



Introduction to Computer Graphics

Lecture 10
Lighting and Shading

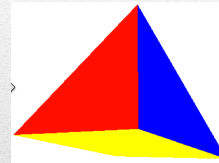


Outline

- Global and Local Illumination
 - Light Sources
 - Phong Illumination Model
 - Normal Vectors
-

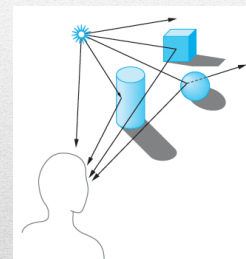
Introduction

- What gives 2D images the appearance of being 3D?
 - the gradations of color
 - shades of color
 - etc...
- Without lighting/shading....
 - a sphere is a uniformly colored circle, and a cube appears as a flat hexagon
- in 3D computer graphics, a group of algorithms are used to add more realistic lighting to 3D scenes

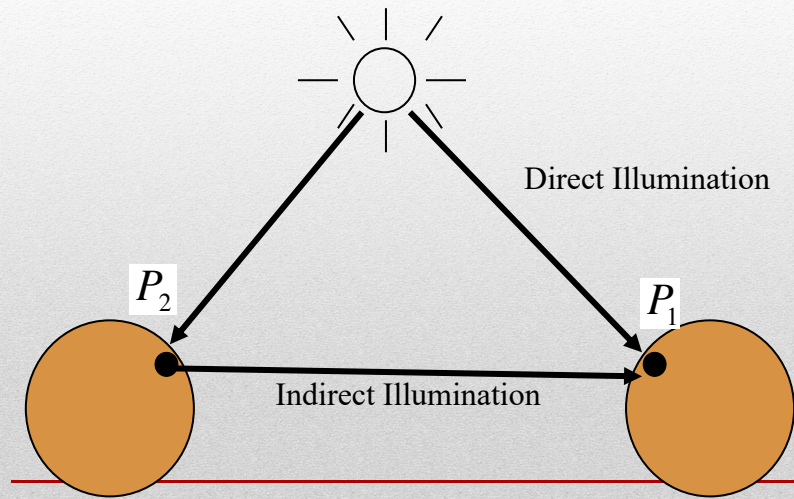


Global illumination

- a group of algorithms are used to add more realistic lighting to 3D scenes
 - Consider both
 - **direct illumination**
 - the light comes directly from a light source
 - **indirect illumination**
 - subsequent cases in which light rays from the same source are reflected by other surfaces in the scene, whether reflective or not

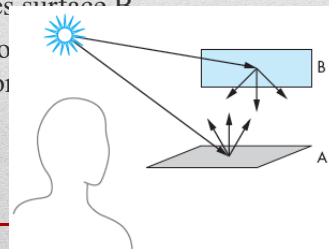


Global versus Local Illumination



Global illumination

- Recursive process:
 - Some light from the source that reaches surface A is scattered
 - Some of this reflected light reaches surface B
 - Some of it is then scattered back to surface A, and so on



Global Illumination

- Follow light rays through a scene
- Accurate, but expensive (off-line)
 - Numerical methods for computing a solution for the recursive process are not fast enough for real-time rendering.
- E.g.,
 - Ray tracing
 - Radiosity
 - Photon Mapping



Ray tracing Example

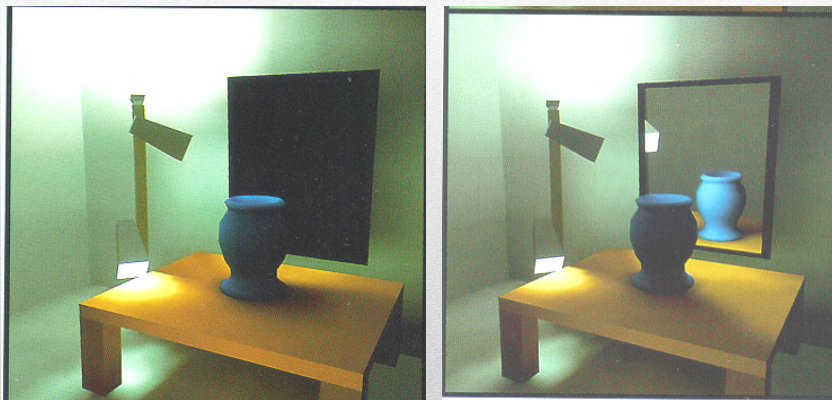


Martin Moeck,
Siemens Lighting

Global versus Local Illumination

- **Global Illumination**
 - Considers direct/indirect illumination
 - Reflection 反射
 - Refraction 折射
 - Shadows
- **Local Illumination**
 - Only considers direct illumination
 - No reflection
 - No refraction
 - Shadows possible

