

```
> summary(model_1)
```

Call:

```
lm(formula = price ~ highwaympg + citympg + peakrpm + horsepower +  
    compressionratio + stroke + bore + enginesize + curbweight +  
    height + width + length + wheelbase)
```

Residuals:

Min	1Q	Median	3Q	Max
-11674.3	-1620.6	4.4	1543.8	13809.5

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-63633.132	16432.763	-3.872	0.000151 ***
highwaympg	287.178	164.689	1.744	0.082918 .
citympg	-305.769	182.951	-1.671	0.096407 .
peakrpm	2.117	0.677	3.127	0.002063 **
horsepower	37.280	18.211	2.047	0.042109 *
compressionratio	247.104	86.596	2.854	0.004834 **
stroke	-2962.854	797.179	-3.717	0.000270 ***
bore	-838.703	1217.519	-0.689	0.491802
enginesize	127.760	15.208	8.401	1.33e-14 ***
curbweight	1.639	1.739	0.942	0.347275
height	326.301	143.014	2.282	0.023691 *
width	632.908	258.021	2.453	0.015128 *
length	-84.382	57.919	-1.457	0.146894
wheelbase	60.048	104.790	0.573	0.567342

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3168 on 179 degrees of freedom

Multiple R-squared: 0.857, Adjusted R-squared: 0.8466

F-statistic: 82.52 on 13 and 179 DF, p-value: < 2.2e-16

**#it can be seen that p-value of the F-statistics is < 2.26-16, which is highly significant. This means that, at least, one of the 13 explanatory variables is significantly related to the responsive variable**

**#Multiple R-squared is 0.857, which indicate a pretty well fit to the data**

**#based on the coefficients table we can see that**

the coefficient with ***	are statistically significant
the coefficient with **	are somewhat statistically significant
the coefficient with *	are not very statistically significant
the coefficient with	are not statistically significant

**in summary, changing in engine size and stroke are significantly associated to changes in price, changing in compression ratio and peak rpm are somewhat associate to changes in price while changing in rest variables are not significantly associated with price.**

```
> model2 <- lm(price ~ stroke + enginesize, data = df)
```

```
> summary(model2)
```

Call:  
lm(formula = price ~ stroke + enginesize, data = df)

Residuals:

Min	1Q	Median	3Q	Max
-13553.2	-1770.5	-260.7	1128.9	14074.0

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-1126.508	2730.551	-0.413	0.68040
stroke	-2544.482	853.327	-2.982	0.00324 **
enginesize	177.001	6.472	27.350	< 2e-16 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3643 on 190 degrees of freedom  
Multiple R-squared: 0.7993, Adjusted R-squared: 0.7972  
F-statistic: 378.4 on 2 and 190 DF, p-value: < 2.2e-16

**#based on this model, we can tell that engine size have more significantly effect on the price**

```
> model3 <- lm(price ~ enginesize, data = df)
> summary(model3)
```

Call:  
lm(formula = price ~ enginesize, data = df)

Residuals:

Min	1Q	Median	3Q	Max
-11490	-2031	-193	1460	14050

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-8862.79	868.66	-10.2	<2e-16 ***
enginesize	172.86	6.45	26.8	<2e-16 ***

---  
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3717 on 191 degrees of freedom  
Multiple R-squared: 0.7899, Adjusted R-squared: 0.7888  
F-statistic: 718.2 on 1 and 191 DF, p-value: < 2.2e-16

```
> boot.control <- trainControl(method = "boot", number = 500)
> model_1_boot <- train(price ~., data = df, method = "lm", trControl
= boot.control)
> print(model_1_boot)
```

Linear Regression

193 samples  
13 predictor

No pre-processing

Resampling: Bootstrapped (500 reps)

Summary of sample sizes: 193, 193, 193, 193, 193, 193, ...

Resampling results:

RMSE	Rsquared	MAE
3513.489	0.821008	2458.846

Tuning parameter 'intercept' was held constant at a value of TRUE

**The output shows the average model\_1 performance across 500 resamples**

**RMSE (root mean squared error) measures the model prediction error, the lower the better the model.**

**MAE (Mean Absolute Error) measures the model prediction error, the lower the better the model.**

**The R squared represent the proportion of variation in the outcome explained by the predictor variables included in the model. The higher the better.**

```
> boot.control <- trainControl(method = "boot", number = 500)
> model_3_boot <- train(price ~ enginesize, data = df, method = "lm",
trControl = boot.control)
> print(model_2_boot)
Linear Regression
```

193 samples  
2 predictor

No pre-processing

Resampling: Bootstrapped (500 reps)

Summary of sample sizes: 193, 193, 193, 193, 193, 193, ...

Resampling results:

RMSE	Rsquared	MAE
3740.456	0.7973457	2582.375

Tuning parameter 'intercept' was held constant at a value of TRUE

```
boot.control <- trainControl(method = "boot", number = 500)
```

```
model_3_boot <- train(price ~ enginesize, data = df, method = "lm",
trControl = boot.control)
print(model_3_boot)
> print(model_3_boot)
Linear Regression

193 samples
  1 predictor

No pre-processing
Resampling: Bootstrapped (500 reps)
Summary of sample sizes: 193, 193, 193, 193, 193, 193, ...
Resampling results:

    RMSE      Rsquared    MAE
3786.08  0.7873644  2671.926

Tuning parameter 'intercept' was held constant at a value of TRUE
```