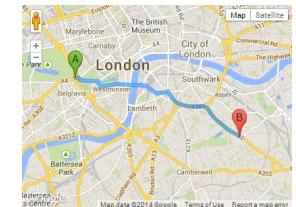
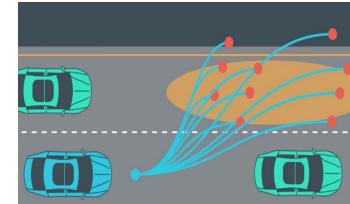
How do we use A*?

- How to choose the Graph?
- How to set Costs?
- Take robot into account
 - Motion model
 - Size/shape





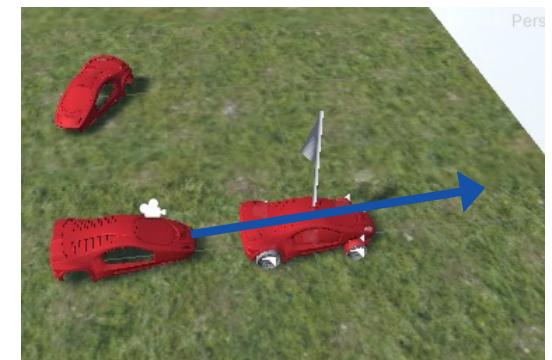
Common Approaches





Configuration space and State space

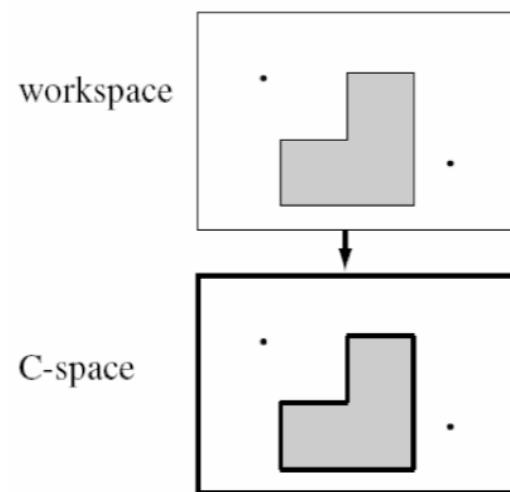
- **Configuration:**
 - Specification of **every position** of the agent
 - Enough to check collisions
 - Ex: (x, y, theta) of a car
- **State:**
 - Specification of **every position and velocity** of the agent
 - Enough to predict the future
 - Ex: (x,y, theta, velocity) of a car
 - Configuration space is subset of State space





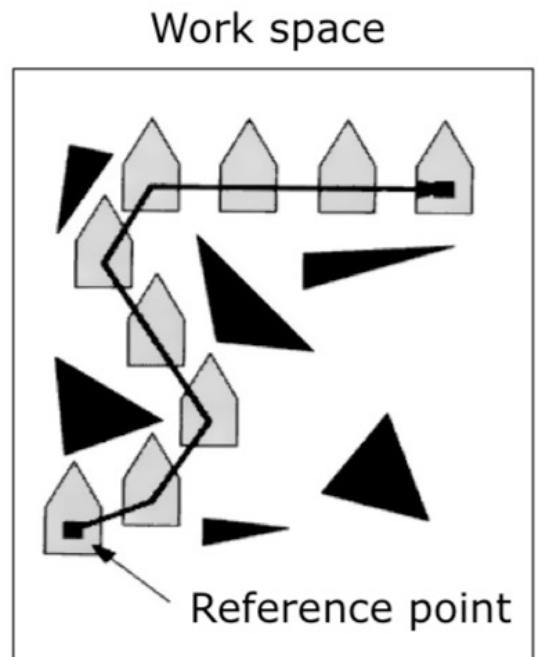
Configuration Space Obstacles

- Part of C-space that induces a collision somewhere



Configuration Space Obstacles

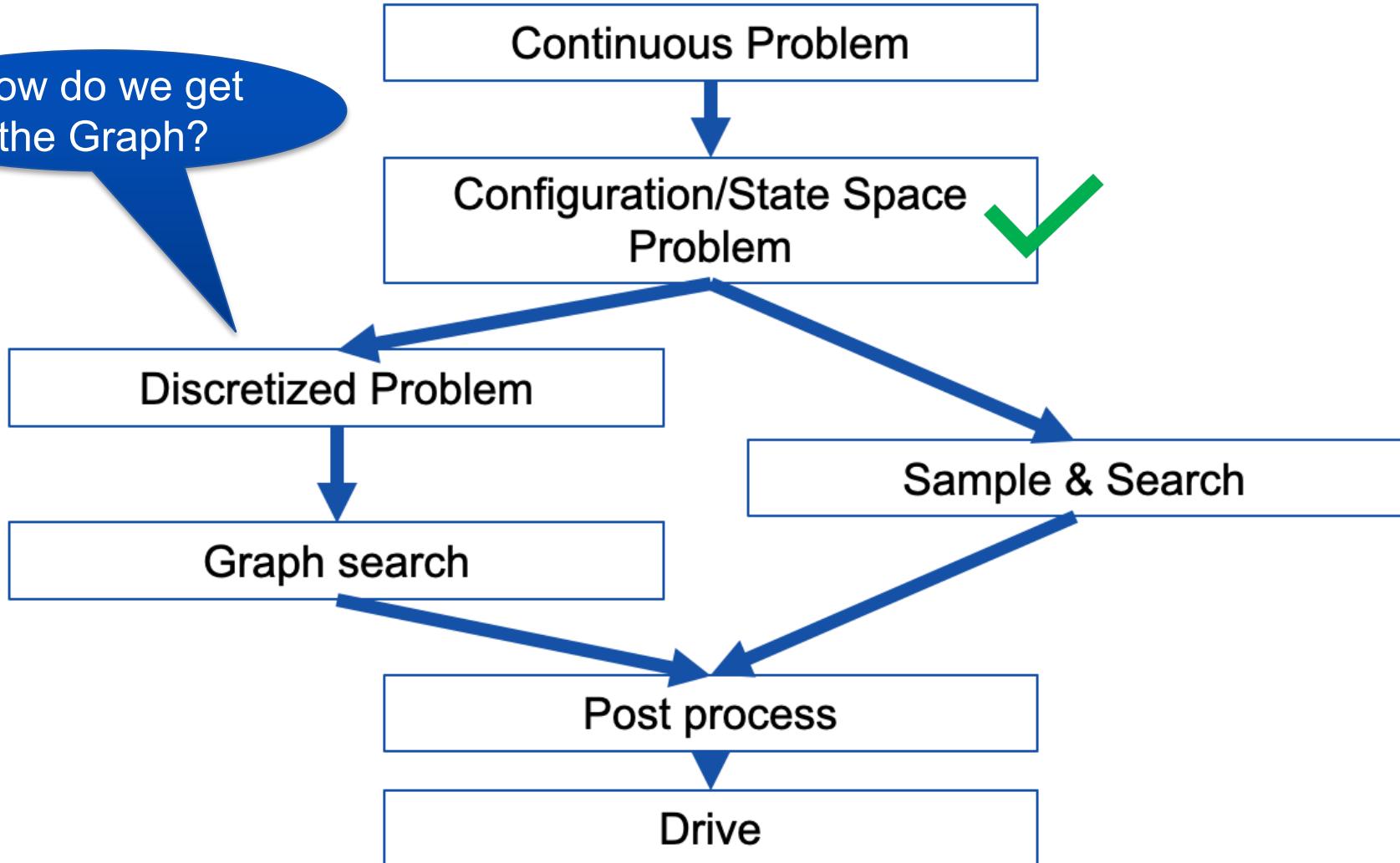
- Part of C-space that induces a collision somewhere





Common Path Planning Approach

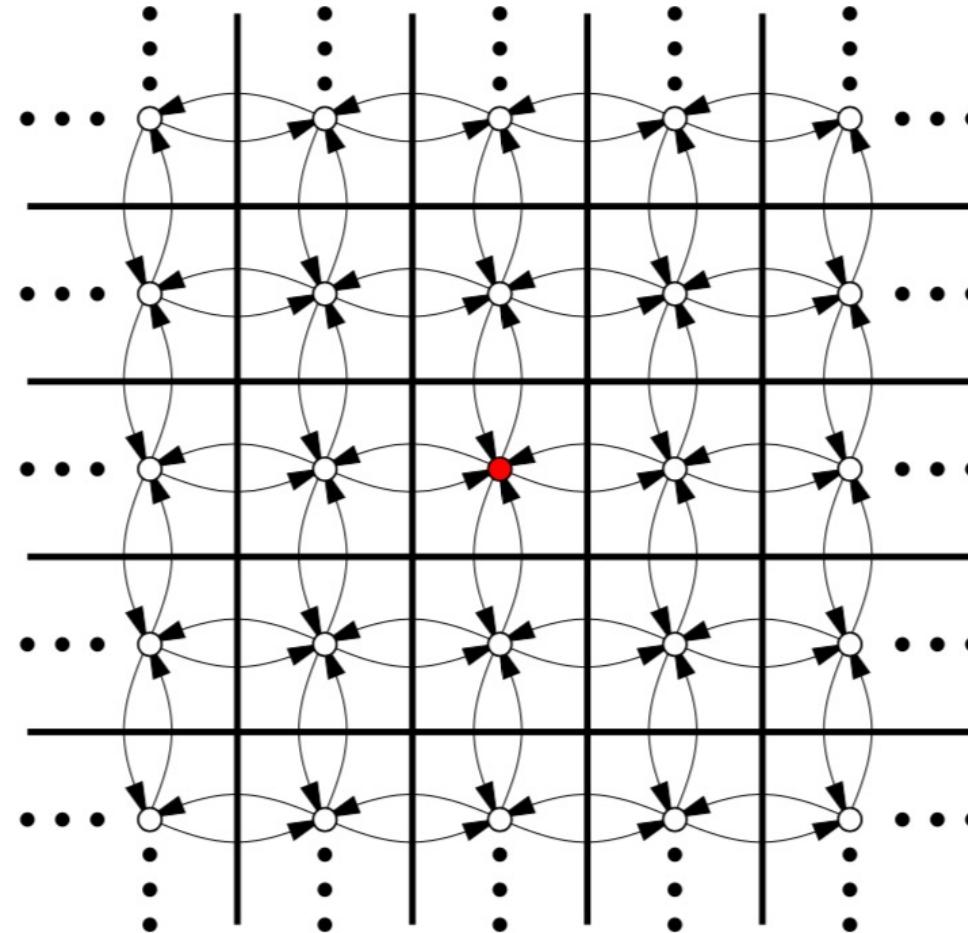
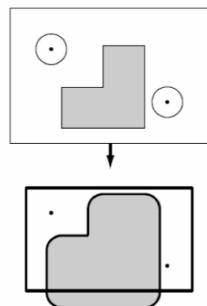
How do we get
the Graph?





How to make a Graph from C-space?

