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Class : IF-3

- 1) Selesaikan persamaan  $f(x) = x^3 + x^2 - 3x - 3 = 0$  . Dengan metode Secant dengan dua nilai awal  $x_1 = 1$  dan  $x_2 = 2$

Jawab :

- a) Ambil  $x_1 = 1$  dan  $x_2 = 2$

Untuk  $x_1$

$$f(x) = 1^3 + 1^2 - 3 \cdot 1 - 3$$

$$y_1 = -4$$

Untuk  $x_2$

$$f(x) = 2^3 + 2^2 - 3 \cdot 2 - 3$$

$$y_2 = 3$$

- ↳ Dimasukkan ke-persamaan

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$$\begin{aligned} X_3 &= X_2 - \frac{f(X_2)(X_2 - X_1)}{f(X_2) - f(X_1)} \\ &= 2 - \frac{3(2 - 1)}{3 - (-4)} \\ &= 1,57142 \end{aligned}$$

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$$X_3 = 1,57142$$

- b) Iterasi II

$$X_2 = 2 \text{ dan } X_3 = 1,57142$$

$$\begin{aligned} f(x) &= 1,57142^3 + 1,57142^2 - 3 \cdot 1,57142 - 3 \\ &= 3,8809 + 2,4693 - 4,71426 - 3 \\ &= -6,3 \end{aligned}$$

- ↳ Dimasukkan ke-persamaan.

$$\begin{aligned} X_4 &= X_3 - \frac{f(X_3)(X_3 - X_2)}{f(X_3) - f(X_2)} \\ &= 1,57142 - \frac{(-6,3)(1,57142 - 2)}{-6,3 - 3} \end{aligned}$$

$$X_4 = 1,86172$$

- c) Iterasi III

$$X_3 = 1,57142 \text{ dan } X_4 = 1,86172$$

$$\begin{aligned} f(1,86172) &= 1,86172^3 + 1,86172^2 - 3 \cdot 1,86172 - 3 \\ &= 6,4527 + 3,4660 - 5,5851 - 3 \\ &= 1,3336 \end{aligned}$$

2) Selesaikan persamaan dengan metode Newton Rapshon, dg awal = 1

$$f(x) = x^3 + x^2 - 3x - 3 = 0$$

Jawab:

↳ Turunan pertama dari persamaan

$$f'(x) = 3x^2 + 2x - 3$$

a) Iterasi I

$$x_1 = 1$$

$$f(x_1) = 1^3 + 1^2 - 3 \cdot 1 - 3 = -4$$

$$f'(1) = 3 \cdot (1)^2 + 2 \cdot (1) - 3 = 2$$

↳ Dimasukan ke-persamaan.

$$x_2 = 1 - \frac{-4}{2}$$

$$= 3$$

b) Iterasi II

$$x_2 = 3$$

$$f(3) = 3^3 + 3^2 - 3 \cdot 3 - 3 = 24$$

$$f'(3) = 3 \cdot (3)^2 + 2 \cdot (3) - 3 = 30$$

↳ Dimasukan kedalam persamaan

$$x_3 = 3 - \frac{24}{30}$$

$$= 2,2$$

c) Iterasi III

$$x_3 = 2,2$$

$$f(2,2) = 2,2^3 + 2,2^2 - 3 \cdot 2,2 - 3 = 5,888$$

$$f'(2,2) = 3 \cdot (2,2)^2 + 2 \cdot (2,2) - 3 = 14,52 + 4,4 - 3 = 15,92$$

↳ Dimasukan persamaan

$$x_4 = 2,2 - \frac{5,888}{15,92}$$

$$= 1,83$$

d) Iterasi IV

$$x_4 = 1,83$$

$$f(1,83) = 1,83^3 + 1,83^2 - 3(1,83) - 3 = 0,9873$$

$$f'(1,83) = 3(1,83)^2 + 2(1,83) - 3 = 10,0467 + 3,66 - 3 = 10,7067$$

$$x_5 = 1,83 - \frac{0,9873}{10,7067} = 1,73778$$

e) Iterasi V

$$x_5 = 1,73778$$

$$f(1,73778) = 1,73778^3 + 1,73778^2 - 3(1,73778) - 3 = 0,05442$$

$$f'(1,73778) = 3(1,73778)^2 + 2(1,73778) - 3 = 9,0596 + 3,4755 - 3 = 9,5351$$

↳ Dimasukan ke persamaan.

$$x_6 = 1,73778 - \frac{0,05442}{9,5351}$$

$$= 1,73207$$