

```
In [1]: library(gridExtra)
library(broom)
library(tidyverse)
library(car)
```

Warning message:

"package 'lubridate' was built under R version 4.4.2"

— **Attaching core tidyverse packages** — tidyverse  
2.0.0 —

```
✓ dplyr      1.1.4      ✓ readr      2.1.5
✓ forcats    1.0.0      ✓ stringr    1.5.1
✓ ggplot2    3.5.1      ✓ tibble     3.2.1
✓ lubridate  1.9.4      ✓ tidyr      1.3.1
✓ purrr      1.0.2
```

— **Conflicts** — tidyverse\_conflicts() —

✖ dplyr::combine() masks gridExtra::combine()

✖ dplyr::filter() masks stats::filter()

✖ dplyr::lag() masks stats::lag()

i Use the conflicted package (<http://conflicted.r-lib.org/>) to force all conflicts to become errors

Loading required package: carData

Attaching package: 'car'

The following object is masked from 'package:dplyr':

recode

The following object is masked from 'package:purrr':

some

```
In [2]: git_URL <- "https://raw.githubusercontent.com/mfouzan/STAT301/main/
raw_sleep_data <- read.csv(git_URL, sep = ",")

(raw_sleep_data)
```

Person.ID	Gender	Age	Occupation	Sleep.Duration	Quality.of.Sleep	Physical
<int>	<chr>	<int>	<chr>	<dbl>	<int>	
1	Male	27	Software Engineer	6.1	6	
2	Male	28	Doctor	6.2	6	

3	Male	28	Doctor	6.2	6
4	Male	28	Sales Representative	5.9	4
5	Male	28	Sales Representative	5.9	4
6	Male	28	Software Engineer	5.9	4
7	Male	29	Teacher	6.3	6
8	Male	29	Doctor	7.8	7
9	Male	29	Doctor	7.8	7
10	Male	29	Doctor	7.8	7
11	Male	29	Doctor	6.1	6
12	Male	29	Doctor	7.8	7
13	Male	29	Doctor	6.1	6
14	Male	29	Doctor	6.0	6
15	Male	29	Doctor	6.0	6
16	Male	29	Doctor	6.0	6
17	Female	29	Nurse	6.5	5
18	Male	29	Doctor	6.0	6
19	Female	29	Nurse	6.5	5
20	Male	30	Doctor	7.6	7
21	Male	30	Doctor	7.7	7
22	Male	30	Doctor	7.7	7
23	Male	30	Doctor	7.7	7
24	Male	30	Doctor	7.7	7
25	Male	30	Doctor	7.8	7
26	Male	30	Doctor	7.9	7
27	Male	30	Doctor	7.8	7
28	Male	30	Doctor	7.9	7
29	Male	30	Doctor	7.9	7
30	Male	30	Doctor	7.9	7

⋮	⋮	⋮	⋮	⋮	⋮
345	Female	57	Nurse	8.2	9
346	Female	57	Nurse	8.2	9
347	Female	57	Nurse	8.2	9
348	Female	57	Nurse	8.2	9
349	Female	57	Nurse	8.2	9
350	Female	57	Nurse	8.1	9
351	Female	57	Nurse	8.1	9
352	Female	57	Nurse	8.1	9
353	Female	58	Nurse	8.0	9
354	Female	58	Nurse	8.0	9
355	Female	58	Nurse	8.0	9
356	Female	58	Nurse	8.0	9
357	Female	58	Nurse	8.0	9
358	Female	58	Nurse	8.0	9
359	Female	59	Nurse	8.0	9
360	Female	59	Nurse	8.1	9
361	Female	59	Nurse	8.2	9
362	Female	59	Nurse	8.2	9
363	Female	59	Nurse	8.2	9
364	Female	59	Nurse	8.2	9
365	Female	59	Nurse	8.0	9
366	Female	59	Nurse	8.0	9
367	Female	59	Nurse	8.1	9
368	Female	59	Nurse	8.0	9
369	Female	59	Nurse	8.1	9
370	Female	59	Nurse	8.1	9
371	Female	59	Nurse	8.0	9
372	Female	59	Nurse	8.1	9
373	Female	59	Nurse	8.1	9
374	Female	59	Nurse	8.1	9

```
In [3]: # No. of Rows; No. of Observations

rows = nrow(raw_sleep_data)
print(rows)

[1] 374
```

```
In [4]: # No. of Columns; No. of Variables

col = ncol(raw_sleep_data)
print(col)

[1] 13
```

## 1. Data Description

The dataset contains **374 observations** and **13 variables** related to sleep health, lifestyle, and physiological metrics. Variables include demographic information (e.g., `Gender`, `Age`, `Occupation`), sleep metrics (e.g., `Sleep Duration`, `Quality of Sleep`), health indicators (e.g., `BMI Category`, `Blood Pressure`), and lifestyle factors (e.g., `Physical Activity Level`, `Daily Steps`). The data collection method is unspecified, but it appears to be synthetic or aggregated from self-reported surveys or health records.