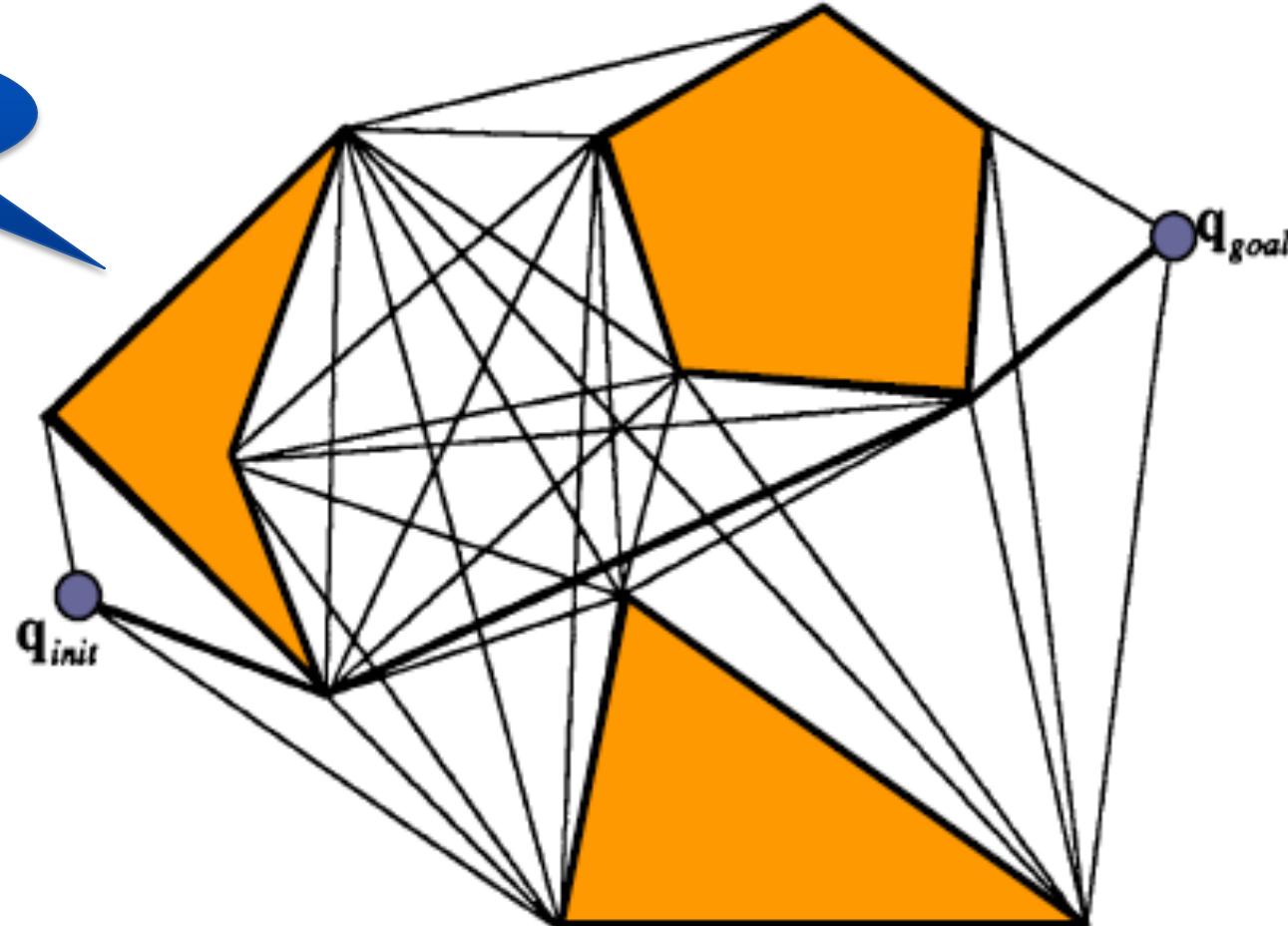
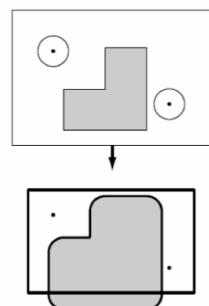
A grid





How to make a Graph from C-space?

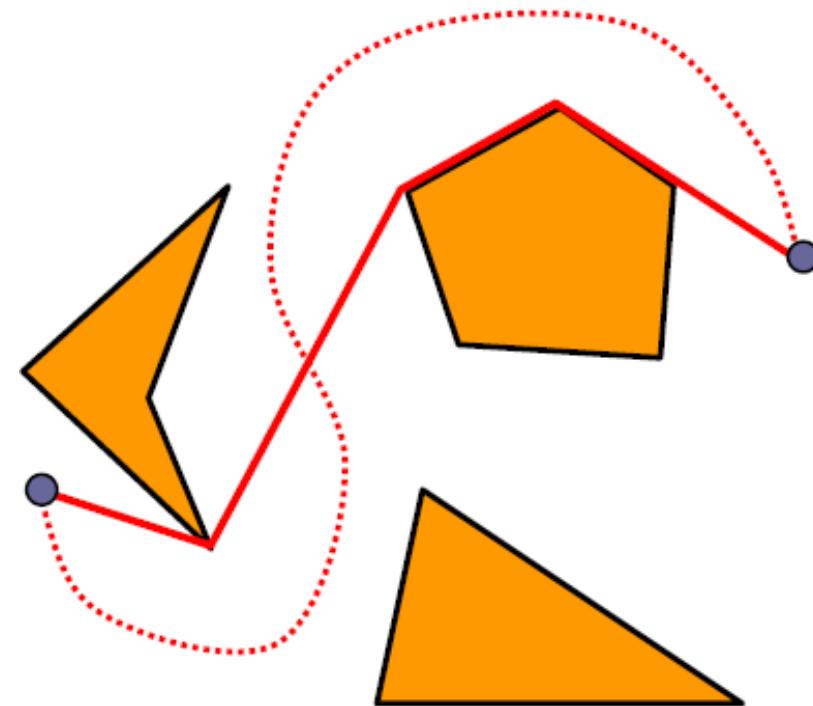
A Visibility
Graph



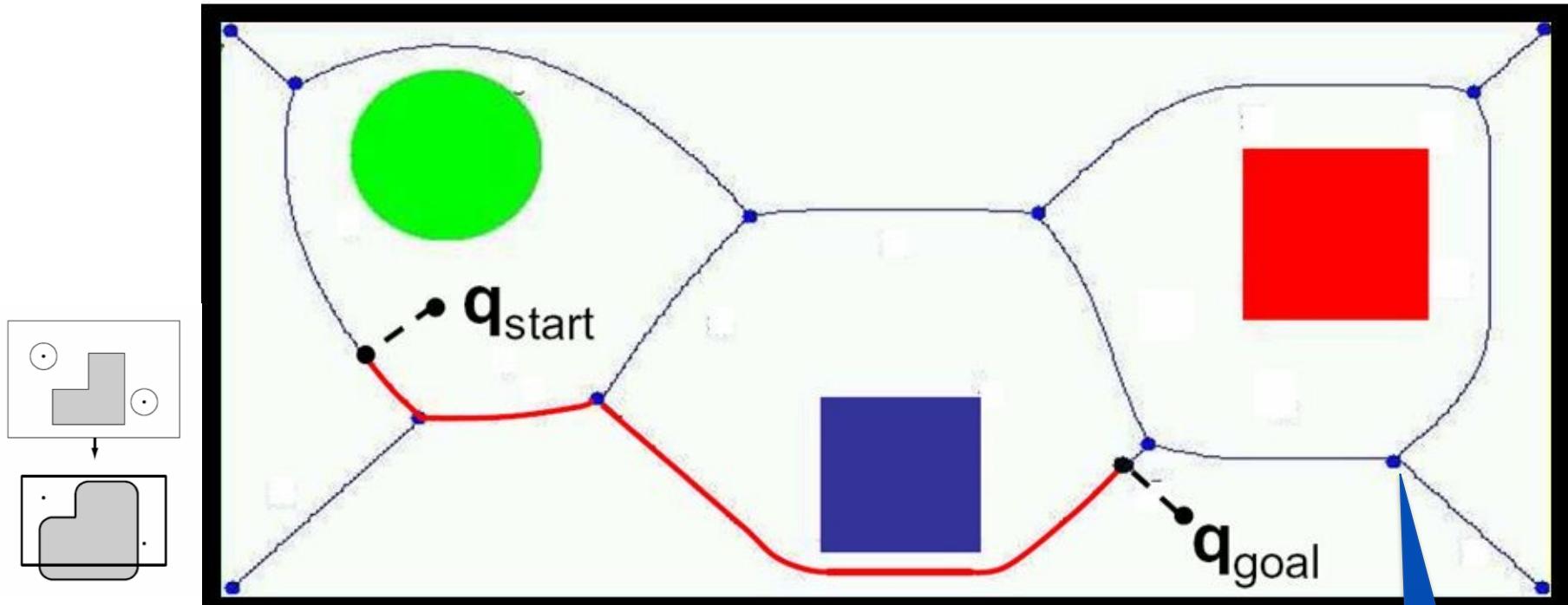
How to make a Graph from C-space?

Observation:

- Shortening any path gives a visibility graph path
- Advantages?
- Drawbacks?



How to make a Graph from C-space?



Points that have equal distance to the two closest obstacles

- Advantages?
- Drawbacks?

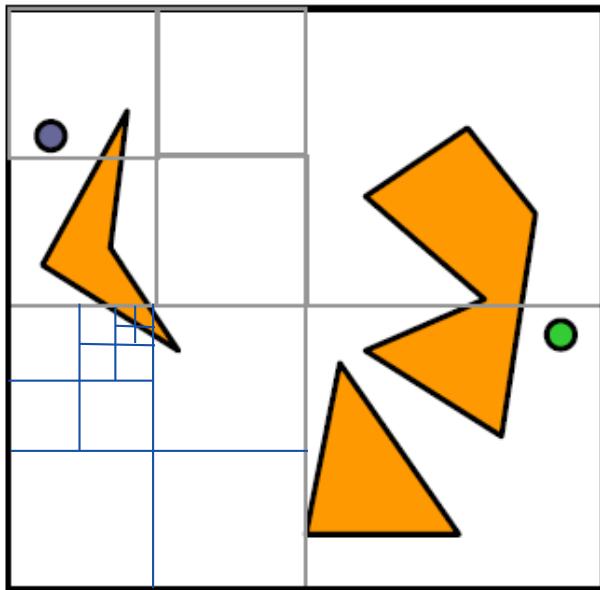
A Voronoi
Graph



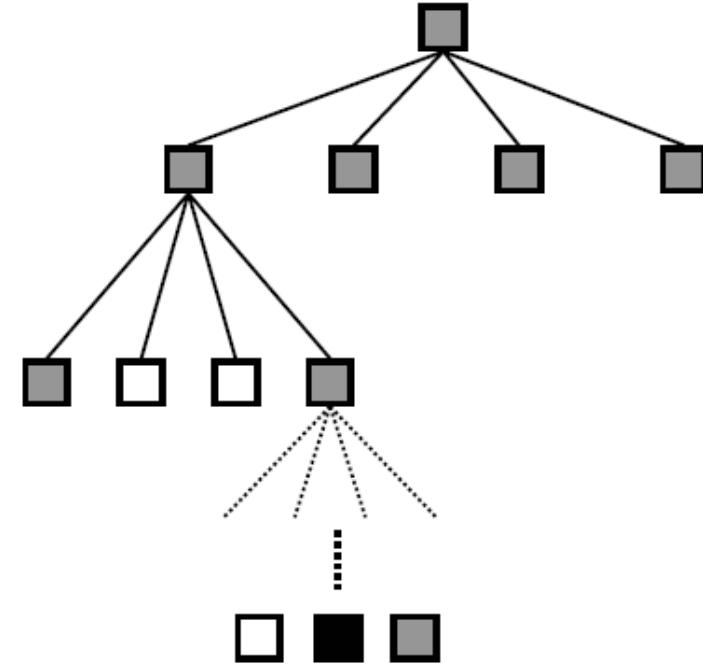
How small should we make the grids?

