

# 電磁波與天線導論 HW9

Name : 郭忠翔

ID : R10522845

## Q1

(a)

$$Y_1 = \frac{1}{j\omega L_1 + \frac{1}{j\omega C_3}}$$

$$Y_2 = j\omega C_1$$

$$Y^1 = Y_1 + Y_2$$

$$Z_{in}^1 = Z_0 \frac{\frac{1}{Y^1} + jZ_0 \tan(36^\circ)}{Z_0 + j\frac{1}{Y^1} \tan(36^\circ)}$$

$$Y^2 = \frac{1}{R_3} + \frac{1}{Z_{in}^1}$$

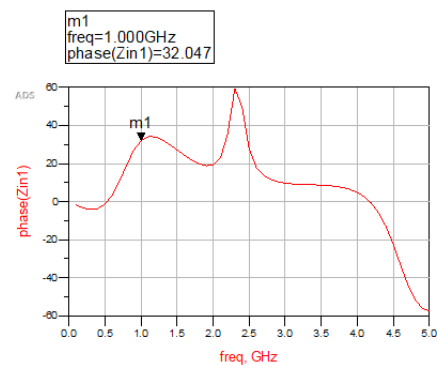
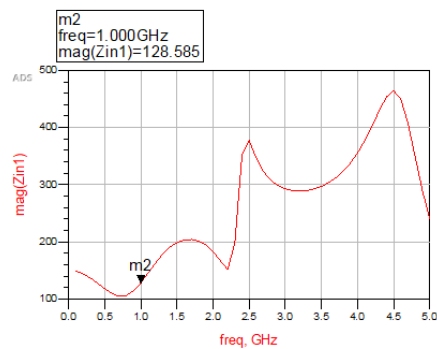
$$Z_{in}^2 = Z_0 \frac{\frac{1}{Y^2} + jZ_0 \tan(25^\circ)}{Z_0 + j\frac{1}{Y^2} \tan(25^\circ)}$$

$$Z_{in} = R_4 + Z_{in}^2 = 108.99 + j68.228(\Omega) - < ans >$$

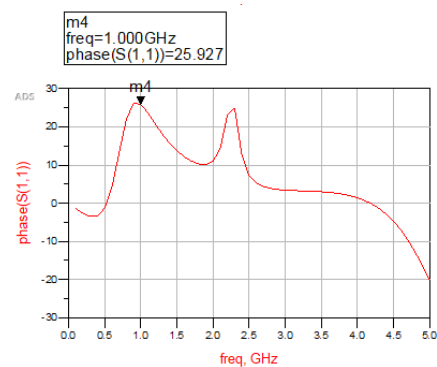
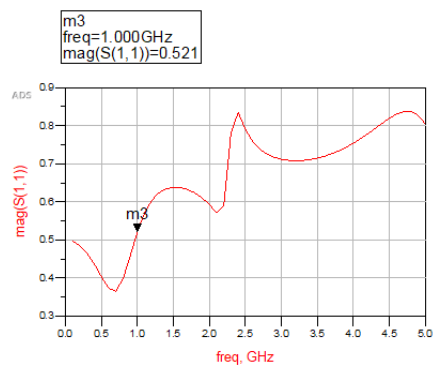
$$\Gamma = \frac{Z_{in} - Z_0}{Z_{in} + Z_0} = 0.4688 + j0.2279 - < ans >$$

(b)

input impedance



reflection



$T$  network :

$$\begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$$

$$Z_{11} = \frac{V_1}{I_1} \Big|_{I_2=0} = \frac{1}{Y_A} + \frac{1}{Y_B}$$

$$Z_{12} = \frac{V_1}{I_2} \Big|_{I_1=0} = \frac{V_2}{I_2} \frac{\frac{1}{Y_B}}{\frac{1}{Y_A} + \frac{1}{Y_B}} = \frac{1}{Y_B}$$

$$Z_{21} = Z_{12}$$

$$Z_{22} = \frac{V_2}{I_2} \Big|_{I_1=0} = \frac{1}{Y_A} + \frac{1}{Y_B}$$

$$Z \text{ matrix} : \begin{bmatrix} \frac{Y_A+Y_B}{Y_A Y_B} & \frac{1}{Y_B} \\ \frac{1}{Y_B} & \frac{Y_A+Y_B}{Y_A Y_B} \end{bmatrix} - < ans >$$

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

$$Y \text{ matrix} : Z^{-1} = \begin{bmatrix} \frac{Y_A(Y_A+Y_B)}{Y_A Y_B} & -\frac{Y_A^2}{2Y_A+Y_B} \\ -\frac{Y_A^2}{2Y_A+Y_B} & \frac{Y_A(Y_A+Y_B)}{Y_A Y_B} \end{bmatrix} - < ans >$$

$\pi$  network :

$$Z_A = \frac{\frac{1}{Y_A^2} + \frac{2}{Y_A Y_B}}{\frac{1}{Y_B}} = \frac{2Y_A + Y_B}{Y_A^2}$$

$$Z_B = \frac{\frac{1}{Y_A^2} + \frac{2}{Y_A Y_B}}{\frac{1}{Y_A}} = \frac{2Y_A + Y_B}{Y_A Y_B}$$

$$\begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

$$Y_{11} = Y_{22} = \frac{1}{Z_A} + \frac{1}{Z_B} = \frac{Y_A(Y_A + Y_B)}{2Y_A + Y_B}$$

$$Y_{12} = Y_{21} = \frac{1}{Z_A} = \frac{Y_A^2}{2Y_A + Y_B}$$

$$Y \text{ matrix} : \begin{bmatrix} \frac{Y_A(Y_A+Y_B)}{2Y_A+Y_B} & \frac{Y_A^2}{2Y_A+Y_B} \\ \frac{Y_A^2}{2Y_A+Y_B} & \frac{Y_A(Y_A+Y_B)}{2Y_A+Y_B} \end{bmatrix} - < ans >$$

$$Z \text{ matrix} : \begin{bmatrix} \frac{Y_A+Y_B}{Y_A Y_B} & -\frac{1}{Y_B} \\ -\frac{1}{Y_B} & \frac{Y_A+Y_B}{Y_A Y_B} \end{bmatrix} - < ans >$$

**Q3**

$$Z_{in} = \frac{1}{\frac{1}{z} + \frac{1}{z_0}} = \frac{z_0 z}{z + z_0}$$

$$S_{11} = S_{22} = \frac{Z_{in} - z_0}{Z_{in} + z_0} = \frac{-z_0}{2z + z_0} - < ans >$$

$$S_{12} = S_{21} = 1 - < ans >$$