### Variable Summary Table

Variable Name	Type	Description
Person ID	Numeric	Unique identifier for individuals
Gender	Categorical	Male or Female
Age	Numeric	Age in years
Occupation	Categorical	Job role (e.g., Doctor, Engineer)
Sleep Duration	Numeric	Hours of sleep per night
Quality of Sleep	Numeric	Self-rated sleep quality (scale likely 1-10)
Physical Activity Level	Numeric	Daily activity minutes
Stress Level	Numeric	Stress score (scale likely 1-10)
BMI Category	Categorical	Obesity classification (e.g., Normal, Overweight)
Blood Pressure	String	Blood pressure measurement (e.g., "126/83")
Heart Rate	Numeric	Resting heart rate (bpm)
Daily Steps	Numeric	Number of steps per day

Sleep Disorder      Categorical      Sleep disorder diagnosis (e.g., None, Insomnia)

**Data Source:** Attached file `Sleep_health_and_lifestyle_dataset.csv`.

**Citation:** Tharmalingam, L. (2023) Sleep health and lifestyle dataset, Kaggle.  
Available at: [https://www.kaggle.com/datasets/uom190346a/sleep-health-and-lifestyle-dataset/data?select=Sleep\\_health\\_and\\_lifestyle\\_dataset.csv](https://www.kaggle.com/datasets/uom190346a/sleep-health-and-lifestyle-dataset/data?select=Sleep_health_and_lifestyle_dataset.csv)

## 2: Predictive Research Question

### a) Research Question

"How do stress level, physical activity level, occupation, and BMI category contribute to the variability in sleep duration(In Hours Per Night), as measured by a linear regression model?"

- **Response Variable:** `Sleep Duration` (numeric, hours).
- **Explanatory Variables:**
  - `Stress Level` (numeric: 1-10 scale),
  - `Physical Activity Level` (numeric: daily activity minutes),
  - `Occupation` (categorical: e.g., Doctor, Engineer),
  - `BMI Category` (categorical: Normal, Overweight, Obese).

### b) Focus: Prediction

**Goal:** Build a regression model to predict sleep duration as a continuous numerical outcome.

#### Why Linear Regression Works Here:

- `Sleep Duration` is a **continuous numerical variable** (hours), making linear regression appropriate.
- The model will estimate the relationship between predictors and sleep duration, allowing for straightforward interpretation of coefficients.
- Alternative models (e.g., decision trees, gradient boosting, Exponential/log models) can also be explored if non-linear relationships exist.

## 3: Exploratory Data Analysis and Visualization

```
In [5]: # Load and clean the dataset
sleep_data <- read.csv(git_URL) |>
  # Trim whitespace in categorical variables
  mutate(across(c(Gender, Occupation, BMI.Category, Sleep.Disorder), ~
  # Convert categorical variables to factors
```

```

mutate(
  Gender = factor(Gender),
  Occupation = factor(Occupation),
  BMI.Category = factor(BMI.Category),
  Sleep.Disorder = factor(Sleep.Disorder)
) |>
# Convert daily steps to thousands for cleaner interpretation
mutate(Daily.Steps = Daily.Steps / 1000) |>
# Remove person ID column
select(-Person.ID) |>
select(-Occupation) |>
# Split blood pressure into numeric variables
separate(Blood.Pressure, into = c("Systolic", "Diastolic"), sep = "/"

# Verify structure
glimpse(sleep_data)
head(sleep_data)
tail(sleep_data)

```

Rows: 374

Columns: 12

\$ Gender	<fct> Male, Male, Male, Male, Male, Male, Male, Male...
\$ Age	<int> 27, 28, 28, 28, 28, 28, 29, 29, 29, 29, 29, 29...
\$ Sleep.Duration	<dbl> 6.1, 6.2, 6.2, 5.9, 5.9, 5.9, 6.3, 7.8, 7.8, 7...
\$ Quality.of.Sleep	<int> 6, 6, 6, 4, 4, 4, 6, 7, 7, 7, 6, 7, 6, 6, 6, 6...
\$ Physical.Activity.Level	<int> 42, 60, 60, 30, 30, 30, 40, 75, 75, 75, 30, 75...
\$ Stress.Level	<int> 6, 8, 8, 8, 8, 8, 7, 6, 6, 6, 8, 6, 8, 8, 8, 8...
\$ BMI.Category	<fct> Overweight, Normal, Normal, Obese, Obese, Obese...
\$ Systolic	<int> 126, 125, 125, 140, 140, 140, 140, 120, 120, 1...
\$ Diastolic	<int> 83, 80, 80, 90, 90, 90, 90, 80, 80, 80, 80, 80...
\$ Heart.Rate	<int> 77, 75, 75, 85, 85, 85, 82, 70, 70, 70, 70, 70...
\$ Daily.Steps	<dbl> 4.2, 10.0, 10.0, 3.0, 3.0, 3.0, 3.5, 8.0, 8.0, 8...
\$ Sleep.Disorder	<fct> None, None, None, Sleep Apnea, Sleep Apnea, In...

A data.frame

	Gender	Age	Sleep.Duration	Quality.of.Sleep	Physical.Activity.Level	Stress.
	<fct>	<int>	<dbl>	<int>		<int>
1	Male	27	6.1	6		42
2	Male	28	6.2	6		60
3	Male	28	6.2	6		60
4	Male	28	5.9	4		30
5	Male	28	5.9	4		30
6	Male	28	5.9	4		30

A data.frame

	Gender	Age	Sleep.Duration	Quality.of.Sleep	Physical.Activity.Level	Stress.
	<fct>	<int>	<dbl>	<int>		<int>
369	Female	59	8.1	9		75
370	Female	59	8.1	9		75
371	Female	59	8.0	9		75
372	Female	59	8.1	9		75
373	Female	59	8.1	9		75
374	Female	59	8.1	9		75

In [6]: *# Printing summary of the cleaned data*

summary(sleep\_data)

Gender	Age	Sleep.Duration	Quality.of.Sleep
Female:185	Min. :27.00	Min. :5.800	Min. :4.000
Male :189	1st Qu.:35.25	1st Qu.:6.400	1st Qu.:6.000
	Median :43.00	Median :7.200	Median :7.000
	Mean :42.18	Mean :7.132	Mean :7.313
	3rd Qu.:50.00	3rd Qu.:7.800	3rd Qu.:8.000
	Max. :59.00	Max. :8.500	Max. :9.000

Physical.Activity.Level	Stress.Level	BMI.Category	Systolic
Min. :30.00	Min. :3.000	Normal	:195
1st Qu.:45.00	1st Qu.:4.000	Normal Weight: 21	1st Qu.:12
Median :60.00	Median :5.000	Obese	: 10
Mean :59.17	Mean :5.385	Overweight	:148
3rd Qu.:75.00	3rd Qu.:7.000		
Max. :90.00	Max. :8.000		