7	6	5	6	7	8	9	10	11		19	20	21	22
6	5	4	5	6	7	8	9	10		18	19	20	21
5	4	3	4	5	6	7	8	9		17	18	19	20
4	3	2	3	4	5	6	7	8		16	17	18	19
3	2	1	2	3	4	5	6	7		15	16	17	18
2	1	0	1	2	3	4	5	6		14	15	16	17
3	2	1	2	3	4	5	6	7		13	14	15	16
4	3	2	3	4	5	6	7	8		12	13	14	15
5	4	3	4	5	6	7	8	9	10	11	12	13	14
6	5	4	5	6	7	8	9	10	11	12	13	14	15

High resolution in narrow areas Low resolution in open areas...



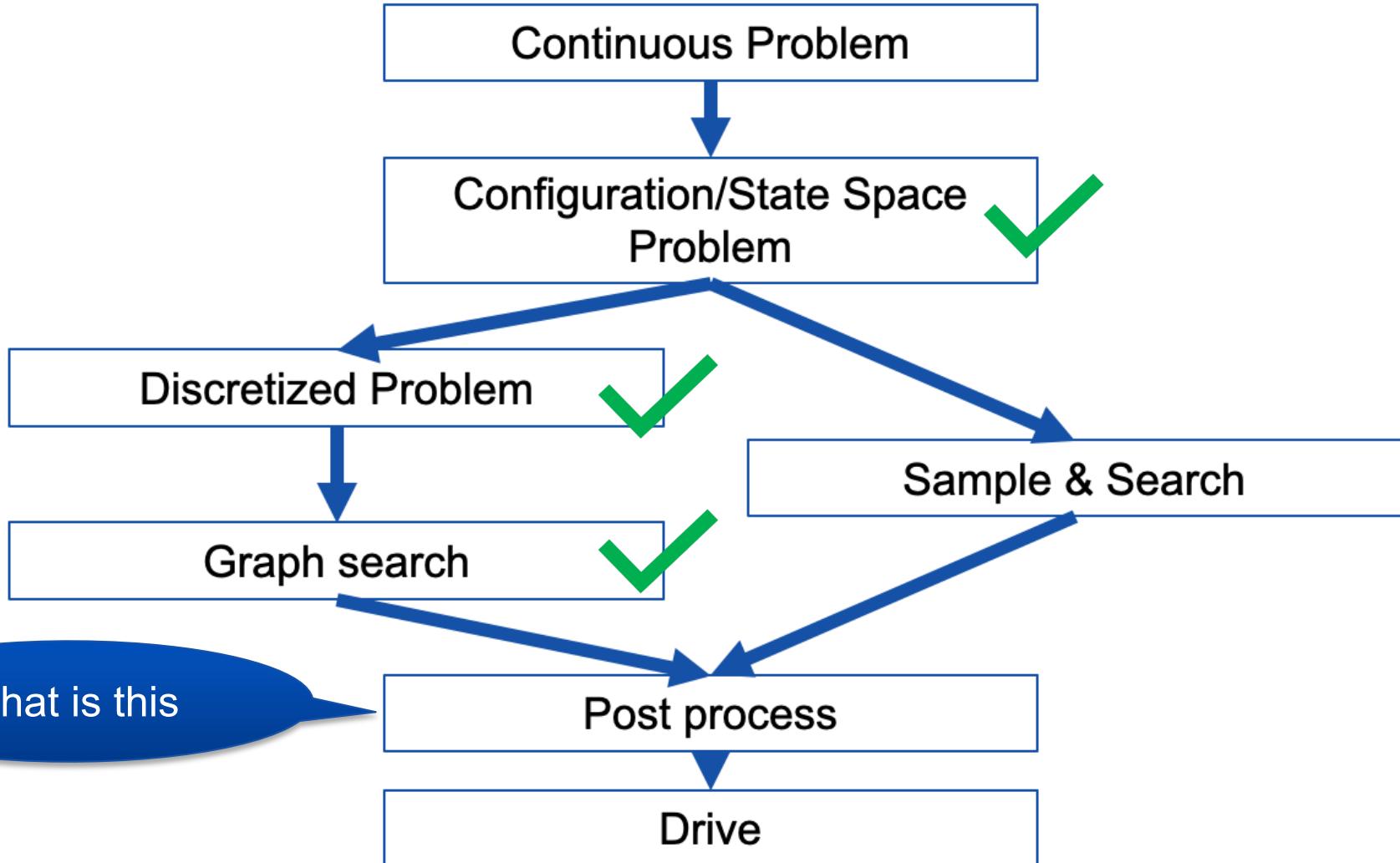
Quadtree
Decomposition



□ empty □ mixed ■ full

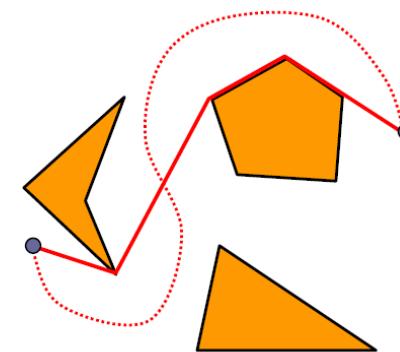
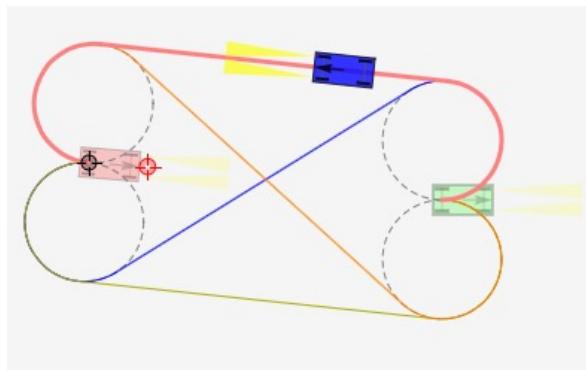


Common Path Planning Approach



What about undrivable trajectories?

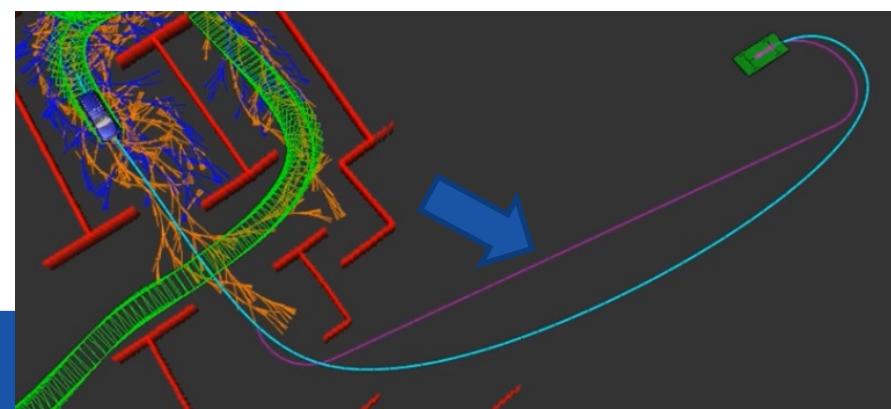
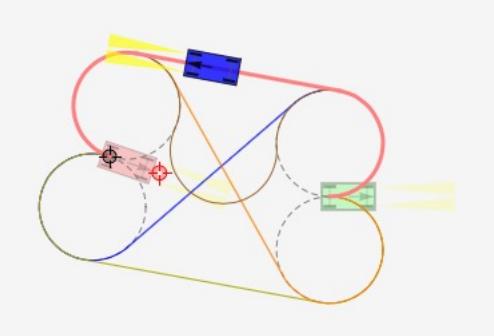
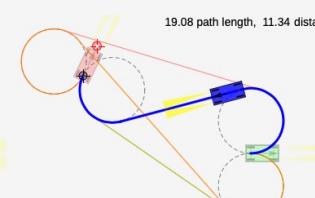
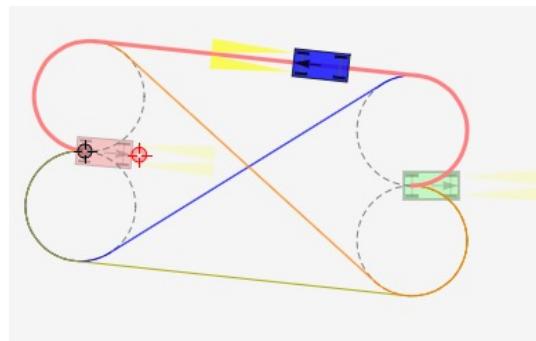
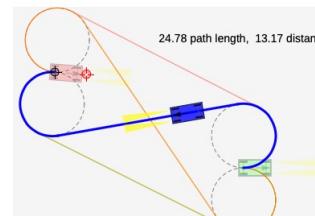
Can a car drive any path?



Kinematic

Dubins car

The optimal path for a car can be created using at most 3 circles and 1 straight line



Can we fix an undrivable path?

Plan and Transform

Algorithm

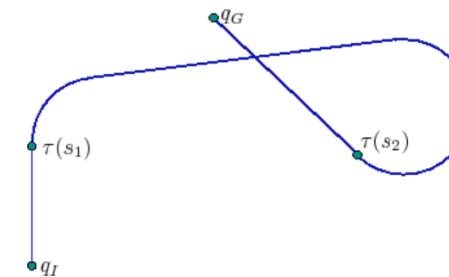
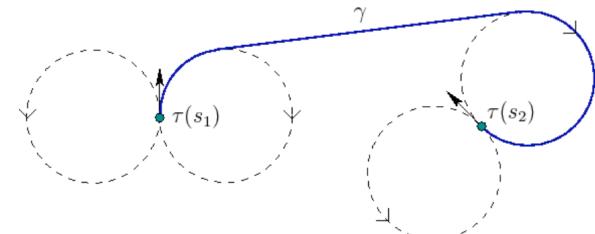
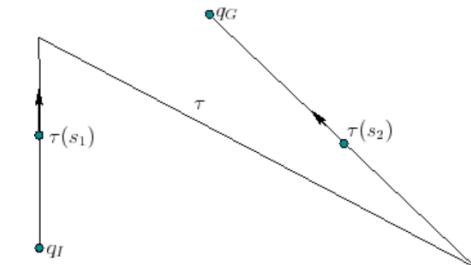
1. Plan a short non-traversable path
2. Pick two points on path
3. Connect with traversable sub-path
4. Iterate from 2, until whole path is traversable

Not always possible

Hard to know when to stop

Can yield very good solutions for visibility graph

not	always
possible	...

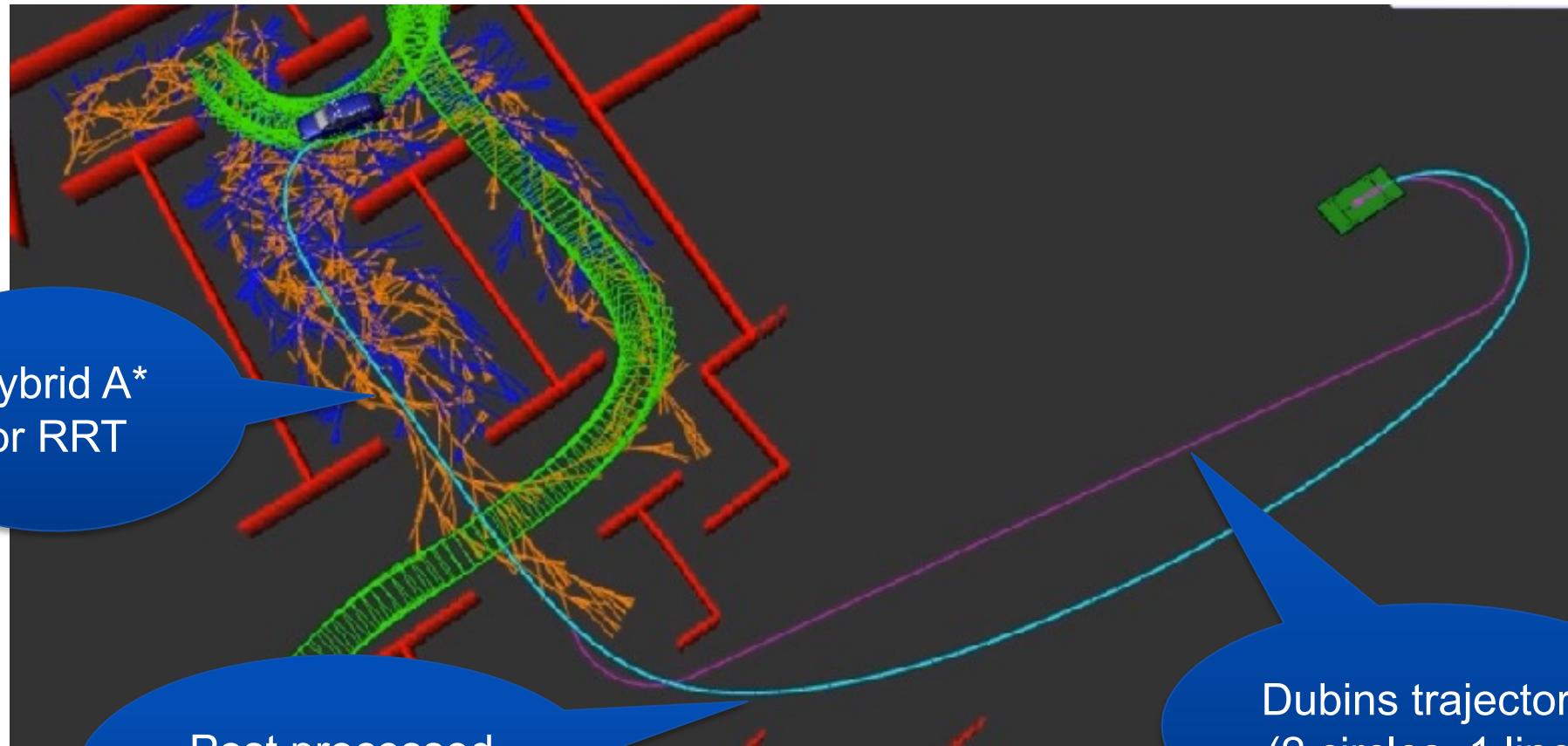
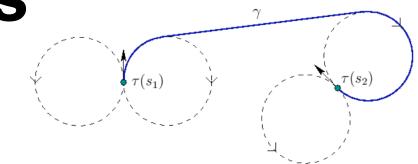




Post processing can also improve performance of drivable trajectories

Smoothen trajectory to enable higher speed using

- Optimization problem
- Heuristic method

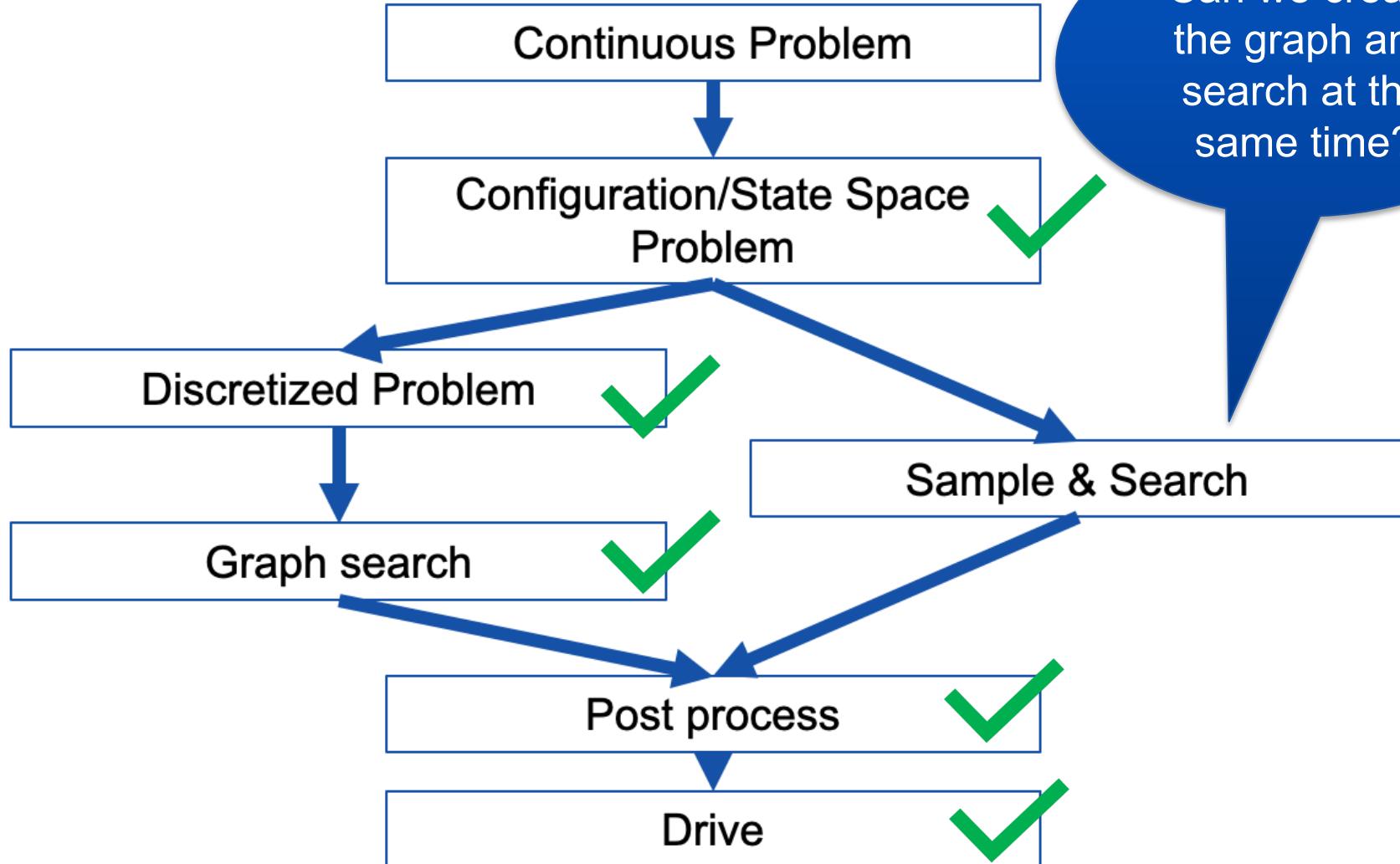


Post processed
trajectory

Dubins trajectory
(2 circles, 1 line)



Common Path Planning Approach

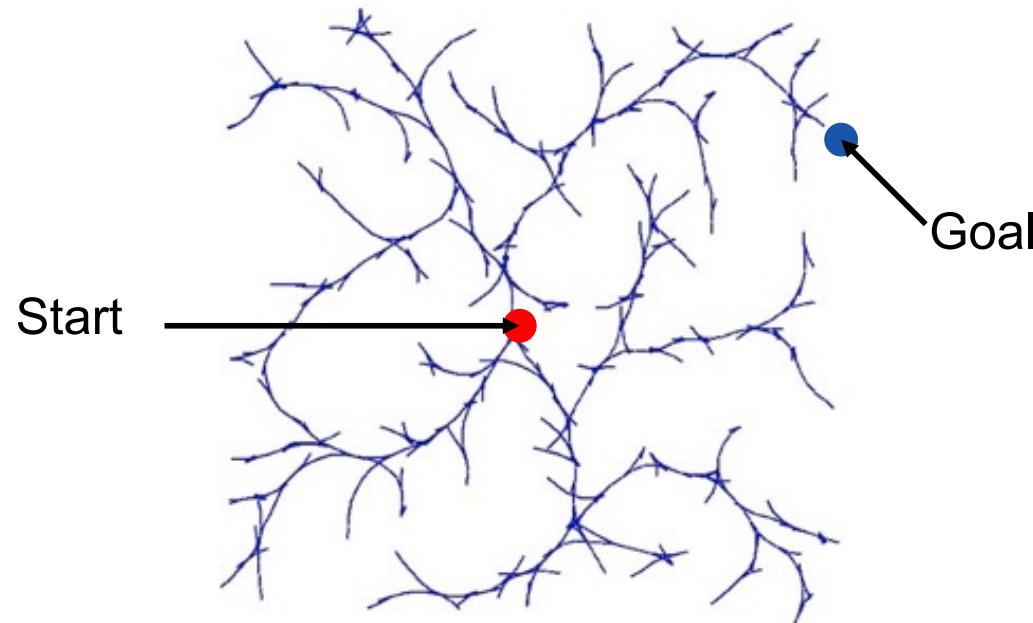


Can we create
the graph and
search at the
same time?



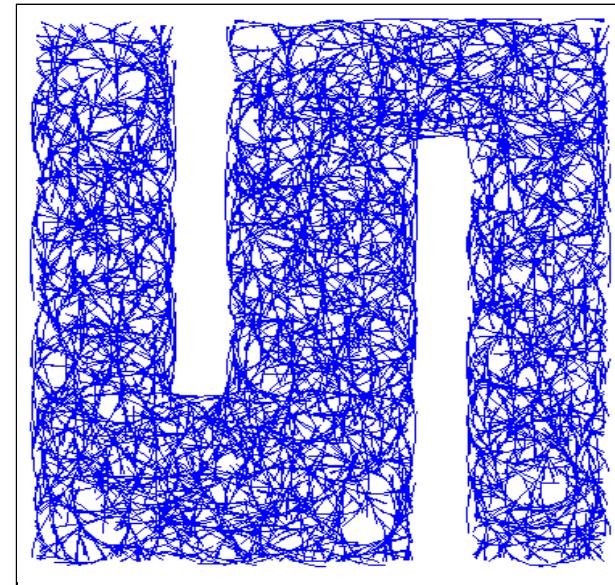
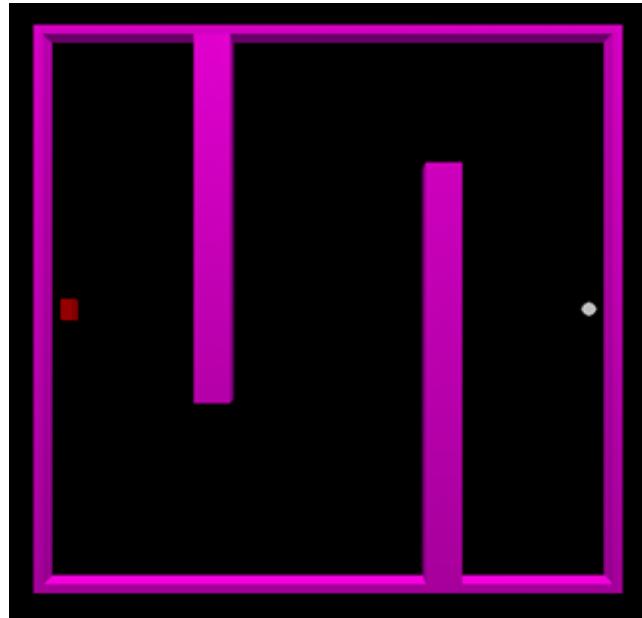
Sample & Search: RRT

RRT: Rapidly Exploring Random Trees





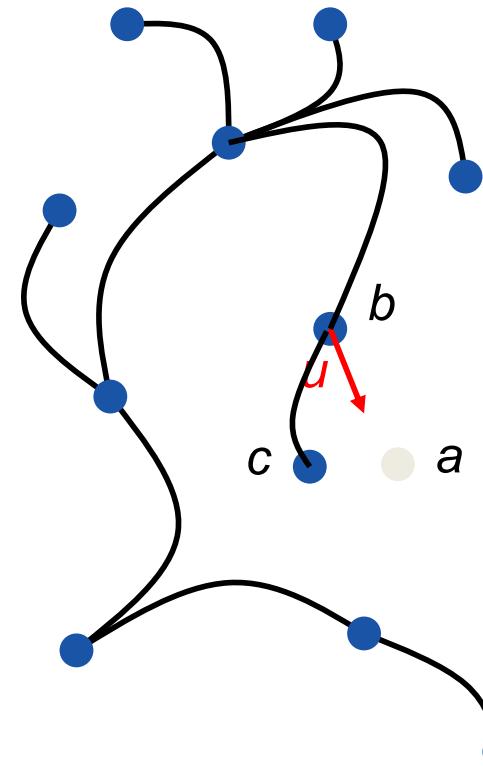
Example: Simple RRT Planner



Building an RRT

To extend an RRT:

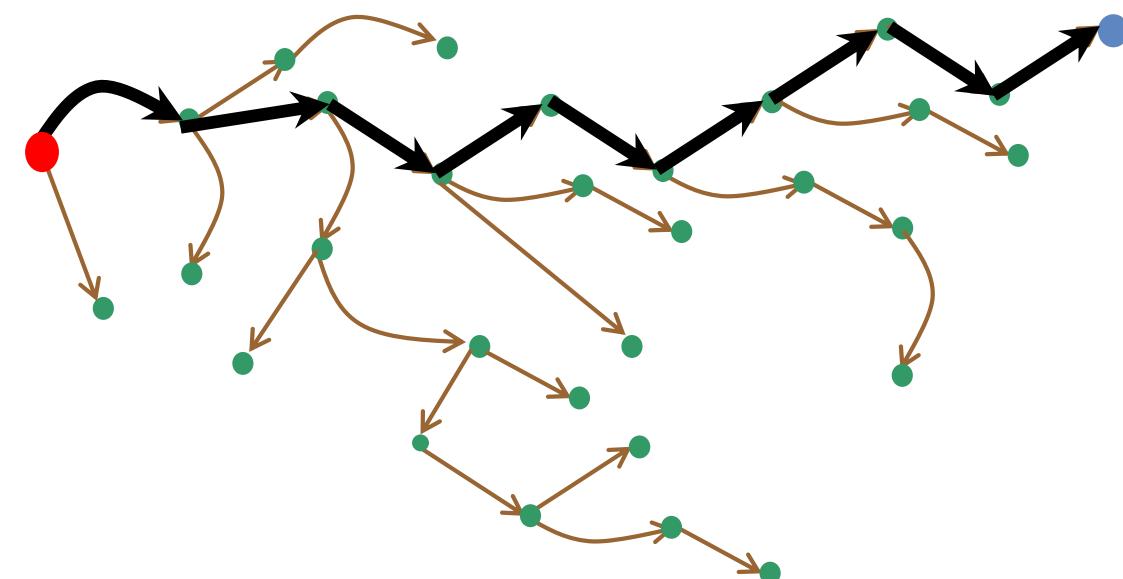
- Pick a **random** point a in X
- Find b , the node of the tree closest to a
- Find control inputs u to steer the robot from b to a
- Apply control inputs u for time δ , so robot reaches c
- If no collisions occur in getting from a to c , add c to RRT and record u with new edge



Executing the Path

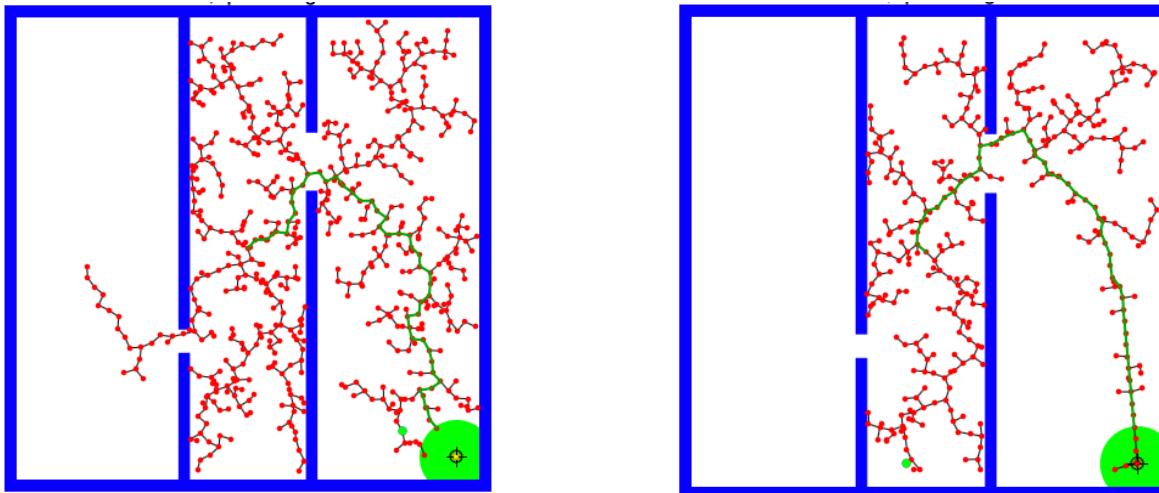
Once the RRT reaches s_{goal}

- Backtrack along tree to identify edges that lead from s_{start} to s_{goal}
- Drive robot using control inputs stored along edges in the tree





Example: Simple RRT Planner



Problem: ordinary RRT explores X uniformly

- slow convergence

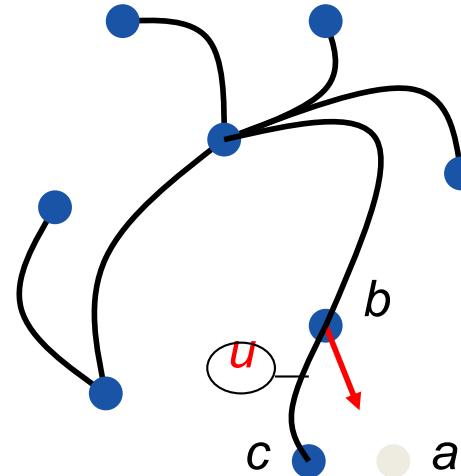
Solution: bias distribution towards the goal

- Pick the goal point with $X\%$ probability

Things to think about...

To extend an RRT

- Pick a random point a in X
- Find b , the node of the tree closest to a
- Find control inputs u to steer the robot from b to a
- Apply control inputs u for time δ , so robot reaches c
- If no collisions occur in getting from a to c , add c to RRT and record u with new edge



- $(x,y)?$
- $(x,y,\theta)?$
- $(x,y,\theta,v)?$

Closest in what sense?

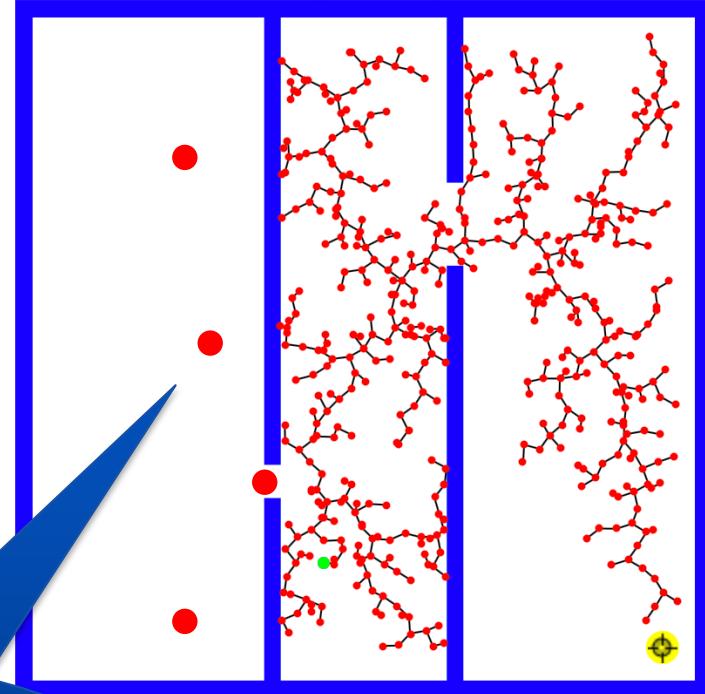


Things to think about...

To extend an RRT

- Pick a random point a in X
- Find b , the node of the tree closest to a
- Find control inputs u to steer the robot from b to a
- Apply control inputs u for time δ , so robot reaches c
- If no collisions occur in getting from a to c , add c to RRT and record u with new edge

Why are there
no Nodes here



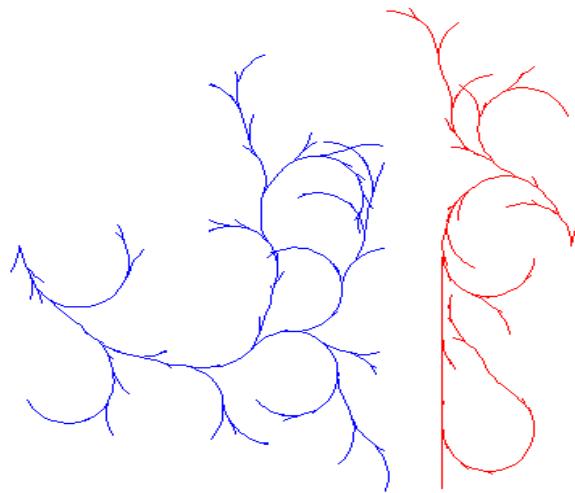
Consider sampling bias

- In narrow gaps
- Along optimal grid path
- ...



