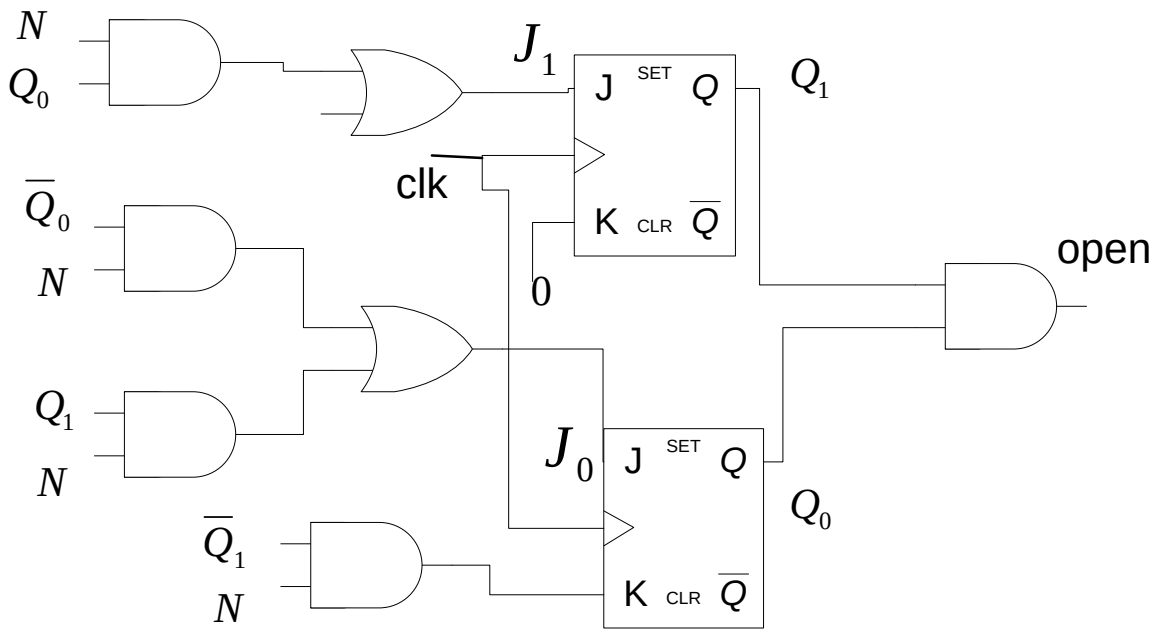
Timing

Vending Machine- J-K flip flops implementation



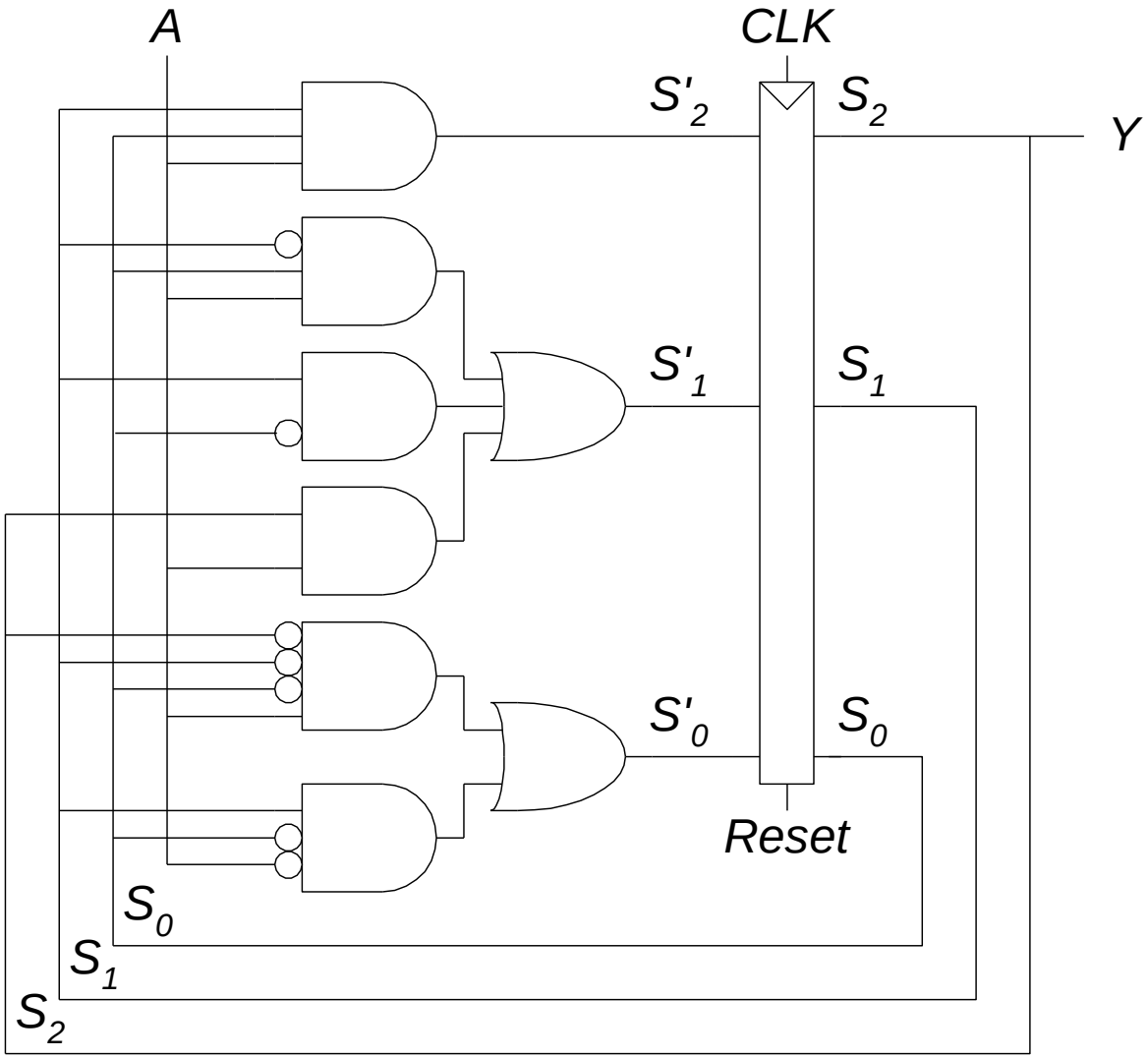
$J_1 = D+Q_0 .N$

$J_0 = Q_1' . N + Q_1 . D$

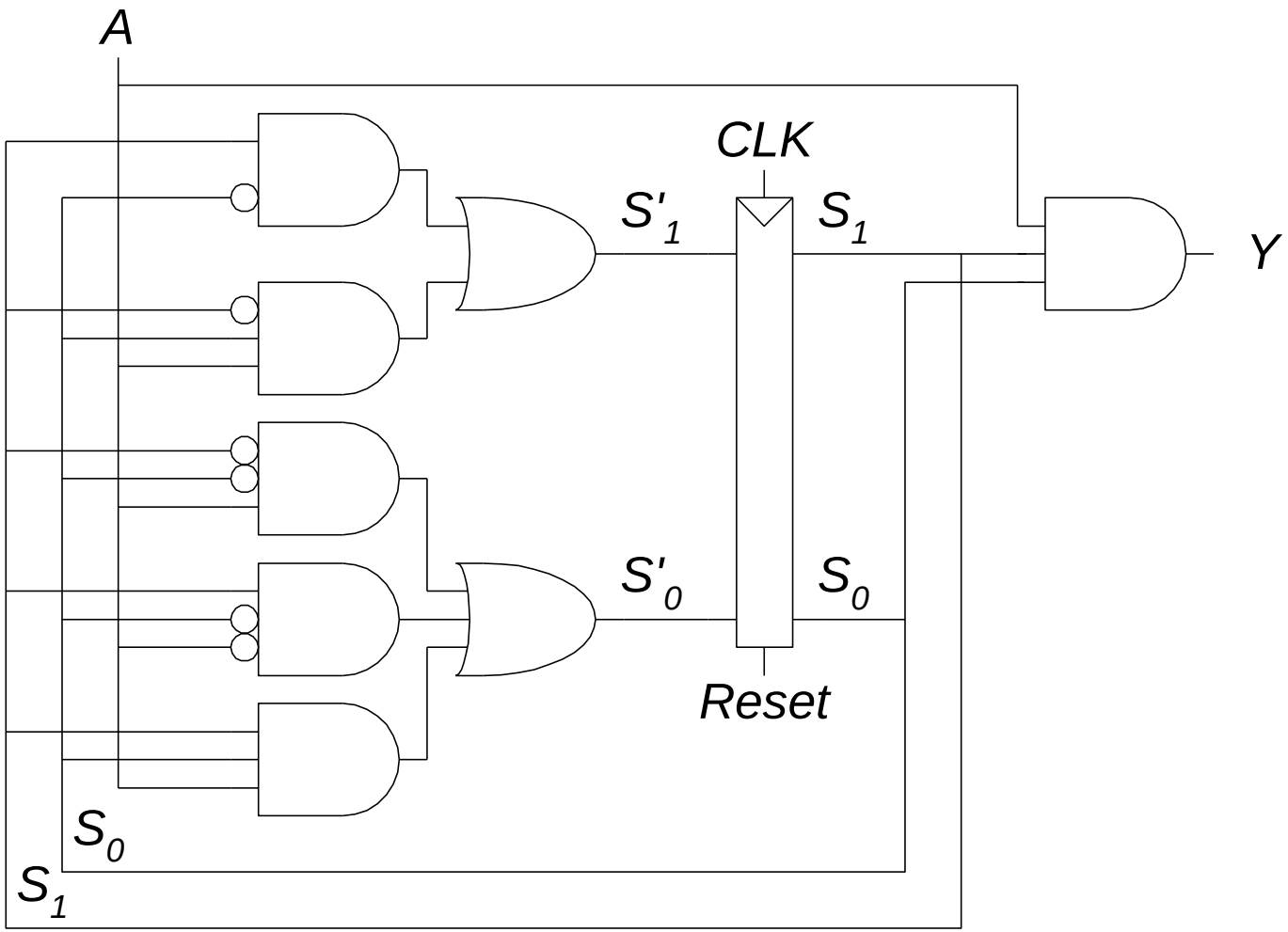
$K_1 = 0$

$K_0 = Q_1' . N$

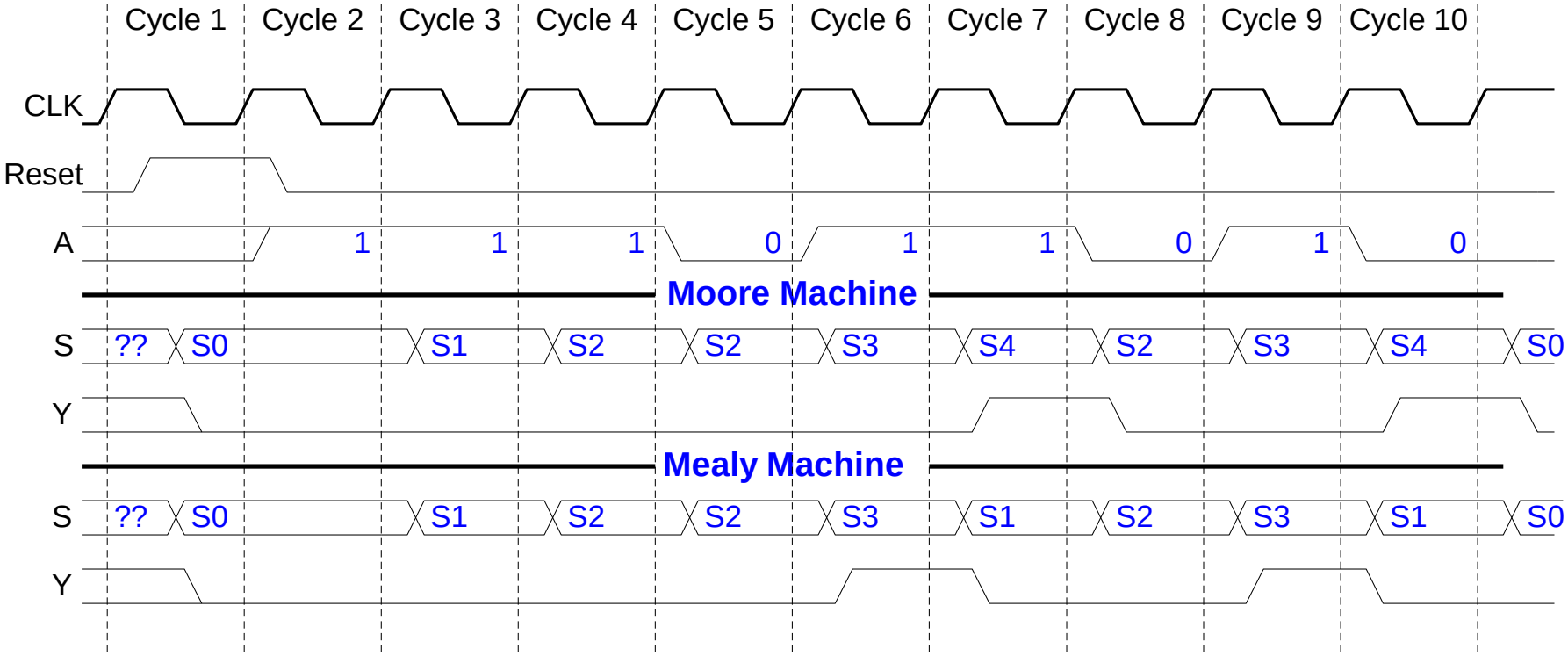
Moore FSM Schematic



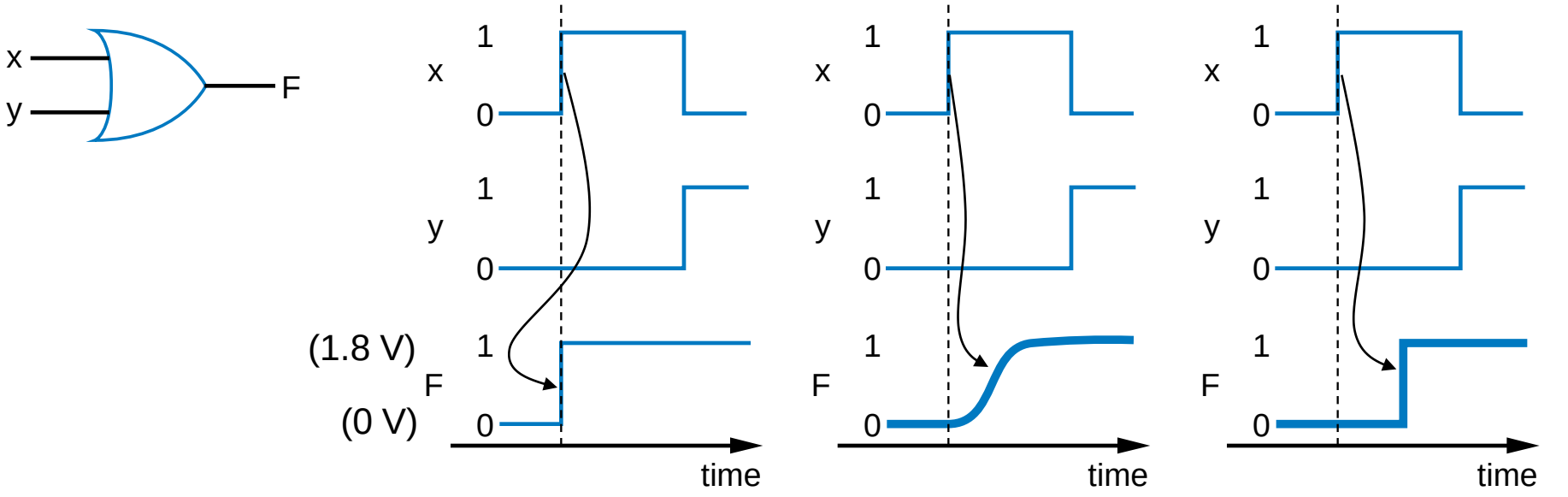
Mealy FSM Schematic



Moore and Mealy Timing Diagram

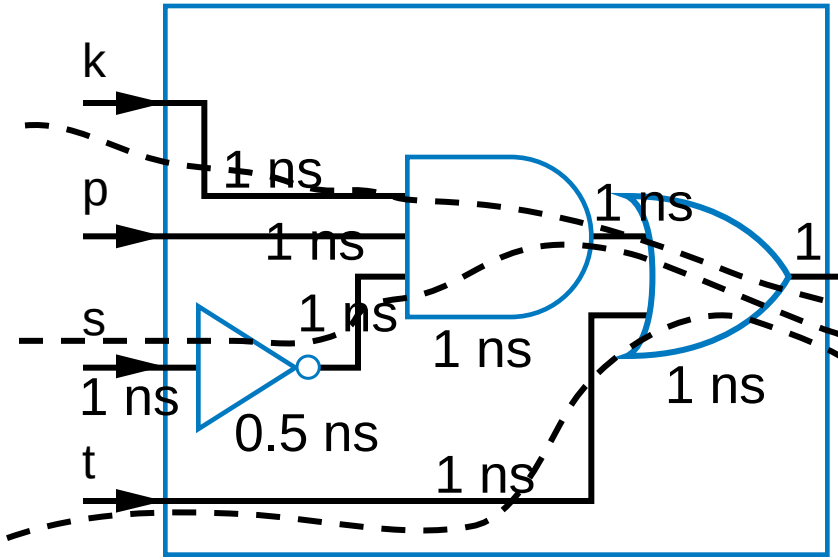


Additional Considerations
Non-Ideal Gate Behavior -- Delay



- Real gates have some delay
  - Outputs don't change immediately after inputs change

Circuit Delay and Critical Path



1+1+1+1+1 = 5 ns

1+0.5+1+1+1+1+1 = 6.5 ns

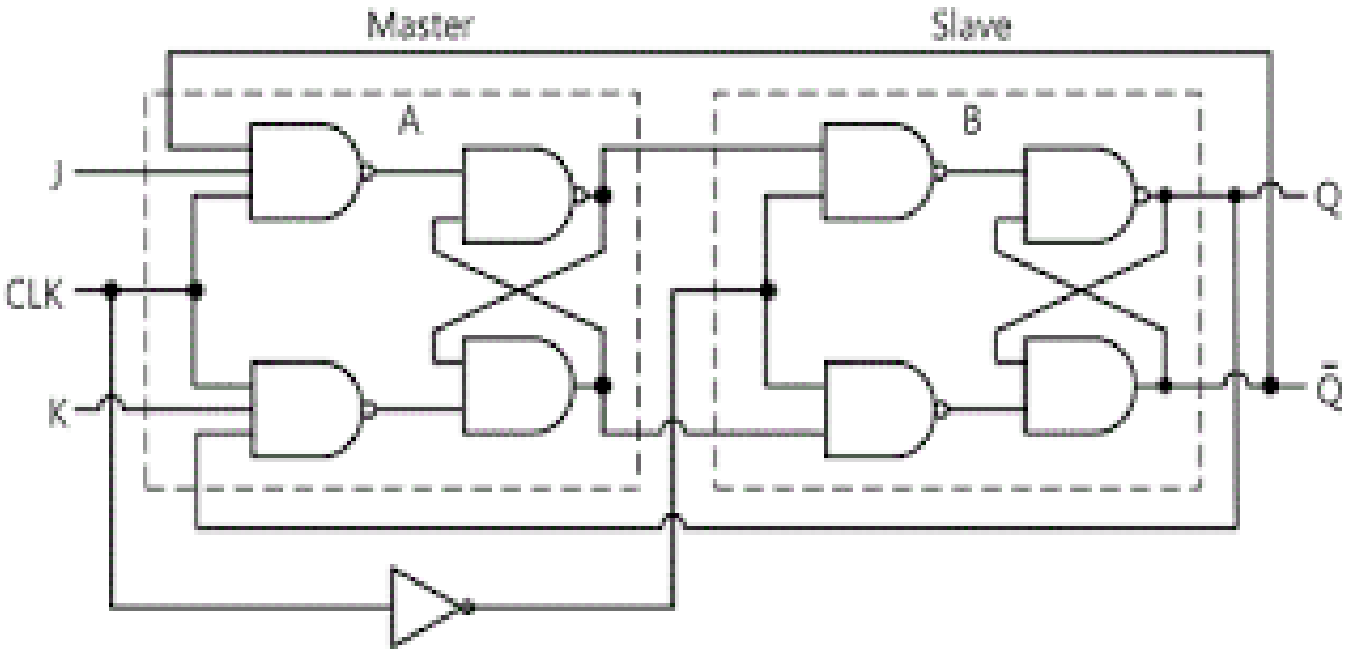
1+1+1 = 3 ns

Critical path delay = 6.5 ns

Hence, circuit's delay is 6.5 ns

- Wires also have delay
- Assume gates and wires have delays as shown
- Path delay – time for input to affect output
- Critical path – path with longest path delay
- Circuit delay – delay of critical path

J-K Flip Flop

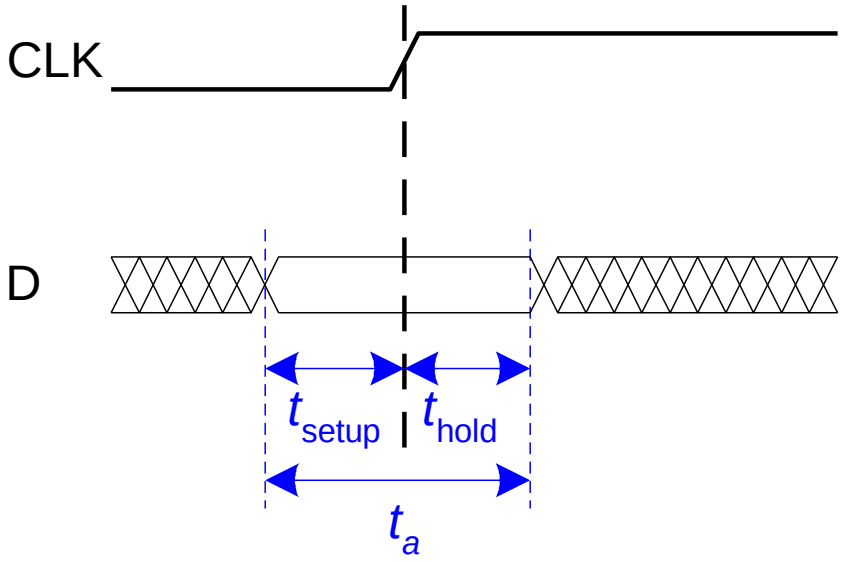


Timing

- Flip-flop samples *D* at clock edge
- *D* must be stable when it is sampled
- Similar to a photograph, *D* must be stable around the clock edge
- If *D* is changing when it is sampled, metastability can occur

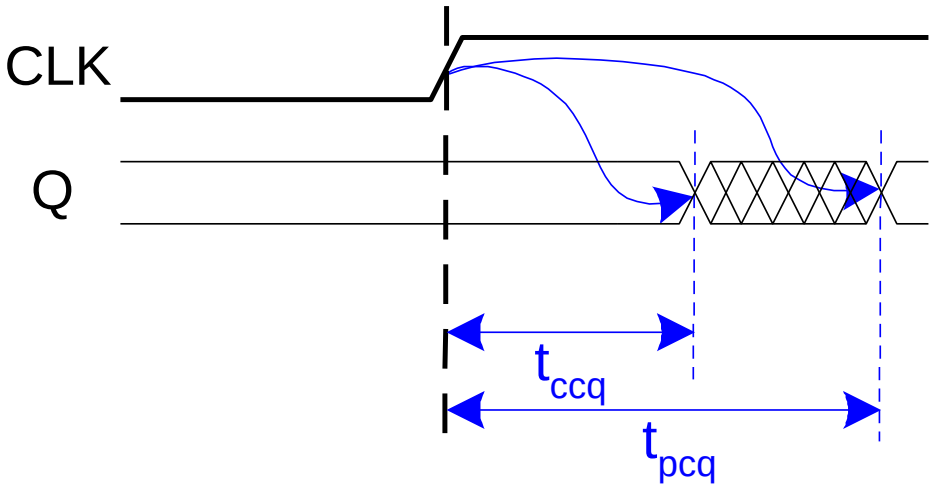
Input Timing Constraints

- Setup time: t_{setup} = time *before* the clock edge that data must be stable (i.e. not changing)
- Hold time: t_{hold} = time *after* the clock edge that data must be stable
- Aperture time: t_a = time around clock edge that data must be stable ($t_a = t_{setup} + t_{hold}$)



Output Timing Constraints

- Propagation delay: t_{pcq} = time after clock edge that the output Q is guaranteed to be stable (i.e., to stop changing)
- Contamination delay: t_{ccq} = time after clock edge that Q might be unstable (i.e., start changing)

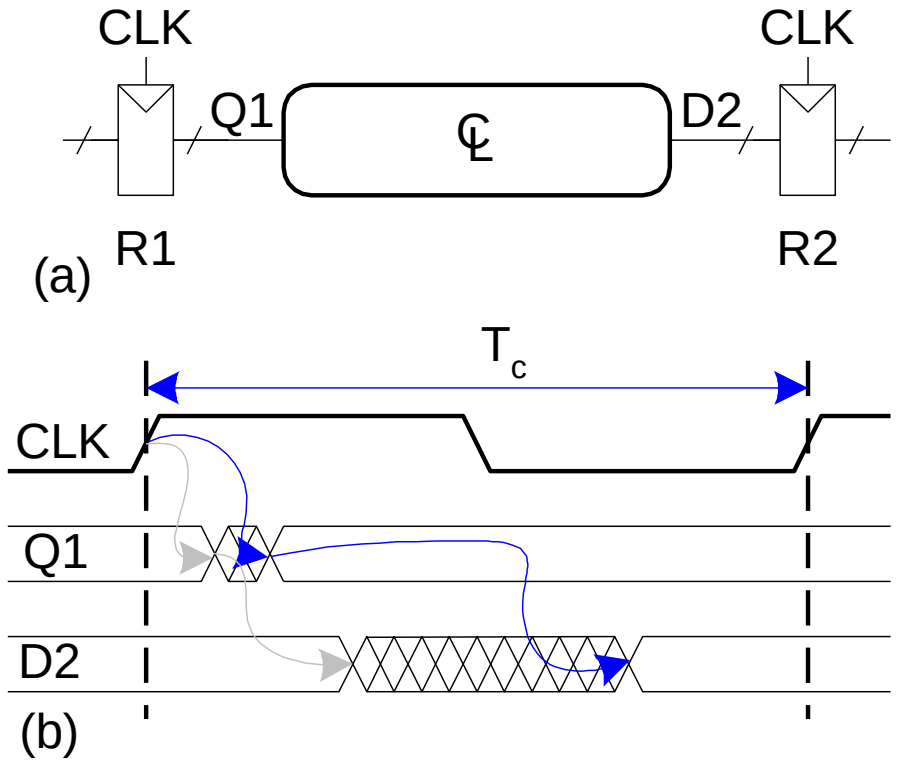


Dynamic Discipline

- The input to a synchronous sequential circuit must be stable during the aperture (setup and hold) time around the clock edge.
- Specifically, the input must be stable
  - at least t_{setup} before the clock edge
  - at least until t_{hold} after the clock edge

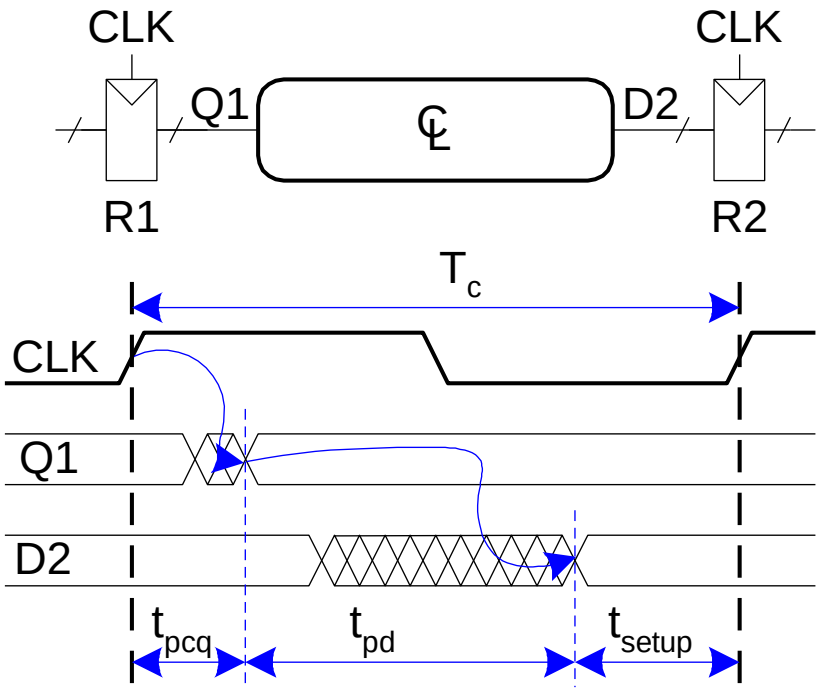
Timing

- The delay between registers has a **minimum** and **maximum** delay, dependent on the delays of the circuit elements



Setup Time Constraint

- The setup time constraint depends on the **maximum** delay from register R1 through the combinational logic.
- The input to register R2 must be stable at least t_{setup} before the clock edge.



$$T_c \geq$$

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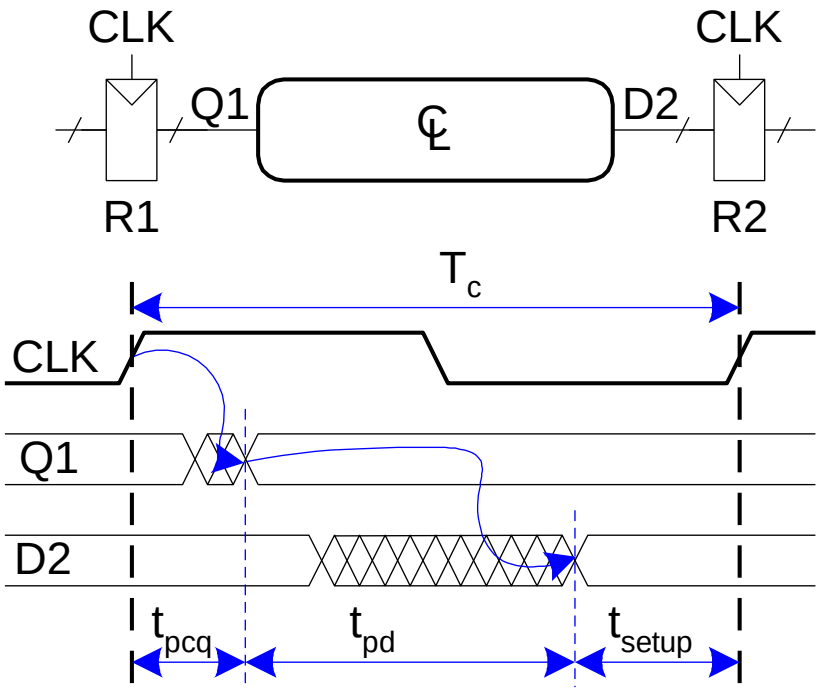

$$T_c \geq t_{pcq} + t_{pd} + t_{\text{setup}}$$

$$t_{pd} \leq$$

Setup Time Constraint

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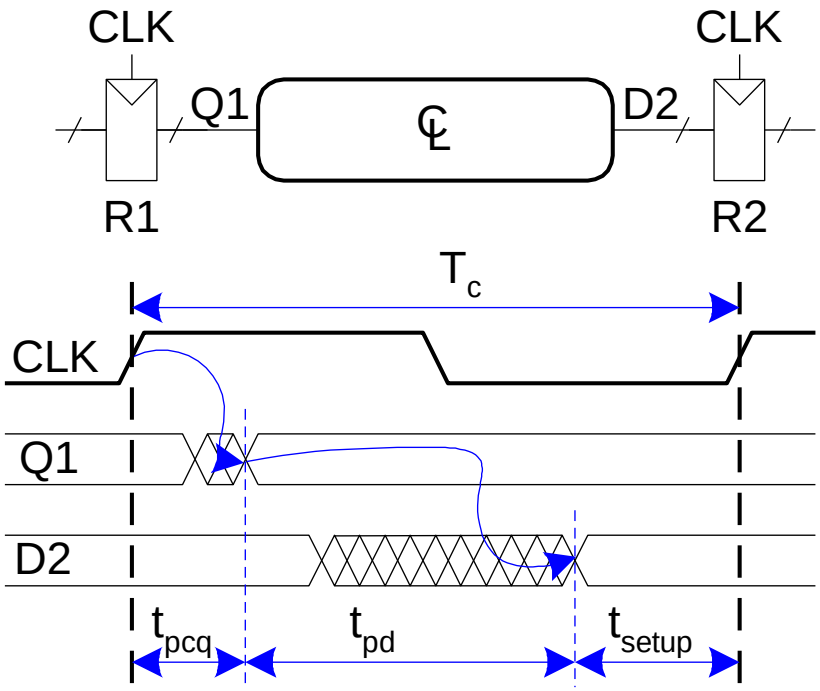
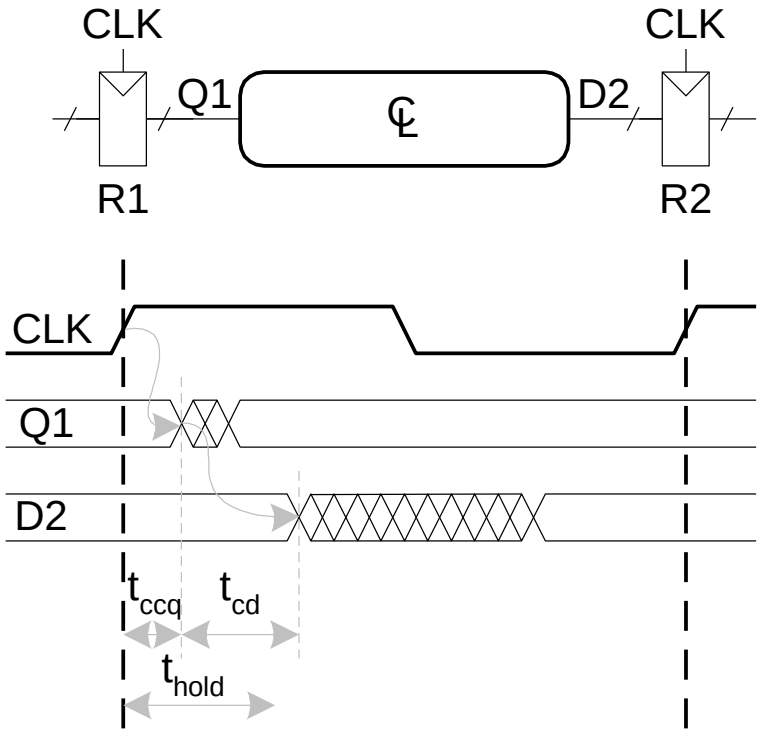


$$T_c \geq t_{pcq} + t_{pd} + t_{setup}$$

$$t_{pd} \leq T_c - (t_{pcq} + t_{setup})$$

Hold Time Constraint

- The hold time constraint depends on the **minimum** delay from register R1 through the combinational logic.
- The input to register R2 must be stable for at least t_{hold} after the clock edge.



$t_{hold} <$

Hold Time Constraint

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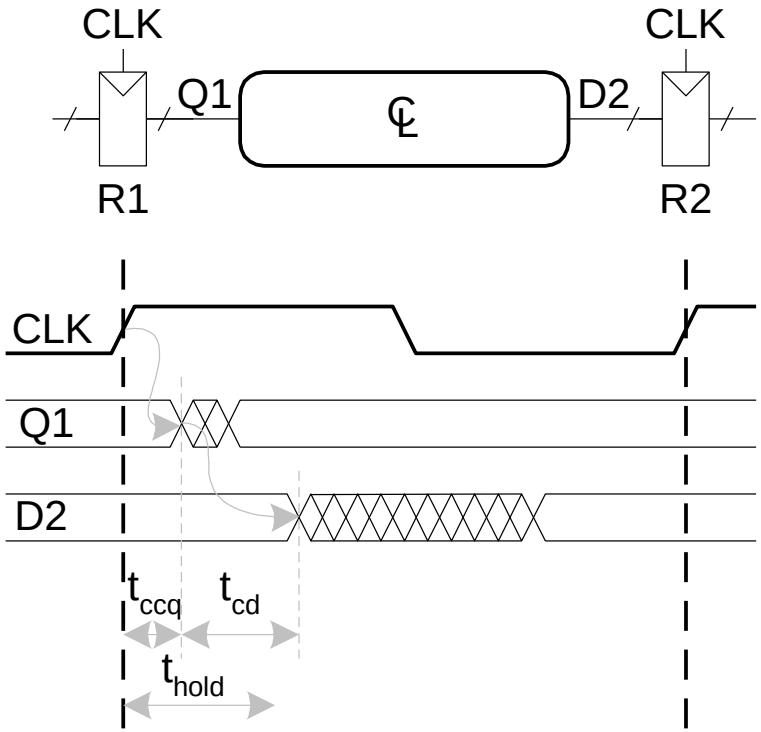
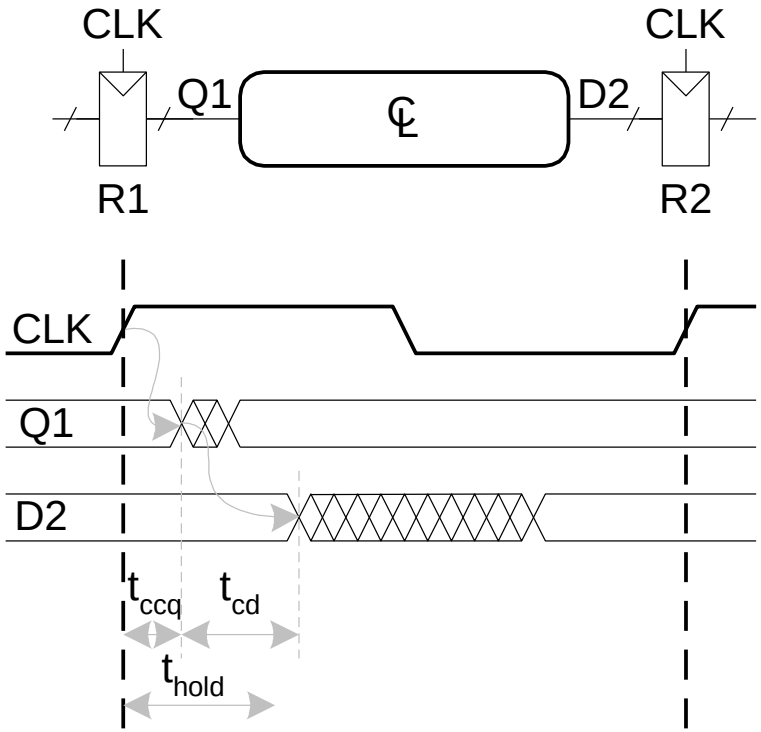


$$t_{hold} < t_{ccq} + t_{cd}$$

$$t_{cd} >$$

Hold Time Constraint

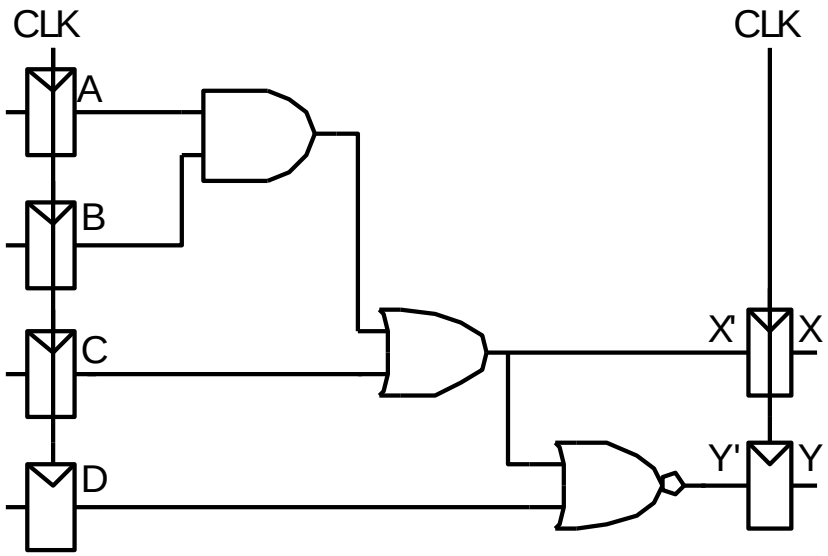
- The hold time constraint depends on the **minimum** delay from register R1 through the combinational logic.
- The input to register R2 must be stable for at least t_{hold} after the clock edge.



$$t_{hold} < t_{ccq} + t_{cd}$$

$$t_{cd} > t_{hold} - t_{ccq}$$

Timing Analysis



Timing Characteristics

t_{ccq} = 30 ps

t_{pcq} = 50 ps

t_{setup} = 60 ps

t_{hold} = 70 ps

per gate

t_{pd} = 35 ps

t_{cd} = 25 ps

t_{pd} =

t_{cd} =

Setup time constraint:

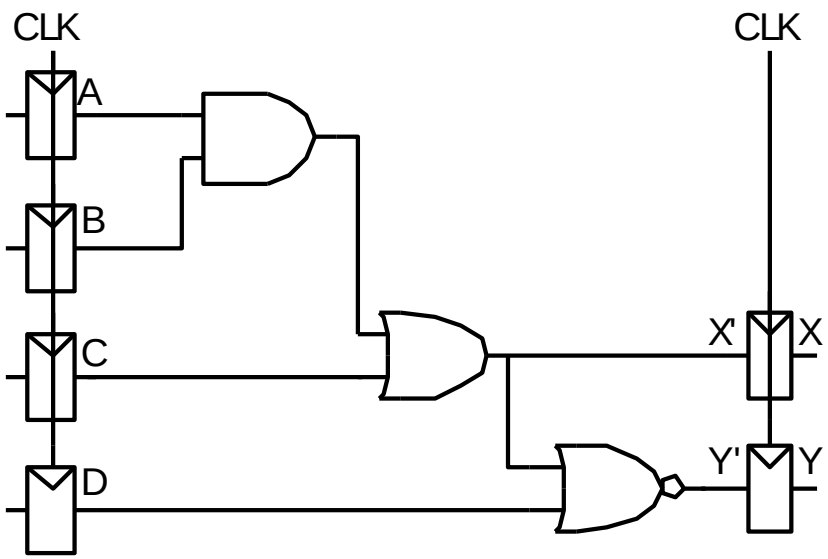
$T_c \geq$

$f_c = 1/T_c =$

Hold time constraint:

$t_{ccq} + t_{pd} > t_{hold}$?

