# Serenity

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## 1 Template

```
#include <algorithm>
#include <iostream>
#include <cassert>
#include <climits>
#include <utility>
#include <sstream>
#include <iomanip>
#include <cstdlib>
#include <cstring>
#include <complex>
#include <cctype>
#include <cstdio>
#include <bitset>
#include <vector>
#include <string>
#include <queue>
#include <stack>
#include <cmath>
#include <map>
#include <set>
using namespace std;
#define SET(t,v) memset((t), (v), sizeof(t))
typedef long long LL;
typedef long double LD;
#define sz size()
#define mp make_pair
#define pb push_back
#define x first
#define y second
```

```
#define Rep(i, n) for(int i = 0; i < (n); ++i)
#define Repe(i, n) for(int i = 0; i \le (n); ++i)
#define For(i,a,b) for(int i=(a); i<(b); i++)
#define Fore(i,a,b) for(int i=(a); i<=(b); i++)
#define Ford(i,a,b) for(int i=(a); i>=(b); i--)
#define Dhelper(X) " " << #X << "='" << (X) << "'"
#define D(X) {cerr << __LINE__ << ":" << Dhelper(X) << endl;}</pre>
#define D2(X,Y) {cerr << __LINE__ << ":" << Dhelper(X) << Dhelper(Y) << endl;}</pre>
#define Dv(X) {cerr << __LINE__ << ": " << #X << " = {"; for(int __i=0;__i<(X).size();__i++) \
    cerr<<" "<<(X)[__i];cerr<<" }"<<endl;}
#define Da(X,n) {cerr << __LINE__ << ": " << #X << " = {"; for(int __i=0;__i<(n);__i++) \
   cerr<<" "<<(X)[__i];cerr<<" }"<<endl;}</pre>
template<class T> inline void checkmin(T &a, const T &b) { if(a > b) a = b; }
template<class T> inline void checkmax(T &a, const T &b) { if(a < b) a = b; }
typedef pair<int,int> PII;
typedef pair<LL,int> PLI;
typedef pair<LL,LL> PLL;
template<class T> inline T gcd(T a,T b) {if(a<0)return gcd(-a,b);if(b<0)return gcd(a,-b);
   return (b==0)?a:gcd(b,a%b);}
template<class T> T lcm(const T &a,const T &b) { return a*(b/gcd(a,b)); }
template<class T> inline T sqr(T X) { return X * X; }
const long double PI=acos(-1.0L);
#define ALL(c) (c).begin(), (c).end()
#define RALL(c) (c).rbegin(), (c).rend()
#define SORT(c) sort(ALL(c))
#define RSORT(c) sort(RALL(c))
#define UNIQUE(c) (c).resize(unique(ALL(c))-(c).begin())
typedef vector<int> VI;
typedef vector<LD> VLD;
typedef vector<LL> VLL;
typedef vector<PII> VPII;
typedef vector<vector<int> > VVI;
typedef vector<string> VS;
#define Foreach(it,X) for(__typeof((X).begin())it=(X).begin();it!=(X).end();++it)
template<class T> inline T iabs(T a) { if(a<0) return -a; return a; }</pre>
template<class T> T Dist(T x1,T y1,T x2,T y2) { return sqrt(sqr(x1-x2)+sqr(y1-y2)); }
template<class T> T DistSqr(T x1,T y1,T x2,T y2) { return sqr(x1-x2)+sqr(y1-y2); }
#define iss istringstream
#define oss ostringstream
template<class T> string toString(T n) { oss ost; ost<<n; return ost.str(); }</pre>
int toInt(string s){int r=0; iss sin(s); sin>>r; return r; }
LL toLL(string s){ LL r=0; iss sin(s); sin>>r; return r; }
double toDouble(string s){double r=0;iss sin(s);sin>>r;return r;}
LD toLD(string s){LD r=0; iss sin(s); sin>>r; return r; }
#define present(c,X) ((c).find(X) != (c).end())
#define cpresent(c,X) (find(ALL(c),(X)) != (c).end())
#define two(X) (1 << (X))
#define contains(S,X) (((S)&two(X))!=0)
#define twoL(X) (((long long)(1))<<(X))
#define containsL(S,X) ((S&twoL(X))!=0)
#define ones(X) (two(X)-1)
#define onesL(X) (twoL(X)-1)
template<class T> inline int countones(T n) { int c = 0; for(;n;c++) n &= (n-1); return c; }
template<class T> inline T lowbit(T n) { return (n^(n-1))&n; }
#define ForSubset(a,b) for(long long (a) = (b); (a)!=0; (a) = ((b) & ((a)-1)))
template<class T> inline T getmod(T n, T m) {return (n\mm+m)\mm;}
bool isleap(int year) { return (year%400==0) || ((year%4 == 0) && (year%100 != 0)); }
template<class T> T ipow(const T &m, const T &n) { if(n==0)return 1; T a=ipow(m,n/2);
   return (n&1)?a*a*m:a*a; }
```

```
int main() {
    #ifdef MYCOMP
    freopen("input.txt", "r", stdin);
    #endif
    return 0;
}
```