Additional improvement: Bidirectional Planners

Build two RRTs, from start and goal state



Complication: need to connect two RRTs

- **bias** the distribution, so that the trees meet



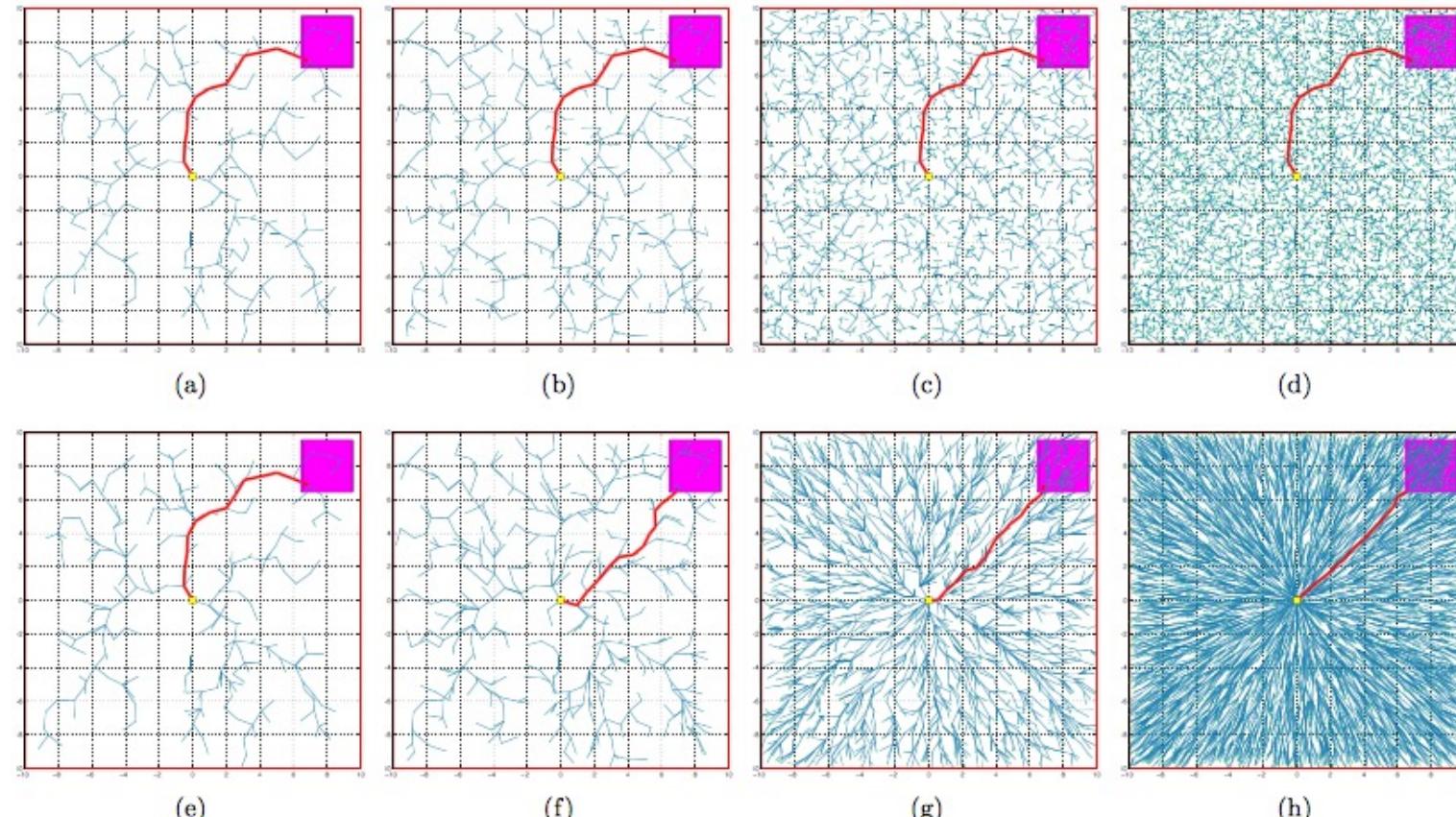
Some notes on RRT

- RRT finds **one** solution with probability $\rightarrow 1$
 - Quality is not perfect...
- Brake through in 2011 (Karaman and Frazzoli)
 - RRT*
- RRT* finds **optimal** solution with probability $\rightarrow 1$



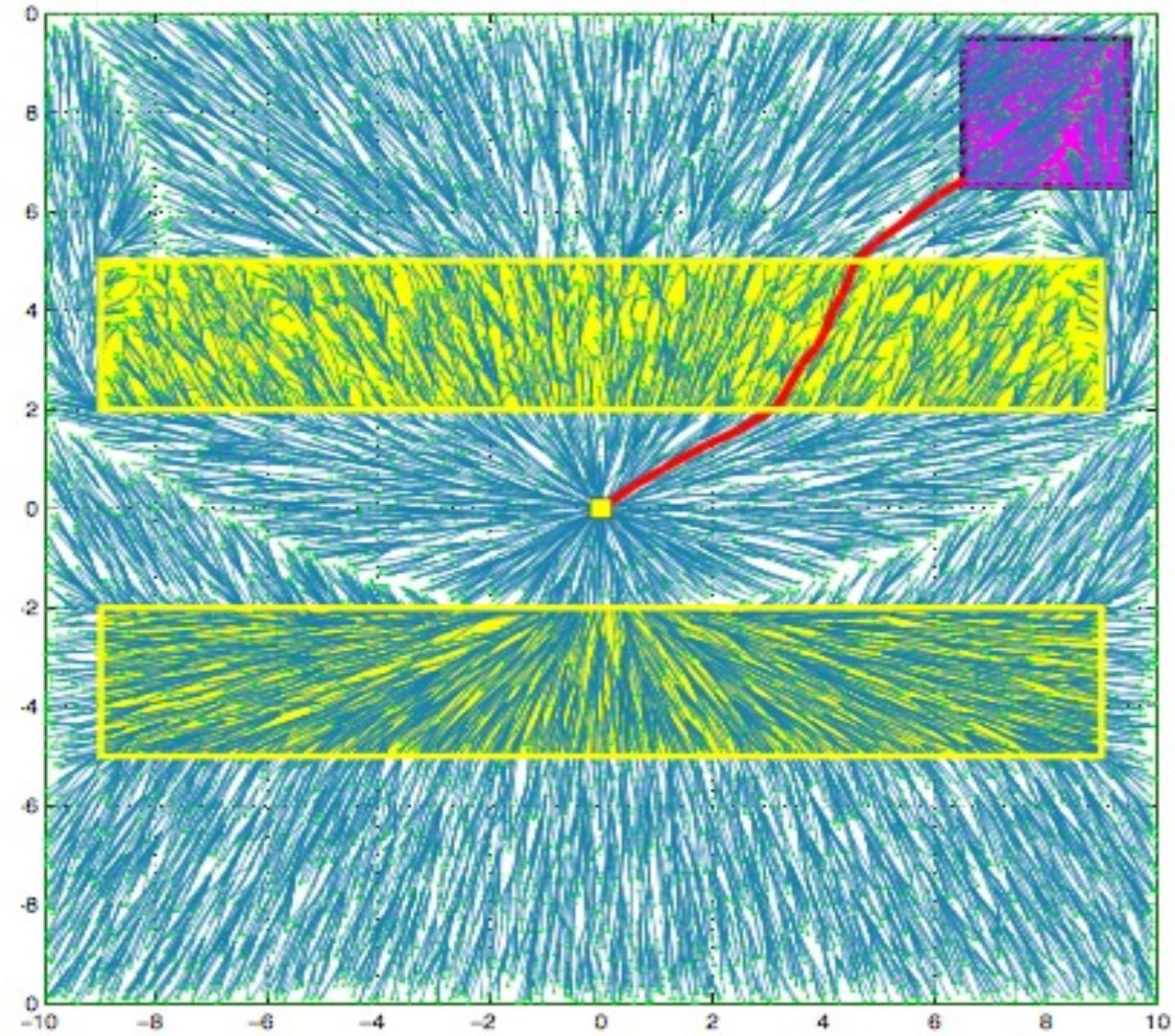


RRT vs RRT* (Karaman and Frazzoli)





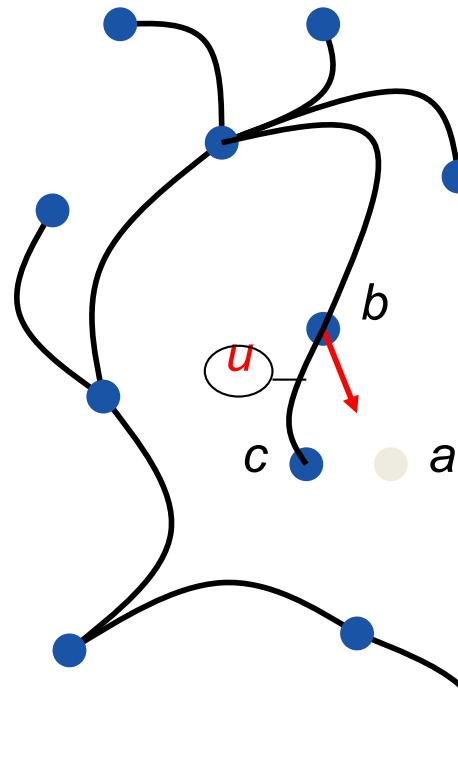
RRT* (High cost and Low cost regions)



How does the RRT* work?

Same start as RRT...

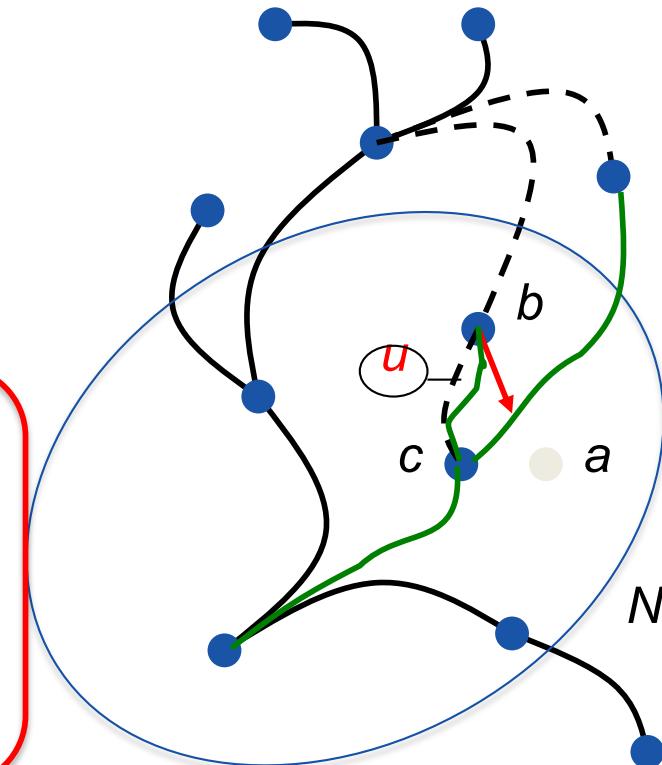
- Pick a **random** point a in X
- Find b , the node of the tree closest to a
- Find control inputs u to steer the robot from b to a
- Apply control inputs u for time δ , so robot reaches c
- If no collisions occur in getting from a to c , add c to RRT and record u with new edge



How does the RRT* work?