Timing Analysis



Timing Characteristics

t_{ccq} = 30 ps

t_{pcq} = 50 ps

t_{setup} = 60 ps

t_{hold} = 70 ps

per gate

t_{pd} = 35 ps

t_{cd} = 25 ps

t_{pd} = 3 x 35 ps = 105 ps

t_{cd} = 25 ps

Setup time constraint:

$T_c \geq (50 + 105 + 60)$ ps = 215 ps

$f_c = 1/T_c$ = 4.65 GHz

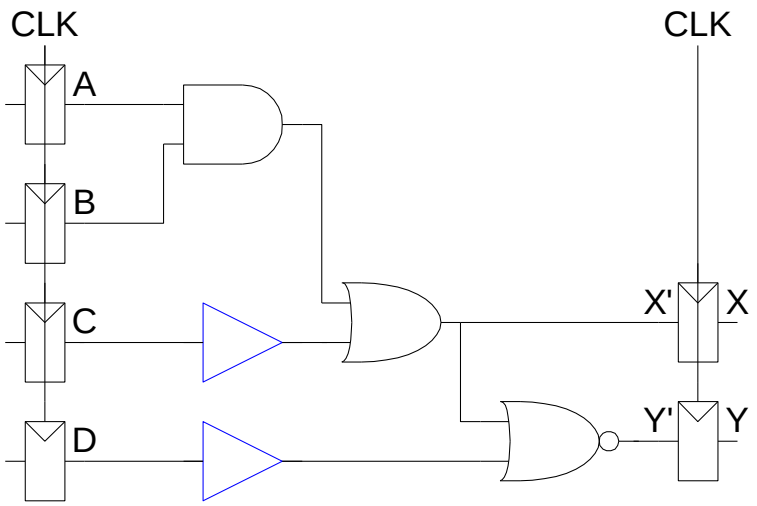
Hold time constraint:

$t_{ccq} + t_{pd} > t_{hold}$?

(30 + 25) ps > 70 ps ? No!

Fixing Hold Time Violation

Add buffers to the short paths:



Timing Characteristics

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Setup time constraint:

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f_c =

Hold time constraint:

$t_{ccq} + t_{pd} > t_{hold}$?

Fixing Hold Time Violation

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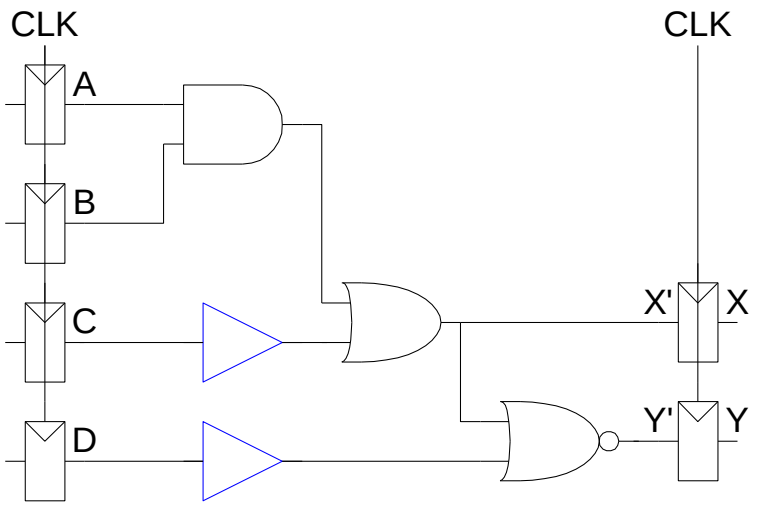


t_{pd} = 3 x 35 ps = 105 ps

t_{cd} = 2 x 25 ps = 50 ps

Setup time constraint:

$T_c \geq (50 + 105 + 60)$ ps = 215 ps

$f_c = 1/T_c$ = 4.65 GHz

Timing Characteristics

t_{ccq} = 30 ps

t_{pcq} = 50 ps

t_{setup} = 60 ps

t_{hold} = 70 ps

per gate

t_{pd} = 35 ps

t_{cd} = 25 ps

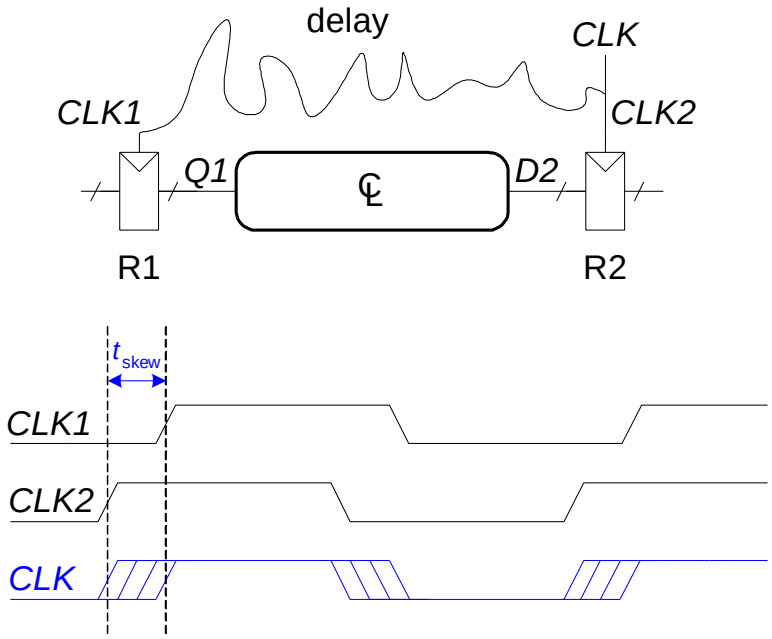
Hold time constraint:

$t_{ccq} + t_{pd} > t_{hold}$?

(30 + 50) ps > 70 ps ? Yes!

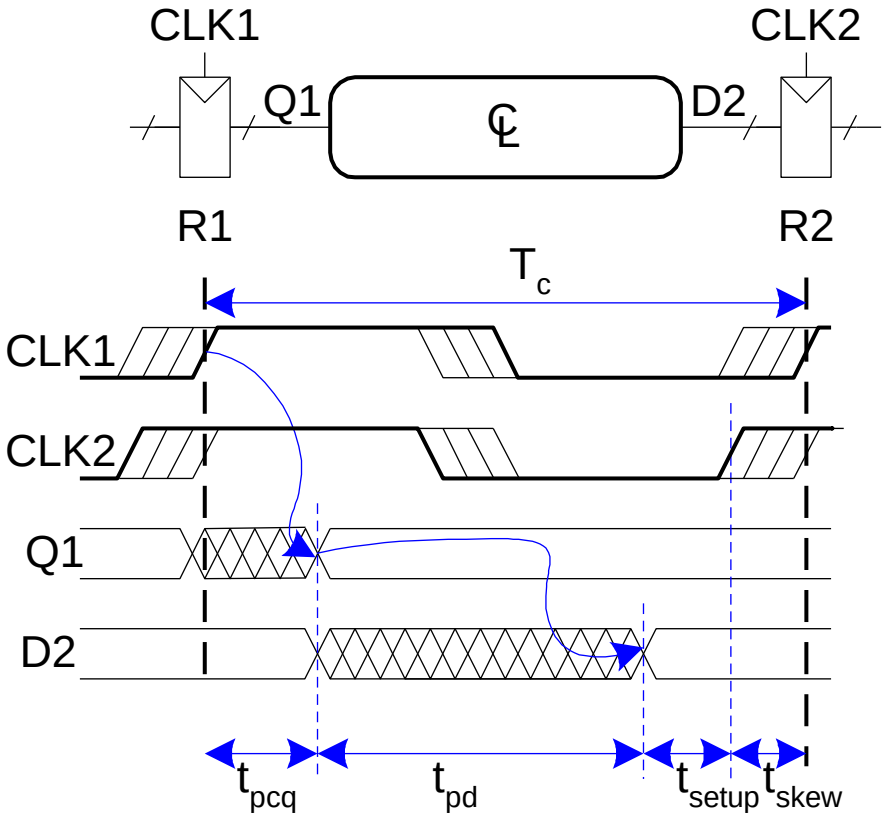
Clock Skew

- The clock doesn't arrive at all registers at the same time
- Skew is the difference between two clock edges
- Examine the worst case to guarantee that the dynamic discipline is not violated for any register – many registers in a system!



Setup Time Constraint with Clock Skew

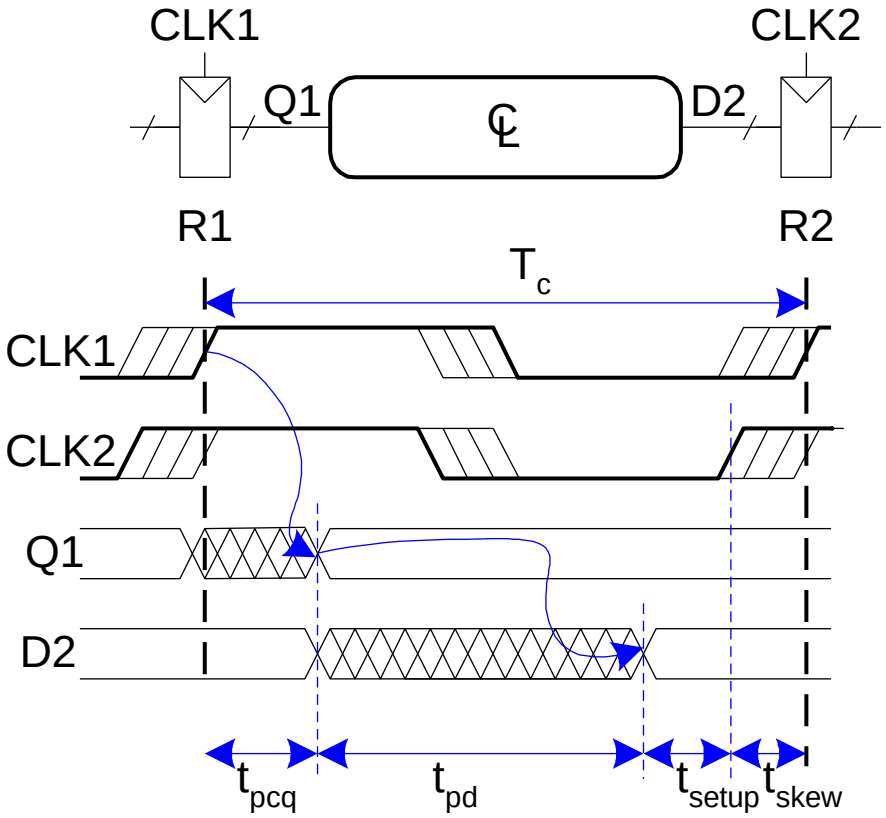
- In the worst case, the CLK2 is earlier than CLK1



$T_c \geq$

Setup Time Constraint with Clock Skew

- In the worst case, the CLK2 is earlier than CLK1



$$T_c \geq t_{pcq} + t_{pd} + t_{\text{setup}} + t_{\text{skew}}$$

$$t_{pd} \leq$$

Setup Time Constraint with Clock Skew

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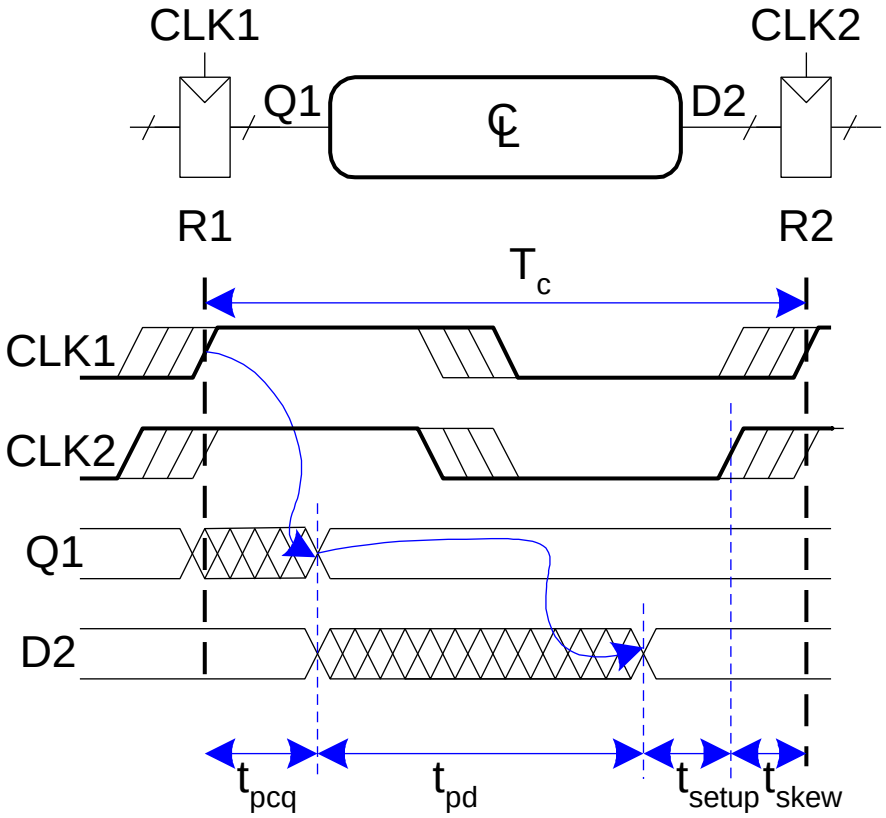

$$T_c \geq t_{pcq} + t_{pd} + t_{\text{setup}} + t_{\text{skew}}$$

$$t_{pd} \leq T_c - (t_{pcq} + t_{\text{setup}} + t_{\text{skew}})$$