

CS 225: Switching Theory

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Previous Class

- Number Systems and Codes
 - Different Number systems (positional)
 - Conversion
 - Representation (complement)
 - Binary Arithmetic

This Class

- Number Systems and Codes
 - Codes
 - BCD, cyclic code etc.
 - Gray code
 - Parity and Error correcting code

Signed binary number

Positive numbers can be defined with Sign bit 0

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- Ex. In 8-bit representation of +9 = 00001001
- Negative numbers can be represented in three different ways:
 - Signed magnitude: -9 = 10001001
 - Signed 1's complement: -9 = 1110110
 - Signed 2's complement: -9 = 1110111

- Undesired aspect in signed binary and 1's complement method:
- representation of 0s:
 - +0 has different code from -0

Radix Complements (r-1's complement)

- r-1's Complements:
 - Diminished Radix (r-1)'s Complement
 - (r-1)'s complement of a number N with n digits is $(r^n - 1) - N$.

Ex.: 9's complement of 346 is $999 - 346 = 653$ ($10^3 - 1 = 999$)

- 1's complement of a binary number can be determined as just replacing 1's with 0's and vice-versa..

Radix Complements (r's complement)

- Radix complement:
 - r's complement of a number N with n digits is $r^n - N = (r^n - 1) - N + 1$.
Ex. 10's complement of 346 is = 654 (653+1)
2's complement of 1011 = 0101

NB: complement of complement of N is N $r^n - (r^n - N) = N$

Subtraction using r's complement

- Addition
 - Care for overflow
- Subtraction:
 - Complements:
- M and N are two n digit numbers with radix r
- To subtract N from M
 - Compute the r's complement of N ($= r^n - N$)
 - Add M with r's complement of N i.e. $M - N + r^n$

If $M \geq N$ result **produce the carry** r^n which may be discarded so resulting $M - N$

If $M < N$ result **does not produce carry** that may be treated as $M - N + r^n = r^n - (N - M)$ so the answer is r's complement of the result.

Overflow

- Overflow is said to occur if the result needs more than n-bits.
- If c is a carry into the sign-bit position and o is the carry from sign-bit position; then overflow is said to occur if and only if $c \text{ XOR } o = 1$

Ex.:

Answer the following

Q1. $(1010100)_2 - (1000011)_2 = ?$ Use 2' complement method

Ans.: $10010001 = 0010001$ (17=84-67)

Q2. $(1000011)_2 - (1010100)_2 = ?$ Use 2' complement method

Ans.: $\underline{1101111} = -0010001$ (-17=67-84)

Q3. $1100101_2 \times 111101_2 = ?$

Ans.: 1100000010001 (101 x61 =6161)

Q4. $100101_2 \div 101_2 = ?$

Ans.: Q= 111, rem= 10 ($37_{10} \div 5_{10} = Q(7), \text{rem}(2)$)

Binary Coded Decimal (BCD)

To code a number with n decimal digits, we need $4n$ bits in BCD

$$\text{e.g. } (365)_{10} = (0011\ 0110\ 0101)_{\text{BCD}}$$

This is different to converting to binary, which is $(365)_{10} = (101101101)_2$

- Use 4-bit binary to represent one decimal digit
- Easy conversion
- **Wasting bits** (4-bits can represent 16 different values, but only 10 values are used). Clearly, BCD requires more bits. BUT, it is **easier to understand/interpret**

DECIMAL DIGIT	0	1	2	3	4	5	6	7	8	9
BCD	0000	0001	0010	0011	0100	0101	0110	0111	1000	1001

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