

Microbial Network Evolution

*via critical connectors in directed reaction-centric
graphs metabolic networks*

Tara Pande

Background

Models and methods from the graph theory have been developed to characterize structural properties in various kinds of complex networks in social, technological, and biological areas [1, 2]. In the analysis of biological networks, graph theory has been successful in detecting global topological features of biological networks such as short path lengths, scale-freeness with the appearance of hubs [3], hierarchical modular structures [4], and network motifs [5].

"While the **topological analysis as a whole can give insight on network evolution** and cellular robustness, investigation of influences of individual nodes in a biological network has potential for practical applicability..."

analyses have been mostly performed using undirected bionetworks. Recent studies extended several global measures, such as in/out-degree distribution, betweenness, closeness, clustering coefficient, and modularity for application into directed networks [1, 12, 13]. These measures are strongly correlated with high degrees, focusing on densely connected sub-structures. Although they discovered global topological properties and global roles of individual nodes, they are insufficient to explain connections between modules and local connectivity, typically within a few of steps of neighbors surrounding the node, in networks with directed flows. For example, nodes of high degree have global topological importance in a network, however, the fact that they have so many interactions means that they are poor channels for conveying

[Sections](#)
[Figures](#)
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Fig. 1

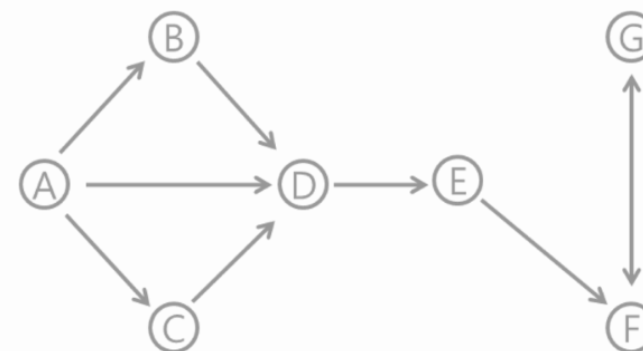
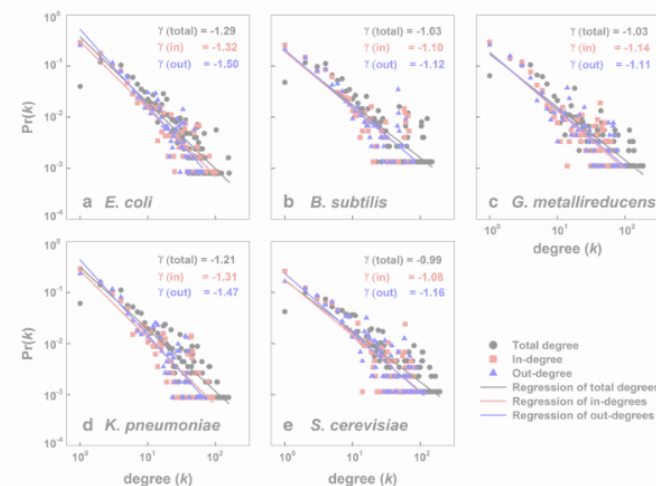
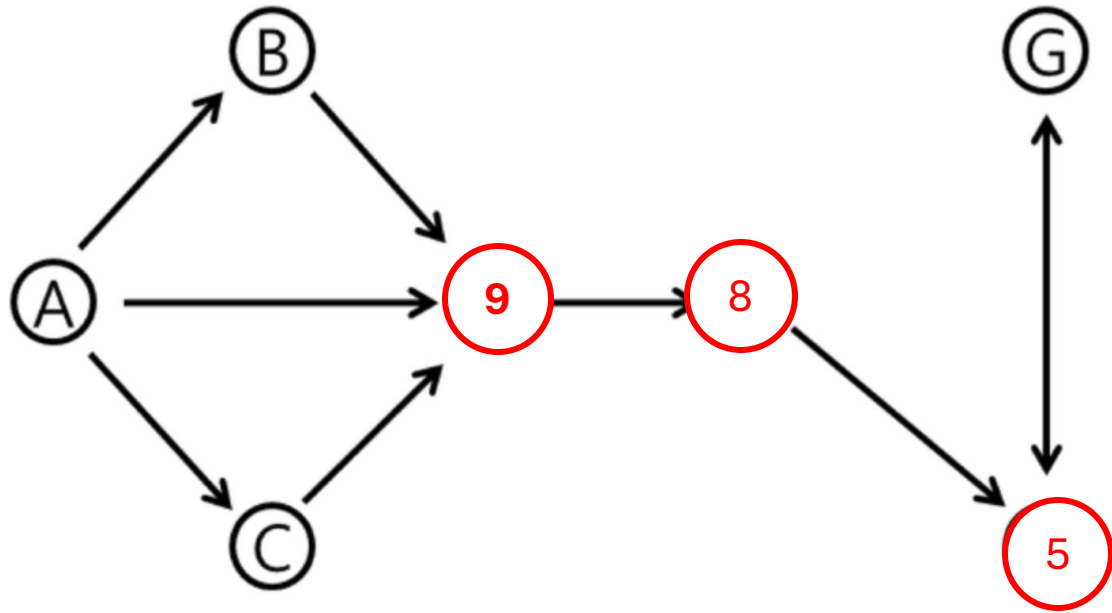

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Fig. 2


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Topology Metrics

Betweenness Centrality (B)

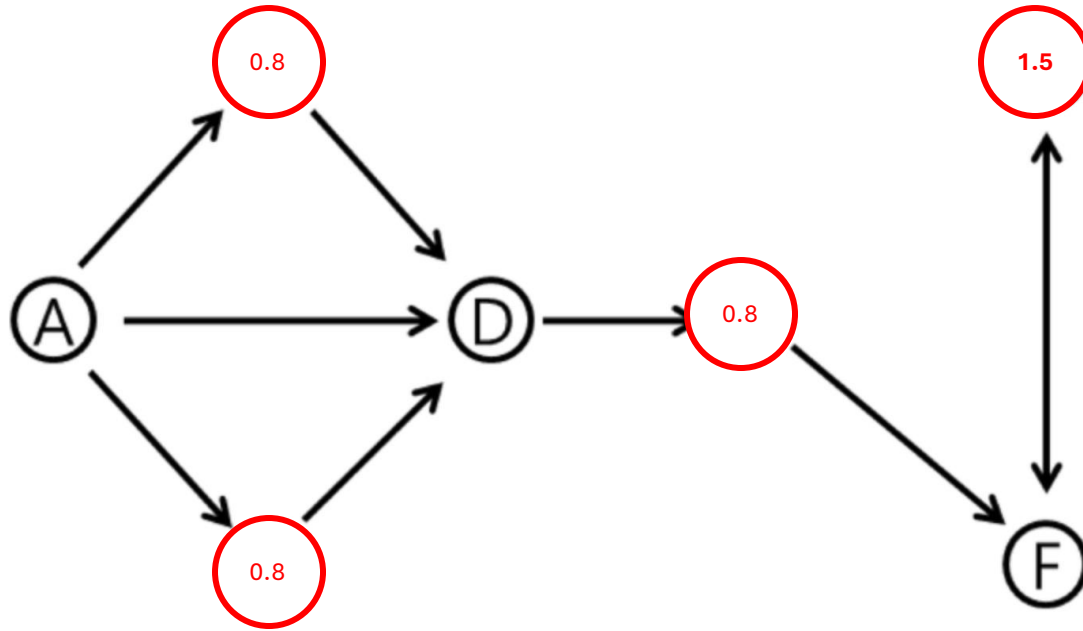


Node	B	BC	BrC	CN
A	0	0.2667	0	4
B	0	0.8571	0	0
C	0	0.8571	0	0
D	9	0.1364	1.2273	1
E	8	0.8571	6.8571	0
F	5	0.3333	1.6667	1
G	0	1.5000	0	0

$$B(i) = \sum_{j \neq i \neq k} \frac{\sigma_{jk}(i)}{\sigma_{jk}}$$

Bridging Coefficient (BC)

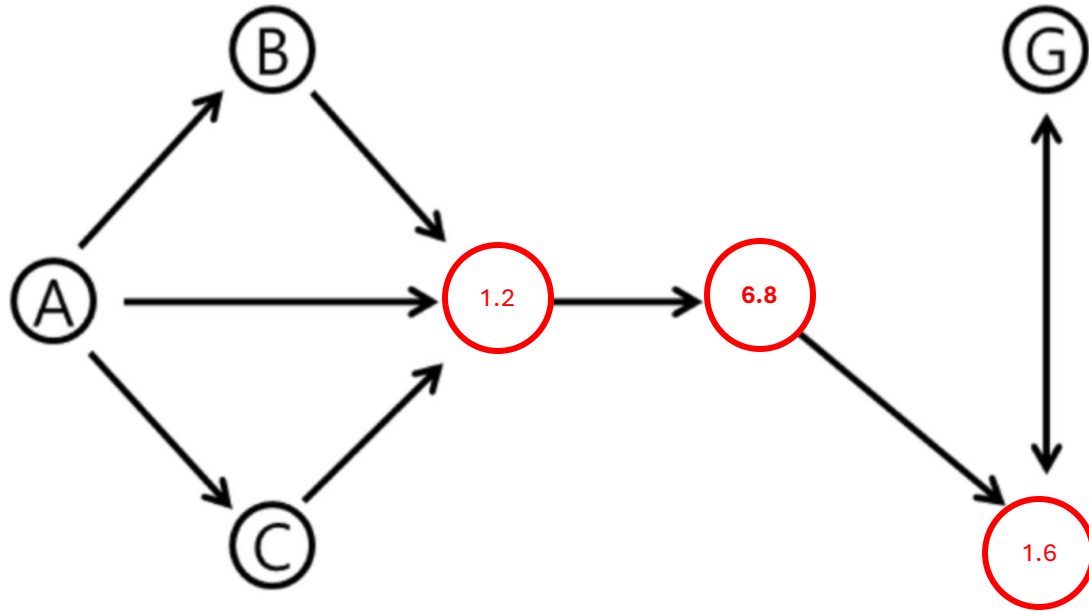
Undirected
calculation!