Diastolic	Heart.Rate	Daily.Steps	Sleep.Disorder
Min. :75.00	Min. :65.00	Min. : 3.000	Insomnia : 77
1st Qu.:80.00	1st Qu.:68.00	1st Qu.: 5.600	None :219
Median :85.00	Median :70.00	Median : 7.000	Sleep Apnea: 78
Mean :84.65	Mean :70.17	Mean : 6.817	
3rd Qu.:90.00	3rd Qu.:72.00	3rd Qu.: 8.000	
Max. :95.00	Max. :86.00	Max. :10.000	

```
In [7]: # Custom theme for readability
theme_custom <- theme_minimal() +
  theme(
    plot.title = element_text(size = 14, face = "bold", hjust = 0.5),
    strip.text = element_text(face = "bold", size = 10),
    legend.position = "bottom",
    axis.text = element_text(size = 8)
  )

# Create the plot
sleep_data |>
  ggplot(aes(x = Stress.Level, y = Sleep.Duration)) +
  # Scatterplot: Color = Physical Activity, Size = Systolic BP
  geom_point(aes(color = Physical.Activity.Level, size = Systolic), al
  # Trendlines for each BMI group
  geom_smooth(aes(group = BMI.Category), method = "loess", color = "bl
  # Facet by BMI Category
  facet_wrap(~ BMI.Category, nrow = 1) +
  # Color gradient for physical activity
  scale_color_gradientn(
    name = "Physical Activity (minutes/day)",
    colors = c("#2c7bb6", "#abd9e9", "#fdae61", "#d7191c")
  ) +
  # Size scale for systolic blood pressure
```



```

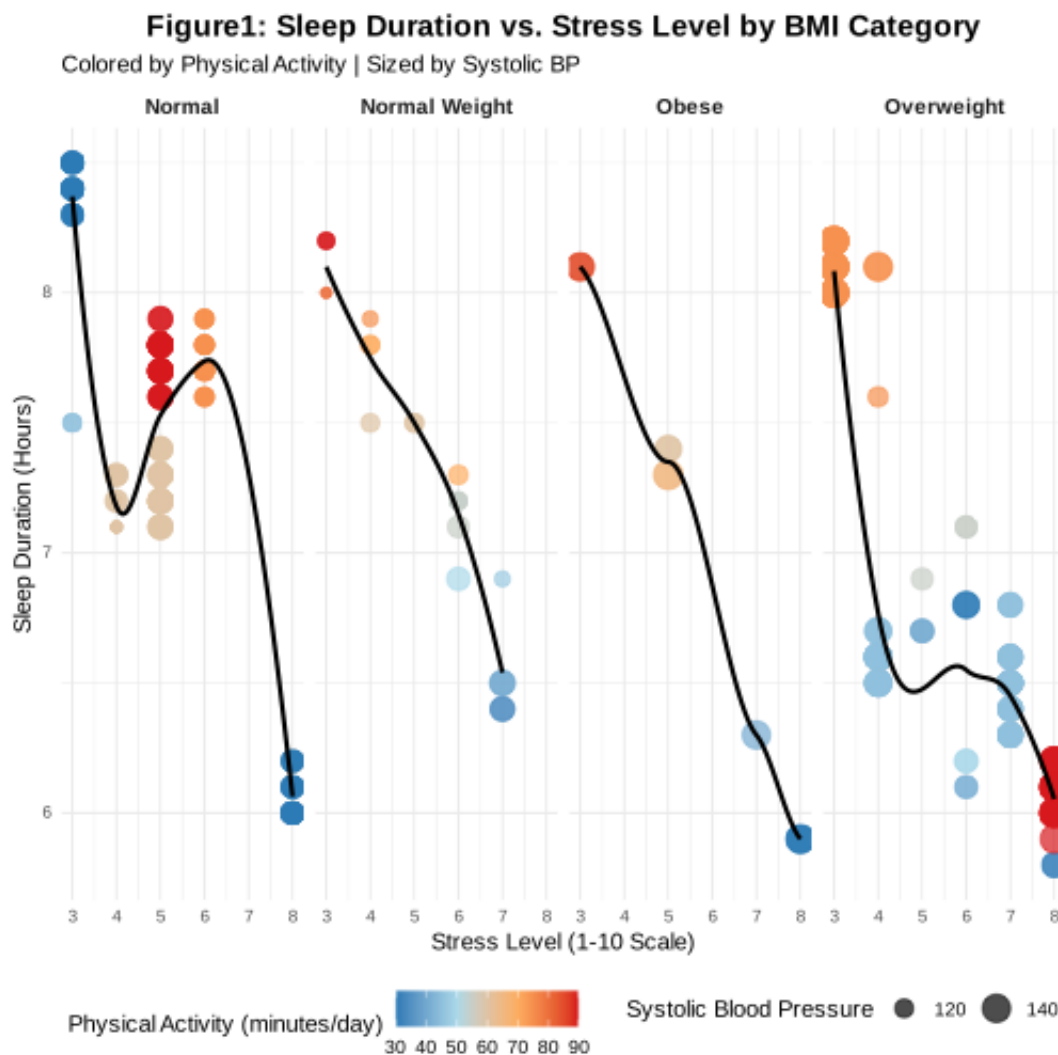
scale_size_continuous(
  name = "Systolic Blood Pressure",
  range = c(2, 6),
  breaks = c(120, 140, 160)
) +
# Labels and titles
labs(
  title = "Figure1: Sleep Duration vs. Stress Level by BMI Category",
  subtitle = "Colored by Physical Activity | Sized by Systolic BP",
  x = "Stress Level (1-10 Scale)",
  y = "Sleep Duration (Hours)"
) +
theme_custom

```

```

`geom_smooth()` using formula = 'y ~ x'
Warning message in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, :
"pseudoinverse used at 6"
Warning message in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, :
"neighborhood radius 2"
Warning message in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, :
"reciprocal condition number 5.4192e-17"
Warning message in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, :
"pseudoinverse used at 2.975"
Warning message in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, :
"neighborhood radius 4.025"
Warning message in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, :
"reciprocal condition number 9.5238e-17"
Warning message in simpleLoess(y, x, w, span, degree = degree, parametric = parametric, :
"There are other near singularities as well. 9.1506"

```



## Key Interpretation

**Figure 1.** Relationship between stress level and sleep duration, stratified by BMI category. Points are colored by daily physical activity level (minutes) and sized by resting heart rate (bpm). Three key observations emerge:

### 1. BMI Moderation:

- The negative relationship between stress and sleep duration is strongest in the **Obese** group (steepest slope).
- Normal BMI individuals maintain relatively stable sleep duration across stress levels.

### 2. Protective Effect of Activity:

- Higher physical activity (yellow points) correlates with better sleep retention at high stress levels, particularly in the Overweight group.

### 3. Physiological Warning Signs:

- Larger points (elevated heart rates) cluster in high-stress/short-sleep regions, suggesting a triad of:
  - Chronic stress
  - Sleep deprivation
  - Cardiovascular strain

### Implications for Modeling:

- Interaction terms between stress and BMI category should be explored.
- Heart rate and physical activity show non-linear relationships worthy of spline terms.

## Methods and Plan (Assignment 2)

### Proposed Method:

We will employ **multiple linear regression** to investigate the relationship between sleep duration (response variable) and various explanatory variables. Following initial model fitting, we will perform **model selection** using Variance Inflation Factor (VIF) analysis and **backward elimination** to identify the most relevant predictors. Residual diagnostics will assess assumptions and model validity.

---

### 1. Why is this method appropriate?

- Sleep duration is a continuous variable, making regression suitable for quantifying associations.
- Multiple regression allows simultaneous evaluation of multiple predictors (e.g., physical activity, screen time, stress levels) while controlling for confounding effects.
- Model selection (VIF/backward elimination) optimizes model simplicity and predictive accuracy by removing redundant or non-significant variables.

### 2. Key Assumptions:

- **Linearity:** Relationships between predictors and response are linear.
- **Independence:** Observations are independent (e.g., data not repeated measures).
- **Homoscedasticity:** Residual variance is constant across predicted values.
- **Normality:** Residuals are approximately normally distributed.
- **No Multicollinearity:** Predictors are not highly correlated (addressed via VIF).

### 3. Limitations and Weaknesses:

- **Linearity Assumption:** Non-linear relationships may be missed; transformations (e.g., log) could mitigate this.
  - **Causality:** Regression identifies associations, not causation.
  - **Outliers/Influential Points:** Extreme values may disproportionately affect results.
  - **Data Quality:** Results depend on accurate measurement of variables (e.g., self-reported data may introduce bias).
- 

### Next Steps:

1. Fit an initial full model with all predictors.
2. Use VIF to detect multicollinearity and remove variables with  $VIF > 5$ .
3. Apply backward elimination (p-value threshold: 0.05) to refine the model.
4. Validate assumptions via residual plots (e.g., residuals vs. fitted values, Q-Q plots).
5. Interpret final model coefficients to answer the research question.

## Code Implementation

```
In [8]: # Fitting full model with sleep duration as response and all explanatory
full_model <- lm(Sleep.Duration ~ ., data = sleep_data)

# Print initial model summary
cat("Initial Full Model Summary:\n")
print(summary(full_model))
```

## Initial Full Model Summary:

Call:

lm(formula = Sleep.Duration ~ ., data = sleep\_data)

Residuals:

Min	1Q	Median	3Q	Max
-0.68042	-0.16786	-0.04472	0.15315	0.83454

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	8.060878	0.924323	8.721	< 2e-16	***
GenderMale	0.538781	0.049525	10.879	< 2e-16	***
Age	0.055239	0.005138	10.750	< 2e-16	***
Quality.of.Sleep	0.054415	0.053286	1.021	0.307849	
Physical.Activity.Level	0.005855	0.001673	3.501	0.000522	***
Stress.Level	-0.245344	0.032093	-7.645	1.93e-13	***
BMI.CategoryNormal Weight	-0.131488	0.070874	-1.855	0.064381	.
BMI.CategoryObese	-0.645782	0.172924	-3.734	0.000219	***
BMI.CategoryOverweight	-0.831307	0.084152	-9.879	< 2e-16	***
Systolic	-0.136503	0.015041	-9.076	< 2e-16	***
Diastolic	0.164952	0.020335	8.112	8.00e-15	***
Heart.Rate	0.026406	0.009658	2.734	0.006564	**
Daily.Steps	-0.133519	0.022569	-5.916	7.70e-09	***
Sleep.DisorderNone	0.050956	0.058319	0.874	0.382838	
Sleep.DisorderSleep Apnea	0.054779	0.064760	0.846	0.398184	