Same start as RRT...

- Pick a **random** point a in X
- Find b , the node of the tree closest to a
- Find control inputs u to steer the robot from b to a
- Apply control inputs u for time δ , so robot reaches c
- If no collisions occur in getting from a to c
 - Find set of Neighbors N of c
 - Choose Best parent!
 - Try to adopt Neighbors (if good)





RRT* (2011, original)

a
b
c

Neighbors N

Find best parent

Adopt new children (if improvement)

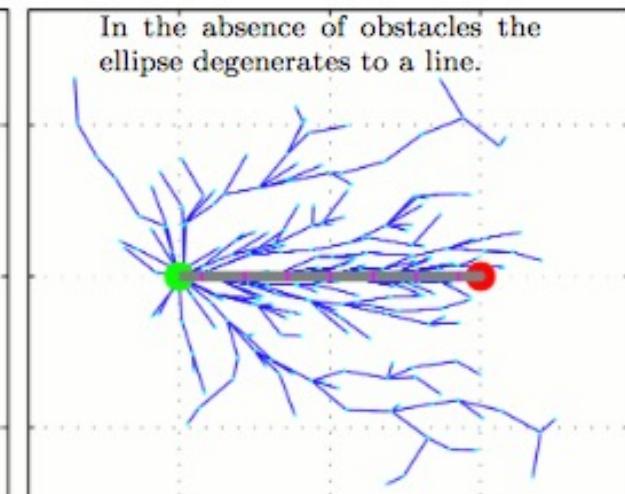
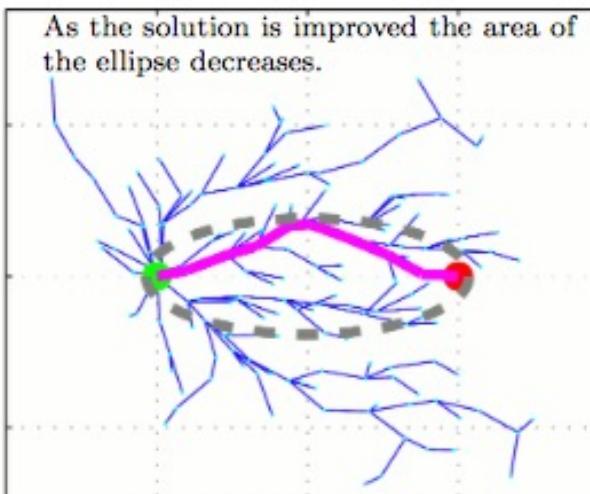
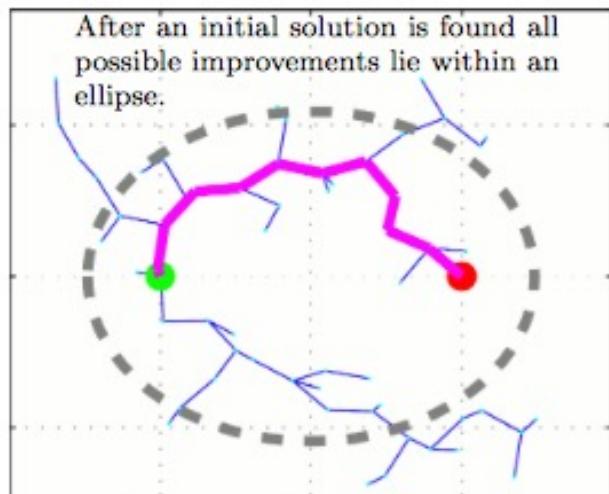
Algorithm 6: RRT*

```
1  $V \leftarrow \{x_{\text{init}}\}; E \leftarrow \emptyset;$ 
2 for  $i = 1, \dots, n$  do
3    $x_{\text{rand}} \leftarrow \text{SampleFree}_i;$ 
4    $x_{\text{nearest}} \leftarrow \text{Nearest}(G = (V, E), x_{\text{rand}});$ 
5    $x_{\text{new}} \leftarrow \text{Steer}(x_{\text{nearest}}, x_{\text{rand}}) ;$ 
6   if  $\text{ObstacleFree}(x_{\text{nearest}}, x_{\text{new}})$  then
7      $X_{\text{near}} \leftarrow \text{Near}(G = (V, E), x_{\text{new}}, \min\{\gamma_{\text{RRT}^*}(\log(\text{card}(V))/\text{card}(V))^{1/d}, \eta\}) ;$ 
8      $V \leftarrow V \cup \{x_{\text{new}}\};$ 
9      $x_{\text{min}} \leftarrow x_{\text{nearest}}; c_{\text{min}} \leftarrow \text{Cost}(x_{\text{nearest}}) + c(\text{Line}(x_{\text{nearest}}, x_{\text{new}}));$ 
10    foreach  $x_{\text{near}} \in X_{\text{near}}$  do // Connect along a minimum-cost path
11      if  $\text{CollisionFree}(x_{\text{near}}, x_{\text{new}}) \wedge \text{Cost}(x_{\text{near}}) + c(\text{Line}(x_{\text{near}}, x_{\text{new}})) < c_{\text{min}}$  then
12         $x_{\text{min}} \leftarrow x_{\text{near}}; c_{\text{min}} \leftarrow \text{Cost}(x_{\text{near}}) + c(\text{Line}(x_{\text{near}}, x_{\text{new}}))$ 
13     $E \leftarrow E \cup \{(x_{\text{min}}, x_{\text{new}})\};$ 
14    foreach  $x_{\text{near}} \in X_{\text{near}}$  do // Rewire the tree
15      if  $\text{CollisionFree}(x_{\text{new}}, x_{\text{near}}) \wedge \text{Cost}(x_{\text{new}}) + c(\text{Line}(x_{\text{new}}, x_{\text{near}})) < \text{Cost}(x_{\text{near}})$ 
16      then  $x_{\text{parent}} \leftarrow \text{Parent}(x_{\text{near}});$ 
17       $E \leftarrow (E \setminus \{(x_{\text{parent}}, x_{\text{near}})\}) \cup \{(x_{\text{new}}, x_{\text{near}})\}$ 
18
19 return  $G = (V, E);$ 
```

Informed RRT*

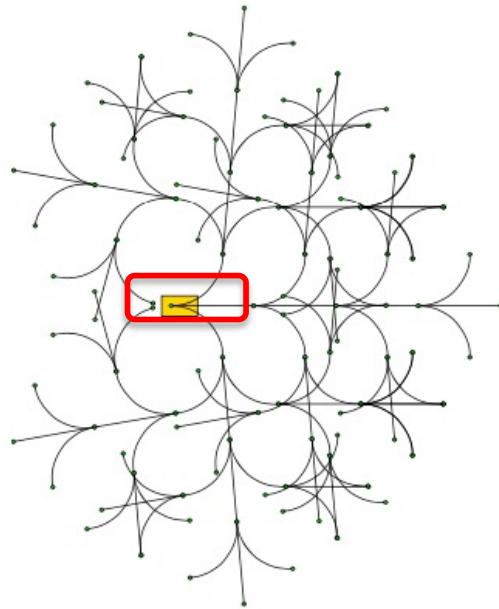
(2013, Gamell et al., searching within ellipsoids)

Key observation!

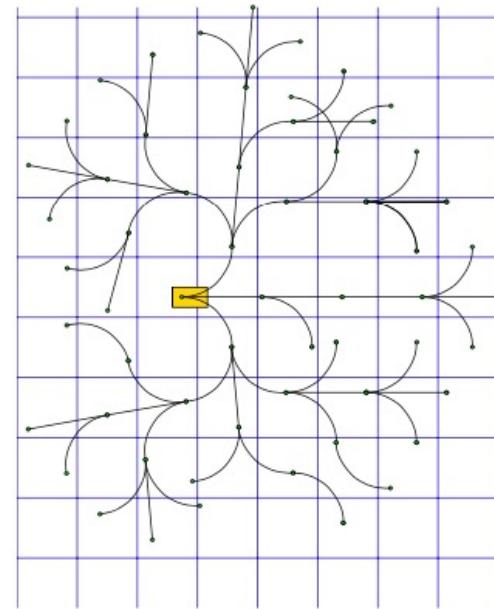


Other ways of biasing sampling are possible: i.e. Close to Visibility Graph solution...

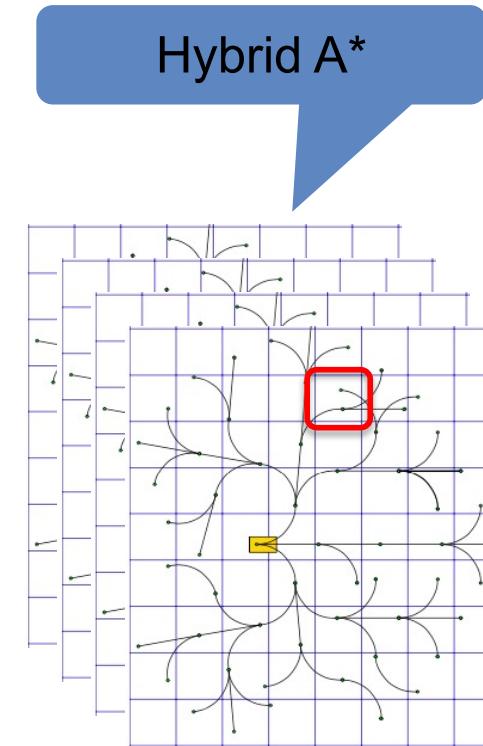
What about A* and grids?