Node	B	BC	BrC	CN
A	0	0.2667	0	4
B	0	0.8571	0	0
C	0	0.8571	0	0
D	9	0.1364	1.2273	1
E	8	0.8571	6.8571	0
F	5	0.3333	1.6667	1
G	0	1.5000	0	0

$$BC(i) = \begin{cases} \frac{(degree_{total}(i))^{-1}}{\sum_{j \text{ in } \Lambda(i)} (degree_{total}(j))^{-1}} & \text{if } degree_{in}(i) \neq 0 \text{ and } degree_{out}(i) \neq 0 \\ 0 & \text{otherwise} \end{cases}$$

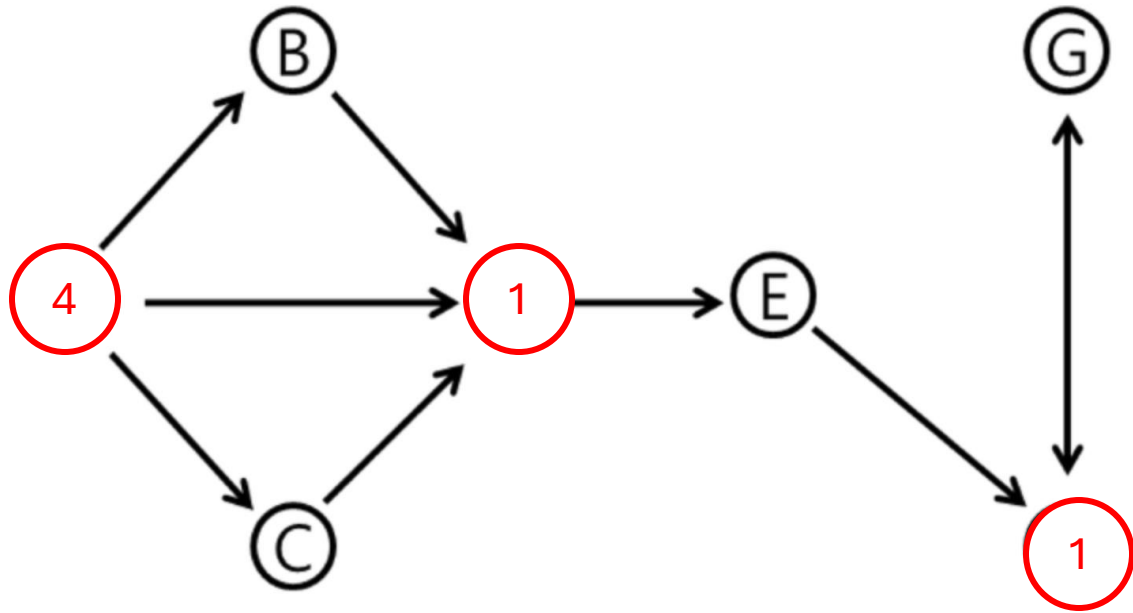
Bridging Centrality (BrC)



Node	B	BC	BrC	CN
A	0	0.2667	0	4
B	0	0.8571	0	0
C	0	0.8571	0	0
D	9	0.1364	1.2273	1
E	8	0.8571	6.8571	0
F	5	0.3333	1.6667	1
G	0	1.5000	0	0

$$BrC(i) = B(i) \times BC(i)$$

Cascade Number (CN)



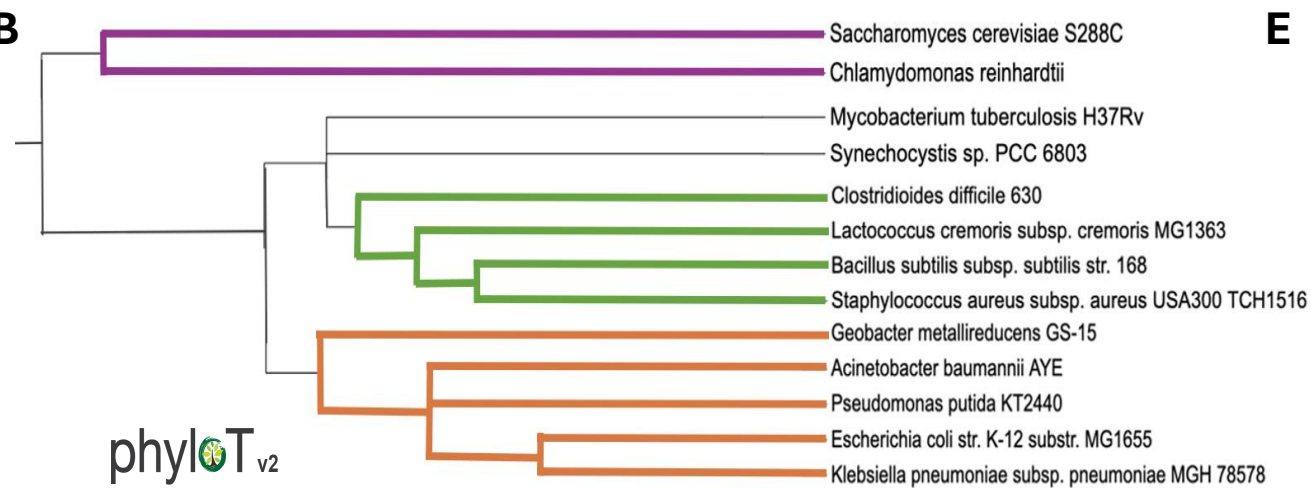
Node	B	BC	BrC	CN
A	0	0.2667	0	4
B	0	0.8571	0	0
C	0	0.8571	0	0
D	9	0.1364	1.2273	1
E	8	0.8571	6.8571	0
F	5	0.3333	1.6667	1
G	0	1.5000	0	0

Methods & Results

A

Model	Organism	Phylum
IAF987	<i>Geobacter metallireducens</i> GS-15	<i>Pseudomonadota</i>
iCN718	<i>Acinetobacter baumannii</i> AYE	<i>Pseudomonadota</i>
iCN900	<i>Clostridioides difficile</i> 630	<i>Bacillota</i>
iEK1008	<i>Mycobacterium tuberculosis</i> H37Rv	<i>Actinomycetota</i>
iJN678	<i>Synechocystis</i> sp. PCC 6803	<i>Cyanobacteriota</i>
iJN1463	<i>Pseudomonas putida</i> KT2440	<i>Pseudomonadota</i>
iJO1366	<i>Escherichia coli</i> str. K-12 substr. MG1655	<i>Pseudomonadota</i>
iMM904	<i>Saccharomyces cerevisiae</i> S288C	<i>Ascomycota</i> (E)
iNF517	<i>Lactococcus lactis</i> subsp. <i>cremoris</i> MG1363	<i>Bacillota</i>
iRC1080	<i>Chlamydomonas reinhardtii</i>	<i>Chlorophyta</i> (E)
iYL1228	<i>Klebsiella pneumoniae</i> subsp. <i>pneumoniae</i> MGH 78578	<i>Pseudomonadota</i>
iYO884	<i>Bacillus subtilis</i> subsp. <i>subtilis</i> str. 168	<i>Bacillota</i>
iYS854	<i>Staphylococcus aureus</i> subsp. <i>aureus</i> USA300_TCH1516	<i>Bacillota</i>

B



E

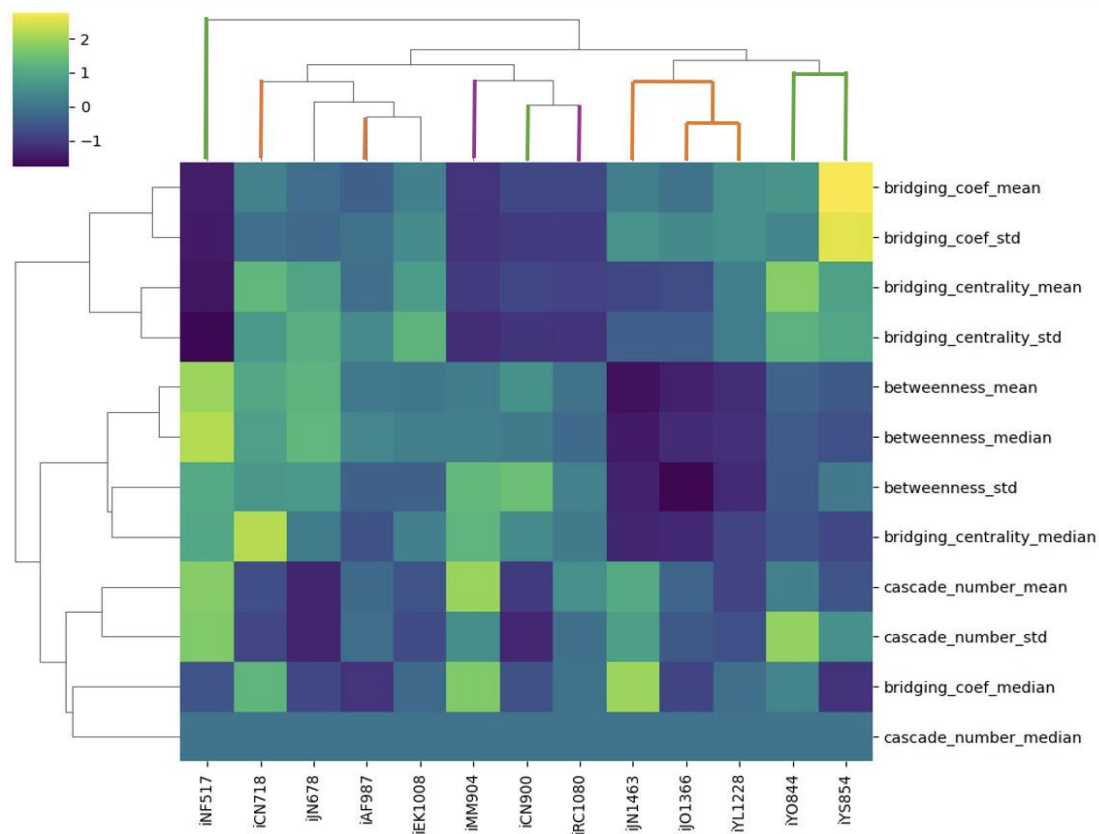
Robinson–Foulds (RF) Distance Ratio

	NT	FE
GT	14/18 (0.778)	14/18 (0.778)
NT		18/20 (0.900)