Global versus Local Illumination

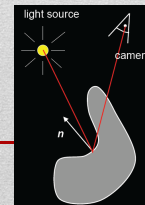


Images courtesy of Foley & van Dam, Computer Graphics

We start with simple local illumination and then extend those concepts/models to global illumination

Global versus Local Illumination

- **Local lighting** models
 - Approximate model
 - To add shading to a **fast** pipeline graphics architecture
 - E.g., **OpenGL** applications
 - Local interaction between light, surface, viewer
 - depend only on
 - the locations and properties of the light sources.
 - the material properties & the local geometry of the surface
 - Viewer positions
 - independent of any other surfaces in the scene
 - as opposed to global lighting models



Light Sources and Material Properties

- Appearance depends on
 - Light sources, their locations and properties
 - Material (surface) properties:
 - Viewer positions



Local Illumination

we consider **only single interactions** between light sources and surfaces

- Two independent parts of the problem :
 - model the **light sources** in the scene
 - follow rays of light from light-emitting surfaces
 - build a **reflection model** that deals with the interactions between materials and light.
 - model what happens to these rays as they interact with reflecting surfaces in the scene

Light Sources & Reflection Model

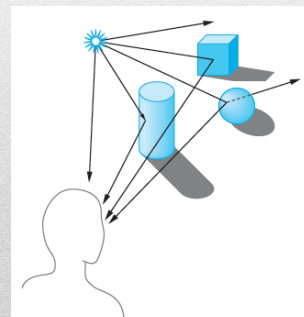
- What color we see?

If a ray of light enters her eye directly from the source:

→ she sees the color of the source

If the ray of light hits a surface visible to our viewer:

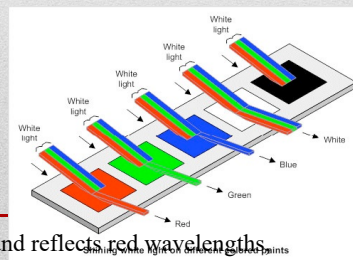
→ she sees the color that based on the light reflected from the surface toward her eyes



shows both single and multiple interactions between rays and objects

Light Sources & Reflection Model

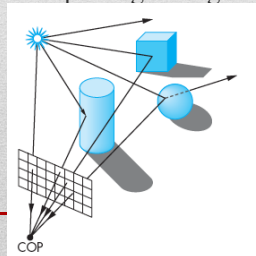
- What color?
 - the color that we see is determined by multiple interactions among light sources and reflective surfaces
 - Emission is what light sources do
 - Emission produces light
 - Adsorption is what paints, inks, dyes etc. do
 - adsorption removes light



E.g., Red paint absorbs green and blue wavelengths, and reflects red wavelengths, resulting in you seeing a red appearance

Light Sources & Reflection Model

- Which rays we should trace?
 - Only need to consider those rays that leave the source and reach **the viewer's eye**
 - replace the viewer by the projection plane
 - Only consider the rays that reach **the center of projection (COP)** after passing through the clipping rectangle



most rays leaving a source do not contribute to the image and are thus of no interest to us

Local Illumination

- In OpenGL
 - Phong model
 - fast
 - provides a compromise between physical correctness and efficient calculation
 - consider **only single interactions** between light sources and surfaces
 - Two independent parts of the problem
 - model the **light sources** in the scene
 - build a **reflection model**
 - that deals with the interactions between materials and light.
 - model what happens to these rays as they interact with reflecting surfaces in the scene

Defining a Light Source

- Use vectors {r, g, b, a} for light properties
- Beware: light positions will be transformed by the modelview matrix

```
GLfloat light_ambient[] = {0.2, 0.2, 0.2, 1.0};
GLfloat light_diffuse[] = {1.0, 1.0, 1.0, 1.0};
GLfloat light_specular[] = {1.0, 1.0, 1.0, 1.0};
GLfloat light_position[] = {-1.0, 1.0, -1.0, 0.0};
```

```
glLightfv(GL_LIGHT0, GL_AMBIENT, light_ambient);
glLightfv(GL_LIGHT0, GL_DIFFUSE, light_diffuse);
glLightfv(GL_LIGHT0, GL_SPECULAR, light_specular);
glLightfv(GL_LIGHT0, GL_POSITION, light_position);
```

Defining Material Properties

- OpenGL is a state machine:
- material properties stay in effect until changed

```
GLfloat mat_a[] = {0.1, 0.5, 0.8, 1.0};  
GLfloat mat_d[] = {0.1, 0.5, 0.8, 1.0};  
GLfloat mat_s[] = {1.0, 1.0, 1.0, 1.0};  
GLfloat low_sh[] = {5.0};
```

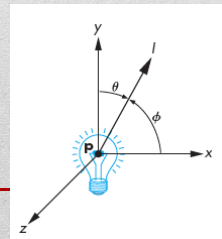
```
glMaterialfv(GL_FRONT, GL_AMBIENT, mat_a);  
glMaterialfv(GL_FRONT, GL_AMBIENT, mat_d);  
glMaterialfv(GL_FRONT, GL_SPECULAR, mat_s);  
glMaterialfv(GL_FRONT, GL_SHININESS, low_sh);
```

Outline

- Global and Local Illumination
- **Light Sources**
- Phong Illumination Model
- Normal Vectors

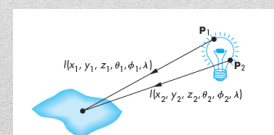
Light Sources

- Light can leave a surface through two fundamental processes:
 - **self-emission** and **reflection**
 - e.g., a light bulb can also reflect light that is incident on it from the surrounding environment.
 - the emissive term in our simple models is usually omitted



Light Sources

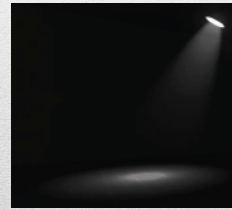
- Problem: How much is a surface illuminated by this source?
 - Obtain the total contribution of the source by integrating over its surface
 - accounts for the emission angles that reach this surface and the distance between the source and the surface
- Too difficult!!
- it is easier to model the distributed source with
 - Polygons (each of which is a simple source)
 - Or an approximating set of point sources



Types of Light Sources

These lighting types are sufficient for rendering most simple scenes:

- Ambient light
 - no identifiable source or direction
- Point source
 - given only by point
- Distant light
 - given only by direction
- Spotlight
 - from source in direction
 - Cut-off angle defines a cone of light
 - Attenuation function (brighter in center) (衰减)



Ambient Light

- Uniform lighting
- Lights entire scene
- Computationally inexpensive
- Simply add $[I_{ar} \ I_{ag} \ I_{ab}]$ to every pixel on every object
- A cheap hack to make the scene brighter.

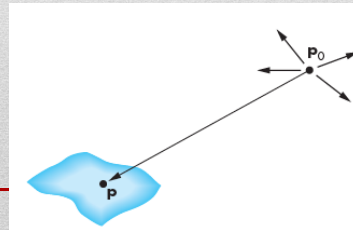
$$\mathbf{I}_a = \begin{bmatrix} I_{ar} \\ I_{ag} \\ I_{ab} \end{bmatrix}$$

Point Source

- Given by a point p_0
- Light emitted equally in all directions
- Intensity decreases with square of distance
 - At a point p , the intensity of light received from the point source p_0 :

$$I(p_0) = \begin{bmatrix} I_r(p_0) \\ I_g(p_0) \\ I_b(p_0) \end{bmatrix}$$

$$i(p, p_0) = \frac{1}{|p - p_0|^2} I(p_0)$$



Point Sources

Limitations

- Shading and shadows inaccurate
 - objects appear either bright or dark

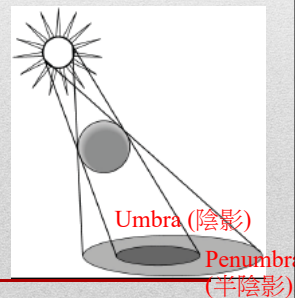
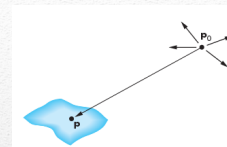
Example: penumbra (partial “soft” shadow)

- Compensate with attenuation

$$\frac{1}{a + bq + cq^2}$$

q : distance $|p - p_0|$
 a, b, c : constants

- Softens lighting

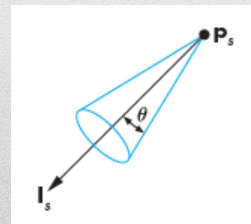


Shadows created by
finite-size light source

Spotlight

- Light still emits from point
 - Spotlight is constructed from a point source by limiting the angles at which light can be seen
- Cut-off by a cone
 - apex is at P_s
 - width is determined by an angle θ
 - points in the direction l_s

a narrow range of angles through which light is emitted



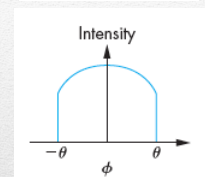
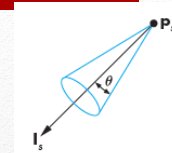
If $\theta = 180$, the spotlight becomes a point source

Spotlight

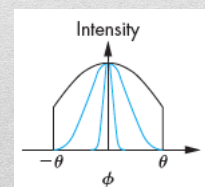
- Attenuation of a spotlight (More realistic)
 - most of the light concentrated in the center of the cone
 - Use the intensity function

$$\cos^e \varphi$$

- Φ : the angle between the direction of the source l_s and a vector s to a point on the surface
- $\Phi < \theta$
- exponent e : determines how rapidly the light intensity drops off
- Easy to compute: $\cos \Phi = u \cdot v$, if u, v are unit vector



$$\cos \varphi$$



$$\cos^e \varphi$$

Distant Light Source

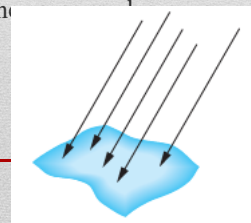
- Given by a direction vector
- Simplifies some calculations
 - most shading calculations require the direction
 - from the point on the surface to the light source position
 - if the light source is far from the surface, the vector does not change much as we move from point to point
 - E.g., the sun strikes all objects at proximity the
- In OpenGL:

$$\mathbf{p}_0 = \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$

Point source

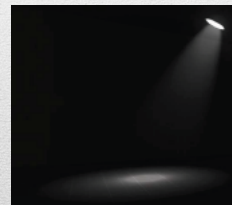
$$\mathbf{p}_0 = \begin{bmatrix} x \\ y \\ z \\ 0 \end{bmatrix}$$

Distant source



Light Sources Summary

- Ambient light
 - no identifiable source or direction
- Point source
 - given only by point
- Distant light
 - given only by direction
- Spotlight
 - from source in direction
 - Cut-off angle defines a cone of light
 - Attenuation function (brighter in center) (衰减)



Outline

- Global and Local Illumination
 - Light Sources
 - **Phong Reflection Model**
 - Normal Vectors
-

Phong Reflection Model

- Introduced by Phong
 - later modified by Blinn.
 - An efficient approach compromises between realism and efficiency
 - can be a close-enough approximation to physical reality to produce good renderings
-

Phong Reflection Model

$$I = \frac{1}{a + bq + cq^2} (k_d L_d (l \cdot n) + k_s L_s (r \cdot v)^\alpha) + k_a L_a$$

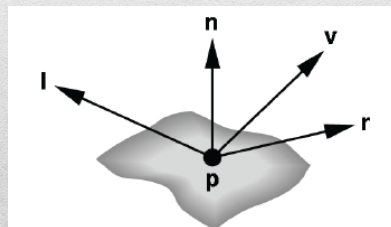
- Light components for each color:
 - Ambient (L_a), diffuse (L_d), specular (L_s)
- Material coefficients for each color:
 - Ambient (k_a), diffuse (k_d), specular (k_s)
- Distance q for surface point from light source

l : unit vector to light
 r : l reflected about n

n : surface normal
 v : vector to viewer

Phong Reflection Model

- The Phong model uses the four vectors, (l, v, n, r)
 - to calculate a color for an arbitrary point p on a surface
- Basic inputs are material properties and l, n, v



l = unit vector to light source
 v = unit vector to viewer
 n = surface normal
 r = reflection of l at p
 (determined by l and n)

Phong Reflection Model

Overview

The Phong model supports the three types of material–light interactions:

- Light source contributions decomposed into
 - Ambient reflection
 - Diffuse reflection
 - Specular reflection
- Calculate each color channel (R,G,B) separately

Light – Material Interactions

Diffuse surfaces:

- reflected light being scattered in all directions.
- Perfectly diffuse surfaces scatter light equally in all directions
 - appears the same to all viewers.
- E.g., many natural materials
 - such as terrain viewed from an airplane
 - Walls painted with matte/flat paint



Light – Material Interactions

Specular surfaces (appear shiny)

- appear shiny
- Light is reflected in a narrow range of angles
 - close to the angle of reflection
 - the angle of incidence = the angle of reflection
 - may be partially absorbed, but all reflected light emerges at a single angle
- E.g., Mirrors



Specular surface

Phong Reflection Model Overview

1. Start with global ambient light $[I_{ar} \ I_{ag} \ I_{ab}]$
2. Add contributions from each light source
 - Light source contributions decomposed into
 - Ambient reflection
 - Diffuse reflection
 - Specular reflection
 - Calculate each color channel (R,G,B) separately
3. Clamp the final result to $[0, 1]$

```
GLfloat ambientLight[] = { 0.5f, 0.5f, 0.5f, 1.0f };
glLightModelfv(GL_LIGHT_MODEL_AMBIENT, ambientLight);
glLightfv(GL_LIGHT0, GL_DIFFUSE, ambientLight);
glLightfv(GL_LIGHT0, GL_SPECULAR, specular);
glLightfv(GL_LIGHT0, GL_POSITION, lightPos);
```

Phong Reflection Model

Overview

1. Start with global ambient light [I_{ar} I_{ag} I_{ab}]
2. Add contributions from each light source
3. Clamp the final result to $[0, 1]$

$$I = \sum_i (I_{ia} + I_{id} + I_{is}) + I_a$$

Example

```
//Example Lighting Properties
GLfloat lmodel_ambient[] = { 0.2, 0.2, 0.2, 1.0 };
glLightModelfv(GL_LIGHT_MODEL_AMBIENT, lmodel_ambient);

GLfloat light_ambient[] = {0.2, 0.2, 0.2, 1.0};
GLfloat light_diffuse[] = {1.0, 1.0, 1.0, 1.0};
GLfloat light_specular[] = {1.0, 1.0, 0.0, 1.0};
glLightfv(GL_LIGHT0, GL_AMBIENT, light_ambient);
glLightfv(GL_LIGHT0, GL_DIFFUSE, light_diffuse);
glLightfv(GL_LIGHT0, GL_SPECULAR, light_specular);

//Example Material Properties
GLfloat mat_ambient[] = {0.8, 0.6, 0.4, 1.0};
GLfloat mat_specular[] = {0.0, 0.0, 0.0, 1.0};
GLfloat mat_diffuse[] = {0.8, 0.6, 0.4, 1.0};
GLfloat mat_shininess[] = {20.0};

glMaterialfv(GL_FRONT, GL_SPECULAR, mat_specular);
glMaterialfv(GL_FRONT, GL_AMBIENT, mat_ambient);
glMaterialfv(GL_FRONT, GL_DIFFUSE, mat_diffuse);
glMaterialf(GL_FRONT, GL_SHININESS, mat_shininess);
```


Phong Reflection Model

$$I = \frac{1}{a + bq + cq^2} (k_d L_d (l \cdot n) + k_s L_s (r \cdot v)^\alpha) + k_a L_a$$

- Light components for each color:
 - Ambient (L_a), diffuse (L_d), specular (L_s)
- Material coefficients for each color:
 - Ambient (k_a), diffuse (k_d), specular (k_s)
- Distance q for surface point from light source

l : unit vector to light
 r : l reflected about n

n : surface normal
 v : vector to viewer

Ambient Reflection

$$I_a = k_a L_a$$

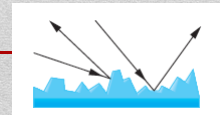
- L_a : ambient component of light source
 - L_a can be any of the individual light sources, or a global ambient term
- K_a : Ambient reflection coefficient $k_a = R_a$, $0 \leq k_a \leq 1$
 - A surface has three k_a components — k_{ar} , k_{ag} , k_{ab}
 E.g. a sphere appears yellow under white ambient light if its k_{ab} is small and its k_{ar} , k_{ag} are large
 - k_a may be different for every surface
- Intensity of ambient light is uniform at every point



Diffuse Reflection

$$I_d = k_d L_d (\mathbf{l} \cdot \mathbf{n})$$

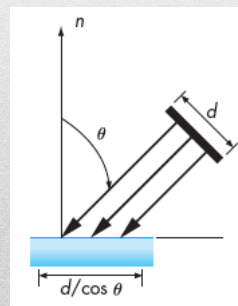
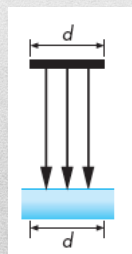
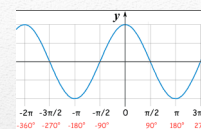
- K_d : Diffuse reflection coefficient, $0 \leq k_d \leq 1$
- the amount of light reflected depends both on
 - the material
 - the position of the light source relative to the surface
 - Angle of incoming light is important
 - can be modeled mathematically with Lambert's law



Diffuse Reflection

$$R_d \propto \cos \theta$$

- Lambert's Law:
 - Intensity depends on angle of incoming light.



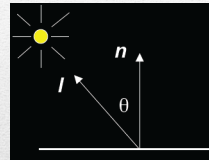
the same amount of light is spread over a larger area, and the surface appears dimmer.

Diffuse Reflection

Diffuse Light Intensity Depends On Angle Of Incoming Light

$$I_d = k_d L_d (\mathbf{l} \cdot \mathbf{n})$$

- $I_d = k_d L_d \cos \theta$
- $\cos \theta = \mathbf{l} \cdot \mathbf{n}$



\mathbf{l} : unit vector to light
 \mathbf{n} : unit surface normal
 θ : angle to normal

k_d : the fraction of incoming diffuse light that is reflected
 L_d : diffuse component of light

$$\mathbf{A} \cdot \mathbf{B} = \|\mathbf{A}\| \|\mathbf{B}\| \cos \theta$$

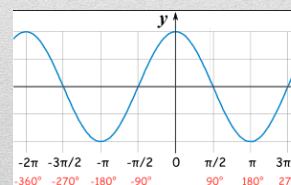
- Attenuation with distance:

$$I_d = \frac{k_d L_d}{a + bq + cq^2} (\mathbf{l} \cdot \mathbf{n})$$

q : distance to light source,

Diffuse Reflection

- Potential Problem: $I_d = k_d L_d (\mathbf{l} \cdot \mathbf{n})$
 - $(\mathbf{l} \cdot \mathbf{n})$ will be negative if the light source is below the horizon
 - use zero rather than a negative value
 - use $\max(\mathbf{l} \cdot \mathbf{n}, 0)$
 - $I_d = k_d L_d \max((\mathbf{l} \cdot \mathbf{n}), 0)$

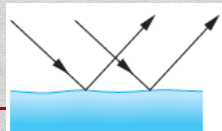


Specular Reflection

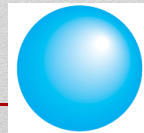
$$I_s = k_s L_s (\cos \phi)^a$$

k_s : Specular reflection coefficient, $0 \leq k_s \leq 1$

- Used to model highlights
 - a diffuse surface is rough, a specular surface is smooth
 - Shiny surfaces have high specular coefficient
 - Does not give mirror effect (need other techniques)

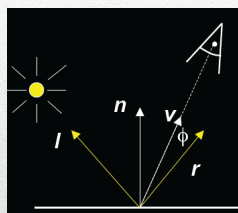


specular reflection



specular highlights

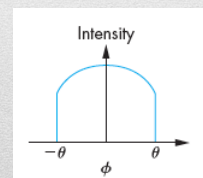
Specular Reflection



v = unit vector to camera
 r = unit reflected vector
 ϕ = angle between v and r

$$I_s = k_s L_s (\cos \phi)^a$$

- L_s is specular component of light
- a is shininess coefficient
- Can add distance term as well



$$\frac{I_s = k_s L_s (\cos \phi)^a}{a + bq + cq^2}$$

```
//Example Material Properties
```

```
GLfloat mat_ambient[]={0.8, 0.6, 0.4, 1.0};
```

```
GLfloat mat_diffuse[]={0.8, 0.6, 0.4, 1.0};
```

```
GLfloat mat_specular[]={0.0, 0.0, 0.0, 1.0};
```

```
GLfloat mat_shininess={50.0};
```

```
glMaterialfv(GL_FRONT, GL_SPECULAR,  
mat_specular);
```

```
glMaterialfv(GL_FRONT, GL_AMBIENT, mat_ambient);
```

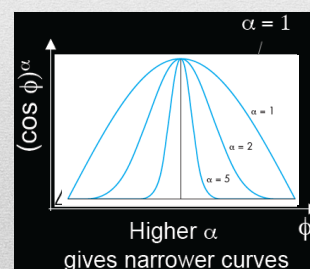
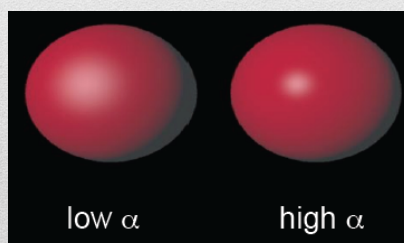
```
glMaterialfv(GL_FRONT, GL_DIFFUSE, mat_diffuse);
```

```
glMaterialf(GL_FRONT, GL_SHININESS, mat_shininess);
```

Shininess Coefficient

$$I_s = k_s L_s (\cos \phi)^{\alpha}$$

- α is the shininess coefficient

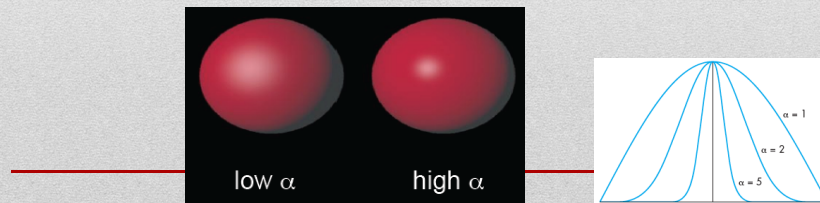


Specular Reflection

$$I_s = k_s L_s (\cos \phi)^\alpha = k_s L_s \max((r \cdot v)^\alpha, 0)$$

$$\cos \phi = v \cdot r$$

- α :
 - Larger value: most metallic surfaces
 - smaller values : materials that show broad highlights



Summary of Phong Model

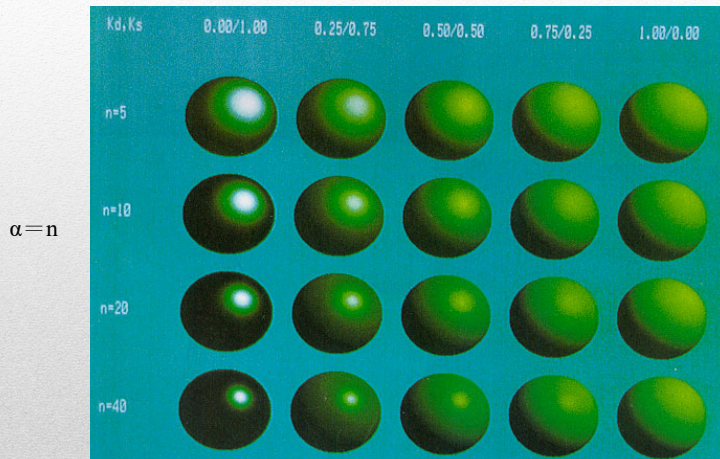
- Light components for each color:
 - Ambient (L_a), diffuse (L_d), specular (L_s)
- Material coefficients for each color:
 - Ambient (k_a), diffuse (k_d), specular (k_s)
- Distance q for surface point from light source

$$I = \frac{1}{a + bq + cq^2} (k_d L_d (l \cdot n) + k_s L_s (r \cdot v)^\alpha) + k_a L_a$$

l : unit vector to light
 r : l reflected about n

n : surface normal
 v : vector to viewer

Phong Example



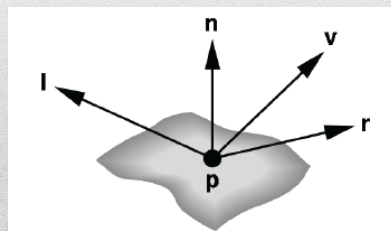
$$I = \frac{1}{a + bq + cq^2} (k_d L_d (l \cdot n) + k_s L_s (r \cdot v)^\alpha) + k_a L_a$$

Outline

- Global and Local Illumination
- Light Sources
- Phong Illumination Model
- Normal Vectors

Phong Reflection Model

- The Phong model uses the four vectors, (l, v, n, r)
 - to calculate a color for an arbitrary point p on a surface
- Basic inputs are material properties and l, n, v



l = unit vector to light source
 v = unit vector to viewer
 n = surface normal
 r = reflection of l at p
 (determined by l and n)

Normal Vectors

- The shading of objects also depends on the orientation of their surfaces
 - a factor that we shall see is characterized by the **normal vector** at each point
- Must calculate and specify the normal vector
 - Even in OpenGL!

Normals of Plane

Method I:

a plane is given by the equation: $ax + by + cz + d = 0$

- Let p_0 be a known point on the plane
 - Let p be an arbitrary point on the plane
 - Recall: $u \cdot v = 0$ if and only if u orthogonal to v
 - $n \cdot (p - p_0) = n \cdot p - n \cdot p_0 = 0$
 - Consequently $n_0 = [a \ b \ c]^T$
 - Normalize to $n = n_0/|n_0|$
-

Normals of Plane

Method II:

plane given by p_0, p_1, p_2

- Points must not be collinear
 - Recall: $u \times v$ orthogonal to u and v
 - $n_0 = (p_1 - p_0) \times (p_2 - p_0)$
 - Order of cross product determines orientation
 - Normalize to $n = n_0/|n_0|$
-

Normals of Sphere

- Implicit Equation : $f(x, y, z) = x^2 + y^2 + z^2 - 1 = 0$
- Vector form: $f(p) = p \cdot p - 1 = 0$
- Normal given by gradient vector

$$n_0 = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \\ \frac{\partial f}{\partial z} \end{bmatrix} = \begin{bmatrix} 2x \\ 2y \\ 2z \end{bmatrix} = 2p$$

- Normalize $n_0/|n_0| = 2p/2 = p$

Angle of Reflection

Perfect reflection (an ideal mirror):

angle of incident θ_i (入射角) = angle of reflection: θ_r (反射角)

- Note: l , n , and r must lie in the same plane
 - In 3D, these two conditions are sufficient to determine r from n and l
- Normalize l , n
 - Such that $|l| = |n| = 1$, also we want $|r| = 1$

$$l \cdot n = \cos(\theta_i) = \cos(\theta_r) = n \cdot r$$

The coplanar condition implies that:

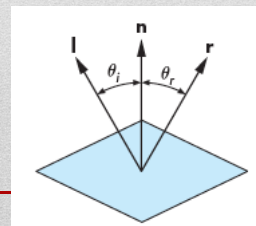
$$r = \alpha l + \beta n$$

$$\rightarrow n \cdot r = \alpha(l \cdot n) + \beta = l \cdot n \quad \text{---(1)}$$

$$\rightarrow r \cdot r = 1 = (\alpha l + \beta n)^2 = \alpha^2 + 2\alpha\beta(l \cdot n) + \beta^2 \quad \text{---(2)}$$

Solution: $\alpha = -1$ and $\beta = 2(l \cdot n)$

$$\rightarrow r = 2(l \cdot n)n - l$$



Summary

- Global and Local Illumination
- Light Sources
- Phong Illumination Model
- Normal Vectors

Lighting Guide:

<http://www.glprogramming.com/red/chapter05.html>