#### 2 Unionfind

```
struct UnionFind {
   int c;
   vector<int> parent, rank;
   UnionFind(int n) : c(n), parent(n), rank(n)
                                  parent[i] = i, rank[i] = 0; }
   { for(int i = 0; i < n; ++i)
   int root(int x) { if(parent[x] != x) parent[x] = root(parent[x]); return parent[x]; }
   bool join(int a, int b) {
       a = root(a); b = root(b);
       if(a == b) return false;
       if(rank[a] > rank[b]) parent[b] = a;
       else { parent[a] = b; if(rank[a] == rank[b]) rank[b]++; }
       --c;
       return true;
    }
};
```

#### 3 Getid

```
map<string,int> mapid;
int getid(string X) { return present(mapid, X)?mapid[X]:mapid[X]=mapid.size()-1; }
```

## 4 SegmentTree

```
const int N = 5000;
int A[N];
inline bool comp(int pos1, int pos2) { return A[pos1] < A[pos2]; }</pre>
int H[4*N];
void initialize(int n, int i, int j) {
    if(i == j) { H[n] = i; return; }
    initialize(2*n,i,(i+j)/2);
    initialize(2*n+1,(i+j)/2+1, j);
    H[n] = comp(H[2*n], H[2*n+1])?H[2*n]:H[2*n+1];
}
int query(int n, int i,int j, int a, int b) {
    if(a<=i && j<=b) return H[n];</pre>
    const int mid = (i+j)/2;
    int p1=(a>mid)?-1:query(2*n,i,mid,a,b);
    int p2=(mid>=b)?-1:query(2*n+1,mid+1,j,a,b);
    if(p1==-1)return p2;
    if (p2==-1) return p1;
    return comp(p1,p2)?p1:p2;
void update(int n, int i, int j, int pos, int v) {
    const int mid = (i+j)/2;
    if(pos<=mid && i<mid) update(2*n,i,mid,pos,v);</pre>
    if (pos>mid && mid+1<j) update(2*n+1,mid+1,j,pos,v);
    H[n] = comp(H[2*n], H[2*n+1])?H[2*n]:H[2*n+1];
}
```

#### 5 BIT

```
int bit[M],n,m;
void update(int x, int v) {
    while( x <= n ) {
        bit[x] += v;
        x += x & -x;
    }
}
int sum( int x ) {
    int ret = 0;
    while( x > 0 ) {
        ret += bit[x];
        x -= x & -x;
    }
    return ret;
}
```

#### 6 BIT2D

```
int bit[M][M];
int n;
int sum( int x, int y ){
    int ret = 0;
    while(x > 0){
        int yy = y;
            while( yy > 0 ) ret += bit[x][yy], yy -= yy & -yy;
        x -= x & -x;
    return ret ;
void update(int x , int y , int val){
    int y1;
    while (x \le n){
        y1 = y;
        while (y1 \le n){
            bit[x][y1] += val;
            y1 += (y1 \& -y1);
        }
        x += (x \& -x);
    }
}
```

#### 7 LIS

```
void LIS() {
   int n,total, nprob = 0;
   vector< int > table;
   while(scanf("%d", &total)==1){
      if( total == 0 ) break;
      table.clear();
      REP(kkk, total) {
            scanf("%d",&n);
            vector< int >::iterator i = lower_bound( table.begin(), table.end(), n );
            if( i== table.end() ) table.push_back( n );
            else *i <?= n;
      }
      printf("Set %d: %d\n",++nprob,table.size());</pre>
```

```
}
}
```

#### 8 StructVec

```
//vector class, also used as a point
template<int d=2, class T=LD> struct Vec {
   T c[d];
   Vec(){ Rep(i,d) c[i]=0; }
   Vec(T input[]) { Rep(i,d) c[i]=input[i]; } //convert from array
   Vec(vector<T> input) { Rep(i,d) c[i]=input[i]; } //convert from vector
   Vec(T a1, T a2){assert(d==2); c[0]=a1; c[1]=a2; }//2d constructor
   Vec(T a1, T a2, T a3){assert(d==3); c[0]=a1; c[1]=a2; c[2]=a3; }//3d constructor
   T& operator[](int dim) { return c[dim]; } //component
   T operator[](int dim) const { return c[dim]; } //constant component
   Vec operator+(const Vec &a)const{ Vec r; Rep(i,d) r[i]=c[i]+a[i]; return r;}//addition
   Vec operator-(const Vec &a)const{ Vec r; Rep(i,d) r[i]=c[i]-a[i]; return r;}//subtraction
   T operator*(const Vec &a)const{ T r=0; Rep(i,d) r+=a[i]*c[i]; return r;}//dot product
   Vec operator*(T a)const{ Vec r; Rep(i,d) r[i]=c[i]*a; return r;}//scale vector
   T len()const { T r=0; Rep(i,d) r+=c[i]*c[i]; return sqrt(r);}//length of vector
   friend ostream& operator<<(ostream &os, const Vec &a){Rep(i,d){if(i)os<<" ";os<<a[i];}return os;}
   T operator%(const Vec<2> &a)const{assert(d==2);return c[0]*a[1]-c[1]*a[0]; }//2d cross product
   Vec operator%(const Vec<3> &a)const{assert(d==3);return Vec(c[1]*a[2]-c[2]*a[1],
        c[2]*a[0]-c[0]*a[2],c[0]*a[1]-c[1]*a[0]);}//3d cross
   Vec rotate(LD angle) {assert(d==2);return Vec(c[0]*cos(angle)-c[1]*sin(angle),
        c[0]*sin(angle)+c[1]*cos(angle));}
   bool operator<(const Vec &v)const{ Rep(i,d)if(c[i]!=v[i])return c[i]<v[i];return false; }
};
```

#### 9 LinePointDist

```
LD linePointDist(Vec<> A, Vec<> B, Vec<> C, bool isSegment){
   LD dist = ((B-A)%(C-A)) / sqrt((B-A)*(B-A));
   if(isSegment){
      if( (C-B)*(B-A) > eps) return (B-C).len();
      if( (C-A)*(A-B) > eps) return (A-C).len();
   }
   return iabs(dist);
}
```

## 10 SegmentsIntersect

```
bool segmentsIntersect( Vec<> A, Vec<> B, Vec<> C, Vec<> E ) {
    Vec<> in = Line<>(A,B).intersect(Line<>(C,E));
    return linePointDist(A,B,in,true) < eps && linePointDist(C,E,in,true) < eps;
}</pre>
```

## 11 AreaOfPolygon

```
template < class T > T two area (vector < Vec < 2, T > p) {
   T ret = p[p.sz-1] % p[0];
   Rep(i,p.sz-1) ret += p[i] % p[i+1];
   return ret;
}
```

#### 12 StructLine

```
template<class T=LD> struct Line {
        T A, B, C;
        Line(){A=B=C=0;}
        Line(T x1,T y1,T x2,T y2) { A=y2-y1; B=x1-x2; C=A*x1+B*y1; }//construct from 4 values
        T dist(T a0, T a1) const { return iabs( a0*A + a1*B - C ) / sqrt(A*A+B*B); }
        Line rot90(T x,T y)const{Line ret;ret.A=-B;ret.B=A;ret.C=ret.A*x+ret.B*y;return ret;}//rot line
        friend ostream& operator<<(ostream& os,const Line &a){return os<<a.A<<"*x + "<<a.B<<"*y = "<<a.C; }
        //requires Vec
        Line(Vec<2,T>a,Vec<2,T>b)\{A=b[1]-a[1];B=a[0]-b[0];C=A*a[0]+B*a[1];\} //construct from two points
        T dist(Vec<2,T> a) const { return ( a[0]*A + a[1]*B - C ) / sqrt(A*A+B*B); }
        Vec<2,T> intersect(const Line &1) const {T det = A*1.B - 1.A*B; if(iabs(det) < eps)det = 0;</pre>
                return Vec<2,T>((1.B*C - B*1.C)/det, (A*1.C - 1.A*C)/det); }
   };
    //for segment segment intersection, check additionally
    //\min(x1,x2) \le x \le \max(x1,x2)
13
      GetMidLine
    // get a line passing between two points
    template<class T>
   Line<T> getmidline(Vec<2,T> a, Vec<2,T> b) {
        Vec<2,T> mid(a+b);
        return LineT>(a,b).rot90(mid[0]/2,mid[1]/2);
    }
     ReflectPoint
14
    //reflect a point into it's "mirror" with repect to a line
    template<class T>
    Vec<2,T> reflectPoint(Vec<2,T> p, Line<T> 1) {
        LineT > r = 1.rot90(p[0], p[1]);
        Vec<2,T> Y=1.intersect(r);
        return Y - (p-Y);
    }
      ConvexHull
15
    // Returns a list of points on the convex hull in counter-clockwise order.
    // Note: the last point in the returned list is NOT the same as the first one. Because of (k-1)
    template<class T>
    vector< Vec<2,T> > convexHull(vector<Vec<2,T> > P) {
        int n = P.size(), k = 0;
        vector< Vec<2,T> > H(2*n);
        sort(P.begin(), P.end());
        // Build lower hull
        for (int i = 0; i < n; i++) {
            while (k \ge 2 \&\& (H[k-2] - H[k-1]) \% (H[k-2] - P[i]) \le 0) k--;
           H[k++] = P[i];
        // Build upper hull
        for (int i = n-2, t = k+1; i >= 0; i--) {
            while (k \ge t \&\& (H[k-2] - H[k-1]) \% (H[k-2] - P[i]) \le 0) k--;
           H[k++] = P[i];
```

H.resize( k-1 );//k-1 to remove last point (duplicate)

```
return H;
}
```

## 16 Bpm

```
#define M 1010
int grid[M][M];
int 1[M], r[M], seen[M];
int rows, cols;
bool dfs(int x) {
    if( seen[x] ) return false;
    seen[x] = true;
    Rep(i,cols) if(grid[x][i]) if(r[i] == -1 || dfs(r[i])) 
        r[i] = x, l[x] = i;
        return true;
    return false;
}
int bpm() {
    SET( 1, -1 );
    SET( r, -1 );
    int ret = 0;
    Rep(i,rows) {
        SET( seen, 0 );
        if( dfs( i ) ) ret ++;
    }
    return ret;
}
bool lT[M], rT[M];
void konigdfs(int x) {
    if( !1T[x] ) return; 1T[x] = 0;
    Rep(i,cols) if(grid[x][i] && i != l[x]) {
        rT[i] = true;
        if( r[i] != -1) konigdfs(r[i]);
}
int konig() {
    SET(1T, 1);
    SET(rT, 0);
    Rep(i,rows) if(l[i] == -1) konigdfs(i);
}
```

## 17 Hopcroft

```
#define M 1000
vector< int > edge[ M ];
int nr, nc;
int n, m;
int l[M], r[M], seen[M];
bool dfs( int x ) {
   if( seen[x] ) return false;
   seen[x] = true;
   REP(i,edge[x].sz) {
     int v = edge[x][i];
     if( r[v] == -1 || dfs( r[v] ) ) {
        r[v] = x, l[x] = v;
        return true;
   }
```

```
}
  return false;
}
int match() {
  int ret = 0;
  REP(i,n) 1[i] = -1; REP(i,m) r[i] = -1;
  bool done;
  do {
     done = true;
     REP(i,n) seen[i] = 0;
     REP(i,n) if( 1[i] == -1 && dfs( i ) ) done = false;
}while( !done );
  REP(i,n) ret += ( 1[i] != -1 );
  return ret;
}
```

## 18 Djikstra-set

```
double d[51][51];
double a[51][4001];
typedef pair<double, pii> st;
Rep(i,n) Rep(j,m) a[i][j] = 1e100;
S.clear();
/*add*/a[0][0] = 0.0; S.insert( make_pair(0.0, pii(0, 0) ));
while (!S.empty()) {
    st curr = *S.begin(), next;
    S.erase(S.begin());
    i = curr.y.x;
    k = curr.y.y;
    for (j = 0; j < n; j++) {
        next.x = curr.x + d[i][j];
        next.y.x = j;
        next.y.y = curr.y.y + get(d[i][j], maxD);
        if (\text{next.x} \le \text{maxT \&\& next.y.y} \le \text{m \&\& next.x} \le \text{a[next.y.x]} [\text{next.y.y}]) {
             S.erase( st(a[next.y.x][next.y.y], next.y) );
             /*add*/a[next.y.x][next.y.y] = next.x; S.insert(next);
        }
    }
}
```

## 19 DijkstraPrqueue

```
VI edge[Z], cost[Z];
int d[Z];
struct data {
    int u, c;
    data() {}
    data( int uu, int cc ) : u( uu ), c( cc ) {}
    bool operator < ( const data& p ) const {
        return c > p.c;
    }
};
int dijkstra( int na, int nb ) {
    priority_queue< data > q;
    q.push( data( na, 0 ) );
    FOR(i,1,ncity) d[i] = -1;
    d[na] = 0;
    while( !q.empty() ) {
```

```
data u = q.top(); q.pop();
    if( d[ u.u ] < u.c ) continue;
    if( u.u == nb ) break;
    REP(i,edge[u.u].sz) {
        int v = edge[u.u][i];
        if( d[v] == -1 || d[v] > d[u.u] + cost[u.u][i] ) {
            d[v] = d[u.u] + cost[u.u][i];
            q.push( data( v, d[v] ) );
        }
    }
} return d[ nb ];
}
```

#### 20 ArticulationPoint

```
//articulation, root is a special case
DFS_Visit(v) { color[v]=GREY;time=time+1;d[v] = time;
    low[v] = d[v];
    for each w in Adj[v]{
        if(color[w] == WHITE){
            prev[w]=u;
            DFS_Visit(w);
            if low[w] >= d[v]
                record that vertex v is an articulation
                    if (low[w] < low[v]) low[v] := low[w];
        else if w is not the parent of v then
            //--- (v,w) is a BACK edge
            if (d[w] < low[v]) low[v] := d[w];
    color[v] = BLACK; time = time+1;
                                        f[v] = time;
}
```

## 21 StronglyConnectedC

```
// Inputs (populate these).
int deg[NN]; int adj[NN][NN];
// Union-Find.
int uf[NN];
int FIND( int x ) { return uf[x] == x ? x : uf[x] = FIND( uf[x] ); }
void UNION( int x, int y ) { uf[FIND( x )] = FIND( y ); }
// dfsn[u] is the DFS number of vertex u.
int dfsn[NN], dfsnext;
// mindfsn[u] is the smallest DFS number reachable from u.
int mindfsn[NN];
// The O(1)-membership stack containing the vertices of the current component.
int comp[NN], ncomp;
bool incomp[NN];
void dfs( int n, int u ) {
  dfsn[u] = mindfsn[u] = dfsnext++;
  incomp[comp[ncomp++] = u] = true;
 for( int i = 0, v; v = adj[u][i], i < deg[u]; i++) {
   if( !dfsn[v] ) dfs( n, v );
   if( incomp[v] ) mindfsn[u] <?= mindfsn[v];</pre>
  if( dfsn[u] == mindfsn[u] ) {
   // u is the root of a connected component. Unify and forget it.
```

```
do {
     UNION( u, comp[--ncomp] );
     incomp[comp[ncomp]] = false;
     } while( comp[ncomp] != u );
}

void scc( int n ) {
     // Init union-find and DFS numbers.
     for( int i = 0; i < n; i++ ) dfsn[uf[i] = i] = ncomp = incomp[i] = 0;
     dfsnext = 1;
     for( int i = 0; i < n; i++ ) if( !dfsn[i] ) dfs( n, i );
}</pre>
```

#### 22 Kruskal

```
sort( s, s+nedge, comp );
unionfind u;
int cost = 0;
REP(i,nedge) {
    if( u.find( s[i].a ) != u.find( s[i].b ) ) {
       cost += s[i].c;
       u.Union( s[i].a , s[i].b );
    }
}
```

#### 23 Maxflow

```
#define MM 1211
VI edges[MM];
int visited[MM];
int cap[MM][MM];
int dfs(int src, int end, int fl) {
    if(visited[src])return 0;
    if(src==end)return fl;
    visited[src]=1;
    Foreach(v,edges[src]) {
        int x = min(fl, cap[src][*v]);
        if(x>0) {
            x = dfs(*v,end,x);
            if(x==0)continue;
            cap[src][*v] -= x;
            cap[*v][src] += x;
            return x;
        }
    }
    return 0;
int flow(int src, int sink) {
    int ret = 0;
    while(1) {
        SET(visited,0);
        int d = dfs(src,sink,INT_MAX);
        if(d==0)break;
        ret += d;
    }
    return ret;
}
void addEdge(int from, int to, int value) {
```

```
cap[ from ][to]=value;
edges[from].pb(to);
edges[to].pb(from);
}
```

#### 24 MaxflowDinic

```
#include<limits>
#define NN 5010
const long long INF = numeric_limits<long long>::max();
struct edge { int point, next; LL flow, capa; };
vector<edge> edges;
int head[NN], dist[NN], Q[NN], work[NN];
int node, src, dest;
void flowinit(int _node,int _src,int _dest) {
    node=_node;
    src=_src;
    dest=_dest;
    SET(head,-1);
    edges.clear();
    edges.reserve(60010);
bool dinic_bfs() {
    SET(dist,-1); dist[src]=0;
    int sizeQ=0;
    Q[sizeQ++]=src;
    for (int cl=0;cl<sizeQ;cl++)</pre>
        for (int k=Q[c1],i=head[k];i>=0;i=edges[i].next)
            if (edges[i].flow<edges[i].capa && dist[edges[i].point]<0)</pre>
                dist[edges[i].point]=dist[k]+1, Q[sizeQ++]=edges[i].point;
    return dist[dest]>=0;
}
LL dinic_dfs(int x, LL exp) {
    if (x==dest) return exp;
    for (int &i=work[x];i>=0;i=edges[i].next) {
        int v=edges[i].point;
        LL tmp;
        if (edges[i].flow<edges[i].capa && dist[v]==dist[x]+1</pre>
                && (tmp=dinic_dfs(v,min(exp,edges[i].capa-edges[i].flow)))>0)
            return edges[i].flow+=tmp,edges[i^1].flow-=tmp, tmp;
    }
    return 0;
}
LL dinic_flow() {
    LL result=0;
    while (dinic_bfs()) {
        Rep(i,node) work[i]=head[i];
        for(LL delta; delta=dinic_dfs(src,INF); result+=delta);
    }
    return result;
}
void addEdge(int u,int v, LL c1=1, LL c2=0) {
// cout << "add edge " << u+1 << " to " << v+1 << endl;
    edges.pb( (edge) { v,head[u],0,c1 } ); head[u] = edges.sz-1;
    edges.pb( (edge) { u,head[v],0,c2 } ); head[v] = edges.sz-1;
}
```

#### 25 MincostMaxflow

```
#define N 705
int n, nE;
int d[N], pre[N];
struct edge {
    int to, cost, cap;
    int back;
};
edge E[N*N];
vector< int > e[N];
int mincost( int s, int t, int lim ) {
    int flow = 0, ret = 0;
    while( flow < lim ) {</pre>
        SET( d, -1 ); SET( pre, -1 );
        d[s] = 0;
        // bellman ford
        int jump = n-1;
        bool done = 0;
        while( !done && --jump >= 0) {
            done = 1;
            REP(i,n) if (d[i] != -1) REP(j,e[i].sz) {
                edge& x = E[e[i][j]];
                int v = x.to;
                if( x.cap > 0 && (d[v] == -1 || d[v] > d[i] + x.cost )) {
                    d[v] = d[i] + x.cost;
                    pre[v] = x.back;
                    done = 0;
                    //cout<<v<" "<<d[v]<<endl;
                }
            }
            if( done ) break;
        if( d[t] == -1 ) break;
        // traverse back
        int x = t, cflow = 1 << 30;
        while(x != s) {
            edge& ed = E[ pre[x] ];
            cflow = min( cflow, E[ ed.back ].cap );
            x = ed.to;
        }
        if( !cflow ) break;
        int take = min( lim - flow, cflow );
        ret += d[t] * take;
        flow += take;
        x = t;
        while(x != s) {
            edge& back = E[ pre[x] ];
            edge& forw = E[ back.back ];
            back.cap += take;
            forw.cap -= take;
            x = back.to;
        }
    if( flow < lim ) return -1;</pre>
    return ret;
// remember to add -cost in the opposite direction
void add( int u, int v, int uv, int vu, int fuv, int fvu ) {
```

```
int a = nE, b = nE+1;
nE += 2;
E[ a ].to = v, E[ a ].cost = uv, E[ a ].cap = fuv, E[ a ].back = b;
E[ b ].to = u, E[ b ].cost = vu, E[ b ].cap = fvu, E[ b ].back = a;
e[ u ].pb( a ), e[ v ].pb( b );
}
```

## 26 BigNumInt

```
const int B = 10;// If you change this value, then you
                  // will also have to change operator<<.</pre>
class num : public vector<char>
{public:
    num(){}
    num(int n) {
        for(;n;n/=B) push_back(n%B);
    num(string n) {
        int down=0,sign=1;
        if(n[down] == '-') {
             down++;
            sign=-1;
        }
        for(int i=n.size()-1;i>=0;i--)
            push_back(sign*(n[i]-'0'));
        norm();
    void norm() {
        while(!empty()&&!back())
            pop_back();
        int r = 0;
        for(int i=0;i<size();i++) {</pre>
            at(i) += r;
            r = at(i) / B;
            at(i) %= B;
        for(;r;r/=B) push_back(r);
    }
};
ostream& operator<<(ostream &s, const num &a) {
    if(!a.size()) return s << '0';
    if(a.back()<0)s << '-';
    for(int i = a.size()-1;i>=0;i--)
        s << char(iabs(a[i])+'0');</pre>
    return s;
}
bool operator==(const num &a, const num &b) {
    if(a.size()!=b.size())return false;
    for(int i=0;i<a.size();i++)</pre>
        if(a[i]!=b[i])return false;
    return true;
bool operator!=(const num &a, const num &b) {
    return !(a==b);
bool operator<(const num &a, const num &b) {</pre>
    if(!a.size() && !b.size())return false;
    if(!a.size()) return 0 < b.back();</pre>
```

```
if(!b.size()) return a.back() < 0;</pre>
    if(a.back()*b.back()<0)return a.back()<0;</pre>
    if(a.size()!=b.size())return (a.size()<b.size())^(a.back()<0);</pre>
    for(int i=a.size()-1;i>=0;i--)
         if(a[i]!=b[i])return a[i]<b[i];</pre>
    return false;
}
bool operator <= (const num &a, const num &b) {
      if(!a.size() && !b.size())return true;
    if(!a.size()) return 0 <= b.back();</pre>
    if(!b.size()) return a.back() <= 0;</pre>
    if(a.back()*b.back()<0)return a.back()<0;</pre>
    if(a.size()!=b.size())return (a.size()<b.size())^(a.back()<0);</pre>
    for(int i=a.size()-1;i>=0;i--)
         if(a[i]!=b[i])return a[i]<=b[i];
    return true; */
    return a < b || a == b; //inefficient?</pre>
}
num operator-(const num &a) {
    num b(a);
    for(int i=0;i<b.size();i++) b[i]=-b[i];</pre>
    return b;
}
num operator-(const num &a, const num &b);
num operator+(const num &a, const num &b) {
    if(!a.size())return b;
    if(!b.size())return a;
    if(a.back()*b.back()<0)return a -(-b);</pre>
    num c(a);
    int s = min(a.size(),b.size());
    for(int i=0;i<s;i++)</pre>
         c[i]+=b[i];
    while(s<b.size())</pre>
        c.push_back(b[s++]);
    c.norm();
    return c;
}
num operator-(const num &a, const num &b) {
    if(!a.size())return -b;
    if(!b.size())return a;
    if(a.back()*b.back()<0)return a +(-b);</pre>
    num up=iabs(a),down=iabs(b);
    if(up<down)swap(up,down);</pre>
    for(int i=0;i<down.size();i++)</pre>
        up[i]-=down[i];
    for(int i=0;i<up.size();i++)</pre>
        for(;up[i]<0;up[i]+=B)
             up[i+1]--;
    up.norm();
    return (a<b)?-up:up;
}
num operator*(const num &a, const num &b) {
    num c;
    c.resize(a.size()+b.size());
    fill(c.begin(),c.end(),0);
    for(int i=0;i<a.size();i++)</pre>
         for(int j=0; j<b.size(); j++) {</pre>
             int r = c[i+j] + int(a[i])*b[j];
             c[i+j+1] += r/B;
```

```
c[i+j] = r\%B;
            }
        c.norm();
        return c;
    }
    num divByInt(const num &a, int b) {
        num c(a);
        int r=0;
        for(int i=c.size()-1;i>=0;i--) {
            c[i] += r*B;
            r = c[i] \% b;
            c[i] /= b;
        }
        c.norm();
        return c;
    num operator/(const num &a, const num &b) {
        if(a==0 || b==0) return 0;
        num c;
        c.resize(a.size());
        num row,bAbs=iabs(b),aAbs=iabs(a);
        for(int i=a.size()-1;i>=0;i--) {
            row.insert(row.begin(),1,aAbs[i]);
            row.norm();
            for(c[i]=0;bAbs \le row;c[i]++)
                row = row - bAbs;
        }
        c.norm();
        return (a.back()*b.back()<0)?-c:c;</pre>
    }
    num operator%(const num &a, const num &b) {
        if(a==0 || b==0) return 0;
        num row,bAbs=iabs(b),aAbs=iabs(a);
        for(int i=a.size()-1;i>=0;i--) {
            row.insert(row.begin(),1,aAbs[i]);
            row.norm();
            while(bAbs <= row)</pre>
                row = row - bAbs;
        return (a.back()<0)?-row:row;</pre>
        //return a - (a/b)*b;//unefficient?
    }
    num power(const num &m, const num &n) {
        if(n.empty())return 1;
        num a=power(m,n/2);
        return (n[0]%2)?a*a*m:a*a;
    }
      BsearchLE
27
    int down = start;
    int up = end+1;
    while(down+1 < up) {</pre>
        int mid = (down+up)/2;
        if(f1(mid)) down = mid; else up = mid;
```

assert(down == L);

#### 28 BsearchGE

```
int down = start-1;
int up = end;
while(down+1 < up) {
   int mid = (down+up)/2;
   if(f2(mid)) up = mid; else down = mid;
}
assert(down+1 == L);</pre>
```

#### 29 PermIndex

## 30 Geodistance

```
double gdist
( double a_lat, double b_lat, double a_long, double b_long ) {
    return acos(cos(a_lat) * cos(b_lat) * cos(a_long - b_long) + sin(a_lat) * sin(b_lat));
} // don't forget to multiply radius with it!;)
```

#### 31 Matrixmul

```
i64 mod;
struct matrix {
    int m,n;
    i64 a[10][10];
void print( matrix& a ) {
    REP(i,a.m) {
        REP(j,a.n) cout <<" " << a.a[i][j];</pre>
        cout << endl;</pre>
    }
}
matrix operator * ( matrix& x, matrix& y ) {
    matrix ret;
    ret.m = x.m;
    ret.n = y.n;
    REP(i,ret.m) REP(j,ret.n) {
        ret.a[i][j] = 0;
        REP(k, x.n) {
            ret.a[i][j] += (x.a[i][k] * y.a[k][j]);
            ret.a[i][j] %= mod;
        }
```

```
}
    return ret;
}
matrix power( matrix& x , int n ) {
    if( n == 1 ) return x;
    matrix ret = power( x, n/2 );
    ret = ret * ret;
    if( n % 2 == 0 ) return ret;
    ret = ret * x ;
    return ret;
}
```

#### 32 Heron

```
double area( double x, double y, double z ) {
   double s = ( x + y + z ) / 2.;
   double X = s * ( s - x ) * ( s - y ) * ( s - z );
   return sqrt( X );
}
```

### 33 Genprimes

```
#define MAXP 1000000
bool primes[MAXP];
vector<int> plist;
void genprimes() {
    plist.clear();
    int m = (int)sqrt(int(MAXP));
    primes[0]=primes[1]=0;
    for(int i=2;i<MAXP;i++) primes[i] = 1;
    for(int i=2;i<=m;i++)
        if (primes[i])
            for(int j=i*i;j<MAXP;j+=i) primes[j] = 0;
    for(int i=2;i<MAXP;i++)if(primes[i])plist.push_back(i);
}</pre>
```

#### 34 Choose

```
LL choose[50][50];
For(i,1,50) {
    choose[i][0]=choose[i][i]=1;
    For(j,1,i) {
        choose[i][j] = choose[i-1][j]+choose[i-1][j-1];
    }
}
```

#### 35 EuclidExtended

```
template < class T > inline T euclid(T a,T b,T &X,T &Y) {
    if(a < 0) { T d = euclid(-a,b,X,Y); X = -X; return d; }
    if(b < 0) { T d = euclid(a,-b,X,Y); Y = -Y; return d; }
    if(b = = 0) { X = 1; Y = 0; return a; }
    else {
        T d = euclid(b,a%b,X,Y); T t = X;
        X = Y; Y = t - (a/b) * Y;
        return d;
    }
}</pre>
```

}

## 36 Isprime2MillerRabin

```
bool isprime2(long long p, int iteration){
    if(p<2)
        return false;
    if(p!=2 && p%2==0)
        return false;
    long long s=p-1;
    while(s\%2==0)
        s/=2;
    for(int i=0;i<iteration;i++){</pre>
        long long a=rand()%(p-1)+1,temp=s;
        long long mod=powermod(a,temp,p);
        while(temp!=p-1 && mod!=1 && mod!=p-1){
            mod=multiplymod(mod,mod,p);
            temp *= 2;
        if (mod!=p-1 \&\& temp\%2==0)
            return false;
    return true;
```

#### 37 EulerPhi

```
template < class T> T euler(T n) {
   T result = n;
   for(int i=2;i*i <= n;i++) {
      if (n % i == 0) result -= result / i;
      while (n % i == 0) n /= i;
   }
   if (n > 1) result -= result / n;
   return result;
}
```

#### 38 Euler2Phi

```
template<class T> inline T euler2(T n) {
    vector<pair<T,int> > R=factorize(n);
    T r=n;
    for (int i=0;i<R.size();i++)
        r=r/R[i].first*(R[i].first-1);
    return r;
}</pre>
```

## 39 SGcdCongrModinv

```
LL gcd( LL a, LL b ) {
    return !b ? a : gcd( b, a%b );
}
PII egcd( LL a, LL b ) { // returns x,y | ax + by = gcd(a,b)
    if( b == 0 ) return mp( 1, 0 );
    else {
        PII d = egcd( b, a % b );
        return mp( d.y, d.x - d.y * ( a / b ) );
    }
}
```

```
}
}
LL congruence(int a, int b, int n) { // finds ax = b(mod n)
    int d = \gcd(a, n);
    if( b % d != 0 ) return 1<<30; // no solution</pre>
    PII ans = egcd(a, n);
    LL ret = ans.x * ( b/d + OLL ), mul = n/d;
    ret %= mul;
    if( ret < 0 ) ret += mul;</pre>
    return ret;
}
LL m_inverse( LL num, LL mod ) {
    PII p = egcd( num, mod );
    int ret = p.x % mod;
    if( ret < 0 ) ret += mod;
    return ret;
```

## 40 Sterling1

```
LL S[110][110]; LL fact[110];
fact[0] = 1; For(i,1,110) fact[i] = (fact[i-1] * i) % M;
SET(S,0);
For(n,1,110) {
    S[n][n] = 1; S[n][1] = fact[n-1];
    if(n%2 == 0) S[n][1] *= -1;
    For(k,2,n) {
        S[n][k] = ( - (n-1)*S[n-1][k] + S[n-1][k-1] )%M;
    }
}
if(K==0)
    cout << (N==0) << endl;
else
    cout << iabs(S[N][K]%M) << endl;</pre>
```

## 41 Sterling2

```
LL S[110][110]; LL fact[110];
fact[0] = 1; For(i,1,110) fact[i] = (fact[i-1] * i) % M;
SET(S,0);
For(n,1,110) {
    S[n][n] = 1; S[n][1] = 1;
    For(k,2,n) {
        S[n][k] = ( (k)*S[n-1][k] + S[n-1][k-1] )%M;
    }
}
if(K==0)
    cout << (N==0) << endl;
else
    cout << iabs(S[N][K]%M) << endl;</pre>
```

#### 42 Totient

```
FOR(i,1,M) f[i] = i;

FOR(n,2,M) if(f[n] == n) for(int k=n; k<=M; k+=n) f[k] *= n-1, f[k] /= n;
```

#### 43 SieveBits

```
const int MAX = 100000000;
int p[MAX/64 + 2];
int np = 0;
#define on(x) ( p[x/64] & (1<<((x%64)/2)))
#define turn(x) p[x/64] = (1 << (x%64)/2)
void sieve() {
    for(int i=3;i*i<MAX; i+=2) {
        if( !on(i) ) {
            int ii = i*i;
            int i2 = i+i;
            for(int j=ii; j<MAX; j+=i2) turn(j);</pre>
        }
    }
}
inline bool prime( int num ) {
    return num > 1 && ( num == 2 || ( (num&1) && !on( num ) ) );
```

## 44 KmpExplained

```
f[len] = the longest suffix that we can still use for matching if its mismatched at len
f[0] = f[1] = 0;
FOR(i,2,len) {
    int j = f[i-1]; // think as a recursion - last best matching
    while( true ) {
        if(s[j] == s[i-1]) { // we got a way to maximize
            f[i] = j + 1;
           break;
        }else if( !j ) { // suicide
            f[i] = 0;
            break;
        }else j = f[j]; // think recursively, we couldn't use s[i-1] to improve the match for j
        //now we'll go for the best suffix of j and check if we can improve that by using s[i-1]
    }
}
i = j = 0;
while( true ) {
    if( i == len ) break;
    if( text[i] == s[j] ) { // we got an improve
       i++, j++;
        if( j == slen ) // match found
    f(j > 0) j = f[j]; // then we'll check again if we can improve at i
    else i++;
}
```