Triplets Distance (Local)

	NT	FE
GT	14	14
NT		18

C



D

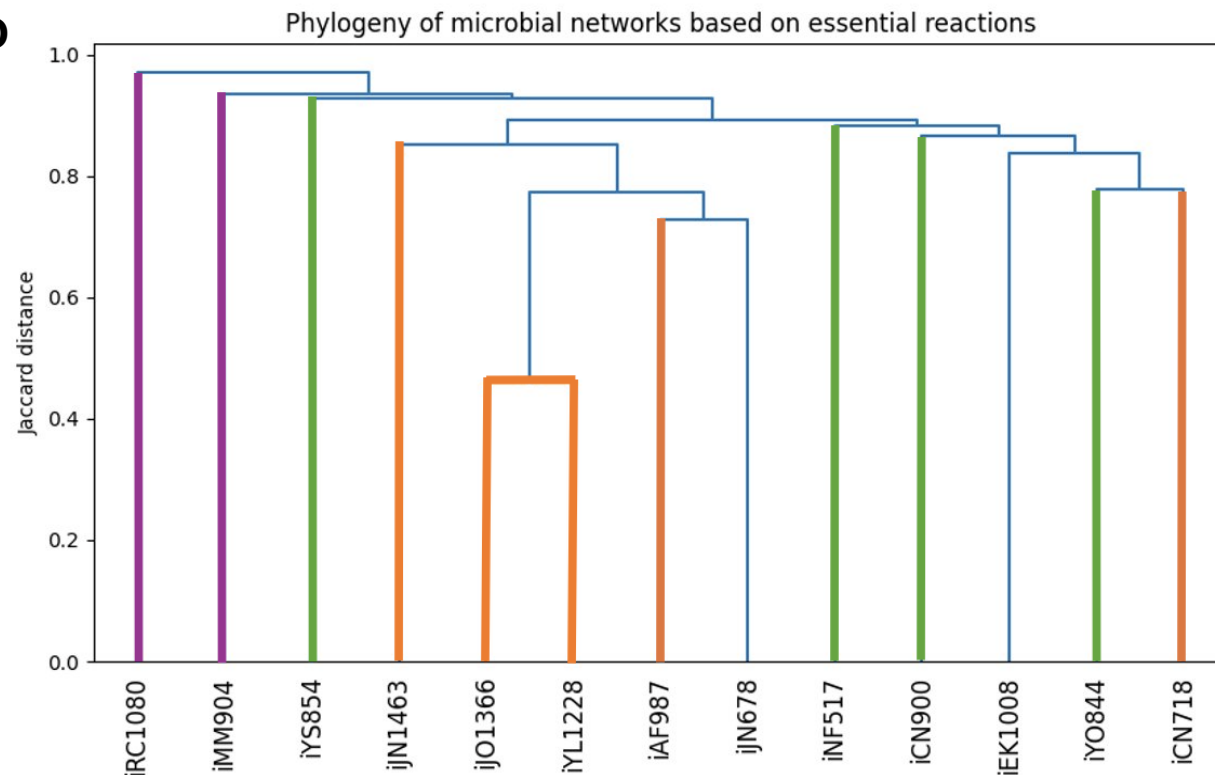


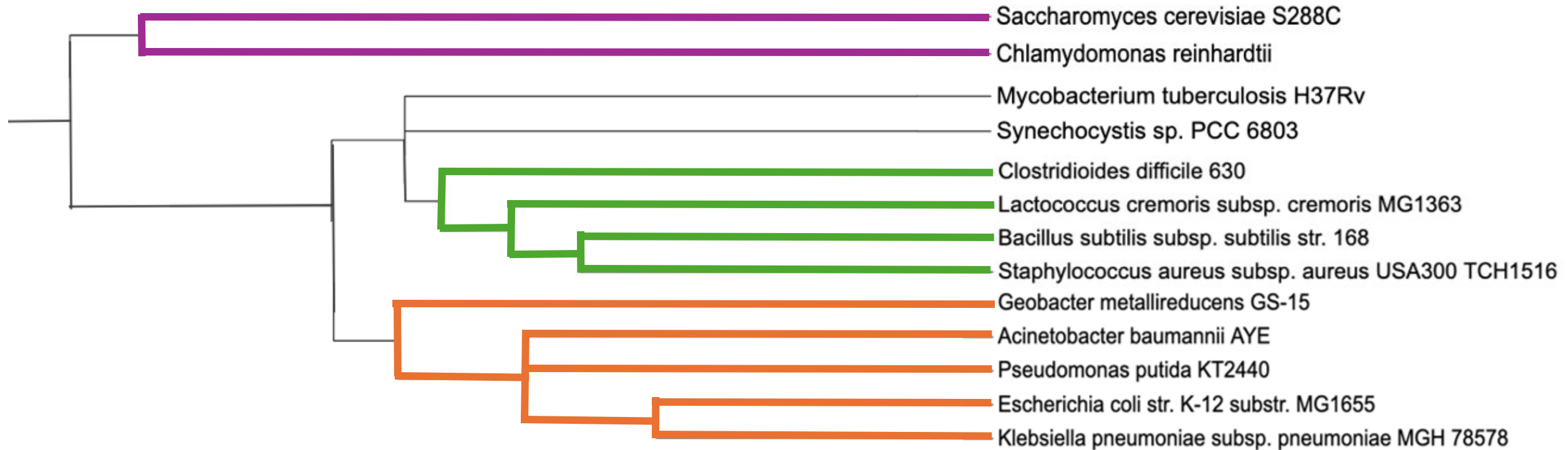
Figure A

Model Organisms Dataset

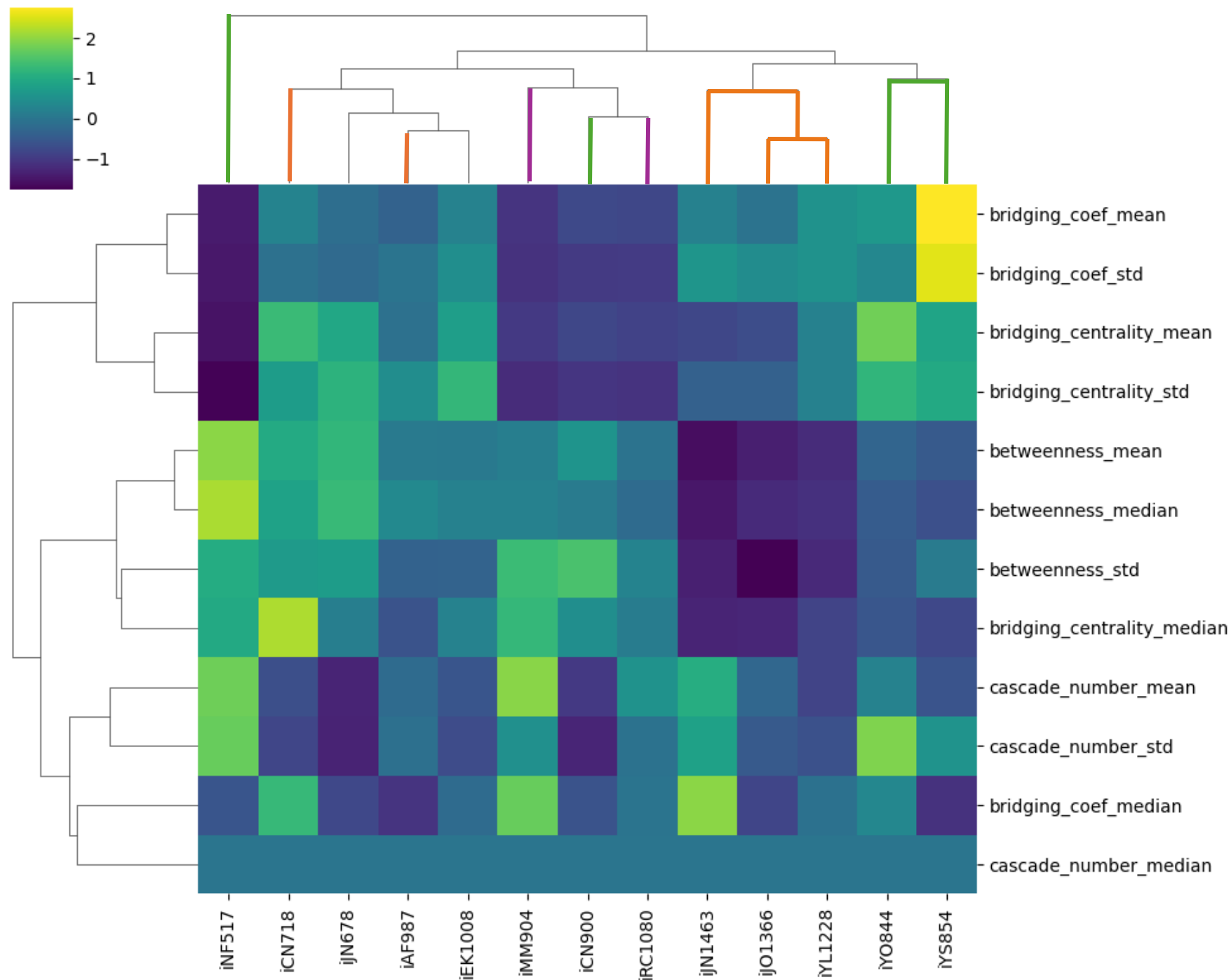
Model	Organism	Phylum	EssR
iAF987	Geobacter metallireducens GS-15	Pseudomonadota	8.79%
iCN718	Acinetobacter baumannii AYE	Pseudomonadota	7.39%
iCN900	Clostridioides difficile 630	Bacillota	8.14%
iEK1008	Mycobacterium tuberculosis H37Rv	Actinomycetota	8.08%
iJN678	Synechocystis sp. PCC 6803	Cyanobacteriota	8.57%
iJN1463	Pseudomonas putida KT2440	Pseudomonadota	7.69%
iJO1366	Escherichia coli str. K-12 substr. MG1655	Pseudomonadota	7.55%
iMM904	Saccharomyces cerevisiae S288C	Ascomycota (E)	10.0%
iNF517	Lactococcus lactis subsp. cremoris MG1363	Bacillota	9.68%
iRC1080	Chlamydomonas reinhardtii	Chlorophyta (E)	7.49%
iYL1228	Klebsiella pneumoniae subsp. pneumoniae MGH 78578	Pseudomonadota	6.76%
iYO884	Bacillus subtilis subsp. subtilis str. 168	Bacillota	6.32%
iYS854	Staphylococcus aureus subsp. aureus USA300_TCH1516	Bacillota	7.70%