---

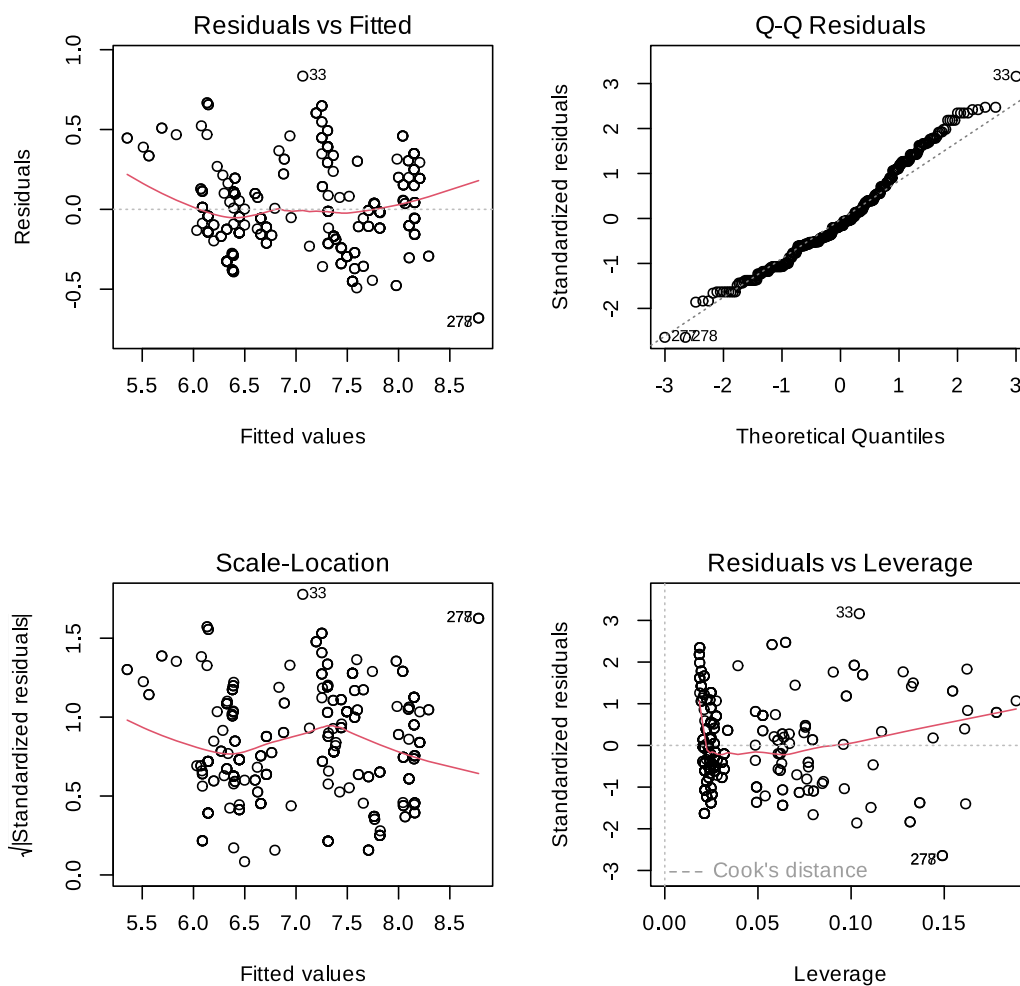
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.279 on 359 degrees of freedom

Multiple R-squared: 0.8816, Adjusted R-squared: 0.877

F-statistic: 191 on 14 and 359 DF, p-value: &lt; 2.2e-16

```
In [9]: # Check residual plots
par(mfrow = c(2, 2))
plot(full_model)
```



The residuals don't seem to have a random pattern, but in fact there is a little obvious pattern that concerns multicollinearity

```
In [10]: # Check for multicollinearity
vif_values <- vif(full_model)
print(vif_values)
```

	GVIF	Df	GVIF^(1/(2*Df))
Gender	2.944807	1	1.716044
Age	9.514085	1	3.084491
Quality.of.Sleep	19.486443	1	4.414345
Physical.Activity.Level	5.814697	1	2.411368
Stress.Level	15.535683	1	3.941533
BMI.Category	27.106903	3	1.733192
Systolic	65.054063	1	8.065610
Diastolic	75.202061	1	8.671912
Heart.Rate	7.642231	1	2.764459
Daily.Steps	6.386890	1	2.527230
Sleep.Disorder	6.906444	2	1.621114

Remove variables that have large VIF Values.

```
In [11]: # Reduced data, removing the variables
reduced_data <- sleep_data %>%
  select(-Systolic, -Diastolic, -Heart.Rate, -BMI.Category, -Quality.o
```

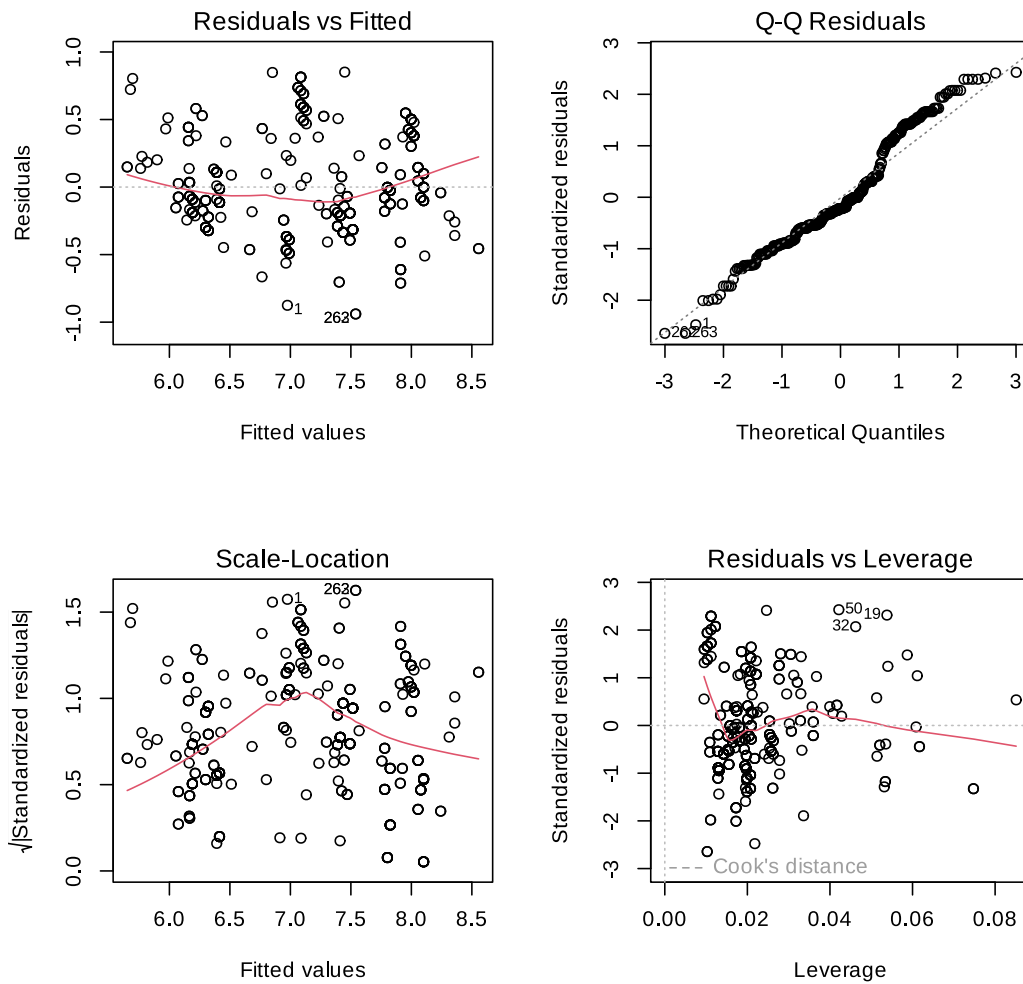
```
In [12]: # Fitting the reduced model
reduced_model <- lm(Sleep.Duration ~ ., data = reduced_data)

print(vif(reduced_model))
```

