

SC Quantum Bootcamp

Week 3:

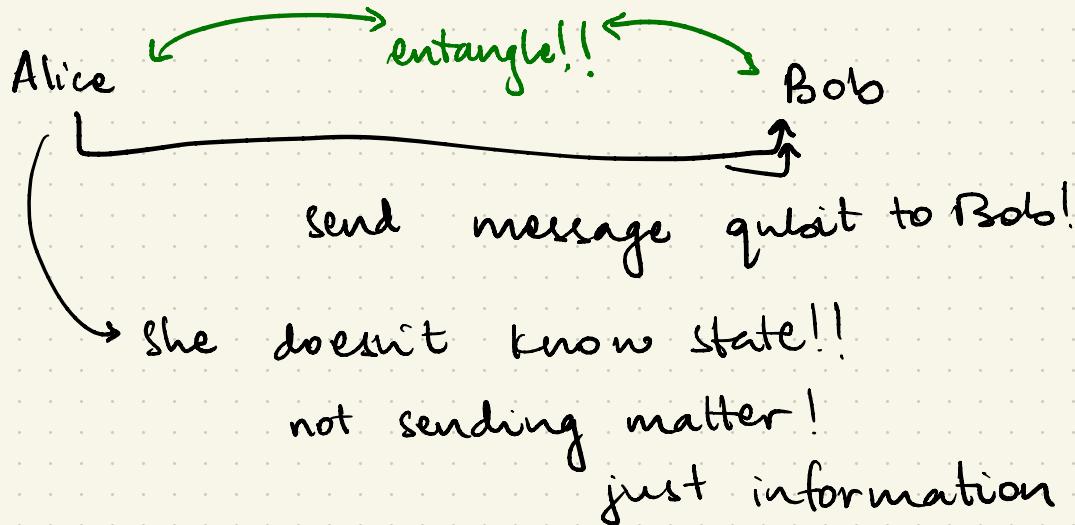
- You should be comfortable:
 - logging in to qBraid
 - launching a Lab instance
 - choosing + fixing the right env for your job
 - requesting more credits when you need them!!
- We've covered:
 - linear algebra
 - basics of quantum programming
 - intro to quantum computing!

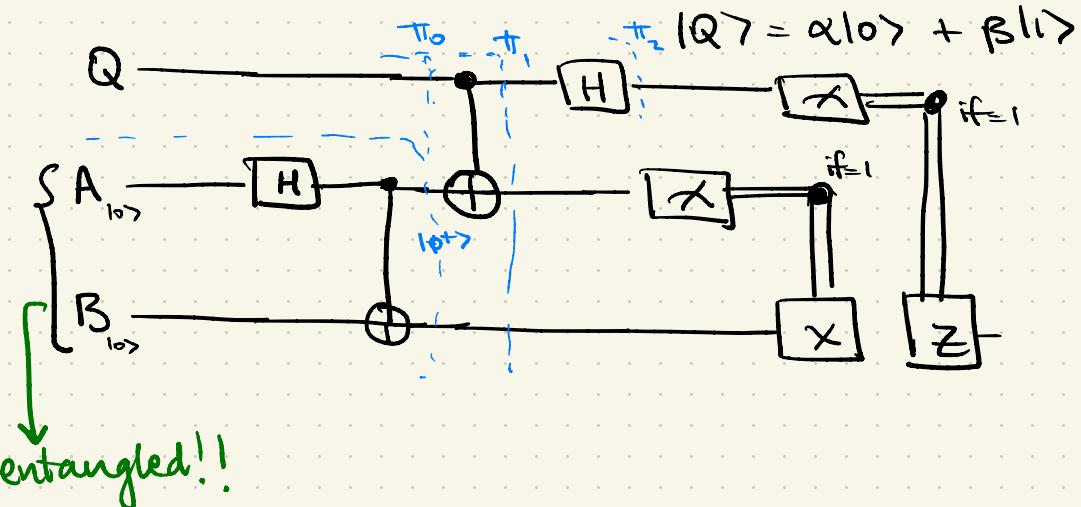
PLEASE DON'T HESITATE TO
ASK QUESTIONS ABOUT
ANY OF THIS!! AND MORE!!

Today!

Quantum Teleportation

- used to perform remote operations on quantum systems specially when qubit can't be moved from one location to another
- important in QEC





Bell state:

$|0\rangle$

$\downarrow H$

$$\frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$$

$$H|0\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \text{ superposition}$$

\downarrow tensor w/ $|0\rangle$

entangled \leftrightarrow

$|1\rangle$

$$H|0\rangle \otimes |0\rangle$$

$$\xrightarrow{\text{CNOT}} \text{CNOT} (H|0\rangle \otimes |0\rangle) = \frac{1}{\sqrt{2}} (|00\rangle + |11\rangle)$$

$$|\Phi^+\rangle, |\Phi^-\rangle, |\Psi^+\rangle, |\Psi^-\rangle$$

\downarrow

\downarrow

\downarrow

\downarrow

$$\frac{1}{\sqrt{2}} (|00\rangle + |11\rangle)$$

$$|00 - 11\rangle$$

$$|01 + 10\rangle$$

$$|01 - 10\rangle$$

$$\frac{1}{\sqrt{2}}$$

Alice is sending Bob a string

00

01

10

11

(B, A, Q) state :

$$|\Pi_0\rangle = |\Phi^+\rangle \otimes (\alpha|0\rangle + \beta|1\rangle)$$

$$= \underline{\alpha|000\rangle + \alpha|110\rangle + \beta|001\rangle + \beta|111\rangle}$$

$\sqrt{2}$

$\downarrow CNOT$

$$|\Pi_1\rangle = \underline{\alpha|000\rangle + \alpha|110\rangle + \beta|101\rangle + \beta|110\rangle}$$

$\sqrt{2}$

\downarrow Hadamard

$$|\Pi_2\rangle = \frac{1}{2} (\alpha|0\rangle + \beta|1\rangle) |00\rangle$$

$$+ \frac{1}{2} (\alpha|0\rangle - \beta|1\rangle) |01\rangle$$

$$+ \frac{1}{2} (\alpha|1\rangle + \beta|0\rangle) |10\rangle$$

$$+ \frac{1}{2} (\alpha|1\rangle - \beta|0\rangle) |11\rangle$$

$$H|\pi_1\rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \underbrace{\langle 100\rangle}_{\sim}$$

$$= \frac{1}{\sqrt{2}} \left(\underbrace{\langle 10\rangle + \langle 11\rangle}_{\sqrt{2}} \right) \langle 100\rangle$$

$$= \frac{1}{\sqrt{2}} (\langle 10\rangle + \langle 11\rangle) \langle 100\rangle$$

state = $\frac{M_i |1\rangle}{\sqrt{p_i}}$

$$M_i = I_o \otimes |100\rangle \langle 001|$$

$$H|10\rangle = \frac{|10\rangle + |11\rangle}{\sqrt{2}}$$

↓
|11>

$$H|11\rangle = \frac{|10\rangle - |11\rangle}{\sqrt{2}}$$

↓
|10>

$$|\pi_1\rangle = \alpha \underbrace{|1000\rangle}_{\downarrow H} + \alpha \underbrace{|110\rangle}_{\uparrow} + \beta \underbrace{|101\rangle}_{\uparrow} + \beta \underbrace{|110\rangle}_{\uparrow}$$

$\frac{\sqrt{2}}$

$$H|\Pi_1\rangle = \alpha|100\rangle H\rangle + \alpha|111\rangle H\rangle + \beta|101\rangle H\rangle$$

$\frac{1}{\sqrt{2}} \left(\underbrace{|100\rangle + |111\rangle}_{|100\rangle} \right)$

$$+ \beta|110\rangle I\rangle$$

$$= \underbrace{\alpha|1000\rangle}_{\frac{1}{2}} + \underbrace{\alpha|1001\rangle}_{-\frac{1}{2}} + \underbrace{\alpha|1110\rangle}_{+\frac{1}{2}} + \underbrace{\alpha|1111\rangle}_{-\frac{1}{2}}$$

$$+ \underbrace{\beta|1010\rangle}_{-\frac{1}{2}} - \underbrace{\beta|1011\rangle}_{\frac{1}{2}} + \underbrace{\beta|1100\rangle}_{\frac{1}{2}} - \underbrace{\beta|1101\rangle}_{-\frac{1}{2}}$$

$$\text{state} = \frac{1}{\sqrt{P_i}} I_0 \otimes |100\rangle \langle 001|\Pi_2\rangle$$

$$= \underbrace{(\alpha|10\rangle + \beta|11\rangle) \langle 001|00\rangle}_{\sqrt{1/4}} \cdot 2$$

$$\text{state} = \alpha|10\rangle + \beta|11\rangle$$

$$a, q = 0, 0$$

$$P(00) = 1/4$$

$$(B, A, Q) = \boxed{(\alpha|10\rangle + \beta|11\rangle)} |100\rangle$$

Bob does nothing

$$a, q = 0, 1 \quad p(01) = 1/4$$

$$(BA, Q) = (\alpha|0\rangle - \beta|1\rangle) \quad |01\rangle$$

Bob applies \bar{z}

$$a, q = 1, 0 \quad p(10) = 1/4$$

$$BAQ = (\alpha|1\rangle + \beta|0\rangle) \quad |10\rangle$$

Bob applies x

$$p(11) = 1/4$$

$$a, q = 1, 1$$

$$BAQ = (\alpha|1\rangle - \beta|0\rangle) \quad |10\rangle$$

Bob applies xz

$$z(\alpha|0\rangle - \beta|1\rangle) = \alpha|0\rangle + \beta|1\rangle$$

$$x(\alpha|1\rangle + \beta|0\rangle) = \alpha|0\rangle + \beta|1\rangle$$

$$zx(\alpha|1\rangle - \beta|0\rangle) = \alpha|0\rangle + \beta|1\rangle$$

$$I(\alpha|0\rangle + \beta|1\rangle) = \alpha|0\rangle + \beta|1\rangle$$

In every case!!

Bob ends up w/ $\alpha|0\rangle + \beta|1\rangle$

which is the message qubit $Q!!$

preserve no-cloning theorem!!