

# Foundations of Electrical Engineering

## Queensland University of Technology

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# 1 Electrical Circuits

## 1.1 Fundamental Quantities

Name	Definition	Symbol	Unit
Charge	Electric charge is a fundamental property of matter that governs how particles are affected by an electromagnetic field.	$q$	Coulomb (C)
Current	$i = \frac{dq}{dt} \iff 1 \text{ A} = 1 \text{ C s}^{-1}$	$i$	Ampere (A)
Voltage	$v = \frac{dw}{dq} \iff 1 \text{ V} = 1 \text{ J C}^{-1}$	$v$	Volt (V)
Power	$p = \frac{dw}{dt} \iff 1 \text{ W} = 1 \text{ J s}^{-1}$	$p$	Watt (W)

**Charge in an electron.**  $q = 1.6022 \times 10^{-19} \text{ C}$ .

**Electric Power.**  $p = \frac{dw}{dt} = vi$ .

## 1.2 Passive Sign Convention

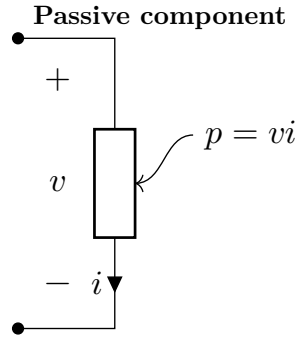


Figure 1: Energy dissipated.

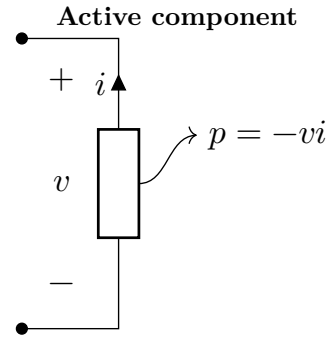


Figure 2: Energy produced.

**Theorem 1.2.1** (Power Balance).

$$p_{\text{net}} = 0$$

**Theorem 1.2.2** (Energy).

$$w(\tau) = \int_0^\tau p(t) dt$$

## 1.3 Circuits and Sources

**Definition 1.3.1** (Circuits). A circuit is a mathematical model that approximates a real system. It is built from ideal circuit elements connected by ideal wires.

**Definition 1.3.2** (Voltage Source). Produces or dissipates power at a specified voltage with whatever current is required.

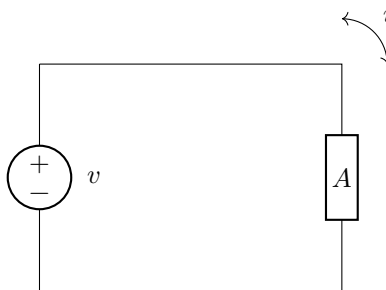


Figure 3: Voltage Source –  $v$  is specified,  $i$  varies depending on circuit element  $A$ .

**Definition 1.3.3** (Current Source). Produces or dissipates power at a specified current with whatever voltage is required.

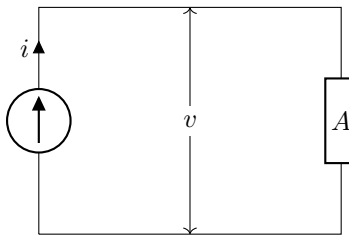


Figure 4: Current Source –  $i$  is specified,  $v$  varies depending on circuit element  $A$ .

## 1.4 Connected Sources

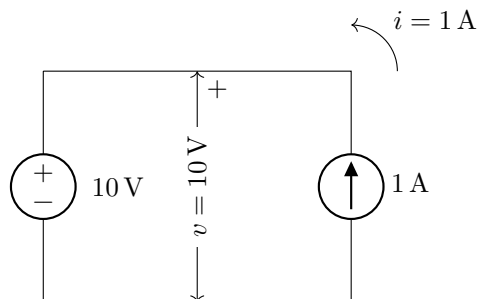


Figure 5: Example of a connected voltage and current source.

- The voltage source sets  $v$  to 10 V, with the upper wire being positive.

- The current source sets  $i$  to 1 A, flowing anticlockwise.
  - Therefore 10 W of power is produced by the current source and dissipated by the voltage source.
1. Two voltage sources must be connected at the same terminals and supply the same voltage.
  2. Two current sources must flow in the same direction and supply the same current.

