

IIUM cat-us-trophy

Contents

Sums 1

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$$\begin{array}{ll} \sum_{k=0}^{n} k = n(n+1)/2 & \sum_{k=0}^{b} k = (a+b)(b-a+1)/2 \\ \sum_{k=0}^{n} k^2 = n(n+1)(2n+1)/6 & \sum_{k=0}^{n} k^3 = n^2(n+1)^2/4 \\ \sum_{k=0}^{n} k^4 = (6n^5+15n^4+10n^3-n)/30 & \sum_{k=0}^{n} k^5 = (2n^6+6n^5+5n^4-n^2)/12 \\ \sum_{k=0}^{n} x^k = (x^{n+1}-1)/(x-1) & \sum_{k=0}^{n} kx^k = (x-(n+1)x^{n+1}+nx^{n+2})/(x-1)^2 \\ 1+x+x^2+\cdots = 1/(1-x) & \sum_{k=0}^{n} kx^k = (x-(n+1)x^{n+1}+nx^{n+2})/(x-1)^2 \end{array}$$