

## ASSIGNMENT - 4 C6206

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Q1

- (a.) Let  $A = \{ \text{set of airline flight from N.York to Delhi} \}$   
 $B = \{ \text{set of non-stop airline flight from N.York to Delhi} \}$

Every non-stop airline flight from New York to Delhi is a flight from New York to Delhi.

Thus  $B \subset A$

- (b.) Let  $A = \{ \text{set of people speaking English} \}$   
 $B = \{ \text{set of people speaking Chinese} \}$

Neither  $A$  is subset of  $B$  nor  $B$  is subset of  $A$ .

- (c.) First set  $A = \{ \text{flying squirrels} \}$   
 $B = \{ \text{living creatures that fly} \}$

$$A \subset B$$

Q2

- (a.)  $0 \in \phi$  - False

It means that  $0$  is an element of empty set.  
 But empty set contains no element

(b.)  $\phi \in \{0\}$  - False

empty set does not belong to  $\{0\}$ , it has only one element '0'.

(c.)  $\phi < \{0\}$  - True

(d.)  $\{0\} \in \{0\}$  - False

(e.)  $\{0\} < \{0\} \rightarrow$  False

sets are completely identical hence false

(f.)  $\{\phi\} \subseteq \{\phi\}$  - True

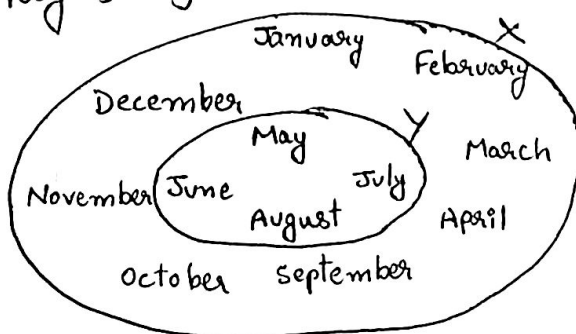
A set is always an inclusive subset of itself

Q3

Sol

Let  $X = \{ \text{set of all months in a year: January, February, February, March, April, May, June, July, August, September, October, november, december?} \}$

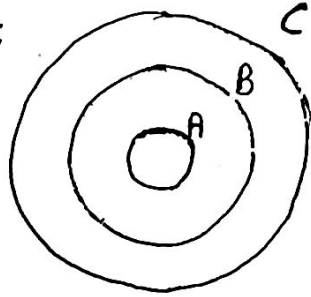
$Y = \{ \text{set without letter R in X: May, June, July, August} \}$



Q4Sol

given :  $A \subset B$  and  $B \subset C$

Venn diagram:

Q5Sol

Cardinality = no. of elements present in the set

$$(a) \{a\} \Rightarrow 1$$

$$(b) \{\{a\}\} \Rightarrow 1$$

$$(c) \{a, \{a\}\} \Rightarrow 2$$

$$(d) \{a, \{a\}, \{a, \{a\}\}\} \Rightarrow 3$$

Q6Sol

Let  $A$  be a set

$$\text{To show } \Rightarrow \phi \times A = A \times \phi = \phi$$

The cardinality of the output set is equal to product of cardinality of input set.

$$|A \times \phi| = |A| \times |\phi| = 0$$

But 0 is cardinality of  $\phi$ .

$$\therefore \phi \times A = \phi = A \times \phi$$

Q7

Given:  $A - B = \{1, 5, 7, 8\}$

$$B - A = \{2, 10\}$$

$$A \cap B = \{3, 6, 9\}$$

we know,

$$A = (A \cap B) \cup (A - B)$$

$$A = \{3, 6, 9\} \cup \{1, 5, 7, 8\}$$

$$\boxed{A = \{1, 3, 5, 6, 7, 8, 9\}}$$

Similarly

$$B = (A \cap B) \cup (B - A)$$

$$B = \{3, 6, 9\} \cup \{2, 10\}$$

$$\boxed{B = \{2, 3, 6, 9, 10\}}$$

Q8Sol

The cartesian product  $A \times B \times C$  contains triplets of the form  $\{(a, b, c) \mid a \in A \cap b \in B \cap c \in C\}$

whereas,

The cartesian product  $(A \times B) \times C$  contains doublets of the form  $\{(\{a, b\}, c) \mid (a \in A \cap b \in B) \cap c \in C\}$

Thus they are not equal as they have different elements in them.

— END —