

## Operating Systems

# Tutorial Worksheet 03

**Description.** This tutorial worksheet covers the topic of process synchronization.

### 1. Concepts Understanding

- What is a critical section in a program?
- Explain how old uniprocessor operating systems (e.g., earlier version of Unix) handled the critical section problem.
- Explain the two styles of using semaphores.
- Can a process be interrupted (context-switched) during the execution of its critical section? Explain your answer.
- Why disabling interrupt system during critical section execution is not a good idea in multiprocessor systems?
- What are the three requirements for the critical section problem. Explain them.
- What are the two main advantages of implementing the primitives `acquire()` and `release()` using queues instead of using a busy-waiting statement in `acquire()` and an incrementation statement in `release()`.
- Semaphores are mutual-exclusive accessed shared variables used to set up synchronization among cooperative processes. Explain why semaphores cannot be used when cooperative processes are executing on different computers?

### 2. Race condition and non-determinism

Let  $x$  and  $y$  be two shared variables stored in the main memory. Assuming that the two variables are initialized to 10, what can be the possible outcomes for  $x$  and  $y$  if the following two processes are executed concurrently?

Process A :  $x = x + y$

Process B :  $y = x * x$

### 3. Critical section

Consider the following program in which two codes  $C_1$  and  $C_2$  are executed concurrently. These two codes share certain variables and use private variables as well.

**Begin**

**Integer:** x, y, t, p, u, r, h, a, b, c;

**CoBegin**  $C_1; C_2;$  **CoEnd**

**End**

Code  $C_1$ :

Code  $C_2$ :

**Begin**

**Begin**

b = r + 4;                      y = t - p;

c = x \* b;                      x = x + 3;

a = a % b;                      t = u \* x;

a = y - 55;                      h = x \* r + y;

**End**

**End**

- Identify critical sections in each code. Just surround the statements that compose a critical section in the given code and name each critical section (e.g., CS<sub>1</sub>, CS<sub>2</sub>, ...). Note that multiple critical sections may exist in one single code.
- On the above code, use semaphores to implement the entry and exit section for each identified critical section (i.e., make use of P(**sem**) to acquire and V(**sem**) to release a semaphore **sem**). Your implementation should not lead to a deadlock or to mutual exclusion violation. Also, for each semaphore that you use, you need to declare it and initialize it

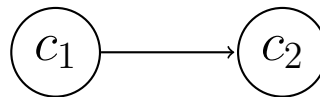
#### 4. Process precedence graphs

Draw a precedence graph (a.k.a., dependency graph) that reflects the parallelism in the following code. Recall a precedence graph is a *directed graph* in which the nodes (vertices) represent processes and the edges represent the causal relation between two processes. If an edge exists from process node  $P_i$  to  $P_j$  then the process  $P_j$  must start executing its code  $c_j$  only when process  $P_i$  finishes executing its code  $c_i$ . Also we use the notation **ParBegin** and **ParEnd** to indicate a block in which program codes (or instructions) must run in parallel. Another alternative notation that can be found in the literature is **CoBegin** and **CoEnd** for concurrent begin/end.

```
Begin
  c0
  ParBegin
    c1
    Begin
      c2; c3; c4
    End
    c5
    c6
    Begin
      c7; c8; c9
    End
  ParEnd
  c10
End
```

#### 5. Using semaphores in waiting-style

- a) Complete the following program code to reflect the process precedence graph shown below (where  $c_i$  refers to the code-i). This code basically consists of creating two processes in parallel: the first process executes program  $P_1$  and the second process executes program  $P_2$ . You should use one semaphore for that.



**ParBegin P1, P2 ParEnd**

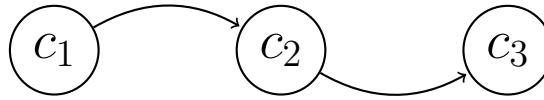
**Program P1:**

```
Begin
  code1
End
```

**Program P2:**

```
Begin
  code2
End
```

- b) Complete the following program code to reflect the process precedence graph shown below (where  $c_i$  refers to the code-i). This code basically consists of creating two processes in parallel: the first process executes program  $P_1$ , and the second process executes program  $P_2$ . You should use semaphores for that.



