### **Extended Binary Tree: -**

- Extended binary tree consists of replacing every null subtree of the original tree with special nodes.
- Empty circle represents internal node and square represents external node.
- The nodes from the original tree are internal nodes and the special nodes are external nodes
- Every internal node in the extended binary tree has exactly two children and every external node is a leaf. It displays the result which is a complete binary tree.



Fig. Extended Binary Tree

#### **Properties of External binary tree**

- 1. The nodes from the original tree are internal nodes and the special nodes are external nodes.
- 2. All external nodes are leaf nodes and the internal nodes are non-leaf nodes.
- **3.** Every internal node has exactly two children and every external node is a leaf. It displays the result which is a complete binary tree

## Complete Binary Tree: -

A binary tree is said to be a complete binary tree in data structure if it meets the following conditions

- All the levels except possibly the last level have the maximum number of possible nodes.
- All the nodes in the last level appear as far left as possible. That is, at the last level, there should not be any right successor of a parent not without a left successor

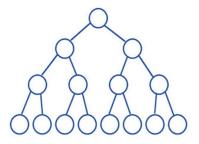
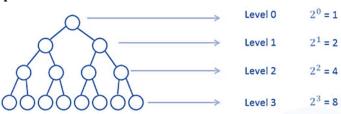


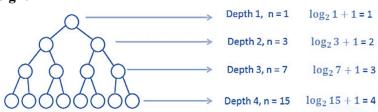
Figure: Complete Binary tree

## Nodes at level r



#### A tree can have atmost $2^r$ nodes at level r

# Depth or height



The depth of the complete tree with n nodes is given by Depth = Height =  $\log_2\,n+1$