If we just build a search tree we get copies of same state



Allowing just one state in each grid

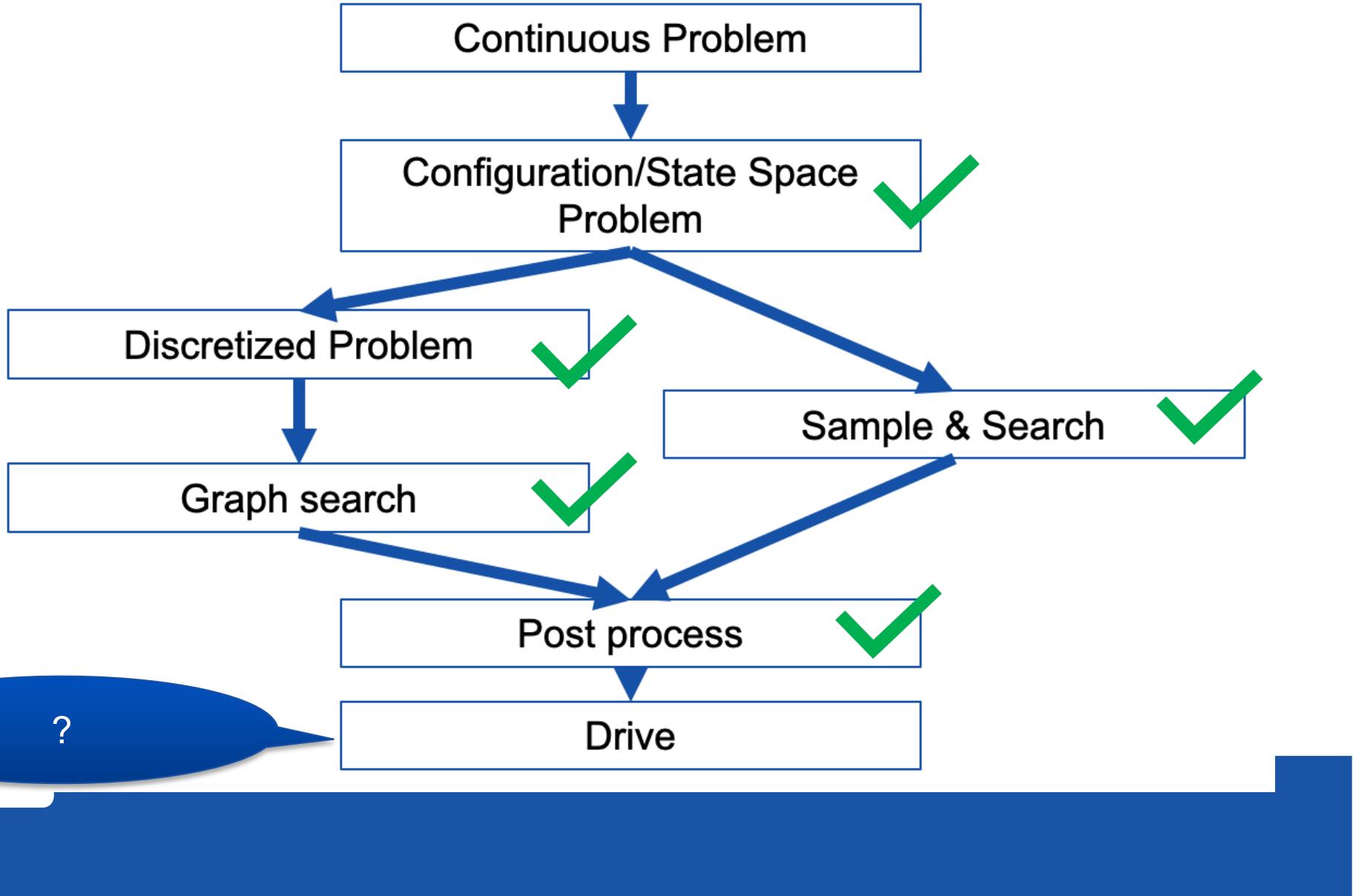


Allowing 4 states in each grid: $\theta=(0,\pi/2,\pi,3\pi/2)$

Hybrid A*



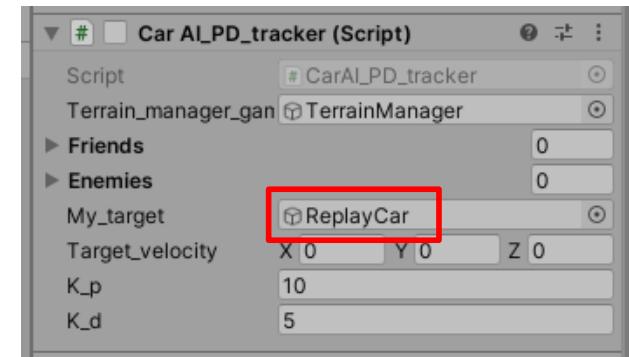
Common Path Planning Approach





How to drive along your planned path?

- Draw inspiration from
 - CarAI_PD_tracker.cs
 - Google “Pure pursuit controller”
- How fast should you go?
- What happens if you collide?
- What is best?
 - Advanced planning and simple driving
 - Simple planning and advanced driving





Driving along a path (youtube video)

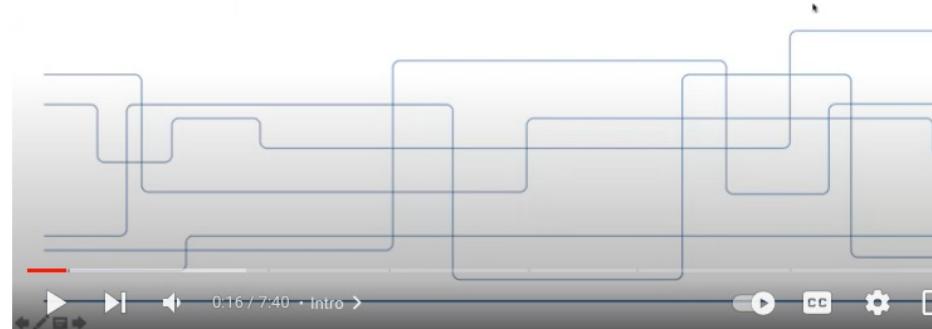
☰ YouTube SE

Search



Creating a very simple PD-controller Trajectory Tracking with the Unity

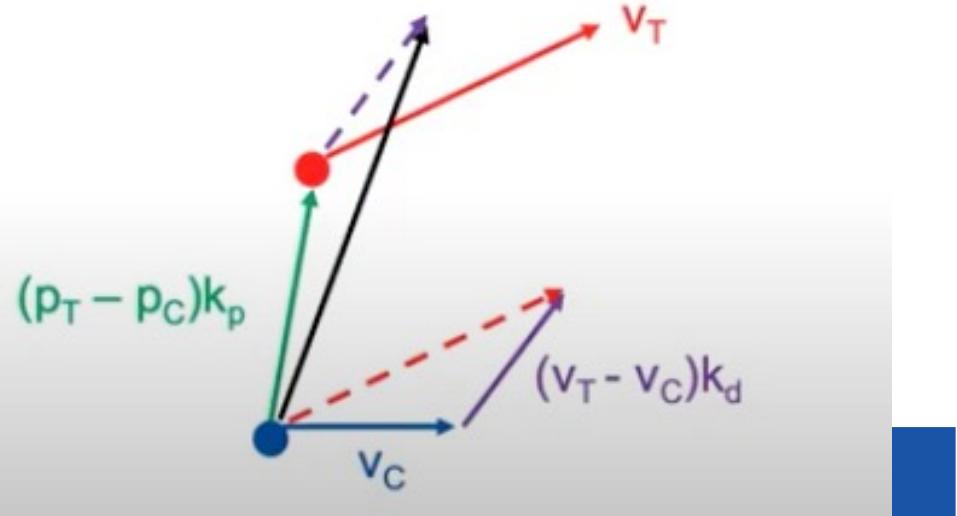
by Petter Ögren



Creating a simple PD-controller for trajectory tracking with a Unity car

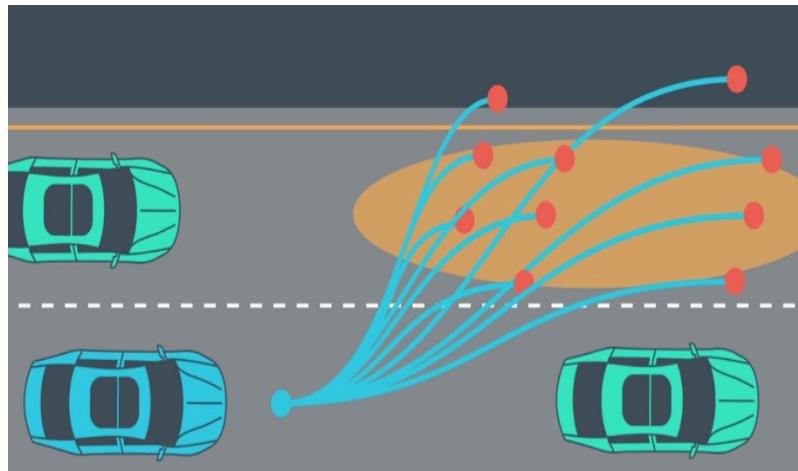
A standard PD-controller

$$\mathbf{a}_{\text{des}} = (\mathbf{p}_T - \mathbf{p}_C)k_p + (\mathbf{v}_T - \mathbf{v}_C)k_d$$

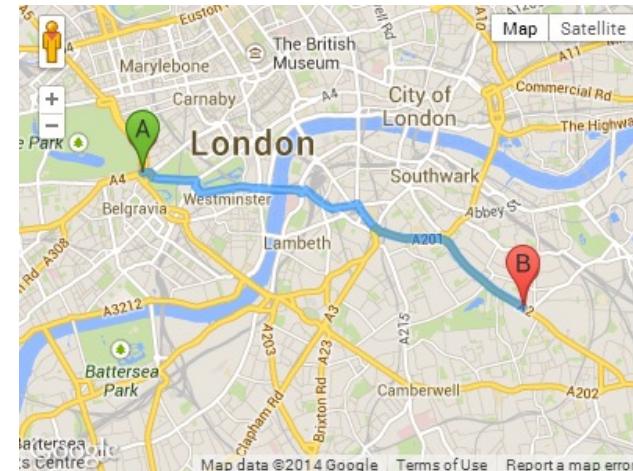


Multi Horizon Path Planning

5 sec horizon
Full vehicle model



5 hour horizon
Position is enough
(not heading/speed)





Remember:

You need at least **5 references described** in your report

The screenshot shows a KTH project reporting interface. On the left is a vertical sidebar with the following navigation links:

- Account
- Dashboard
- Courses
- Calendar
- Inbox (20)
- History
- Commons
- Help

The main content area has a header "Project reporting". Below it, a sub-section titled "Links" contains a list of 23 research papers and concepts, each with a link and a small icon. To the right of the content area is a large search bar with the Google Scholar logo and a placeholder "your text here...".

Project reporting

Project reporting will be carried out in the following form:

- Before the meeting (see deadline) each week:
 - Upload slides
 - Update progress report on Google Sheet ([link ↗](#))
 - Be prepared to give a short presentation at each meeting
- At the final meeting
 - Solve example problems similar to A,B,C
- In a report, in the form of a scientific paper, one week after each final meeting

Details regarding all of these can be found [here](#).

Links

Links to possibly (you decide) interesting material

- [Delayed D*](#) ↗
- [Hybrid A*](#) ↗
- [Hybrid A* in Darpa Urban Challenge](#) ↗
- [RRT](#) ↗
- [Visibility Graph](#) ↗
- [Voronoi diagram](#) ↗
- [RRT*](#) ↗
- [Kinodynamic RRT*](#) ↗
- [Urban Challenge approach](#) ↗
- [Obstacle Distances for Car-like robots](#) ↗
- [Informed RRT](#) ↗
- [Balancing Exploration and Exploitation in Sampling-Based Motion Planning](#) ↗
- [Optimal Motion Planning with the Half-Car Dynamical Model for Autonomous High-Speed Driving](#) ↗
- [Trajectory Tracking of a Car-Trailer System](#) ↗
- [Control of Mobile platforms using a virtual vehicle approach](#) ↗
- [Application of Hybrid A* to an Autonomous Mobile Robot for Path Planning in Unstructured Outdoor Environments](#) ↗
- [Plan and transform](#) ↗

[◀ Previous](#) [Next ▶](#)


your text here...



The End