Figure B

Expected Microbial Evolution



Network Topology Dendrogram



Topology Weaknesses

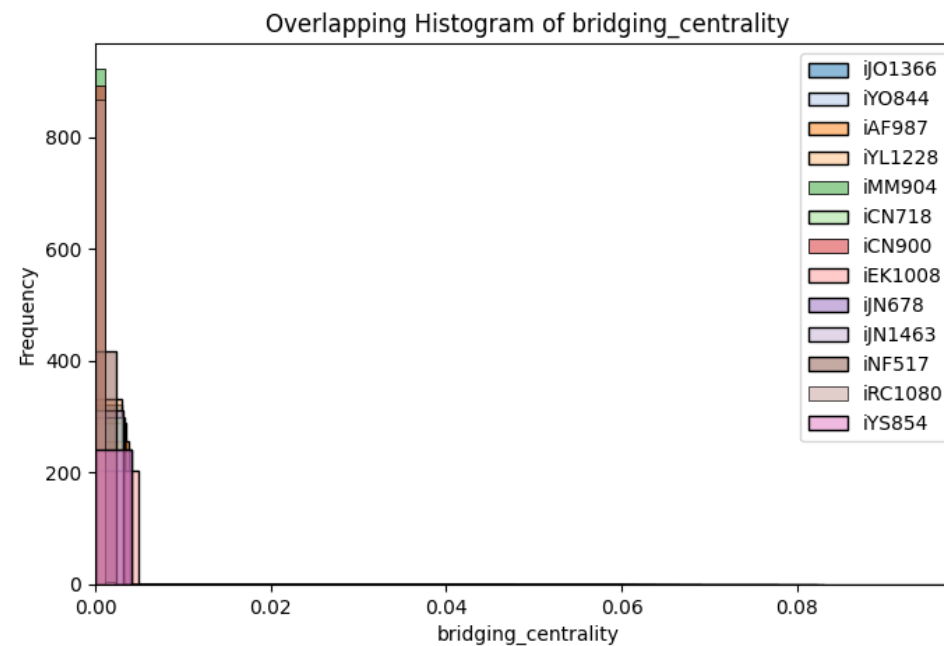
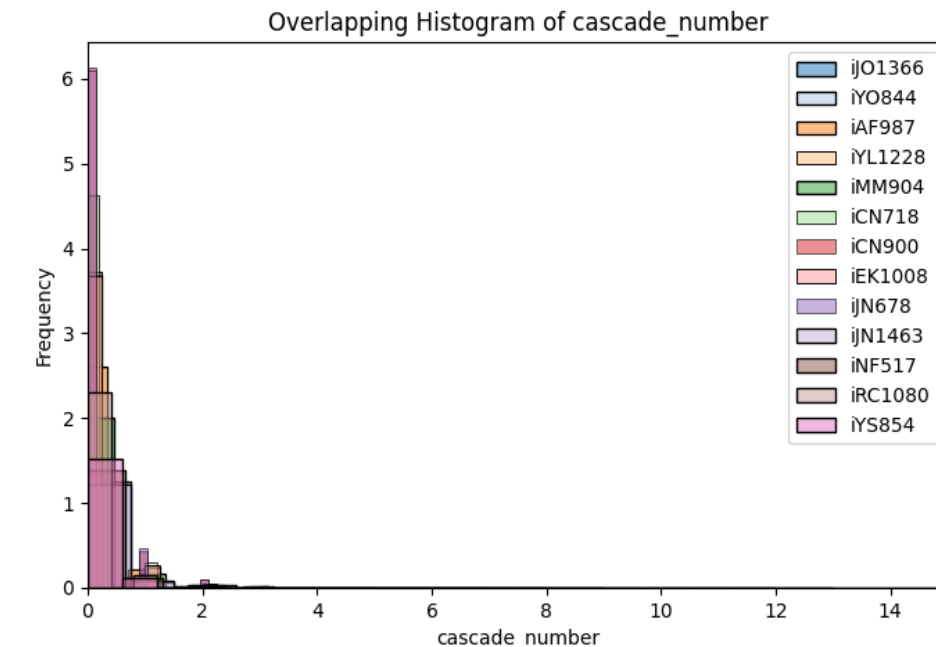
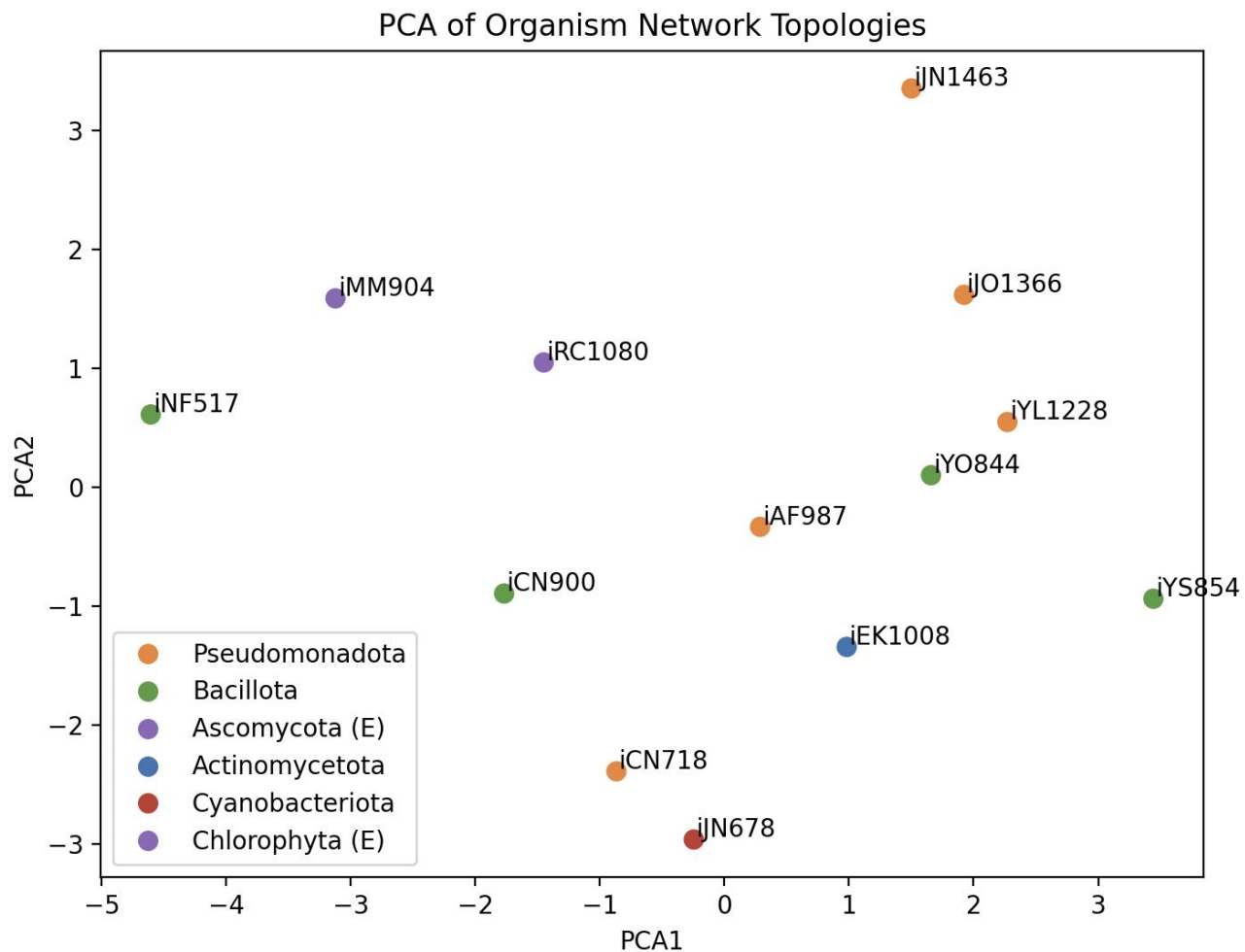


Figure D

Functional
Essentiality
Phylogram

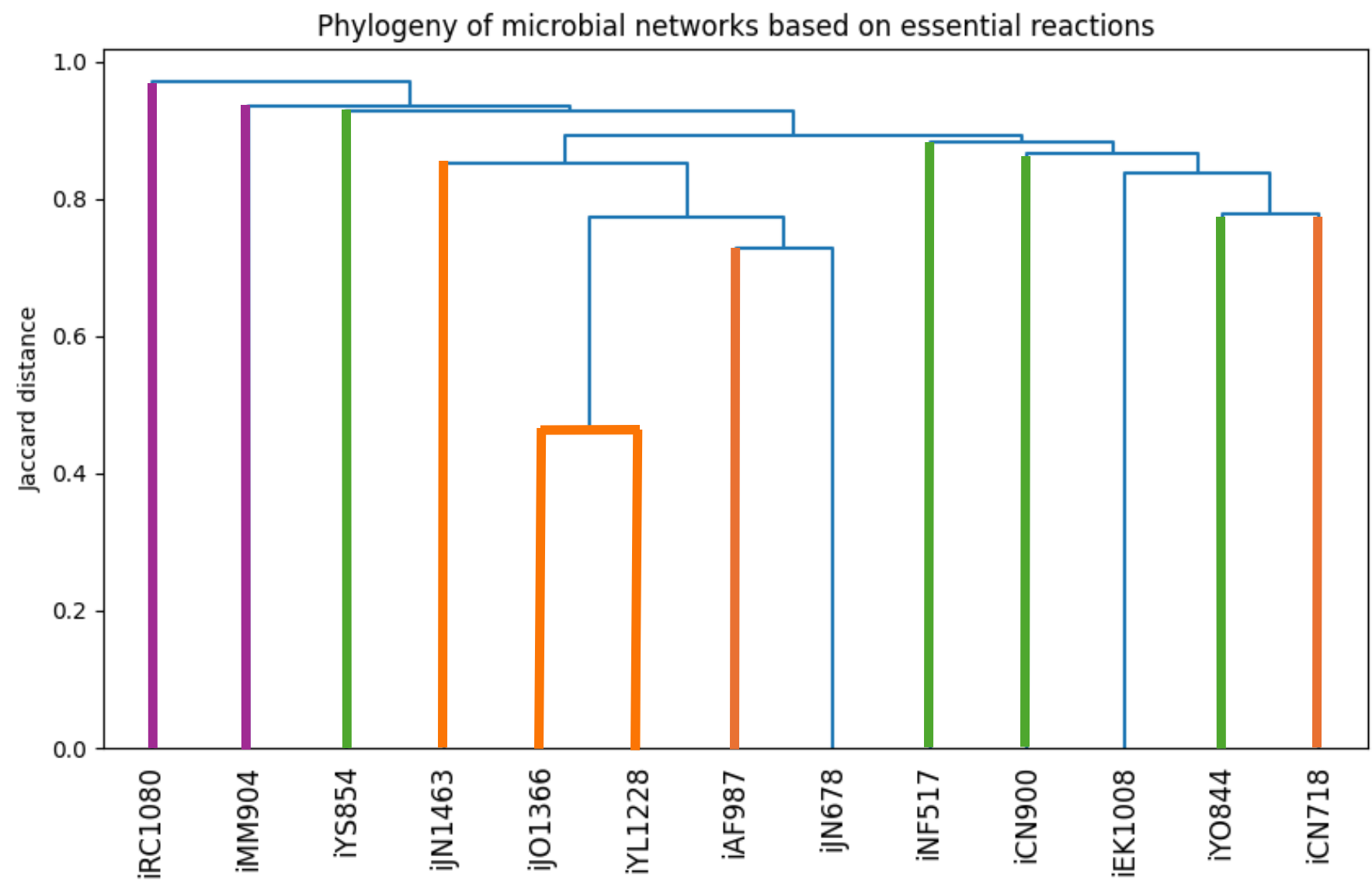


Figure E Phylogeny Metrics

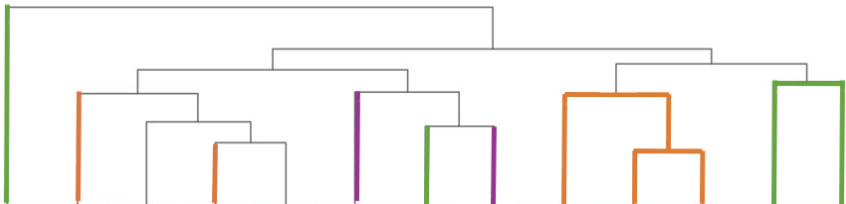
Robinson–Foulds (RF)
Distance Ratio

	NT	FE
GT	14/18 (0.778)	14/18 (0.778)
NT		18/20 (0.900)

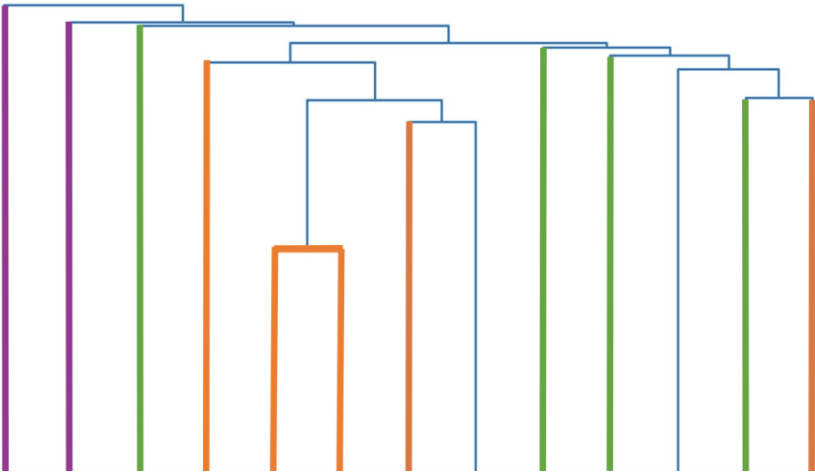
Triplets Distance (Local)

	NT	FE
GT	14	14
NT		18

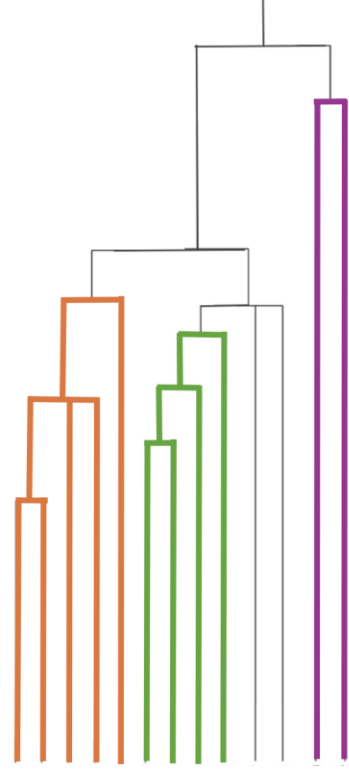
Network Topology (NT)



Functional Essentiality (FE)

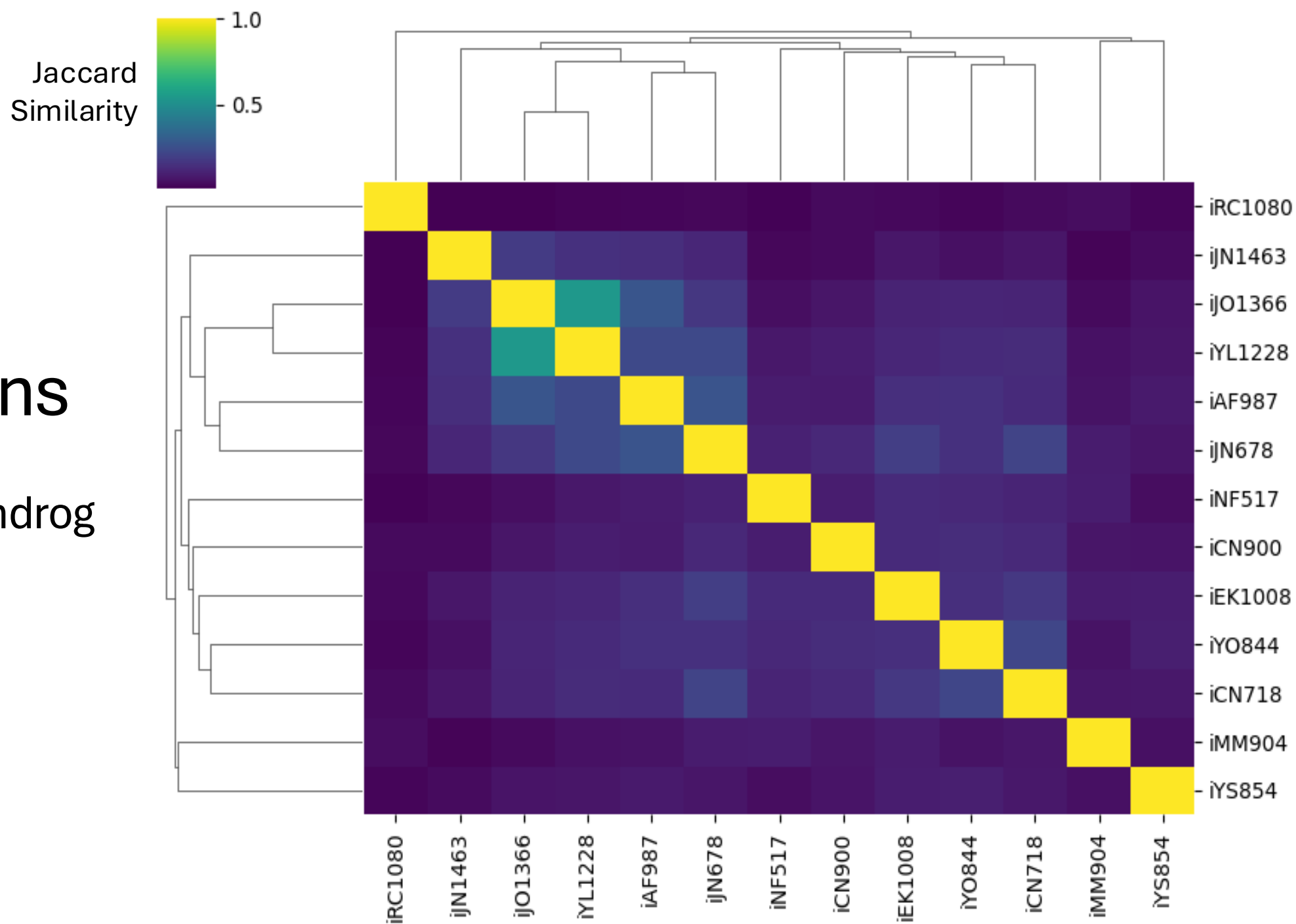


Ground Truth (GT)



Conclusions

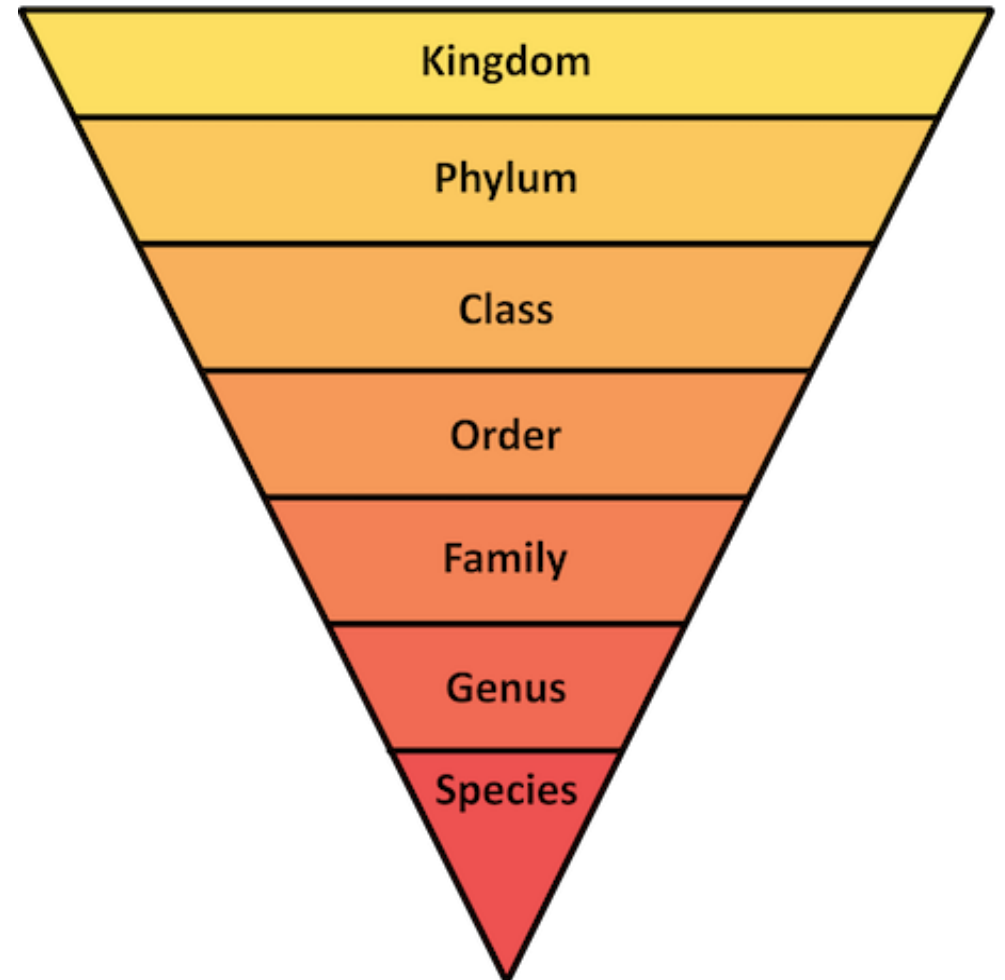
Functional Essentiality Dendro- gram



Conclusions

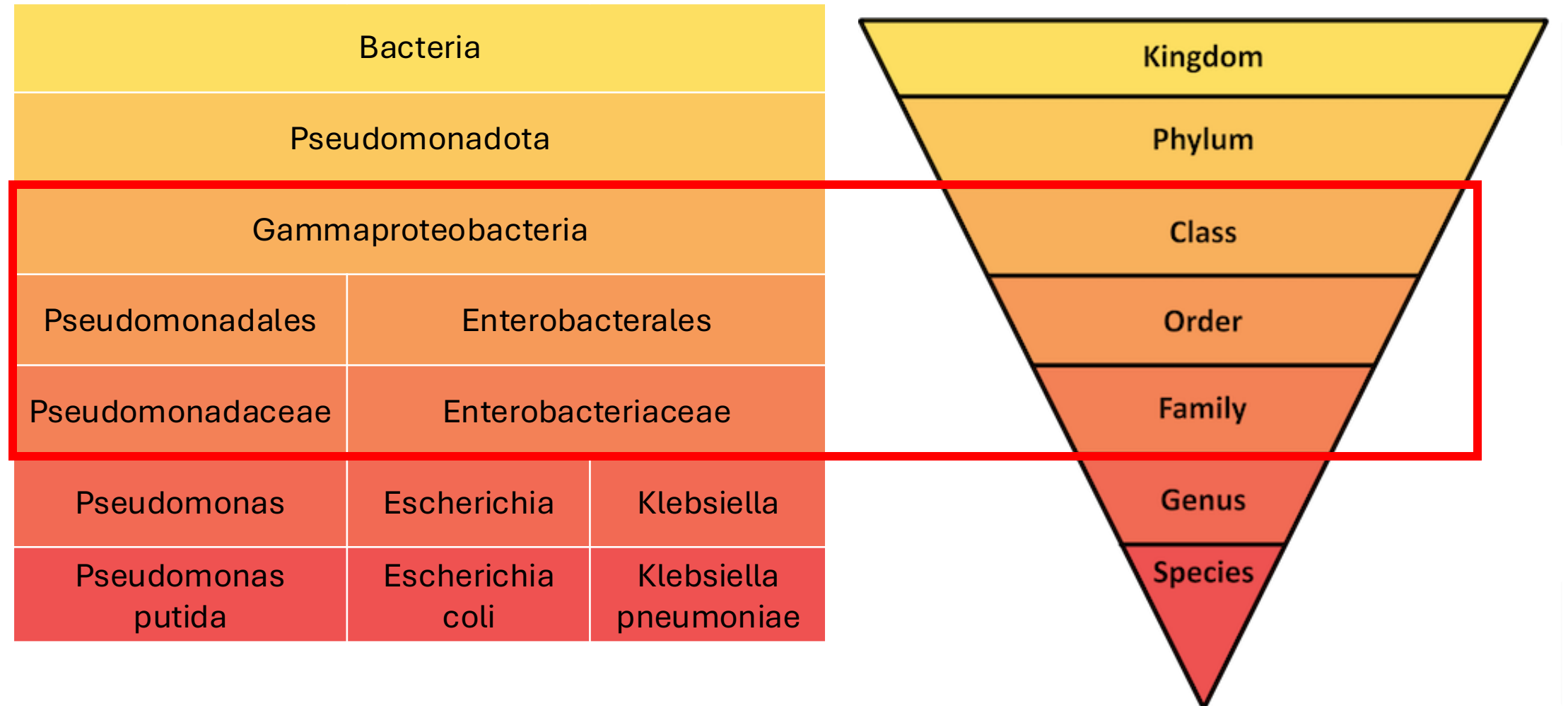
NCBI Taxonomical Hierarchy

Bacteria		
Pseudomonadota		
Gammaproteobacteria		
Pseudomonadales	Enterobacterales	
Pseudomonadaceae	Enterobacteriaceae	
Pseudomonas	Escherichia	Klebsiella
Pseudomonas putida	Escherichia coli	Klebsiella pneumoniae

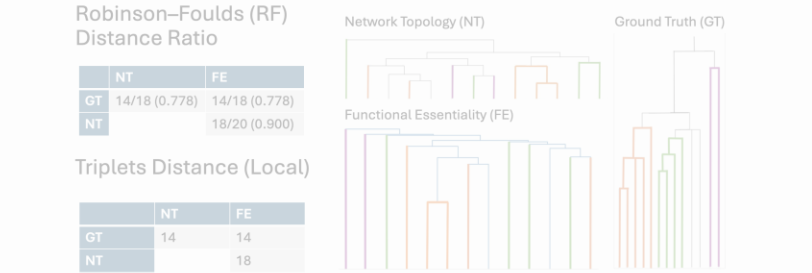
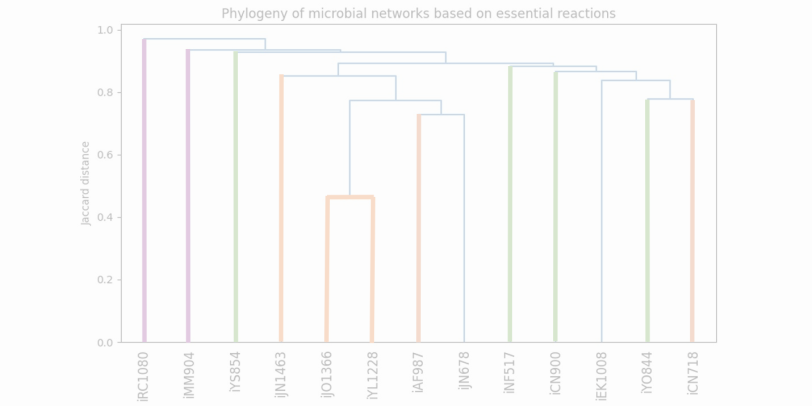
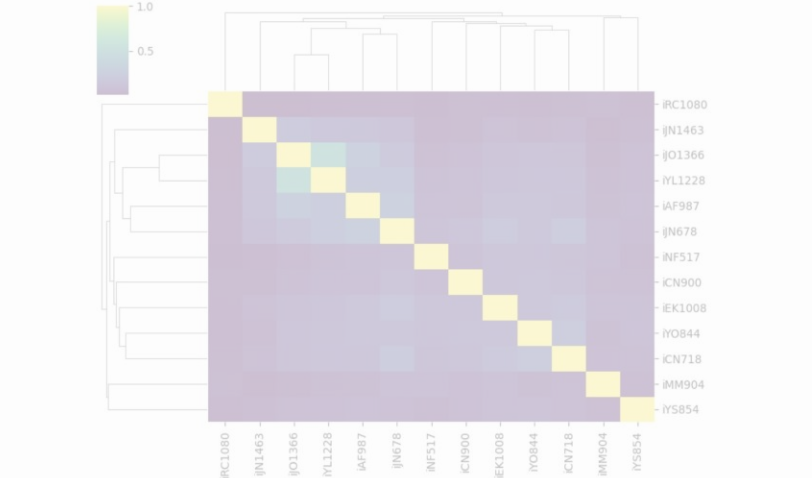
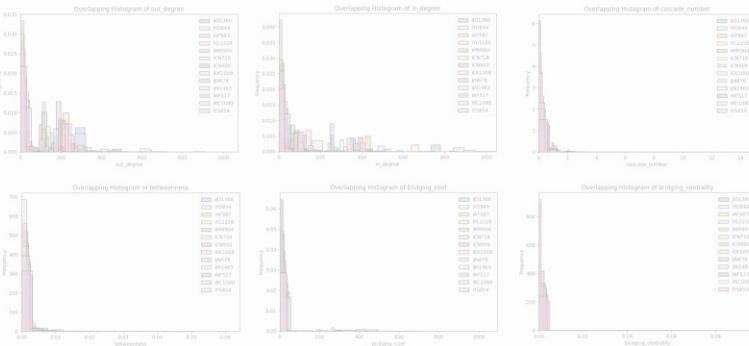
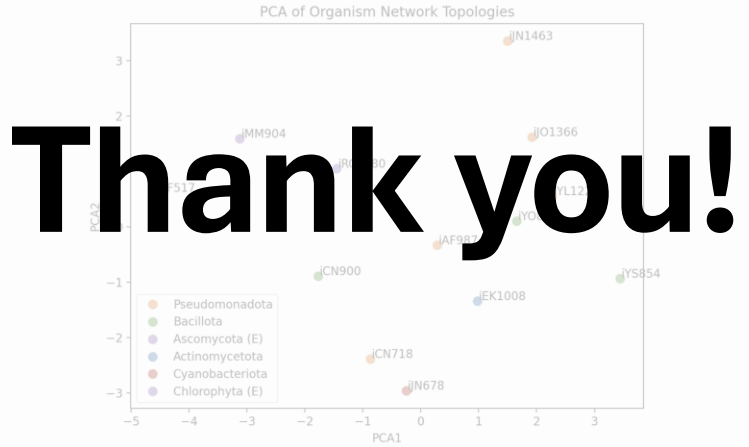
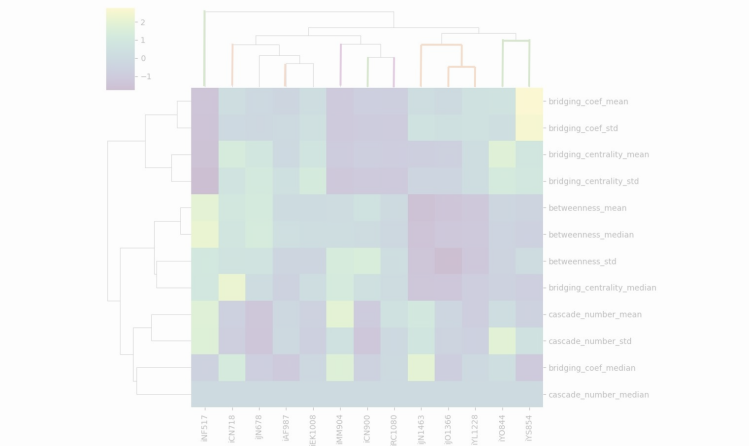
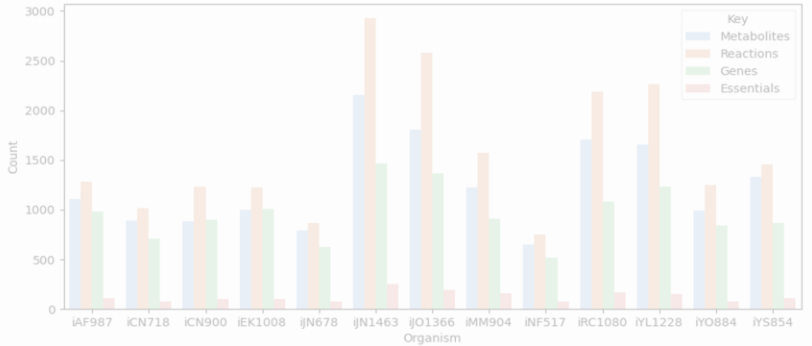
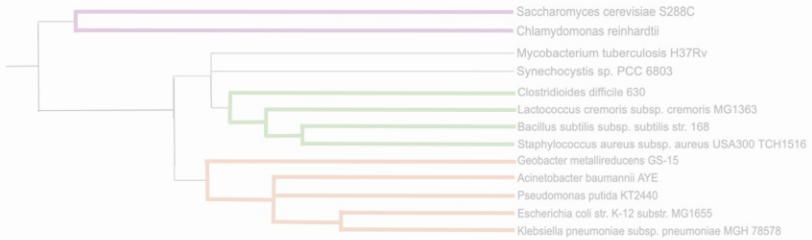


Conclusions

NCBI Taxonomical Hierarchy



Model	Organism	Phylum
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iYO884	Bacillus subtilis subsp. subtilis str. 168	Bacillota
iYS854	Staphylococcus aureus subsp. aureus USA300_TCH1516	Bacillota



Supplemental Figures

Figure S1 Model Organism Network Counts

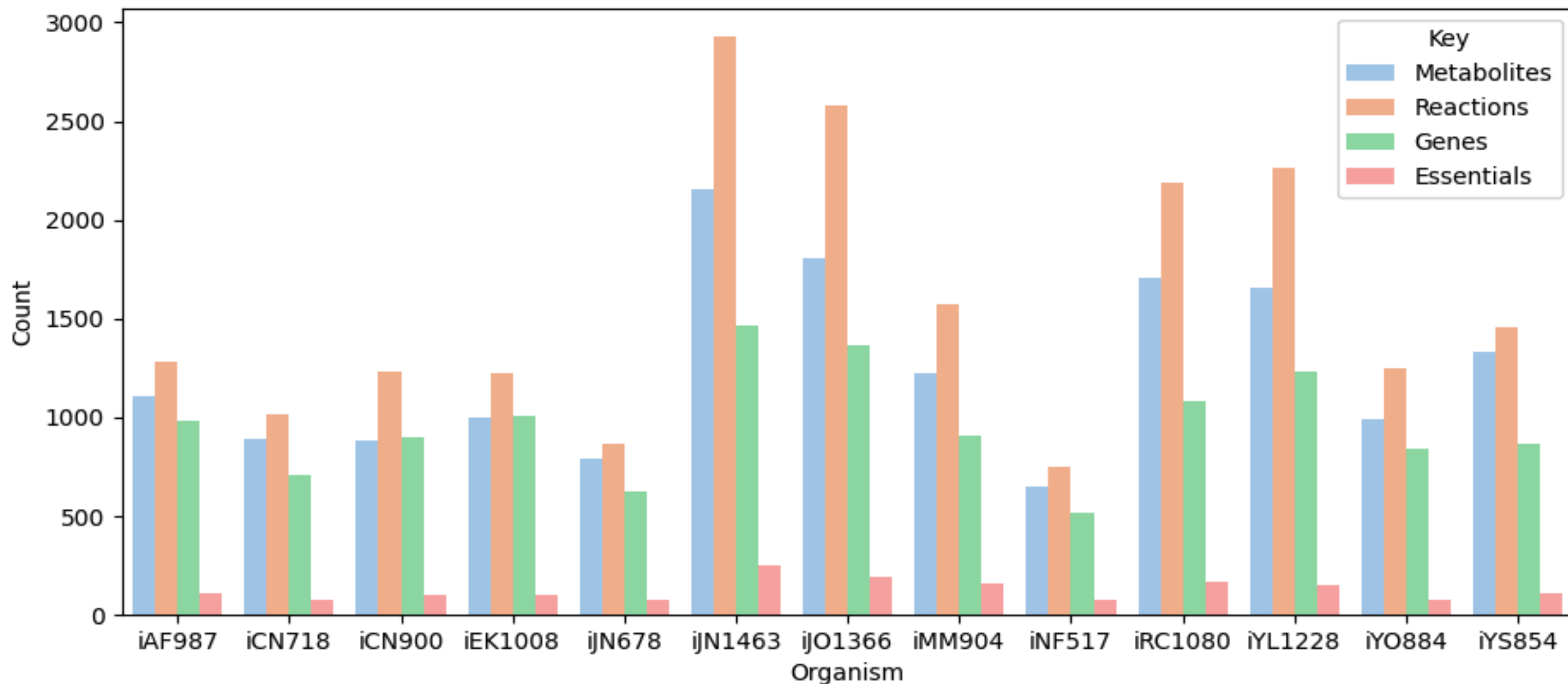


Figure S2

Network
Topology
PCA

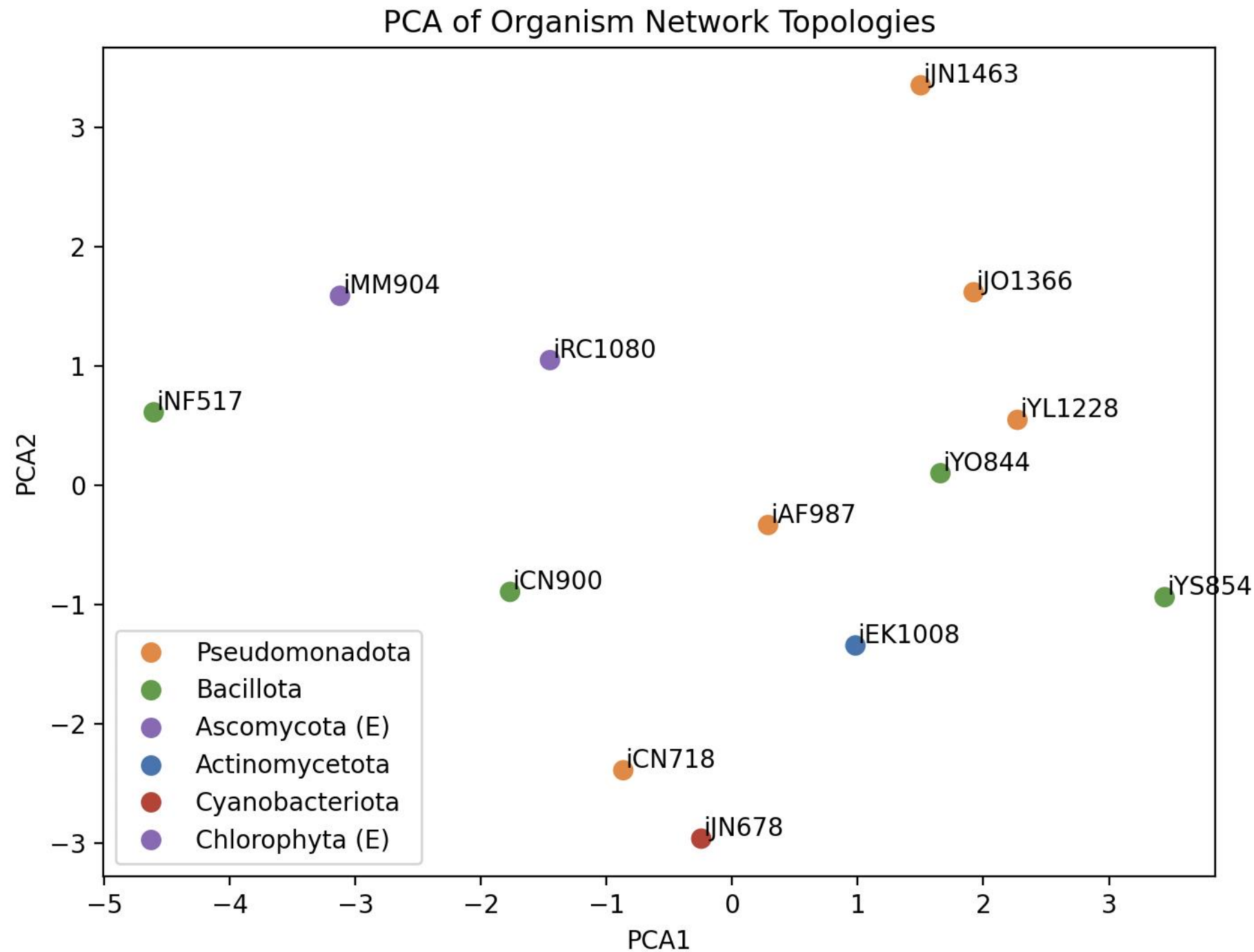
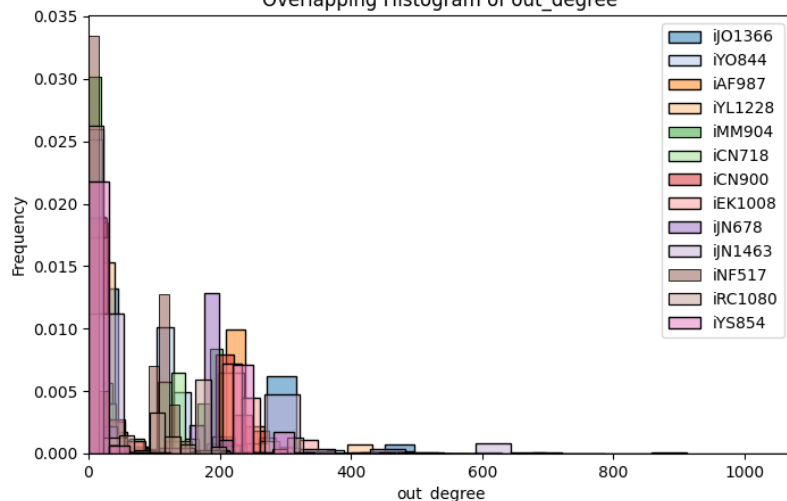
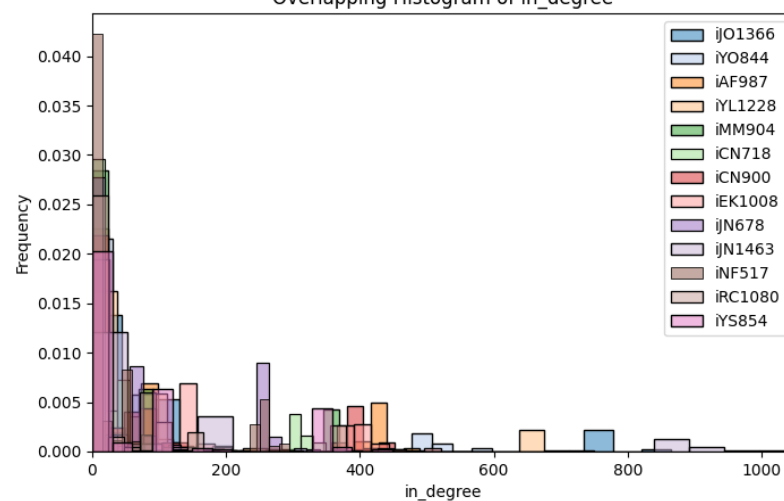


Figure S3 Network Topology Distributions

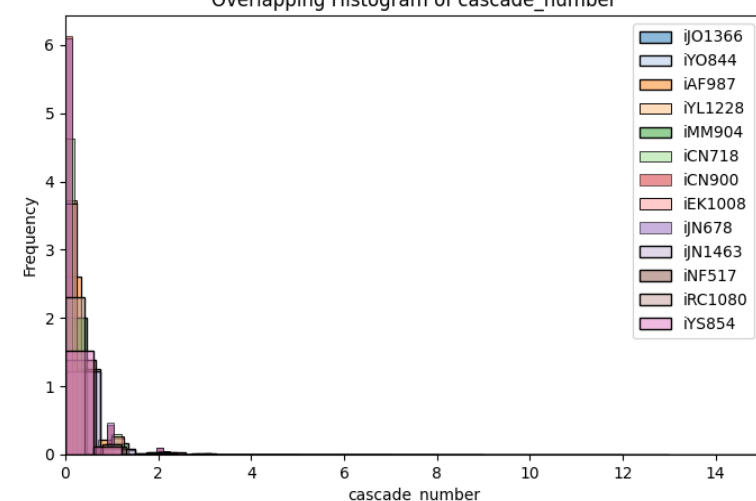
Overlapping Histogram of out_degree



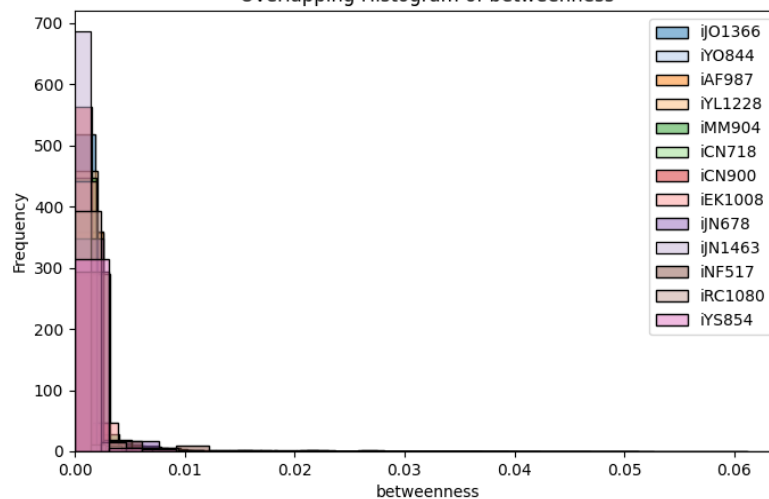
Overlapping Histogram of in_degree



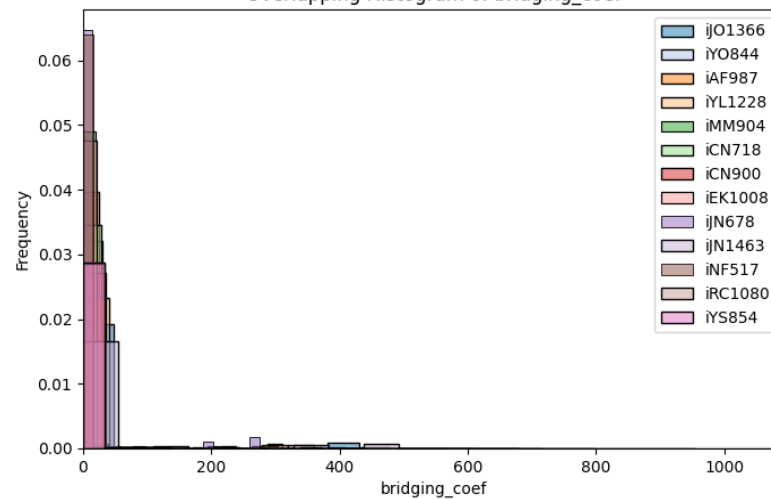
Overlapping Histogram of cascade_number



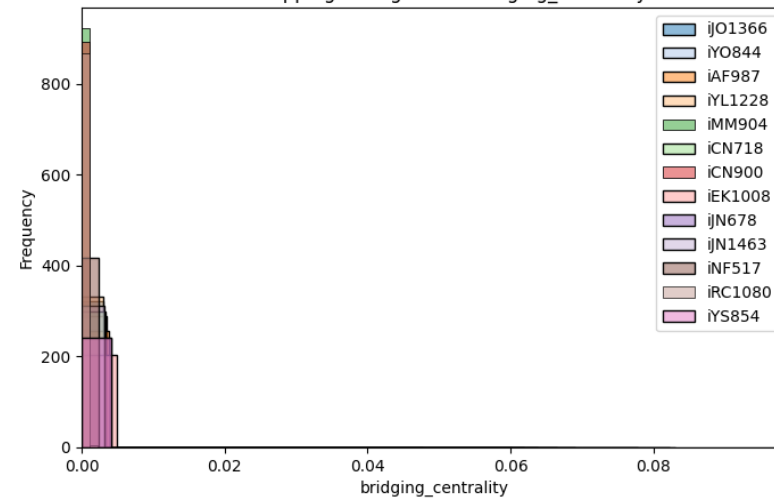
Overlapping Histogram of betweenness



Overlapping Histogram of bridging_coef



Overlapping Histogram of bridging_centralty



Functional Essentiality Heatmap & Dendrogram