**ParBegin P1, P2 ParEnd**

**Program P1:**

**Begin**  
`code1; code3;`  
**End**

**Program P2:**

**Begin**  
`code2`  
**End**

- c) Let Process  $P_1$  and  $P_2$  be two processes that execute concurrently using a shared semaphore  $s$  initialized to 10. Each process increments, in an infinite loop, an integer  $i$  (process  $P_1$ ) or  $j$  (process  $P_2$ ) both initialized to 0. After executing for a while, the values of  $i$  and  $j$  will change considerably. In this case, what will be the relation between the two variables?

**Begin**

Semaphore  $M = 10$ ;

Integer  $i = 0$ ;

Integer  $j = 0$ ;

**ParBegin P<sub>1</sub>, P<sub>2</sub> ParEnd**

**End**

**P1**

Begin

while(true) { P(M); i++; }

End

**P2**

Begin

for(int x=10; x>=0; x-- ) { j++; V(M); }

End

- a)  $i = j$       b)  $j = i + 10$       c)  $i \leq j$       d)  $i = j + 10$       e)  $i \geq j + 10$

- d) Give the precedence graph for the following code and check whether a deadlock may occur or not. If there is a deadlock, then modify the codes to fix that:

**Begin**

Semaphore  $M = 0$ ;

Semaphore  $N = 0$ ;

**ParBegin P<sub>1</sub>, P<sub>2</sub> ParEnd**

**End**

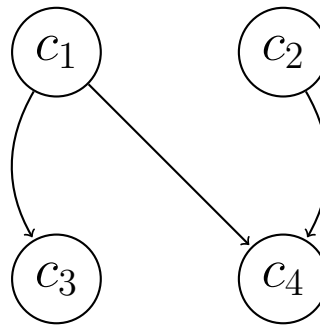
<b>P1</b>	<b>P2</b>
Begin	Begin
P(N)	P(M)
Code 1	Code 2
V(M)	V(N)
End	End

ParBegin P1, P2 ParEnd

- e) Modify the code of the previous question so that the two programs  $P_1$  and  $P_2$  execute alternatively (i.e.,  $\dots, P_1, P_2, P_1, P_2, P_1, \dots$  with  $P_1$  being the first to start execution.
- f) Modify the previous program (using two semaphores) so that the execution order becomes  $\dots, P_1, P_2, P_2, P_1, P_2, P_2, P_1, \dots$  with  $P_2$  being the first to start execution.

## 6. CoBegin/CoEnd with PPGs

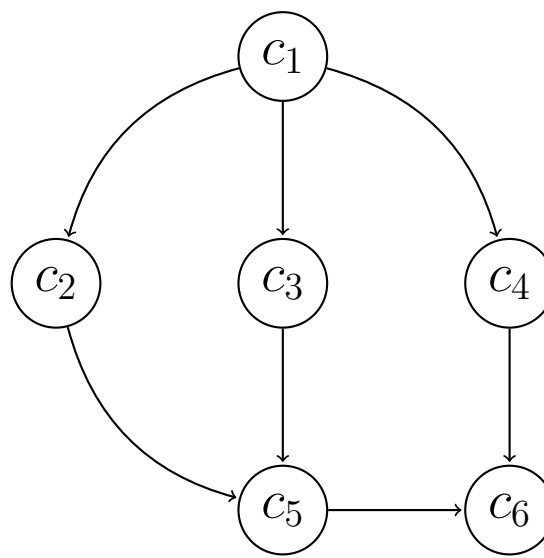
Consider the following notation: let  $Bc_1$  (for Begin  $c_1$ ) expresses the starting of the code  $c_1$  and  $Ec_1$  (for End  $c_1$ ) the ending of the code  $c_1$ , and let the precedence graph shown below reflects the execution order of program codes  $c_1$ ,  $c_2$ ,  $c_3$ , and  $c_4$ . Then, do the execution sequences shown below respect the precedence graph constraints or not?



- |                                       |                                       |
|---------------------------------------|---------------------------------------|
| a) $Bc_1Ec_1Bc_2Ec_2Ec_3Bc_3Ec_4Bc_4$ | e) $Bc_1Bc_2Ec_2Bc_3Ec_1Bc_4Ec_4Ec_3$ |
| b) $Bc_1Bc_2Ec_2Ec_1Bc_3Bc_4Ec_3Ec_4$ | f) $Bc_1Bc_2Ec_2Bc_3Ec_3Ec_1Bc_4Ec_4$ |
| c) $Bc_1Bc_2Ec_1Ec_2Bc_3Bc_4Ec_3Ec_4$ | g) $Bc_1Bc_2Ec_1Bc_3Ec_2Ec_3Bc_4Ec_4$ |
| d) $Bc_1Bc_2Ec_2Ec_1Bc_3Ec_3Bc_4Ec_4$ | h) $Bc_2Ec_2Bc_1Ec_1Bc_4Ec_4Bc_3Ec_3$ |

## 7. Writing synchronization code for PPG

Write the program code that reflects the following precedence graph using six processes  $P_1, \dots, P_6$  each executing its dedicated code  $c_1, \dots, c_6$ . You are required to use three semaphores.



## 8. Peterson's algorithm

Consider the Peterson's algorithm for the critical section problem with two processes.

**Process 0:**

Begin

`while(true)`

{

(1) `Flag[0]=true;`

(2) `turn=1;`

(3) `while(flag[1] && turn==1);`

(4) ... Critical Section ...;

(5) `flag[0] = false;`

}

End

**Process 1:**

Begin

`while(true)`

{

(1) `Flag[1]=true;`

(2) `turn=0;`

(3) `while(flag[0] && turn==0);`

(4) ... Critical Section ...;

(5) `flag[1] = false;`

}

End

- If the two statements (1) and (2) are swapped in both processes, state whether the altered code still satisfies the three requirements of the critical section problem. Explain which requirement has been violated.
- If we change the logical operator in the condition of the `while` statement (Line 3) from `and` to `or` (i.e., `while(flag[1-i] && turn==1-i)` becomes `while(flag[1-i] || turn==1-i)`), state whether the altered code still satisfies the three requirements of the critical section problem. Explain which requirement has been violated.

## 9. Atomic instructions: Test-&-Swap

Hardware solutions to the critical section problem use read-modify-write instructions: these instructions are indivisible because the CPU gets to hold onto the memory bus for two cycles, to both read and then update the shared memory location. As an example, here is code for implementing mutual exclusion using a Swap () machine-code instruction; that instruction has the opcode EXCH in the Pentium instruction set. Each process  $P_i$  executes the same code to access its critical section, where **key** is a boolean local variable and **lock** is a shared memory location among processes  $P_i$  that contains a boolean value, initially set to **false**.

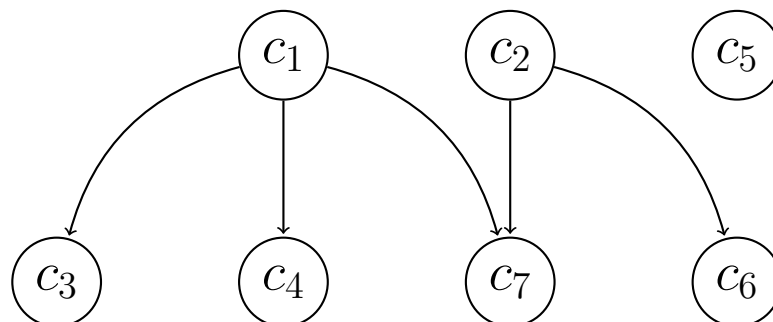
**Process  $P_i$ :**

```
do {  
    key = true;  
    while (key == true) Swap(&lock, &key);  
    ... Critical section of  $P_i$  ...  
    lock = false  
} while(true);
```

Describe what happens if three processes try to enter their critical section at about the same time. How does the given code ensure that only one process gets entry?

## 10. Relaxing precedence constraints in PPGs

Write CoBegin/CoEnd code for the following precedence graph. Make your program express as much parallelism as possible within the limitations of CoBegin/CoEnd, while being sure to enforce all the constraints that are in the precedence graph. (The best solutions introduce two or three extra precedence edges. Try to find one of them.)



## 11. Classical synchronization problem (The Guarantita Problem)

Imagine a bustling food stall selling the popular snack, guarantita. There's one skilled cook preparing these delights, with a few stools for eager customers to wait their turn. Customers arrive randomly, hoping to get their hands on this delicious treat. If a stool is free, they sit down and wait patiently. But if all stools are occupied, they sadly move on to find another snack. Once the cook finishes preparing a guarantita, they glance at the waiting area. If someone's patiently waiting, the cook whips up their order next. However, if no one's there, the cook wouldn't want to stand around idly. This is where your creative problem-solving comes in! Can you design a system using semaphores to guarantee fairness and avoid chaos? Ensure neither the cook waits forever nor hungry customers miss their chance to savor a tasty guarantita.