

```
for (i=left; i <= right; i++)  
    arr[i] = temp[i]
```

return invCount;

{

```
int mergeSort (int arr[], int arrSize)  
{  
    int temp [arrSize];
```

```
    return mergeSortCount (arr, temp, 0, arrSize);
```

{

```
int mergeCount (int arr[], int temp[], int left  
                int right) {
```

```
    int mid, inv=0;
```

```
    if (right > left) {
```

```
        mid = (right + left)/2;
```

```
        inv+= mergeCount (arr, temp, left, mid);
```

```
        inv+= mergeCount (arr, temp, mid, right);
```

```
        inv+= mergeCount (arr, temp, left, right);
```

{

return inv;

}

10 Worst case:-  $\Theta(n^2)$  -  $O(n^2)$

→ The worst case occurs when the partition process picks up greatest or smallest element as pivot

Best case:-  $\Theta(n \log n)$  -  $\Omega(n \log n)$

→ The best case occur when the partition process a picks the middle elent as pivot

- Has running time of  $O(n^2)$  that makes it unacceptable in application.
- More often than not runs of  $O(n \log n)$
- High space efficiency by executing in place
- & most utility in C programming language is provided quicksort.

Q Inversion count for an array indicates how far the array being start if array sorted, then the inversion 0, but if the array is sorted in the reverse order the count is the maximum.

```

int merge(int arr[], int temp[], int left, int mid, int right)
int i, j, K;
int inv_count = 0;
i = left; j = mid, K = left;
while (c.i <= mid - 1) && (j <= right)) {
    if (arr[i] < arr[j]) {
        temp[K++] = arr[i++];
    }
    else {
        temp[K++] = arr[j++];
        inv_count = inv_count + mid - i;
    }
}
while (i <= mid - 1)
    temp[K++] = arr[i++];
while (j <= right)
    temp[K++] = arr[j++]
    
```

## ⑥ Time Complexity:

of Recurrence relation

Best case = O(1)

Average =  $O(n \log n)$

Worst =  $T(n) = T(n/2) + c$

$$T(n) \begin{cases} c & \text{if } i \geq f \\ T(n/2) + c & \text{otherwise.} \end{cases}$$

## ⑦ Recursive:

```
int binary (int arr[], int low, int high , int x)
{
    if (low > high)
        return -1;
    int mid = (low+high)/2;
    if (x == arr[mid])
        return mid;
    else if (x < arr[mid])
        return binary (arr, low, mid-(1));
    else
        return binary (arr, mid+1, high, x);
}
```

8 Quick sort is best in terms of practical use as, most widely sorting algorithm at present

```

if(a[j] > a[j+1])
    temp = a[j]
    a[j] = a[j+1]
    a[j+1] = temp
endif
end for
end for

```

(3) Algorithm	Time Complexity		
	Best	Average	Worst
Selection Sort	$\Omega(n^2)$	$\Theta(n^2)$	$O(n^2)$
Bubble Sort	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$
Insertion Sort	$\Omega(n)$	$\Theta(n^2)$	$O(n^2)$
Heap Sort	$\Omega(n \log n)$	$\Theta(n \log n)$	$O(n \log n)$
Quick Sort	$\Omega(n \log n)$	$\Theta(n \log n)$	<del><math>O(n^2 \log n)</math></del>
Merge Sort	$\Omega(n \log n)$	$\Theta(n \log n)$	$O(n \log n)$

(4) Bubble Sort, insertion sort, Selection Sort in place  
Sorting algo.

- Merge Sort is a stable but not an in-place Algorithm
- Insertion Sort is also used for Online Sorting
- Quick Sort is not stable but is an in-place Algo
- Heap Sort is an in-place but not Stable
- Selection Sort is also an Online Sorting Algo.

for For  $i=0$  to  $n-1$  do:

    small sub =  $i$

    For  $j=0+1$  to  $n-1$  do'

        if  $A(j) < A(\text{small sub})$

            small sub =  $j$

    end if

end of for

    temp =  $A[i]$

$A[i] = A[\text{small sub}]$

$A[\text{small sub}] = \text{temp}$

end for

Insertion Sort ↳

For  $i=1$  to  $n-1$

$j=1$

    do while ( $j > 0$ ) and ( $a[j] < a[j-1]$ )

        temp =  $a[j]$

$a[j] = a[j-1]$

$a[j-1] = \text{temp}$

$j=j-1$

end do

end for.

Bubble Sort ↳

for  $i=0$  to  $n-2$

    for  $j=0$  to  $n-2$

        for  $j=0$  to

NAME = TARUN KUMAR DHIMAN

ROLL No = 1918917

Sec = IT

① Search (arr, n, x)

if (arr[n-1] == x)

{

return "found";

}

int backup = arr[n-1];

arr[n-1] = x;

for (int i=0; ; i++)

{

if (arr[i] == x)

{

arr[n-1] = backup;

if (i < n-1)

return "found";

else

return "Notfound";

}

}

3

②

Selection Sort: