

1. a. In DDA algorithm, there is an extra overhead of using $\text{roundoff}()$ function. The points generated by this algorithm are not accurate.

c. $P_1(5, 3) \rightarrow P_2(12, 7)$

x	y	d
5	3	1
6	4	-5
7	4	3
8	5	-3
9	5	5
10	6	-1
11	6	7
12	7	1

$$\begin{aligned}
 dx &= 12 - 5 = 7 \\
 dy &= 7 - 3 = 4 \\
 d &= 2dy - dx = 8 - 7 = 1 \\
 ds &= 2(dy - dx) = 2(4 - 7) = -6 \\
 dT &= 2dy = 2 \times 4 = 8 \\
 \text{if } (d < 0); \\
 & \quad d = d + ds; \\
 \text{else} \\
 & \quad d = d + dT; \\
 & \quad y = y + 1;
 \end{aligned}$$

2. The steps are to scan convert a line using DDA algorithm:-

Step-1:- Start algorithm.

Step-2:- Declare $x_1, y_1, x_2, y_2, dx, dy$

Step-3:- Enter the value of x_1, y_1, x_2, y_2 . Where, x_1, y_1 are the coordinates of starting point and x_2, y_2 are the coordinates of ending point.

Step-4:- Calculate the value

$$dx = x_2 - x_1$$

$$dy = y_2 - y_1$$

Step-5:- if $(abs(dx)) > (abs(dy))$

$$step = abs(dx)$$

$$\text{else } step = abs(dy)$$

Step-6:- $x_{inc} = dx/step$

$$y_{inc} = dy/step$$

$$\text{assign, } x = x_1$$

$$y = y_1$$

Step-7:- set pixel (x, y)

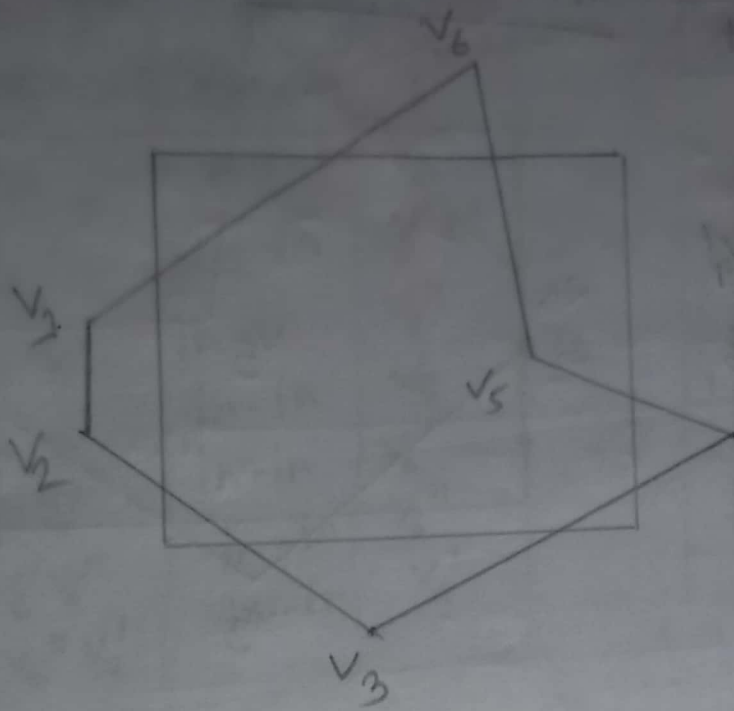
Step-8:- $x = x + x_{inc}$

$$y = y + y_{inc}$$

step 9: Repeat step 8 until $u = u_2$

step 10: Stop algorithm.

C:



Left clipping!

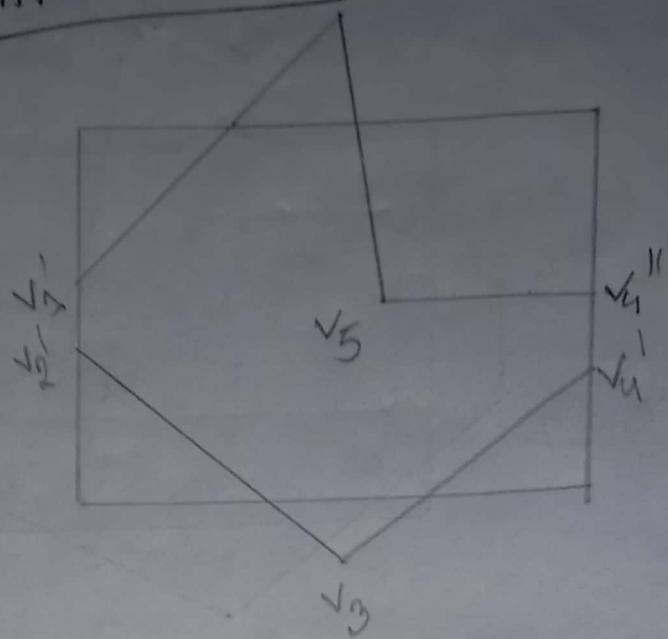
vertices	Case	output
$v_1 - v_2$	out-out	—
$v_2 - v_3$	out-in	$v_2' - v_3$
$v_3 - v_4$	in-in	v_4
$v_4 - v_5$	in-in	v_5
$v_5 - v_6$	in-in	v_6
$v_6 - v_1$	out-in	$v_6 - v_1' - v_6$



Right Clipping

Vertex	Case	Output
$V_1' V_2'$	in-in	V_2'
$V_2' V_3$	in-in	V_3
$V_3 V_4$	out-in	$V_3 V_4'$
$V_4 V_5$	out-in in-out	$V_4'' V_5$
$V_5 V_6$	in-in	V_6
$V_6 V_1'$	in-in	V_1'

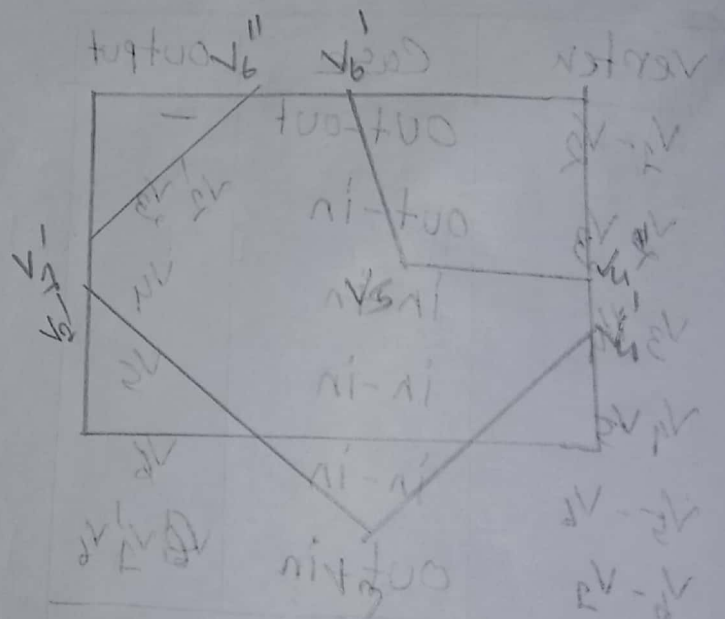
After Clipping:



Left Clipping

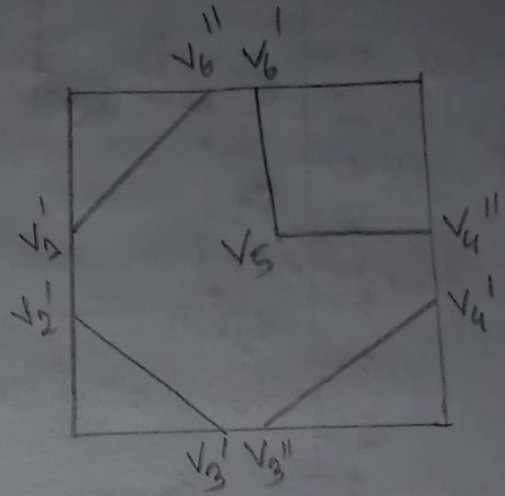
Vertex	Case	Output
$V_1' V_2'$	in-in	V_2'
$V_2' V_3$	in-in	V_3
$V_3 V_4'$	in-in	V_4'
$V_4' V_4''$	in-in	V_4''
$V_4'' V_5$	in-in	V_5
$V_5 V_6$	in-out	V_6'
$V_6 V_1'$	out-in	$V_6'' V_1'$

After Clipping:



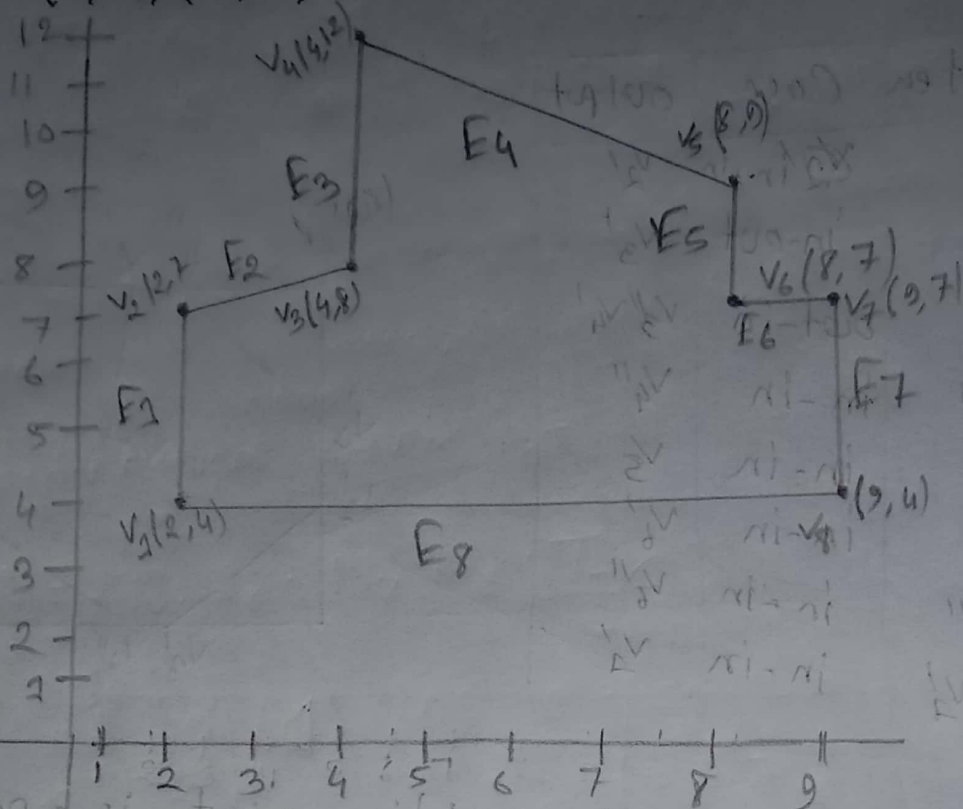
Bottom Clipping:-

Vertex	Case	Output
$V_1' V_2'$	2 in-in	V_2'
$V_2' V_3'$	in-out	V_3'
$V_3' V_4'$	out-in	$V_3'' V_4'$
$V_4' V_4''$	in-in	V_4''
$V_4'' V_5$	in-in	V_5
$V_5 V_6'$	in-in	V_6'
$V_6' V_6''$	in-in	V_6''
$V_6'' V_1'$	in-in	V_1'



3. a. Vanishing point:- A vanishing point is a point on image plane of a perspective rendering where two-dimensional parallel lines in three-dimensional space appear to converge.

C $(2,4), (2,7), (4,8), (4,12), (8,9), (8,7), (9,7), (9,4)$.



Edge	y_{\min}	y_{\max}	u when $y = y_{\min}$	$1/m$
E_3	8	12	4	$1/m_3$
E_5	7	$9-1=8$	8	$1/m_5$
E_2	7	$8-1=7$	2	$1/m_2$
E_6 E_1	4	$7-1=6$	2	$1/m_1$
E_7 E_7	4	$7-1=6$	9	$1/m_7$
E_8 E_4	9	12	8	$1/m_4$

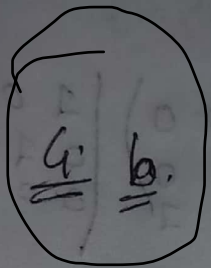
$$y=5 \rightarrow E_1, E_7,$$

$$y=7 \rightarrow E_2, E_5,$$

$$y=8 \rightarrow E_2, E_3, E_5$$

$$y=9 \rightarrow E_3, E_4$$

$$y=11 \rightarrow \text{all } E_3, E_4.$$



$$\theta = 45^\circ; A(0,0), B(1,1), C(5,2).$$

$$R_\theta = \begin{pmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$= \begin{pmatrix} \cos 45^\circ & -\sin 45^\circ & 0 \\ \sin 45^\circ & \cos 45^\circ & 0 \\ 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} \sqrt{2}/2 & -\sqrt{2}/2 & 0 \\ \sqrt{2}/2 & \sqrt{2}/2 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$\therefore R_\theta(ABC) = \begin{pmatrix} \sqrt{2}/2 & -\sqrt{2}/2 & 0 \\ \sqrt{2}/2 & \sqrt{2}/2 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 0 & 1 & 5 \\ 0 & 1 & 2 \\ 1 & 1 & 1 \end{pmatrix}$$

$$= \begin{pmatrix} 0+0+0 & \sqrt{2}/2 - \sqrt{2}/2 + 0 & 5\sqrt{2}/2 - \sqrt{2} + 0 \\ 0+0+0 & \sqrt{2}/2 + \sqrt{2}/2 + 0 & 5\sqrt{2}/2 + \sqrt{2} + 0 \\ 0+0+1 & 0+0+0 & 0+0+1 \end{pmatrix}$$

$$= \begin{pmatrix} 0 & 0 & 3\sqrt{2}/2 \\ 0 & \sqrt{2} & 7\sqrt{2}/2 \\ 1 & 1 & 1 \end{pmatrix}$$

$$A'(0,0), B'(0,\sqrt{2}), C'(3\sqrt{2}/2, 7\sqrt{2}/2)$$

C.

$$V = \begin{pmatrix} -1 & 0 & 1 & 0 \\ 0 & -2 & 0 & 2 \\ 1 & 1 & 1 & 1 \end{pmatrix}$$

The line $y=2$ has intercept $(0,2)$ and makes an angle of 0° with the x axis, so, with $\theta=0$, and $V=2J$.

the transformation matrix is -

$$M_L = T_v \cdot R_\theta \cdot M_u \cdot R_{-\theta} \cdot T_{-v}$$

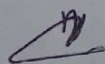
$$M_L = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 2 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{pmatrix} =$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 2 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & -2 \\ 0 & 0 & 1 \end{pmatrix} =$$

$$\boxed{0+2+2}$$

$$\begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 4 \\ 0 & 0 & 1 \end{pmatrix}$$



5. a. Window to viewport mapping:- The process that converts object in WCS to normalized device coordinates (NDCs) is called window to viewport mapping.

b. The window aspect ratio is $a_w = \frac{4}{3}$.

We choose the x extent from 0 to 1 and y extent from 0 to $\frac{4}{3}$.

$$\therefore a_v = \frac{1}{3/4} = \frac{4}{3}$$

$$w_{x_{\max}} = 4, \quad w_{x_{\min}} = 0;$$

$$w_{y_{\max}} = 3, \quad w_{y_{\min}} = 0;$$

$$v_{x_{\max}} = 1, \quad v_{x_{\min}} = 0$$

$$v_{y_{\max}} = \frac{3}{4}, \quad v_{y_{\min}} = 0$$

$$M = \begin{pmatrix} \frac{1}{4} & 0 & 0 \\ 0 & \frac{3}{4} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

6. $P_1(2, 2, 0)$, $P_2(2, 4, 6)$, $P_3(-5, -10, -60)$, $P_4(3, 6, 20)$
 $C(0, 0, -10)$

$\Rightarrow P_0(u_0, y_0, z_0)$, $P_1(u_1, y_1, z_1)$

$$\overrightarrow{P_0P_1} = (u_1 - u_0)\hat{i} + (y_1 - y_0)\hat{j} + (z_1 - z_0)\hat{k}$$

$$u = u_0 + (u_1 - u_0)t$$

$$y = y_0 + (y_1 - y_0)t$$

$$z = z_0 + (z_1 - z_0)t$$

$P_1: x = u_0 + (u_1 - u_0)t$

$$= 0 + (1 - 0)t$$

$$= t$$

$$u = t \text{ or } t = u \quad \text{--- (1)}$$

$$y = y_0 + (y_1 - y_0)t$$

$$\Rightarrow y = 0 + (2 - 0)t$$

$$\Rightarrow y = 2t$$

$$z = z_0 + (z_1 - z_0)t$$

$$= -10 + (0 - 10)t$$

$$= -10 + 10t$$

$C P_2$: from equation 1

$$x = t \text{ or } t = x$$

$$x = 2 \text{ or } t = 2$$

$$y = 2t$$

$$= 2 \times 2 = 4$$

$$z = -10 + 10t$$

$$= -10 + (10 \times 2)$$

$$= 10$$

P_2 lies on the projection line through C and P_1 .

P_2 is not on the projection line. So, it neither projection observes nor line through C and P_1 observes P_1 and P_2 .

CP3: $x = -5$
 $t = -5$

$$y = 2t$$

$$= 2 \times (-5)$$

$$= -10$$

$$z = -10 + 10t$$

$$= -10 + 10(-5)$$

$$= -10 - 50$$

$$= -60$$

P_3 lies on the projection line through C and P_3 .

CP4: $x = 3$
 $t = 3$

$$y = 2t$$

$$= 2 \times 3$$

$$z = -10 + 10t$$

$$= -10 + (10 \times 3)$$

$$= -10 + 30$$

$$= 20$$

P_4 lies on the projection line through C and P_4 .

C occurs on the line at $t = 0$

P_1 occurs at $t = 1$

P_3 occurs at $t = -5$

P_4 occurs at $t = 3$

Thus comparing t values P_3 is in the front of P_4 and P_4 obscures P_1 and P_4 with respect to C . Hence, P_3