## 1.5 Resistors

**Definition 1.5.1** (Resistor). Resistors dissipate power, and the voltage across both terminals is proportional to the current.

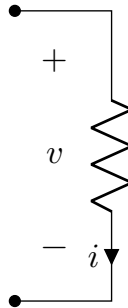


Figure 6: Resistor Circuit Symbol

**Theorem 1.5.1** (Voltage through a resistor).

$$v = iR$$

**Corollary 1.5.1.1** (Power dissipated by a resistor).

$$p = vi = i^2R = \frac{v^2}{R}$$

## 2 Simple Resistive Circuits

### 2.1 Ignored Physics

1. Electrical effects occur instantaneously, so there is no time delay along the wires.
2. The net charge on every component is zero. Charge is never lost or gained.
3. There is no magnetic coupling between the components.

### 2.2 Kirchhoff's Laws

**Definition 2.2.1** (Kirchhoff's Current Law (KCL)). The sum of all currents into a node equals zero.

$$\sum i_{\text{node}} = 0$$

**Definition 2.2.2** (Kirchhoff's Voltage Law (KVL)). The sum of all voltages around a loop equals zero.

$$\sum v_{\text{loop}} = 0$$

### 2.3 Series and Parallel Circuits

**Definition 2.3.1.** Elements connected end-to-end are in series. If both ends of an element are connected directly to another element, the two elements are in parallel.

Element	Series	Parallel
Current Source	$i_{eq} = i_{k \geq 1}$	$i_{eq} = \sum_{k \geq 1} i_k$
Voltage Source	$v_{eq} = \sum_{k \geq 1} v_k$	$v_{eq} = v_{k \geq 1}$
Resistor	$R_{eq} = \sum_{k \geq 1} R_k$	$\frac{1}{R_{eq}} = \sum_{k \geq 1} \frac{1}{R_k}$
Inductor	$L_{eq} = \sum_{k \geq 1} L_k$	$\frac{1}{L_{eq}} = \sum_{k \geq 1} \frac{1}{L_k}$
Capacitor	$\frac{1}{C_{eq}} = \sum_{k \geq 1} \frac{1}{C_k}$	$C_{eq} = \sum_{k \geq 1} C_k$

Table 1: Equivalent values for various components connected in series and parallel.

These equations can be used to simplify a complex circuit.

### 2.4 Voltage and Current Dividers

**Definition 2.4.1** (Voltage Divider). A voltage divider is a circuit that divides a voltage in the proportion of the series resistances.

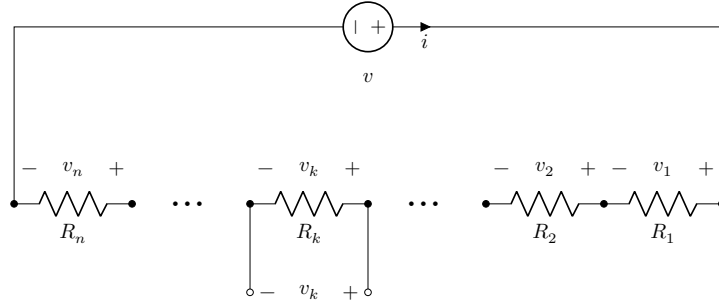


Figure 7: Resistors connected in series to a voltage source.

**Theorem 2.4.1.**

$$v_k = v \frac{R_k}{R_{eq}}$$

*Proof.* The current through any resistor is

$$i = \frac{v}{R_{eq}}$$

Therefore the voltage drop in any resistor is

$$v_k = iR_k$$

$$v_k = \frac{v}{R_{eq}} R_k$$

□

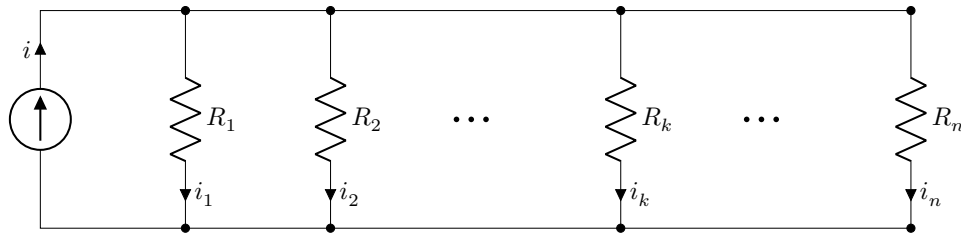
**Definition 2.4.2** (Current Divider). A voltage divider is a circuit that divides a voltage in the proportion of the series resistances.

Figure 8: Resistors connected in parallel to a current source.

**Theorem 2.4.2.**

$$i_k = i \frac{R_{eq}}{R_k}$$



*Proof.* Using KCL we have

$$\begin{aligned}i &= \sum_{k \geq 1} i_k \\i &= \sum_{k \geq 1} \frac{v}{R_k} \\i &= \frac{v}{R_{eq}}\end{aligned}$$

Solving for  $v$  gives

$$v = iR_{eq}$$

Hence the current through any resistor in parallel is given by

$$i_k = \frac{v}{R_k} = \frac{iR_{eq}}{R_k}$$

□

### 3 Diodes

**Definition 3.0.1** (Diode). A diode is a semiconductor component in which current flows only in one direction. A diodes requires a voltage to start the flow of current in the forward direction.

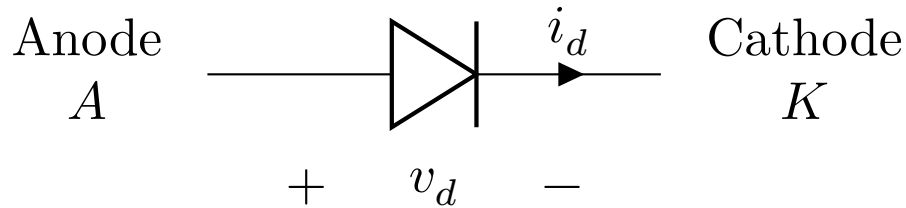


Figure 9: Diode Circuit Symbol

#### 3.1 V-I Characteristic

The Voltage-Current characteristic of linear circuit elements can be plotted as shown below.

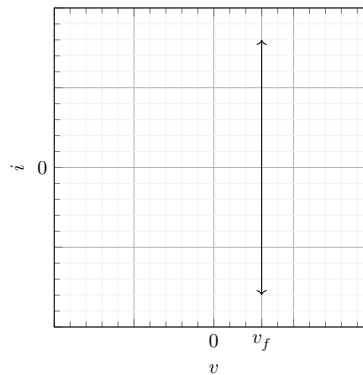


Figure 10: V-I characteristic for a voltage source.

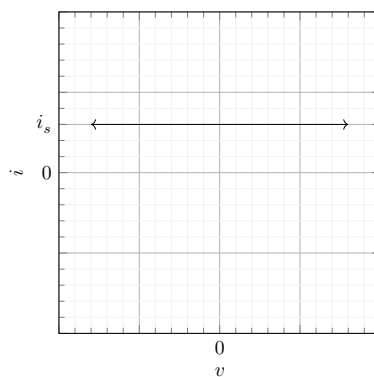


Figure 11: V-I characteristic for a current source.

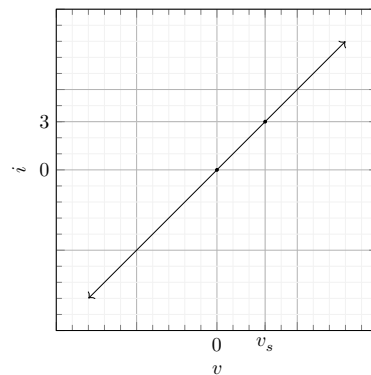


Figure 12: V-I characteristic for a resistor.

### 3.2 V-I Characteristic for Diodes

A diode has a non-linear characteristic curve, hence it is often simplified.

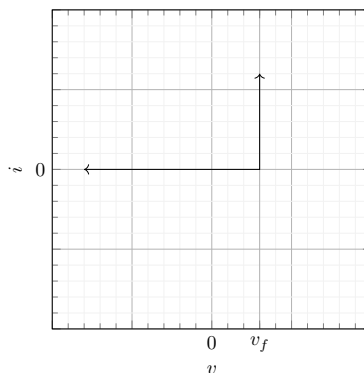


Figure 13: V-I characteristic for a diode.

**Theorem 3.2.1** (Shockley's Diode Equation). *A diode can be better modelled using Shockley's equation.*

$$i_D = I_S \exp\left(\frac{v_D}{0.026}\right)$$

where  $I_S$  is the saturation current and 0.026 is the thermal voltage.

### 3.3 Operating Points and Load Lines

**Definition 3.3.1** (Operating Point). The operating point for two elements can be found by determining the intersection of the two V-I characteristic curves.

**Definition 3.3.2** (Load Lines). If a circuit contains three or more elements including a diode, the V-I characteristic curve is found around the diode. This curve is called a load line.

### 3.4 Operating Point of Non-Linear Component

Given the following circuit with a non-linear component

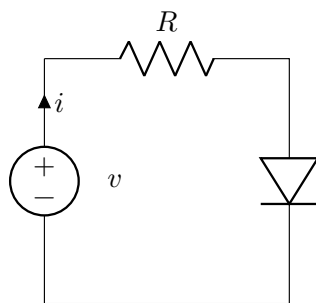


Figure 14: Circuit with non-linear element.

the load line is given by the equation

$$i(v) = -\frac{i_{sc}}{v_{oc}} + i_{sc}$$

where the short-circuit current is the current through the non-linear component, and the open circuit voltage is the voltage across the open circuit nodes of the component.

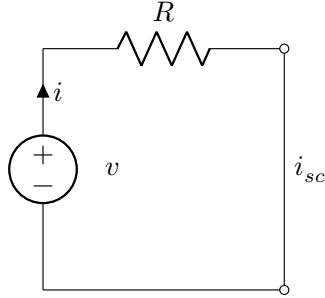


Figure 15: Circuit for Short Circuit Current.

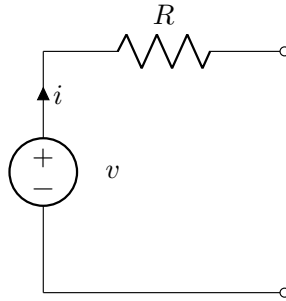


Figure 16: Circuit for Open Circuit Voltage.

## 4 Mesh Analysis

**Definition 4.0.1** (Node). A point where two or more circuit elements join.

**Definition 4.0.2** (Essential Node). A point where three or more circuit elements join.

**Definition 4.0.3** (Loop). A path with the same start and end node.

**Definition 4.0.4** (Mesh). A loop that does not enclose any other loops.

### 4.1 Mesh Analysis Steps

1. Label the unknown mesh currents.
2. Find the voltage across each of the circuit elements in terms of mesh currents.
3. Use KVL around each mesh to create simultaneous equations.
4. Solve simultaneous equations for mesh currents.

### 4.2 Mesh Analysis with Current Sources

If the current source is in a single mesh, then treat the mesh current as known and solve as before.

If the current source is between two meshes, then we must use a supermesh.

**Definition 4.2.1** (Supermesh). A supermesh is a special mesh that surrounds the current source.

1. Label meshes and identify supermesh.
2. Write KCL equation for current source.
3. Write supermesh equation.
4. Use KVL around supermesh.

## 5 Source Transformations

Real sources often have many limitations in terms of voltage and current delivery. The most commonly modelled, and most useful for linear circuit theory, is some form of resistance associated with the source.

### 5.1 Thévenin Equivalent Circuit

**Definition 5.1.1.** The Thévenin equivalent circuit is a voltage source with a series resistance.

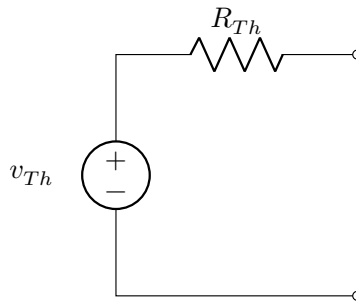


Figure 17: Thévenin Equivalent Circuit.

This circuit has the following properties:

**Open circuit voltage.**  $v_{oc} = v_{Th}$

**Short circuit current.**  $i_{sc} = \frac{v_{Th}}{R_{Th}}$

### 5.2 Norton Equivalent Circuit

**Definition 5.2.1.** Similar to the Thévenin equivalent model, we can use a current source with a resistor in parallel to model the same circuit.

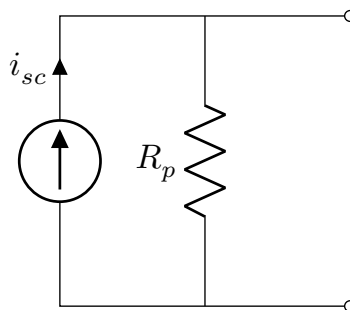


Figure 18: Norton Equivalent Circuit.

This circuit has the following properties:

**Open circuit voltage.**  $v_{oc} = i_{sc} R_p$

**Short circuit current.**  $i_{sc} = i_{sc}$

### 5.3 Source Transformations

A source transformation is the process of simplifying a circuit by transforming voltage sources into current sources, and vice versa, using Thévenin's Theorem and Norton's Theorem.

**Theorem 5.3.1.** *Thévenin and Norton equivalent circuits have the following relationship*

$$R_{Th} = R_p$$

### 5.4 Superposition

**Theorem 5.4.1** (Thévenin's Theorem). *Any linear circuit can be replaced by a voltage source and a resistance in series.*

**Theorem 5.4.2** (Norton's Theorem). *Any linear circuit can be replaced by a current source and a resistance in parallel.*

### 5.5 Maximum Power Transfer

In the circuit shown below, the maximum power transfer to the load is given by

$$P_L = \frac{v_{Th}^2}{4R_L}.$$

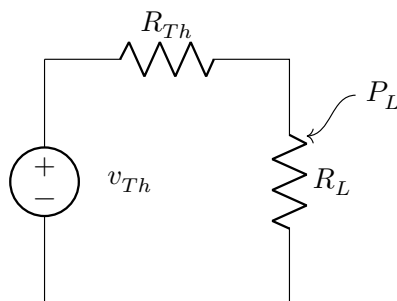


Figure 19: Power Transfer in a Thévenin Model.



## 6 Inductors and Capacitors

### 6.1 Capacitors

**Definition 6.1.1.** Capacitors store electrical energy as a voltage. The ratio of voltage to charge across a capacitor is its capacitance, measured in Farads (F).

$$q = Cv$$

**Definition 6.1.2** (VI Relationship).

$$i = C \frac{dv}{dt}$$

$$v(t) = \frac{1}{C} \int_0^t i(\tau) d\tau + v(0)$$

**Definition 6.1.3** (Energy Stored by an Capacitor).

$$W = \frac{1}{2} Cv^2$$

**Theorem 6.1.1** (Steady State Conditions). *When a circuit is in steady state, capacitors can be modelled as open circuits.*

### 6.2 Inductors

**Definition 6.2.1.** Inductors create voltage to oppose a change in current. The ratio of voltage to the rate of change of current through an inductor is its inductance, measured in Henrys (H).

**Definition 6.2.2** (VI Relationship).

$$v = L \frac{di}{dt}$$

$$i(t) = \frac{1}{L} \int_0^t v(\tau) d\tau + i(0)$$

**Definition 6.2.3** (Energy Stored by an Inductor).

$$W = \frac{1}{2} Li^2$$

**Theorem 6.2.1** (Steady State Conditions). *When a circuit is in steady state, inductors can be modelled as short circuits.*

## 7 RC and RL Circuits

### 7.1 Switches

**Definition 7.1.1.** A switch will engage part of a circuit at a specified point in time, as indicated on the circuit diagram.

**Definition 7.1.2** (Poles). “Pole” refers to the number of circuits one switch can control.

**Definition 7.1.3** (Throw). “Throw” refers to the number of output connections each switch pole can connect its input to.

### 7.2 Natural Response

**Definition 7.2.1** (RC Circuit Natural Response). For the circuit shown below, using KCL gives the following relationship

$$-C \frac{dv}{dt} = \frac{v}{R}.$$

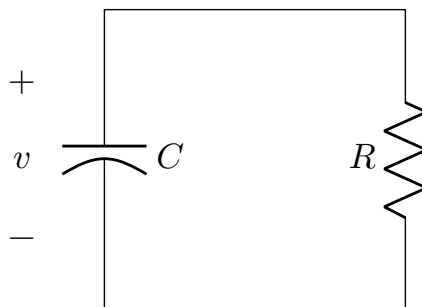


Figure 20: RC Circuit.

By solving this differential equation, we can determine the natural response of a RC circuit.

$$v(t) = v(0) \exp\left(-\frac{t}{RC}\right)$$

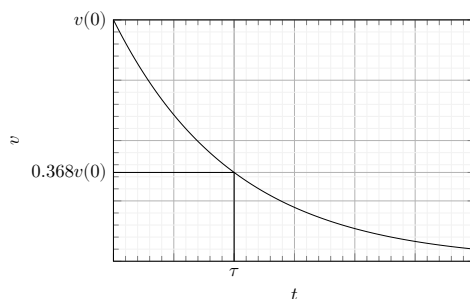


Figure 21: Natural Response of a RC Circuit.

**Definition 7.2.2** (Time Constant). The time constant  $\tau$  is a parameter for switching circuits. The time constant for a RC circuit is given by

$$\tau = RC$$

The voltage at this time is equal to

$$e^{-1}v(0) \approx 0.368v(0)$$

**Definition 7.2.3** (RL Circuit Natural Response). For the circuit shown below, using mesh analysis gives the following relationship

$$L \frac{di}{dt} = -iR.$$

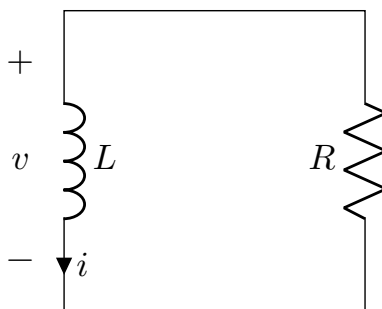


Figure 22: RL Circuit.

By solving this differential equation, we can determine the natural response of a RL circuit.

$$i(t) = i(0) \exp\left(-\frac{t}{\frac{1}{R}L}\right)$$

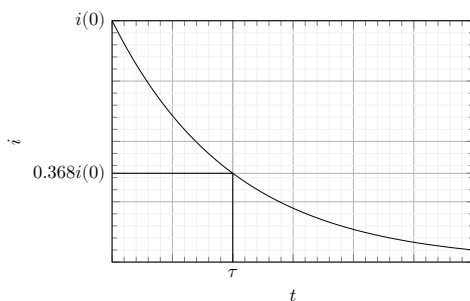


Figure 23: Natural Response of a RL Circuit.

**Definition 7.2.4** (Time Constant). The time constant  $\tau$  is a parameter for switching circuits. The time constant for a RL circuit is given by

$$\tau = \frac{1}{R}L$$

The current at this time is equal to

$$e^{-1}i(0) \approx 0.368i(0)$$

### 7.3 Step Response

**Definition 7.3.1** (RC Circuit Step Response). For the circuit shown below, using KCL at the top node gives the following relationship

$$i_s = C \frac{dv}{dt} + \frac{v}{R}.$$

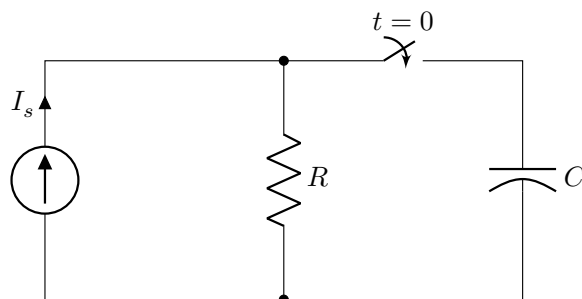


Figure 24: RC Circuit.

By solving this differential equation, we can determine the step response of a RC circuit.

$$v(t) = I_s R + (V_0 - I_s R) \exp\left(-\frac{t}{RC}\right)$$

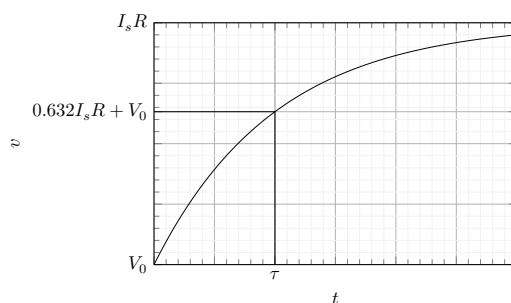


Figure 25: Step Response of a RC Circuit.

The voltage at  $t = \tau$  is equal to

$$\begin{aligned} v(\tau) &= (1 - e^{-1}) I_s R + V_0 \\ &\approx 0.632 I_s R + V_0 \end{aligned}$$

**Definition 7.3.2** (RL Circuit Step Response). For the circuit shown below, using mesh analysis gives the following relationship

$$L \frac{di}{dt} + iR = V_s.$$

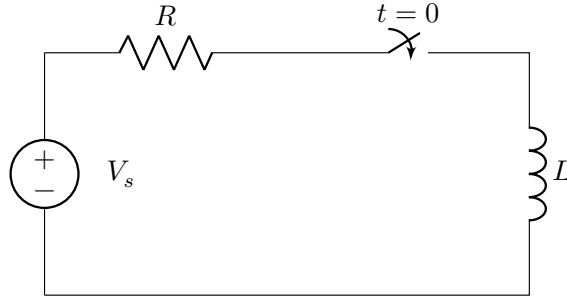


Figure 26: RL Circuit.

By solving this differential equation, we can determine the step response of a RL circuit.

$$i(t) = \frac{V_s}{R} + \left( I_0 - \frac{V_s}{R} \right) \exp \left( -\frac{t}{\frac{1}{R}L} \right)$$

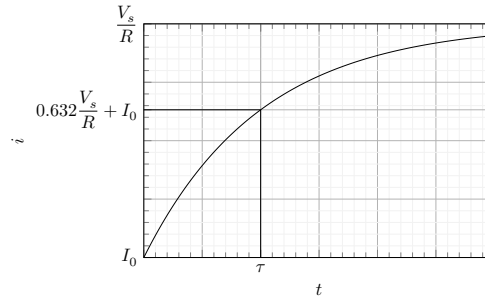


Figure 27: Step Response of a RL Circuit.

The current at  $t = \tau$  is equal to

$$\begin{aligned} i(\tau) &= (1 - e^{-1}) \frac{V_s}{R} + I_0 \\ &\approx 0.632 \frac{V_s}{R} + I_0 \end{aligned}$$

## 8 Operational Amplifiers

**Definition 8.0.1** (Amplifier). An amplifier is a device for increasing the power of a signal through an external energy source. In an electronic amplifier, the “signal” is usually a voltage or current.

**Definition 8.0.2** (Gain). The gain  $K$  of an amplifier, is the ratio of the output signal to the input signal.

$$v_{out} = K v_{in}$$

**Definition 8.0.3** (Operational Amplifier). An operational amplifier (op amp) amplifies the voltage difference between its input terminals. Operational amplifiers require a power supply to amplify voltage. In an operational amplifier:

1. The output cannot exceed the power supply range.
2. The inputs should remain within the power supply range.

The output voltage has the following possibilities:

1. If  $v_p - v_n > 0$ ,  $v_{out} = V_{CC}$ .
2. If  $v_p - v_n < 0$ ,  $v_{out} = V_{EE}$ .
3. If  $v_p - v_n = 0$ ,  $v_{out} = 0$ .

where  $v_p$  is the non-inverting input,  $v_n$  is the inverting input,  $V_{CC}$  is the positive power supply voltage and  $V_{EE}$  is the negative power supply voltage.

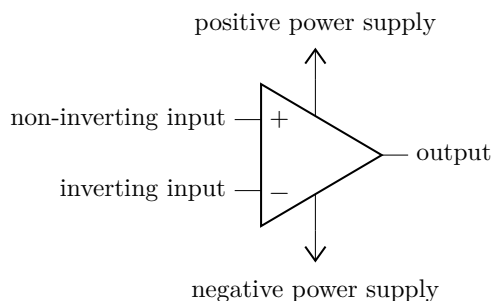


Figure 28: Operational Amplifier Circuit Symbol.

### 8.1 Golden Rules for Op Amps

1. Infinite input impedance, and so zero input current.
2. In a closed loop, the output drives the voltage difference at the inputs to zero.

Note the second rule only applies when the op amp has external negative feedback.

### 8.2 Op Amp Analysis

Using the golden rules above, the following circuits can be constructed.

**8.2.1 Inverting Amplifier**

$$v_{out} = -\frac{R_2}{R_1}v_{in}$$

**8.2.2 Non-Inverting Amplifier**

$$v_{out} = \frac{R_1 + R_2}{R_1}v_{in}$$

**8.2.3 Voltage Follower**

$$v_{out} = v_{in}$$

**8.2.4 Inverting Summing Amplifier**

$$v_{out} = -R_f \left( \frac{v_1}{R_1} + \frac{v_2}{R_2} + \dots + \frac{v_n}{R_n} \right)$$

where  $R_f$  is the feedback resistor.

**8.2.5 Difference Amplifier**

$$v_{out} = \frac{R_2}{R_1}(v_2 - v_1)$$

where the ratio of  $\frac{R_2}{R_1}$  must be equal on both legs.

**8.3 Designing Op Amps**

In each of the following circuits, it is important to choose resistors in the  $1\text{ k}\Omega$  -  $100\text{ k}\Omega$  range, to prevent a large output current.

## 9 Sinusoidal Signals

**Definition 9.0.1.** A sinusoidal signal is commonly referred to as Alternating Current or AC.

### 9.1 Properties of Sinusoidal Signals

These signals will be described using the cosine function.

$$v = V_{\text{rms}} \cos(\omega t + \phi)$$

#### 9.1.1 Magnitude

**Definition 9.1.1.** The magnitude of a signal is the greatest distance from the line of oscillation, commonly zero, to the peak of the signal.

#### 9.1.2 Angular Frequency

**Definition 9.1.2.** The angular frequency  $\omega$  is measured in radians per second ( $\text{rad s}^{-1}$ ), and it allows us to compute the cosine function in radians.

#### 9.1.3 Period and Frequency

**Definition 9.1.3** (Period). The period of a signal is its cycle time  $T$  in seconds (s).

**Definition 9.1.4** (Frequency). The frequency of a signal  $f$  is the number of cycles per second, or the inverse of the period. The frequency is measured in Hertz (Hz).

The following equations relate the angular frequency, period and frequency together.

$$f = \frac{1}{T} \qquad T = \frac{2\pi}{\omega} \qquad \omega = 2\pi f$$

#### 9.1.4 Phase

**Definition 9.1.5.** The phase of a signal is the position of a signal relative to a zero phase signal, measured in degrees ( $^\circ$ ). A **positive** phase corresponds to a “leading” signal, and a **negative** phase corresponds to a “lagging” signal. The phase can be determined by calculating the difference in time  $\tau$  between two signals.

$$\phi = \frac{\tau}{T}$$

### 9.2 Root Mean Square

**Definition 9.2.1.** Root mean square (rms) is a method of obtaining a useful average of a signal that is symmetric about the horizontal axis. It is defined as the square **root** of the **mean** value of the function **squared**. For a sine wave

$$V_{\text{rms}} = \frac{V_{\text{m}}}{\sqrt{2}}$$

The units in rms quantities are also subscripted with rms, for example,  $V_{\text{rms}}$ .



### 9.3 Power

**Definition 9.3.1.** In a resistive load, the power can be determined using the rms current and rms voltage.

$$\begin{aligned} p &= vi \\ p &= 2V_{\text{rms}}I_{\text{rms}} \cos(\omega t + \phi) \cos(\omega t + \phi) \\ p &= V_{\text{rms}}I_{\text{rms}}(1 + \cos(2\omega t + 2\phi)) \end{aligned}$$

The average power is given by

$$P_{\text{avg}} = V_{\text{rms}}I_{\text{rms}}$$

### 9.4 Phasors

**Definition 9.4.1.** To assist in AC analysis, we can express the magnitude and phase of a sinusoidal signal as a phasor.

### 9.5 Phasor Transforms

**Definition 9.5.1.** A sinusoidal signal can be converted to a phasor using the Phasor Transform

$$\begin{aligned} \mathbf{V} &= \mathcal{P}\{v(t)\} \\ &= \mathcal{P}\{V_m \cos(\omega t + \phi)\} \\ &= V_m e^{j\phi} \\ &= V_m \angle \phi^\circ \end{aligned}$$

where  $j^2 = -1$ . Here  $\mathbf{V}$  is the phase-domain representation of the time-domain signal  $v(t)$ .

### 9.6 Inverse Phasor Transforms

**Definition 9.6.1.** A phasor can be converted back to a sinusoidal signal using the Inverse Phasor Transform

$$\begin{aligned} v(t) &= \mathcal{P}^{-1}\{\mathbf{V}\} \\ &= \Re\{\mathbf{V}e^{j\omega t}\} \\ &= \Re\{V_m e^{j\phi} e^{j\omega t}\} \\ &= V_m \Re\{e^{j(\omega t + \phi)}\} \\ &= V_m \cos(\omega t + \phi) \end{aligned}$$

## 10 Frequency Response

## **11 Filters and Rectifiers**

## **12 Zener Diodes and Voltage Regulators**