	GVIF	Df	GVIF^(1/(2*Df))
Gender	1.949089	1	1.396098
Age	2.250244	1	1.500081
Physical.Activity.Level	3.486064	1	1.867100
Stress.Level	2.089803	1	1.445615
Daily.Steps	3.235986	1	1.798885
Sleep.Disorder	2.443517	2	1.250270

```
In [13]: # Backward elimination
final_model <- step(reduced_model, direction = "backward", trace = 0)
```

```
In [14]: # Plotting the final model
par(mfrow = c(2, 2))
plot(final_model)
```



```
In [15]: # Summary of the final model
summary(final_model)
```



Call:

```
lm(formula = Sleep.Duration ~ Gender + Age + Physical.Activity.Level +
    Stress.Level + Daily.Steps + Sleep.Disorder, data = reduced_data)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.93959	-0.21241	-0.07799	0.20063	0.85099

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )	
(Intercept)	7.266641	0.198547	36.599	< 2e-16	***
GenderMale	0.440653	0.051579	8.543	3.57e-16	***
Age	0.022998	0.003199	7.189	3.70e-12	***
Physical.Activity.Level	0.007249	0.001658	4.372	1.60e-05	***
Stress.Level	-0.331366	0.015068	-21.991	< 2e-16	***
Daily.Steps	-0.051977	0.020565	-2.527	0.0119	*
Sleep.DisorderNone	0.549178	0.054366	10.102	< 2e-16	***
Sleep.DisorderSleep Apnea	0.291748	0.068412	4.265	2.55e-05	***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.3572 on 366 degrees of freedom

Multiple R-squared: 0.8022, Adjusted R-squared: 0.7984

F-statistic: 212.1 on 7 and 366 DF, p-value: < 2.2e-16

## Interpretation of the Results

This is the summary of a multiple linear regression model predicting **Sleep Duration** based on various independent variables. Here's the interpretation of key components:

### 1. Model Formula:

$$\text{Sleep.Duration} \sim \text{Gender} + \text{Age} + \text{Physical.Activity.Level} + \text{Stress.Level} + \text{Daily.Steps} + \text{Sleep.Disorder}$$

This means that **Sleep Duration** is being predicted based on gender, age, physical activity level, stress level, daily steps, and sleep disorder type.

### 2. Coefficients Interpretation:

Each coefficient represents the expected change in **Sleep Duration (in hours)** for a one-unit increase in the predictor, holding all else constant.

Predictor	Estimate	Interpretation
-----------	----------	----------------

<b>(Intercept)</b>	7.266	The baseline sleep duration when all predictors are at their reference values.
<b>Gender (Male)</b>	0.441	Males sleep <b>0.441 hours (≈26 minutes) more</b> than females, on average.
<b>Age</b>	0.023	Each additional year of age increases sleep duration by <b>0.023 hours (≈1.4 minutes)</b> .
<b>Physical Activity Level</b>	0.007	Higher physical activity level is associated with <b>0.007 hours (≈25 seconds) more sleep</b> .
<b>Stress Level</b>	-0.331	For each unit increase in stress, sleep duration decreases by <b>0.331 hours (≈20 minutes)</b> .
<b>Daily Steps</b>	-0.052	More steps per day are linked to a <b>slight decrease</b> in sleep duration.
<b>Sleep Disorder (None vs. Disorder)</b>	0.549	People <b>without sleep disorders</b> sleep <b>0.549 hours (≈33 minutes) more</b> than those with sleep disorders.
<b>Sleep Apnea</b>	0.292	People with <b>sleep apnea</b> sleep <b>0.292 hours (≈17 minutes) more</b> than those with other disorders.

### 3. Statistical Significance:

- Stars ( **\*\*\***, **\*\***, **\*** ) indicate significance levels\*\*:
  - \*\*\*** ( $p < 0.001$ ) → Highly significant
  - \*\*** ( $p < 0.01$ ) → Significant
  - \*** ( $p < 0.05$ ) → Moderately significant
- All variables except Daily Steps ( $p = 0.0119$ ) are highly significant ( $p < 0.001$ ), meaning they strongly impact Sleep Duration.

### 4. Model Fit:

- Multiple  $R^2 = 0.8022$**  → The model explains **80.22% of the variance** in Sleep Duration.
- Adjusted  $R^2 = 0.7984$**  → Adjusted for the number of predictors, still strong.
- F-statistic = 212.1, p-value  $< 2.2e-16$**  → The overall model is statistically significant.

In [ ]: